Data Science 2 Final

Group 6

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Set up

Load libraries and data

```
library(caret)
library(mgcv)
library(earth)
library(tidyverse)
library(summarytools)
library(corrplot)
library(ggpubr)
library(rpart)
library(rpart.plot)
library(randomForest)
library(ranger)
library(gbm)
library(pdp)
library(vip)
# setwd("D:/CUMC/Y2S2/DS2/Final/ds2_final")
load("./recovery.RData")
```

Subset 2 df and keep unique observations

```
set.seed(2543)
dat1 <- dat[sample(1:10000, 2000),]
set.seed(4017)
dat2 <- dat[sample(1:10000, 2000),]
dat_bind <- unique(rbind(dat1, dat2))</pre>
```

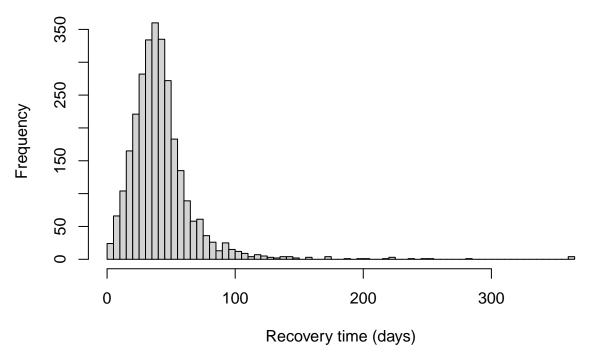
Exploratory analysis and data visualization

Data Partition

Here, we mainly want to investigate the EDA of the training dataset. Therefore, we will start with the data partition.

Understanding the outcome variable recovery_time

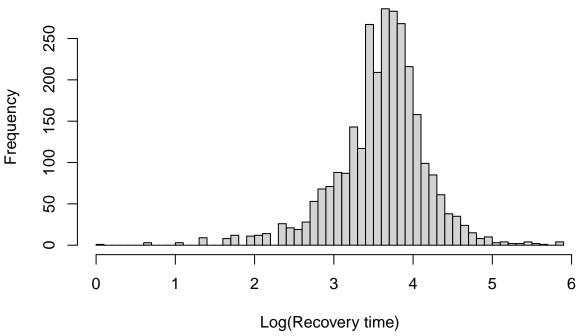
```
# check the outcome variable
hist(dat_bind$recovery_time[trainRows], breaks = 100, xlab = "Recovery time (days)", main = "")
```



The distribution of the outcome variable recovery_time is heavily right-skewed. To account for this, we will take the log-transformation of the outcome and use that variable for following analyses.

```
dat_bind_primary = dat_bind %>%
  na.omit(dat_bind) %>%
  mutate(lrecovery_time = log(recovery_time)) %>%
  dplyr::select(-recovery_time, -id)

# log-transformation helped with making it more normal
hist(dat_bind_primary$lrecovery_time[trainRows], breaks = 50, xlab = "Log(Recovery_time)", main = "")
```



Summary of the dataset

```
st_options(plain.ascii = F,
         style = "rmarkdown",
         dfSummary.silent = T,
         footnote = NA,
         subtitle.emphasis = F)
dfSummary(dat_bind_primary[trainRows, -1])
## ### Data Frame Summary
## **dat_bind_primary**
## **Dimensions:** 2878 x 14
## **Duplicates:** 0
##
## ------
                 Stats / Values
                                               Freqs (% of Valid) Graph
## No
      Variable
Min : 0\
## 1
       gender\
                                               0 : 1490 (51.8%)\
                                                                   IIIIIIIII \
##
       [integer]
                      Mean : 0.5\
                                               1 : 1388 (48.2%)
                                                                   IIIIIIIII
                      Max : 1
##
##
## 2
       race\
                      1\. 1\
                                               1863 (64.7%)\
                                                                   IIIIIIIIII \
                      2\. 2\
                                                                   I\
##
       [factor]
                                               145 ( 5.0%)\
                      3\. 3\
##
                                               569 (19.8%)\
                                                                    III \
                       4\. 4
                                                301 (10.5%)
##
##
## 3
                      1\. 0\
                                                1753 (60.9%)\
                                                                    IIIIIIIIIII \
       smoking\
       [factor]
                       2\. 1\
##
                                                846 (29.4%)\
                                                                    IIIII \
##
                       3\. 2
                                                279 ( 9.7%)
##
       height\
                       Mean (sd) : 170.1 (5.9)
                                                311 distinct values
                                                                    \ \ \ \ \ \ \ . :\
## 4
                                                                    \ \ \ \ \ \ : : \
                       min < med < max:\
##
       [numeric]
                       150.7 < 170.4 < 190.6
                                                                    \ \ \ \ . : : . \
##
##
                       IQR (CV) : 7.9 (0)
                                                                    \ \ \ \ : : : : \
##
                                                                    \ \ . : : : : .
##
## 5
       weight\
                       Mean (sd) : 79.9 (7)
                                                358 distinct values
                                                                   1:1111:1
       [numeric]
                       min < med < max:\
                                                                    \ \ \ \ \ \ : : . \
##
                                                                    \ \ \ \ \ \ : : : \
##
                       55.9 < 80.1 < 111.6
##
                       IQR (CV) : 9.5 (0.1)
                                                                    \ \ \ \ : : : : \
##
                                                                    \ \ . : : : : :
##
## 6
       bmi\
                       Mean (sd) : 27.7 (2.7)
                                                162 distinct values
                                                                    \ \ \ \ \ \ \ . :\
                                                                    \ \ \ \ \ \ : :\
##
       [numeric]
                       min < med < max:\
##
                       19.7 < 27.5 < 38.1
                                                                    \ \ \ \ . : : : \
##
                       IQR (CV) : 3.6 (0.1)
                                                                    \ \ \ \ : : : : . \
##
                                                                    \ \ : : : : : : .
##
       hypertension\
                                                0:1499 (52.1%)
## 7
                       Min : 0\
                                                                    IIIIIIIII \
##
       [numeric]
                       Mean : 0.5
                                                1 : 1379 (47.9%)
                                                                    IIIIIIII
##
                       Max : 1
##
## 8
       diabetes\
                      Min : 0\
                                                0 : 2403 (83.5%)\
                                                                   IIIIIIIIIIIIIII \
```

```
##
        [integer]
                         Mean : 0.2
                                                     1: 475 (16.5%)
                                                                           III
##
                         Max : 1
##
       SBP\
                         Mean (sd) : 130.2 (8)
                                                     51 distinct values
                                                                           \ \ \ \ \ \ \ \ \ : .\
## 9
                                                                           \ \ \ \ \ \ . : : \
##
        [numeric]
                         min < med < max:\
                         106 < 130 < 157\
                                                                           \ \ \ \ \ \ : : : : \
##
                         IQR (CV) : 11 (0.1)
                                                                           \ \ \ \ : : : : : \
##
                                                                           \\:::::::
##
##
       LDL\
                         Mean (sd) : 110.6 (19.9)\ 121 distinct values
                                                                           ## 10
##
        [numeric]
                         min < med < max:\</pre>
                                                                           \ \ \ \ \ \ \ \ \ : : . \
                         28 < 111 < 178\
                                                                           \ \ \ \ \ \ \ \ \ : : : \
##
                         IQR (CV) : 27 (0.2)
                                                                           \ \ \ \ \ \ . : : : : \
##
                                                                           \\\\::::::
##
##
## 11
       vaccine\
                         Min : 0\
                                                     0 : 1189 (41.3%)\
                                                                           IIIIIIII \
                         Mean : 0.6\
                                                     1: 1689 (58.7%)
                                                                           IIIIIIIIII
##
        [integer]
##
                         Max : 1
##
## 12
       severity\
                         Min : 0\
                                                     0 : 2589 (90.0%)\
                                                                           IIIIIIIIIIIIIII \
##
        [integer]
                         Mean : 0.1
                                                     1 : 289 (10.0%)
                                                                           ΤT
##
                         Max : 1
##
       studv\
                         1\. A\
                                                     571 (19.8%)\
## 13
                                                                           III \
                         2\. B\
                                                     1741 (60.5%)\
##
        [character]
                                                                           IIIIIIIIIII \
##
                         3\. C
                                                     566 (19.7%)
                                                                           III
##
       lrecovery_time\
                         Mean (sd) : 3.6 (0.6)
                                                    147 distinct values
                                                                           ##
                                                                           1: / / / / / / / / / : /
##
        [numeric]
                         min < med < max:\
                         0 < 3.7 < 5.9\
                                                                           \ \ \ \ \ \ \ \ \ \ \ : : \
##
                         IQR (CV) : 0.6 (0.2)
                                                                           \ \ \ \ \ \ \ \ \ \ \ : \
##
##
                                                                           \ \ \ \ \ \ \ \ \ : : : :
```

