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MACHINE LEARNING WS17/18
                                                                                                                                    (Exercise 3)
             Max Simon & Debora Fielberg
        1 LDA-Derivation from the LS Error
              decision boundary in LDA given by D-1 dans. hyperplane:
                                                                                                      (here w & x are column vectors!)
                decision rule: \hat{q} = sign(\hat{\omega}^T x + \hat{b}) = \begin{cases} 1 & \hat{\omega}^T x + \hat{b} > 0 \\ -1 & -1 & -\infty \end{cases}
                 traving place: N dangonts fxisien. N, x, ell given
plus & yisien. N 1 Yie }-1,15 labols
                (Ar) Assumption: balanced training set N_1 = N_{-1} = \frac{N}{2}
                  a, b = argnin & (wTx, +b-Y,)2
                a) compute 6 from 36 [(wTX; +6-4:)2=0
                         - 0 0 5 (wx:+6-4:) = 5 2 (wx:+6-4:) = 0
                                               \Rightarrow Nb = -\sum_{i=1}^{N} \omega^{T} x_{i} - y_{i}
                                               = \lambda \qquad = \qquad \sum_{i=1}^{N} y_i - \omega^T x_i
                 b) show that 2 = (wx:+6-4:)2=0 (sw+4s8) = (41-4-1)
                             Sx = (a-b)(a-b) between dass
                                                  Sw = 1 Z (xi - Myi) (x, -Myi) with-class
2 ε (ωτχ; +b-y;)2 = 0 ε εγ; =0 wagen *

βαιση (χ - εχ;) χ (ωτχ; + \( \frac{\pi}{2} \) χ (-ωτχ;) - γ;) = 0

[ (χ - εχ;) χ (ωτχ; + \( \frac{\pi}{2} \) χ (-ωτχ;) - γ;) = 0

ε αιτό ο ωνουρο ατό = \( \frac{\pi}{2} \) (ξχ; + ξχ;) = \( \frac{\pi}{2} \) ξχ;
        6) { (x, - arts ) (wix, - wi arts - y; ) = 0
                        = \[ \langle \left[ \langle \langle \frac{\chi at}{2} - \frac{\chi at}{2} - \frac{\chi xi bt}{2} - \frac{\chi xi t}{2} + \frac{\chi at}{4} + \frac{\chi at}{4} + \frac{\chi at}{4} + \frac{\chi at}{4} = \frac{\chi at}{2} \frac{\ch
        = 1 2x:x1 - x:aT - x:bT - ax1 