Understand categorical variables

```
ggplot(aes(x = factor(diabetes))) + geom_bar() + labs(x = "Diabetes", y = "Count") +
  scale_x_discrete(labels = c("No diabetes", "Diabetes"))+theme_classic()
vaccine = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = factor(vaccine))) + geom_bar() + labs(x = "Vaccination status",
                                                  y = "Count") +
  scale_x_discrete(labels = c("Not vaccinated", "Vaccinated"))+theme_classic()
severity = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = factor(severity))) + geom_bar() + labs(x = "Severity", y = "Count")+
  scale_x_discrete(labels = c("Not severe", "Severe"))+theme_classic()
study = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = study)) + geom bar() + labs(x = "Study Site", y = "Count")+theme classic()
cat_combined_plot = ggarrange(gender, race, smoking, hypertension,
                                 diabetes, vaccine, severity, study,
                            ncol = 2, nrow = 4)
cat_combined_plot
   1500
                                                  1500
  1000
                                                   1000
   500
                                                   500
               Female
                                 Male
                                                           White
                                                                    Asian
                                                                             Black
                                                                                     Hispanic
                       Gender
                                                                        Race
                                                   1500
  1500 -
1000 -
500 -
                                                   1000
                                                    500
            Never
                        Former
                                    Current
                                                            No hypertension
                                                                              Hypertension
            smoked
                        smoker
                                    smoker
                      Smoking
                                                                    Hypertension
                                                   1500
  2000
1500
                                                   1000
  1000
                                                    500
             No diabetes
                                                            Not vaccinated
                                Diabetes
                                                                               Vaccinated
                      Diabetes
                                                                  Vaccination status
                                                   1500
Ont 2000 1000
                                                   1000
                                                    500
                                                                          B
              Not severe
                                 Severe
                       Severity
                                                                      Study Site
```

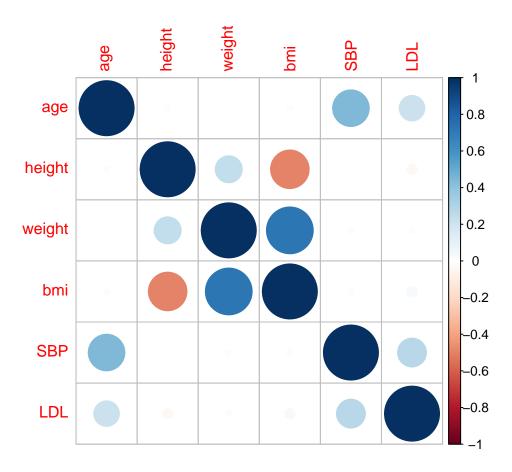
Understand continuous variables

```
par(mar = c(3, 3, 2, 2), mfrow = c(2, 3))
age = hist(dat_bind_primary$age[trainRows], breaks = 50, xlab = "Age (years)", main = "Age")
```

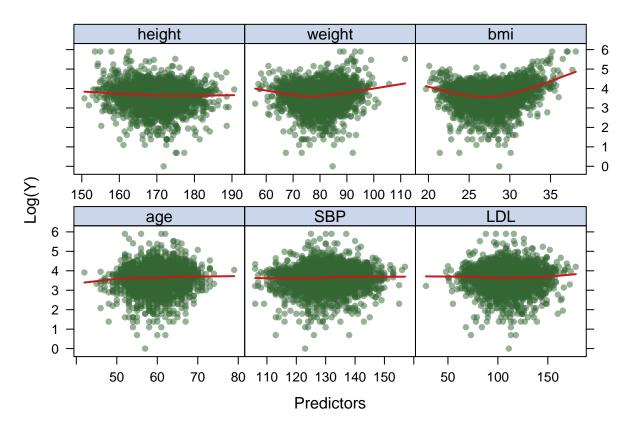
```
bmi = hist(dat_bind_primary$bmi[trainRows], breaks = 50, xlab = "BMI (kg/m^2)", main = "BMI")
height = hist(dat_bind_primary$height[trainRows], breaks = 50, xlab = "Height (cm)", main = "Height")
weight = hist(dat_bind_primary$weight[trainRows], breaks = 50, xlab = "Weight (kg)", main = "Weight")
SBP = hist(dat_bind_primary$SBP[trainRows], breaks = 50, xlab = "SBP (mm/Hg)", main = "Systolic blood p
LDL = hist(dat_bind_primary$LDL[trainRows], breaks = 50, xlab = "LDL (mg/dL)", main = "LDL cholesterol"
             Age
                                                                            Height
200
                                                                150
                                150
                                                                100
                                9
100
                                                                20
                                50
20
        50
             60
                   70
                         80
                                    20
                                         25
                                               30
                                                    35
                                                                   150
                                                                       160
                                                                            170
                                                                                 180
           Weight
                                   Systolic blood pressure
                                                                       LDL cholesterol
                                                                300
                                150
150
                                100
100
                                                                100
                                50
50
                                                                20
     60 70 80 90
                       110
                                     110
                                             130
                                                     150
                                                                       50
                                                                             100
                                                                                    150
```

Understand the correlation between continuous predictors

```
correlation <- model.matrix(lrecovery_time ~ ., dat_bind_primary)[trainRows,-1]
corrplot(cor(dat_bind_primary[trainRows,c(1,5,6,7,10,11)]), method = "circle", type = "full")</pre>
```



Understand the relationship with continuous predictors and the outcome



Understand the relationship between categorical predictors and continuous outcome

```
gender3 = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = as.factor(gender), y = lrecovery_time)) + geom_boxplot() + labs(x = "Gender", y = "Log
race3 = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = as.factor(race), y = lrecovery_time)) + geom_boxplot() + labs(x = "Race", y = "Log Recovery_time))
  scale_x_discrete(labels = c("White", "Asian", "Black", "Hispanic"))+ theme_classic()
smoking3 = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = as.factor(smoking), y = lrecovery_time)) + geom_boxplot() + labs(x = "Smokoing Status")
  scale_x_discrete(labels = c("Never\nsmoked", "Former\nsmoker", "Current\nsmoker"))+ theme_classic()
hypertension3 = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = as.factor(hypertension), y = lrecovery_time)) + geom_boxplot() + labs(x = "Hypertension") + geom_boxplot() + labs(x = "Hypertension")
  scale_x_discrete(labels = c("No", "Yes"))+ theme_classic()
diabetes3 = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = as.factor(diabetes), y = lrecovery_time)) + geom_boxplot() + labs(x = "Diabetes Status") + geom_boxplot() + labs(x = "Diabetes Status")
  scale_x_discrete(labels = c("No", "Yes"))+ theme_classic()
vaccine3 = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = as.factor(vaccine), y = lrecovery_time)) + geom_boxplot() + labs(x = "Vaccination Stat")
  scale_x_discrete(labels = c("No", "Yes"))+ theme_classic()
severity3 = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = as.factor(severity), y = lrecovery_time)) + geom_boxplot() + labs(x = "Severity", y = lrecovery_time)) + geom_boxplot() + labs(x = "Severity", y = lrecovery_time)) + geom_boxplot() + labs(x = "Severity", y = lrecovery_time))
```

```
scale_x_discrete(labels = c("Not severe", "Severe"))+ theme_classic()
study3 = (dat_bind_primary[trainRows, -1]) %>%
  ggplot(aes(x = as.factor(study), y = lrecovery_time)) + geom_boxplot() + labs(x = "Study", y = "Log R)
cat_combined_plot3 = ggarrange(gender3, race3, smoking3, hypertension3,
                                       diabetes3, vaccine3, severity3, study3,
                                 ncol = 2, nrow = 4)
cat_combined_plot3
Log Recovery Timag Recovery Timag Recovery Tung Recovery T
                                                        Recovery .
   2
                                                           2
                                                           0
               Female
                                      Male
                                                                  White
                                                                             Asian
                                                                                         Black
                                                                                                   Hispanic
                                                        Recovery Tilcong Recovery Tilcong
                         Gender
                                                                                   Race
                                                           6
                                                           2
                          Former
           Never
                                         Current
                                                                                               Yes
           smoked
                          smoker
                                         smoker
                                                                         No
                    Smokoing Status
                                                                          Hypertension Status
                                                           0
                                                                         No
                                       Yes
                                                        Recovery Tilmag
                    Diabetes Status
                                                                           Vaccination Status
                                                           6
                                                           2
                                                                                                    Ċ
             Not severe
                                     Severe
                                                        Log –
                                                                      Α
                                                                                   Study
                         Severity
```

Considering variables based on the EDA

From the correlation plot, we can observe that bmi is highly correlated with weight and height, which makes sense because BMI is calculated by weight divided by the square of height. This demonstrates collinearity between the variables.

We believe that the study variable is more of a geographical indicator to distinguish different study sites, and it will not be critical in predicting recovery time. Therefore, we will remove the study variable.

Lastly, we will remove variables race and smoking since we have created dummy variables for them and we will use the dummy variables in further analyses.

```
race_2 = ifelse(race == 2, 1, 0),
    race_3 = ifelse(race == 3, 1, 0),
    race_4 = ifelse(race == 4, 1, 0),

# set up 2 dummy variables for `smoking`, reference = Never smoked:
    smoking_1 = ifelse(smoking == 1, 1, 0),
    smoking_2 = ifelse(smoking == 2, 1, 0))

# remove variables that will not be used

primary = primary %>%
    select(-study, -race, -smoking)

# partition again based on the new outcome variable
x <- model.matrix(lrecovery_time ~ ., primary)[trainRows,-1]
y <- primary$lrecovery_time[trainRows]

x2 <- model.matrix(lrecovery_time - ., primary)[-trainRows,-1]
y2 <- primary$lrecovery_time[-trainRows]

ctrl1 <- trainControl(method = "cv")</pre>
```

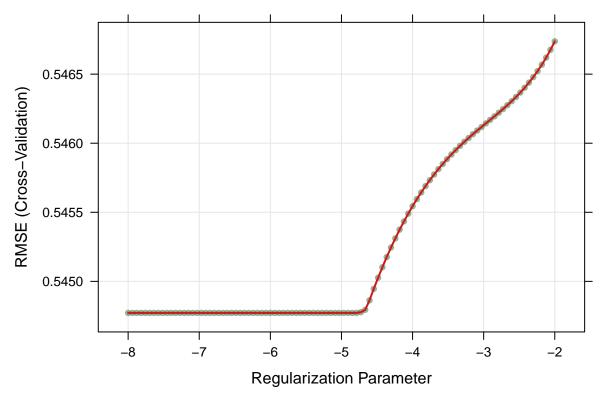
Primary analysis: continuous time to recovery

Model 1: Linear model

```
set.seed(2460)
lm.fit <- train(x, y,</pre>
             method = "glm",
             preProcess = c("center", "scale"),
             trControl = ctrl1)
summary(lm.fit)
##
## Call:
## NULL
## Deviance Residuals:
  Min 1Q Median 3Q
                                   Max
## -3.4481 -0.2424 0.0685 0.3126
                                 2.0007
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.601182 0.010003 360.010 < 2e-16 ***
             ## age
## gender
            ## height
            1.002011 0.103072 9.722 < 2e-16 ***
## weight
            -1.279007 0.129968 -9.841 < 2e-16 ***
         1.509986  0.144853  10.424  < 2e-16 ***
## bmi
## hypertension 0.036686 0.016726 2.193 0.02836 *
## diabetes -0.008605 0.010030 -0.858 0.39098
```

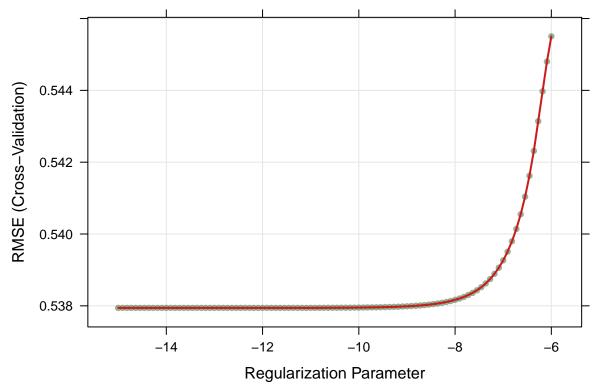
```
-0.001969 0.017667 -0.111 0.91125
-0.009753 0.010504 -0.929 0.35320
## SBP
## LDL
## vaccine
             -0.089295 0.010018 -8.914 < 2e-16 ***
              ## severity
               0.009397 0.010144 0.926 0.35432
## race_2
## race 3
              -0.006895 0.010253 -0.672 0.50134
## race_4 0.001614 0.010243 0.158 0.87481 ## smoking_1 0.046423 0.010264 4.523 6.35e-06 ***
## smoking_2 0.053878 0.010270 5.246 1.67e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for gaussian family taken to be 0.287973)
##
##
      Null deviance: 937.87 on 2877 degrees of freedom
## Residual deviance: 823.89 on 2861 degrees of freedom
## AIC: 4603.6
##
## Number of Fisher Scoring iterations: 2
coef(lm.fit$finalModel) %>% round(2) %>%
 as.matrix() %>% as.data.frame() %>% View()
```

Model 2: Ridge



```
coef(ridge.fit$finalModel, s = ridge.fit$bestTune$lambda) %>%
  round(2) %>%
  as.matrix() %>% as.data.frame() %>% View()
```

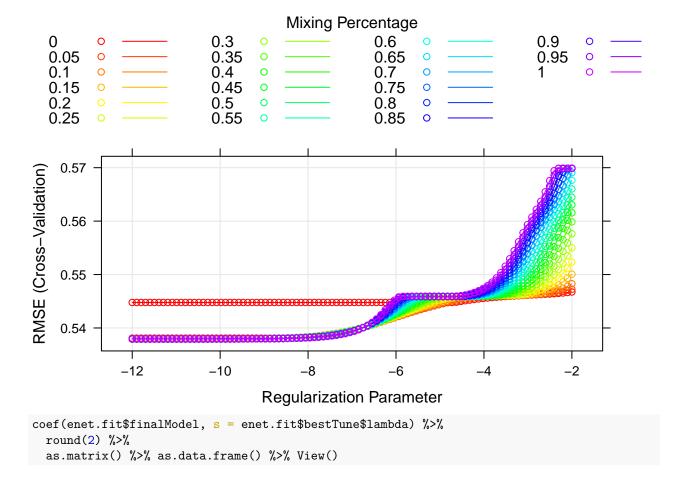
Model 3: Lasso



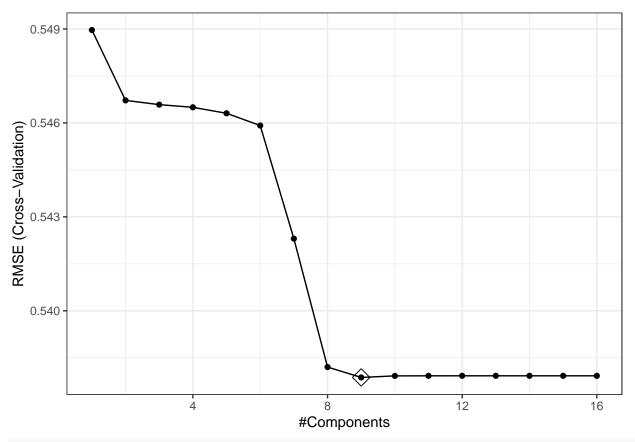
```
coef(lasso.fit$finalModel, s = lasso.fit$bestTune$lambda) %>%
  round(2) %>%
  as.matrix() %>% as.data.frame() %>% View()
```

Model 4: Elastic net

```
set.seed(2460)
enet.fit <- train(x, y,</pre>
                  method = "glmnet",
                   tuneGrid = expand.grid(alpha = seq(0, 1, length = 21),
                                           lambda = exp(seq(-12, -2,
                                                             length = 100))),
                   preProcess = c("center", "scale"),
                   trControl = ctrl1)
enet.fit$bestTune
        alpha
                     lambda
## 1808 0.9 1.246072e-05
myCol <- rainbow(25)</pre>
myPar <- list(superpose.symbol = list(col = myCol),</pre>
              superpose.line = list(col = myCol))
plot(enet.fit, par.settings = myPar, xTrans = log)
```



Model 5: Partial least square



summary(pls.fit)

```
X dimension: 2878 16
## Data:
## Y dimension: 2878 1
## Fit method: oscorespls
## Number of components considered: 9
## TRAINING: % variance explained
##
             1 comps 2 comps 3 comps 4 comps 5 comps 6 comps
                                                                  7 comps
## X
               9.942
                      19.262
                                30.232
                                         35.946
                                                  39.500
                                                           45.093
                                                                     49.15
               7.980
                        8.969
                                 9.033
                                          9.078
                                                            9.273
                                                                     10.31
## .outcome
                                                   9.185
            8 comps 9 comps
## X
               51.69
                        57.20
## .outcome
               12.06
                        12.15
coef(pls.fit$finalModel) %>% round(2) %>%
 as.matrix() %>% as.data.frame() %>% View()
```

Model 6: GAM

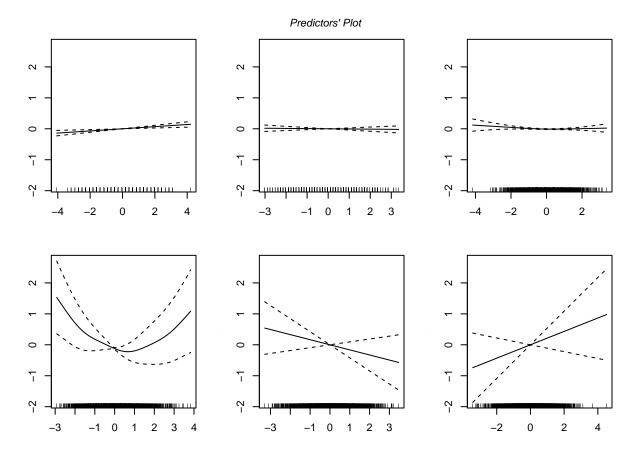
```
gam.fit$bestTune
    select method
## 1 FALSE GCV.Cp
gam.fit$finalModel
##
## Family: gaussian
## Link function: identity
##
## Formula:
## .outcome ~ gender + hypertension + diabetes + vaccine + severity +
##
      race_2 + race_3 + race_4 + smoking_1 + smoking_2 + s(age) +
##
      s(SBP) + s(LDL) + s(bmi) + s(height) + s(weight)
##
## Estimated degrees of freedom:
## 1.00 1.00 1.89 6.33 1.00 1.00 total = 23.22
## GCV score: 0.2698475
summary(gam.fit)
##
## Family: gaussian
## Link function: identity
## Formula:
## .outcome ~ gender + hypertension + diabetes + vaccine + severity +
      race_2 + race_3 + race_4 + smoking_1 + smoking_2 + s(age) +
      s(SBP) + s(LDL) + s(bmi) + s(height) + s(weight)
##
##
## Parametric coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
               ## (Intercept)
## gender
              -0.0596870  0.0096791  -6.167  7.96e-10 ***
## hypertension 0.0452988 0.0161533
                                    2.804 0.00508 **
## diabetes -0.0040637 0.0096880 -0.419 0.67491
## vaccine
             -0.0894786 0.0096702 -9.253 < 2e-16 ***
## severity
             0.0452155 0.0096825 4.670 3.15e-06 ***
## race_2
             0.0028659 0.0098071 0.292 0.77014
## race_3
             -0.0052124 0.0098904 -0.527 0.59822
             0.0002138 0.0098871 0.022 0.98275
## race_4
               ## smoking_1
               0.0572652  0.0099145  5.776  8.48e-09 ***
## smoking_2
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
##
             edf Ref.df
                            F p-value
## s(age)
           1.000 1.000 10.180 0.00143 **
## s(SBP)
          1.000 1.000 0.118 0.73090
## s(LDL)
           1.890 2.414 1.318 0.24710
           6.332 7.422 44.640 < 2e-16 ***
## s(bmi)
```

s(height) 1.000 1.000 1.631 0.20171

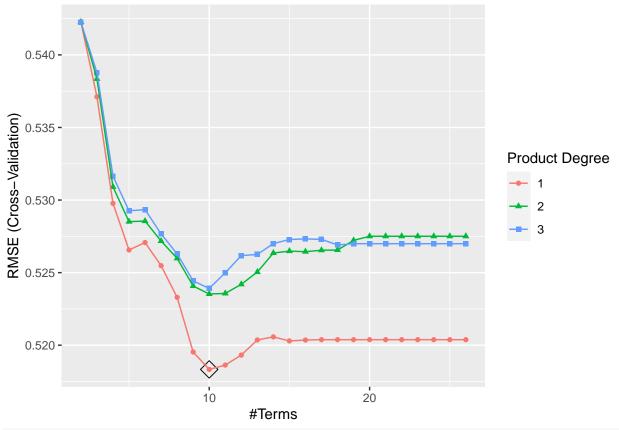
```
## s(weight) 1.000 1.000 1.752 0.18568
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) = 0.179 Deviance explained = 18.5%
## GCV = 0.26985 Scale est. = 0.26767 n = 2878
```

Plot continuous predictors in GAM

```
var.names <- c("age", "SBP", "LDL", "bmi", "height", "weight")</pre>
# make a matrix for easier comprehension of the plot with 16 predictors
matrix <- matrix(var.names, nrow = 2, ncol = 3, byrow = TRUE)</pre>
# use the matrix to correspond each plot with each predictor
print(matrix)
##
        [,1] [,2]
                      [,3]
## [1,] "age" "SBP"
                       "LDL"
## [2,] "bmi" "height" "weight"
gam.plot <- gam.fit$finalModel</pre>
# make 16 plots into one
par(mar = c(3, 3, 2, 2), mfrow = c(2, 3))
plot(gam.plot)
title(main = "Predictors' Plot", cex.main = 1, font.main = 3, outer = TRUE, line = -1)
```



Model 7: MARS



mars.fit\$bestTune

```
## nprune degree
## 9 10 1
summary(mars.fit)
```

GCV 0.2705204 RSS 768.3118

```
## Call: earth(x=matrix[2878,16], y=c(3.584,3.761,3...), keepxy=TRUE, degree=1,
##
               nprune=10)
##
##
                   coefficients
## (Intercept)
                     2.32744078
                    -0.06033598
## gender
## hypertension
                     0.03804629
## vaccine
                    -0.08929877
## severity
                     0.04637756
## smoking_1
                     0.04943934
## smoking_2
                     0.05566747
## h(age- -2.7261)
                     0.03261911
## h(bmi- -1.4908)
                     0.49599535
## h(0.638255-bmi)
                     0.53847499
##
## Selected 10 of 19 terms, and 8 of 16 predictors (nprune=10)
## Termination condition: RSq changed by less than 0.001 at 19 terms
```

Importance: bmi, vaccine, gender, hypertension, smoking_2, smoking_1, ...
Number of terms at each degree of interaction: 1 9 (additive model)

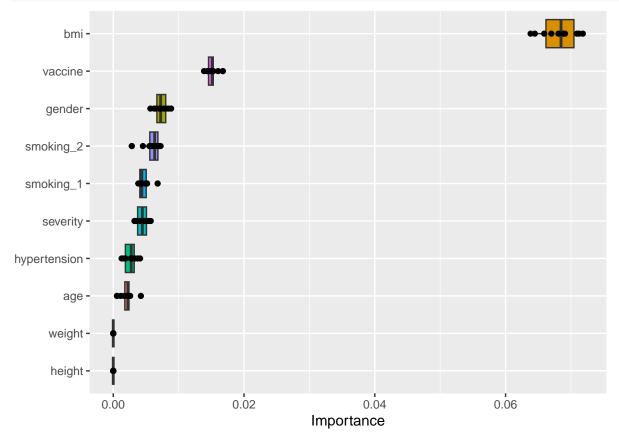
RSq 0.1807888

GRSq 0.170441

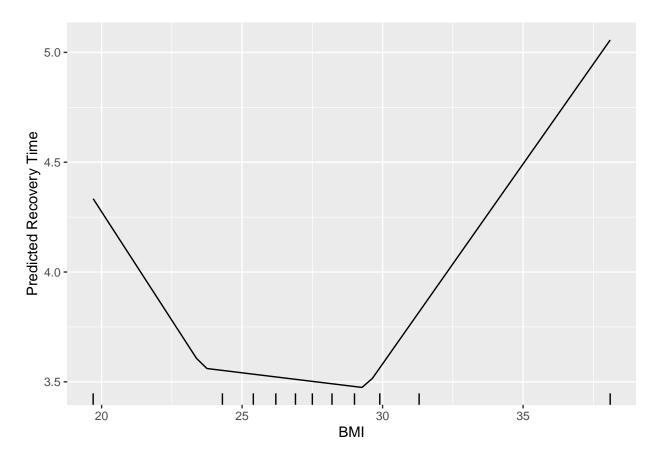
```
coef(mars.fit$finalModel) %>% round(2) %>%
as.matrix() %>% as.data.frame() %>% View()
```

Variable importance

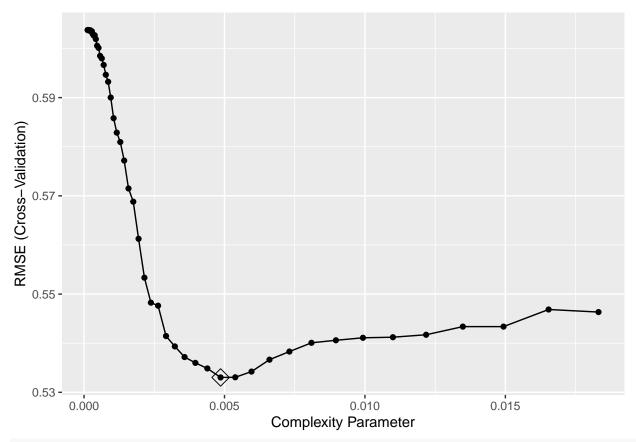
```
vip(mars.fit,
    method = "permute",
    train = primary[trainRows,],
    target = "lrecovery_time",
    metric = "RMSE",
    nsim = 10,
    pred_wrapper = predict,
    geom = "boxplot",
    all_permutations = TRUE,
    mapping = aes_string(fill = "Variable"))
```



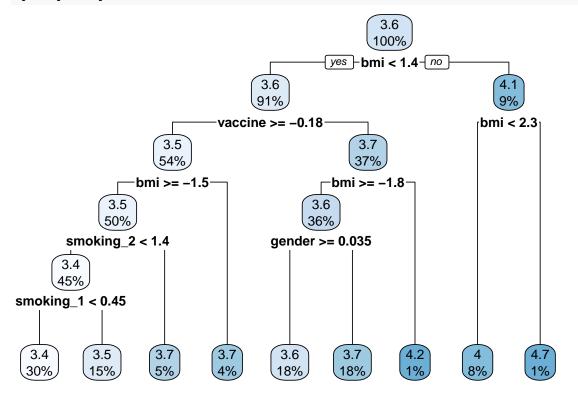
Partial dependence



Model 8: Regression tree



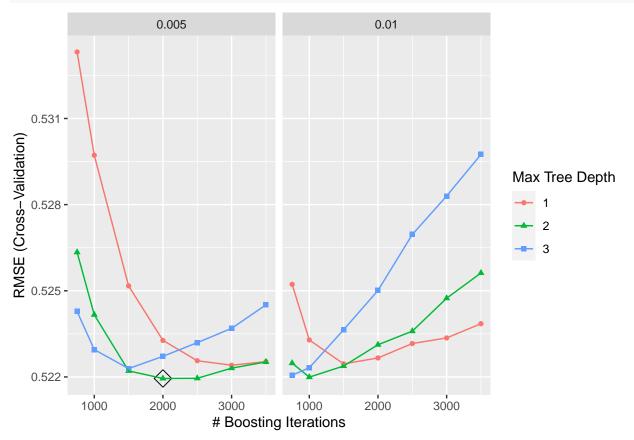
rpart.plot(rpart.fit\$finalModel)



Model 9: Random forest

```
rf.grid <- expand.grid(mtry = 1:16, #16 predictors</pre>
                         splitrule = "variance",
                         min.node.size = 1:6)
set.seed(2460)
rf.fit <- train(lrecovery_time ~ . ,</pre>
                 primary[trainRows,],
                 method = "ranger",
                 tuneGrid = rf.grid,
                 trControl = ctrl1,
                 preProcess = c("center", "scale"))
rf.fit$bestTune
     mtry splitrule min.node.size
         2 variance
ggplot(rf.fit, highlight = TRUE)
   0.545 -
RMSE (Cross-Validation)
                                                                           Minimal Node Size
                                                                               2
                                                                    16
                        #Randomly Selected Predictors
```

Model 10: Boosting

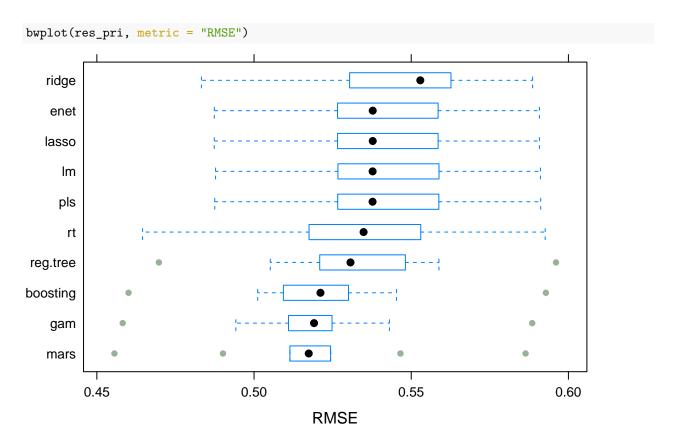


Model comparison

```
mars = mars.fit,
                          reg.tree = rpart.fit,
                          rt = rf.fit,
                          boosting = gbm.fit))
summary(res_pri)
##
## Call:
## summary.resamples(object = res_pri)
## Models: lm, ridge, lasso, enet, pls, gam, mars, reg.tree, rt, boosting
## Number of resamples: 10
##
## MAE
##
                 Min.
                        1st Qu.
                                   Median
                                                Mean
                                                       3rd Qu.
                                                                     Max. NA's
## lm
            0.3715813 0.3801875 0.3891606 0.3905957 0.3974587 0.4168473
## ridge
            0.3668470 0.3845314 0.3995422 0.3946062 0.4045918 0.4198322
            0.3711375 0.3801672 0.3895606 0.3905287 0.3973617 0.4166310
## lasso
            0.3711532 0.3801696 0.3895537 0.3905287 0.3973633 0.4166282
## enet
            0.3714900 0.3799257 0.3891460 0.3905299 0.3973980 0.4169598
## pls
## gam
            0.3563440 0.3714600 0.3789665 0.3798054 0.3835986 0.4138882
## mars
            0.3544547 0.3736366 0.3756004 0.3794879 0.3851627 0.4114350
                                                                             0
## reg.tree 0.3683618 0.3840758 0.3895214 0.3920198 0.3996331 0.4230047
            0.3574498 0.3787421 0.3839666 0.3858224 0.3931670 0.4154785
                                                                             0
## boosting 0.3547992 0.3734574 0.3788330 0.3804563 0.3846729 0.4107268
##
## RMSE
                        1st Qu.
                                   Median
##
                 Min.
                                                Mean
                                                       3rd Qu.
            0.4877568 0.5282710 0.5377199 0.5379234 0.5550979 0.5911010
## lm
            0.4832580 0.5336716 0.5528909 0.5447716 0.5625358 0.5886115
## ridge
            0.4873377 0.5284287 0.5377526 0.5379422 0.5549924 0.5907703
## lasso
## enet
            0.4873523 0.5284252 0.5377535 0.5379415 0.5549939 0.5907646
                                                                             0
            0.4874998 0.5282229 0.5377011 0.5378712 0.5551181 0.5911807
                                                                             0
## pls
## gam
            0.4582162 0.5116572 0.5190892 0.5195132 0.5244718 0.5884876
            0.4555906 0.5116768 0.5174001 0.5183330 0.5236598 0.5863775
## mars
## reg.tree 0.4697322 0.5212018 0.5306794 0.5330292 0.5481066 0.5960468
            0.4645553 \ 0.5195229 \ 0.5348479 \ 0.5312617 \ 0.5502635 \ 0.5926060
## boosting 0.4600815 0.5101843 0.5211270 0.5219467 0.5289549 0.5928327
##
## Rsquared
##
                  Min.
                          1st Qu.
                                       Median
                                                           3rd Qu.
                                                                         Max. NA's
                                                    Mean
## lm
            0.07232202 0.08974674 0.10383362 0.11176919 0.1148894 0.1869123
            0.04866936 0.07546233 0.09240669 0.08803606 0.1037300 0.1154734
## ridge
                                                                                 0
            0.07186500 0.09029708 0.10464976 0.11155582 0.1154413 0.1835720
## lasso
            0.07185371 0.09027505 0.10465331 0.11156003 0.1154374 0.1836312
                                                                                 0
## enet
## pls
            0.07234132 0.09032163 0.10396846 0.11191446 0.1156243 0.1867030
            0.10946228 0.11793949 0.17278765 0.17183125 0.2129779 0.2538031
                                                                                 0
## gam
            0.11528609 0.12615126 0.17235247 0.17567557 0.2128120 0.2518032
## mars
                                                                                 0
## reg.tree 0.05815617 0.08599073 0.12448333 0.13064566 0.1460979 0.2345080
                                                                                 0
            0.07965616 0.10426967 0.13226751 0.13957112 0.1801431 0.2003045
```

0

boosting 0.09382376 0.10886935 0.16338729 0.16429301 0.2016713 0.2678397



Select final model

Since MARS model has the lowest mean RMSE, we selected it as our final model.

Test error

```
mars.pred <- predict(mars.fit, newdata = x2)
mars.testerror = mean((mars.pred - y2)^2)
mars.testerror
## [1] 0.2915917</pre>
```

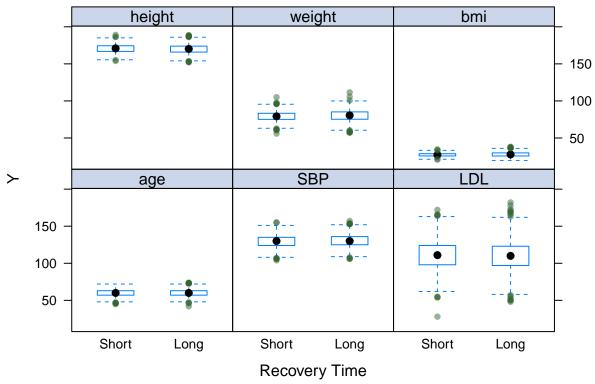
Secondary analysis: binary time to recovery

Set up

```
# lets check the distribution
binary = dat_bind_secondary %>%
  ggplot(aes(x = brecovery_time)) + geom_bar()
binary
  2500 -
  2000 -
  1500 -
count
  1000 -
   500 -
     0 -
                            Short
                                                                   Long
                                          brecovery_time
# partition again based on the new outcome variable
set.seed(2460)
trainRows_sec <- createDataPartition(y = dat_bind_secondary$brecovery_time, p = 0.8, list = FALSE)
ctrl2 <- trainControl(method = "cv",</pre>
                       summaryFunction = twoClassSummary,
                       classProbs = TRUE)
contrasts(dat_bind_secondary$brecovery_time)
##
         Long
## Short
            0
## Long
```

Understand the relationship between continuous predictors and the binary outcome

```
theme1 <- trellis.par.get()
theme1$plot.symbol$col <- rgb(.2, .4, .2, .5)
theme1$plot.symbol$pch <- 16</pre>
```



Understand the relationship between categorical predictors and the binary outcome

```
gender2 = (dat_bind_secondary[trainRows_sec, -1]) %>%
    ggplot(aes(x = brecovery_time, fill = as.factor(gender), group = as.factor(gender))) + geom_bar(posit
    scale_fill_discrete(labels = c("Female", "Male"))

race2 = (dat_bind_secondary[trainRows_sec, -1]) %>%
    ggplot(aes(x = brecovery_time, fill = as.factor(race), group = as.factor(race))) + geom_bar(position = scale_fill_discrete(labels = c("White", "Asian", "Black", "Hispanic"))

smoking2 = (dat_bind_secondary[trainRows_sec, -1]) %>%
    ggplot(aes(x = brecovery_time, fill = as.factor(smoking), group = as.factor(smoking))) + geom_bar(pos = scale_fill_discrete(labels = c("Never smoked", "Former Smoker", "Current smoker"))
```

```
hypertension2 = (dat_bind_secondary[trainRows_sec, -1]) %>%
     ggplot(aes(x = brecovery_time, fill = as.factor(hypertension), group = as.factor(hypertension))) + ge
     scale fill discrete(labels = c("No", "Yes"))
diabetes2 = (dat_bind_secondary[trainRows_sec, -1]) %>%
     ggplot(aes(x = brecovery_time, fill = as.factor(diabetes), group = as.factor(diabetes))) + geom_bar(p
     scale_fill_discrete(labels = c("No", "Yes"))
vaccine2 = (dat_bind_secondary[trainRows_sec, -1]) %>%
     ggplot(aes(x = brecovery_time, fill = as.factor(vaccine), group = as.factor(vaccine))) + geom_bar(pos
     scale_fill_discrete(labels = c("No", "Yes"))
severity2 = (dat_bind_secondary[trainRows_sec, -1]) %>%
     ggplot(aes(x = brecovery_time, fill = as.factor(severity), group = as.factor(severity))) + geom_bar(p
     scale_fill_discrete(labels = c("Not severe", "Severe"))
study2 = (dat_bind_secondary[trainRows_sec, -1]) %>%
     ggplot(aes(x = brecovery_time, fill = as.factor(study), group = as.factor(study))) + geom_bar(position)
cat_combined_plot2 = ggarrange(gender2, race2, smoking2, hypertension2,
                                                                         diabetes2, vaccine2, severity2, study2,
                                                             ncol = 2, nrow = 4)
cat_combined_plot2
                                                                           Gender
                                                                                                                                                                                             White
Ont 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 900 - 90
                                                                                                               1000 -
                                                                                     Female
                                                                                                                                                                                             Asian
                                                                                                                  500
                                                                                     Male
                                                                                                                                                                                             Black
           0 -
                                                                                                                       0
                         Short
                                                Long
                                                                                                                                   Short
                                                                                                                                                         Long
                                                                                                                                                                                            Hispanic
                                                                                                                                   Recovery Time
                         Recovery Time
                                                            Smoking Status
      1200 -
                                                                                                                                                                               Hypertension
                                                                                                                1000 -
        900 -
                                                                                                          Count
                                                                      Never smoked
                                                                                                                  750 -
        600 -
                                                                                                                                                                                         No
                                                                                                                  500 -
                                                                       Former Smoker
        300 -
                                                                                                                  250 -
                                                                                                                                                                                         Yes
             0 -
                                                                                                                       0 -
                                                                       Current smoker
                                                                                                                                  Short
                      Short
                                    Long
                                                                                                                                                      Long
                  Recovery Time
                                                                                                                                Recovery Time
                                                                                                                                                                                   Vaccination
                                                                               Diabetes
00 to 1000 - 1000 - 500 -
                                                                                                          Count
                                                                                                               900 -
                                                                                                               600 -
                                                                                                                                                                                             No
                                                                                         No
        500 -
                                                                                                               300 -
                                                                                          Yes
                                                                                                                                                                                              Yes
             0 -
                                                                                                                    0 .
                           Short
                                                                                                                                  Short
                                                    Long
                                                                                                                                                         Long
                            Recovery Time
                                                                                                                                  Recovery Time
                                                                                                                                                                                               Study
                                                                     Severity
O 1500 - 1000 - 500 -
                                                                                                               900 -
                                                                                                                                                                                                         Α
                                                                                                               600 -
                                                                               Not severe
                                                                                                               300 -
                                                                                                                                                                                                         В
                                                                               Severe
             0 -
                                                                                                                    0 -
                                                                                                                                                                                                         С
                         Short
                                             Long
                                                                                                                                     Short
                                                                                                                                                                  Long
                       Recovery Time
                                                                                                                                        Recovery Time
```

Make dummy variables

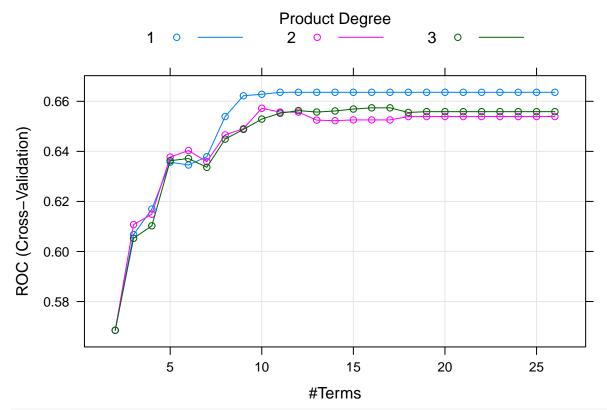
```
# dummy variable creation
secondary = dat_bind_secondary %>%
  mutate(
  # create dummy variables for categorical variables
    # set up 3 dummy variables for `race`, reference = White:
        race_2 = ifelse(race == 2, 1, 0),
         race_3 = ifelse(race == 3, 1, 0),
        race_4 = ifelse(race == 4, 1, 0),
    # set up 2 dummy variables for `smoking`, reference = Never smoked:
         smoking_1 = ifelse(smoking == 1, 1, 0),
         smoking_2 = ifelse(smoking == 2, 1, 0))
# remove variables that will not be used
secondary = secondary %>%
  dplyr::select(-study, -race, -smoking) %>%
 dplyr::select(brecovery_time, everything()) #arrange variable orders
```

Model 1: Logistic regression

```
set.seed(2460)
model.glm <- train(x = secondary[trainRows_sec,2:17],</pre>
             y = secondary$brecovery_time[trainRows_sec],
             method = "glm",
             metric = "ROC",
             trControl = ctrl2,
             preProcess = c("center", "scale"))
summary(model.glm)
##
## Call:
## NULL
##
## Deviance Residuals:
##
    Min 1Q Median
                        3Q
                              Max
## -2.2831 -1.2567 0.6816 0.8716
                            1.4994
##
## Coefficients:
           Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 0.926893 0.043431 21.342 < 2e-16 ***
## age
          ## gender
          ## height
## weight
          -2.740050 0.594517 -4.609 4.05e-06 ***
## bmi
           -0.014487 0.041995 -0.345 0.730121
## diabetes
## SBP
          0.051686 0.074248 0.696 0.486350
## LDL
          -0.084622 0.043824 -1.931 0.053489 .
         ## vaccine
```

```
## severity 0.199213 0.047007 7.102 ## race_2 -0.014534 0.042492 -0.342 0.732321 0.043042 -0.049 0.961097
              ## race_4
             -0.021811 0.042819 -0.509 0.610494
## smoking_1 0.174926 0.043862 3.988 6.66e-05 ***
## smoking_2 0.202077 0.047815 4.226 2.38e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 3506.9 on 2877 degrees of freedom
##
## Residual deviance: 3323.4 on 2861 degrees of freedom
## AIC: 3357.4
##
## Number of Fisher Scoring iterations: 4
```

Model 2: MARS



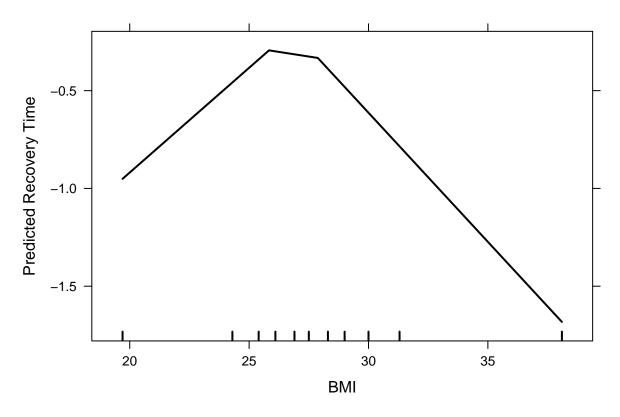
model.mars\$bestTune

nprune degree ## 10 11 1

coef(model.mars\$finalModel)

```
(Intercept) h(bmi- -0.320384) h(-0.320384-bmi)
##
                                                                    vaccine
##
          0.06779826
                            0.73070555
                                               0.59261712
                                                                -0.28696690
              gender h(age- -1.83762)
##
                                         h(-1.83762-age)
                                                                   severity
                            0.15362456
                                              -0.82201440
##
         -0.20048727
                                                                 0.19998994
##
           smoking_2
                             smoking_1 h(-0.675495-LDL)
          0.20415317
                            0.18700246
                                               0.27088201
```

Partial dependence



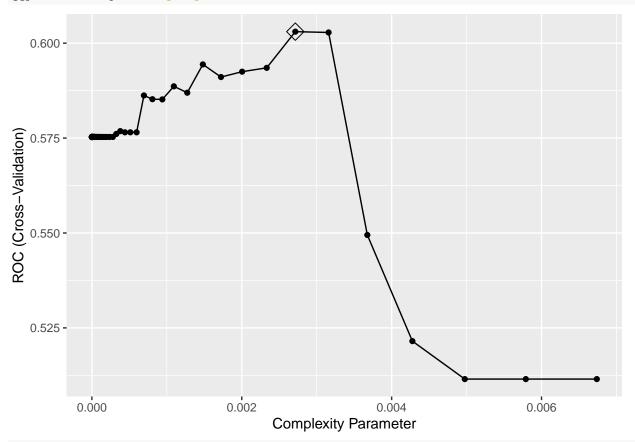
Model 3: LDA

```
##
                Length Class
                                   Mode
## prior
                 2
                       -none-
                                   numeric
## counts
                       -none-
                 2
                                   numeric
## means
                32
                       -none-
                                   numeric
## scaling
                16
                                   numeric
                       -none-
## lev
                 2
                       -none-
                                   character
## svd
                       -none-
                                   numeric
                 1
## N
                 1
                       -none-
                                   numeric
## call
                 3
                       -none-
                                   call
## xNames
                16
                       -none-
                                   character
## problemType
                 1
                       -none-
                                   character
## tuneValue
                       data.frame list
                 1
## obsLevels
                 2
                       -none-
                                   character
## param
                 0
                                   list
                       -none-
```

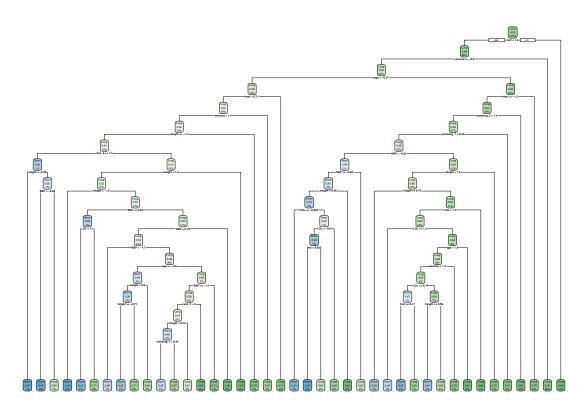
Model 4: Classification tree

cp ## 94 0.002714654

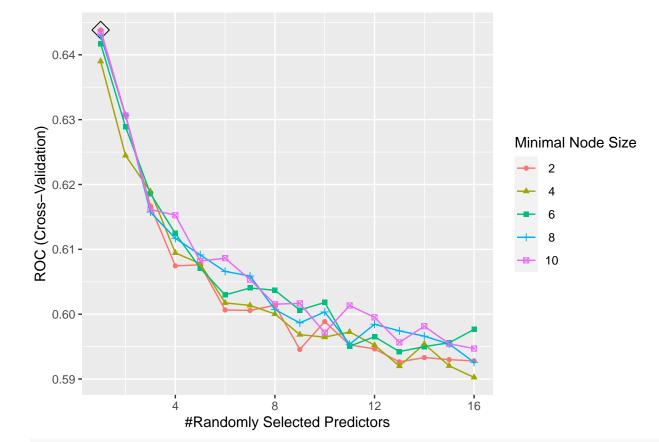
ggplot(model.rpart, highlight = TRUE)



rpart.plot(model.rpart\$finalModel)



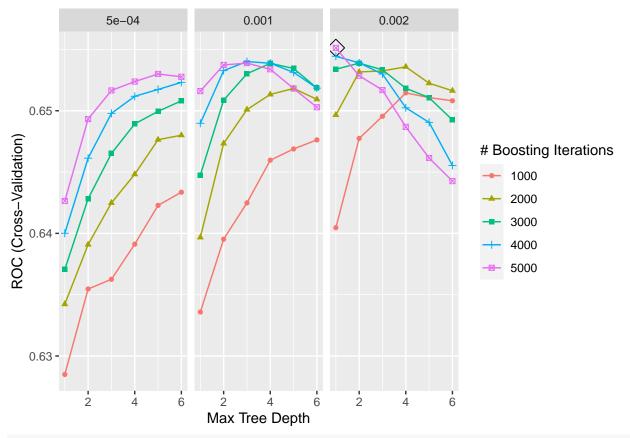
Model 5: Random forest



model.rf\$bestTune

```
## mtry splitrule min.node.size
## 1 1 gini 2
```

Model 6: Boosting



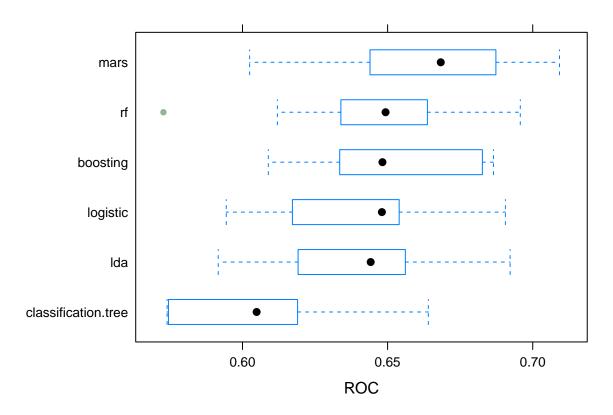
model.gbmA\$bestTune

```
## n.trees interaction.depth shrinkage n.minobsinnode ## 65 5000 1 0.002 1
```

Model comparison

```
##
## Call:
## summary.resamples(object = res_sec)
##
## Models: logistic, mars, lda, classification.tree, rf, boosting
## Number of resamples: 10
##
## ROC
                             Min.
                                    1st Qu.
                                               Median
                                                            Mean
                                                                   3rd Qu.
                       0.5944048\ 0.6244100\ 0.6480330\ 0.6437327\ 0.6534797\ 0.6905941
## logistic
## mars
                       0.6024637 0.6468383 0.6683168 0.6636018 0.6851687 0.7092312
```

```
0.5916417 0.6252159 0.6441691 0.6434160 0.6559550 0.6922058
## classification.tree 0.5740245 0.5764305 0.6048670 0.6030341 0.6173728 0.6640361
                     0.5727608 0.6340663 0.6492998 0.6438254 0.6623590 0.6957172
                      0.6089109 0.6359371 0.6482270 0.6551238 0.6825639 0.6864881
## boosting
                      NA's
## logistic
                         0
## mars
                         0
## lda
                         0
## classification.tree
                         0
                         0
## rf
## boosting
                         0
##
## Sens
                                                                     3rd Qu.
##
                            Min.
                                    1st Qu.
                                                Median
                                                             Mean
## logistic
                      0.03488372 0.04664843 0.06429549 0.07105335 0.08720930
## mars
                      0.06976744 0.08163475 0.09883721 0.12359781 0.15988372
## lda
                      0.03488372 0.04664843 0.05841313 0.06522572 0.07848837
## classification.tree 0.10465116 0.15697674 0.19186047 0.18777018 0.22093023
                      ## rf
                      0.00000000 0.01463748 0.02325581 0.02326949 0.03197674
## boosting
##
                            Max. NA's
## logistic
                      0.12790698
                                    0
## mars
                      0.21176471
                                    0
## lda
                      0.11627907
                                    0
## classification.tree 0.24705882
                      0.00000000
                                    0
## boosting
                      0.04651163
                                    0
##
## Spec
##
                           Min.
                                  1st Qu.
                                             Median
                                                        Mean
                                                                3rd Qu.
## logistic
                      0.9306931 0.9616337 0.9678218 0.9618812 0.9702970 0.9702970
## mars
                      0.9207921 0.9319307 0.9504950 0.9475248 0.9628713 0.9752475
                      0.9356436\ 0.9628713\ 0.9702970\ 0.9663366\ 0.9752475\ 0.9851485
## classification.tree 0.8613861 0.8873762 0.9059406 0.9014851 0.9195545 0.9257426
                      1.0000000 1.0000000 1.0000000 1.0000000 1.0000000
## boosting
                      0.9752475 0.9876238 0.9950495 0.9925743 0.9987624 1.0000000
##
                      NA's
## logistic
                         0
## mars
                         0
## lda
                         0
## classification.tree
                         0
## rf
                         0
## boosting
                         0
bwplot(res_sec, metric = "ROC")
```



Select final model

Since MARS model has the highest mean AUC ROC, we selected it as our final model.

```
Test error
pred.mars <- predict(model.mars, newdata = secondary[-trainRows_sec,])</pre>
confusionMatrix(data = pred.mars, reference = secondary$brecovery_time[-trainRows_sec],
                positive = "Long")
## Confusion Matrix and Statistics
##
##
             Reference
  Prediction Short Long
##
##
        Short
                 16
                       27
                198
                     477
##
        Long
##
##
                  Accuracy : 0.6866
##
                    95% CI: (0.6513, 0.7204)
##
       No Information Rate: 0.7019
##
       P-Value [Acc > NIR] : 0.8261
##
##
                     Kappa: 0.0275
##
    Mcnemar's Test P-Value : <2e-16
##
##
##
               Sensitivity: 0.94643
##
               Specificity: 0.07477
##
            Pos Pred Value: 0.70667
```

```
## Neg Pred Value : 0.37209
## Prevalence : 0.70195
## Detection Rate : 0.66435
## Detection Prevalence : 0.94011
## Balanced Accuracy : 0.51060
##
## 'Positive' Class : Long
##
```

The accuracy of the MARS model was 0.6866. The misclassification (test error) is calculated as 1 - 0.6866 = 0.3134.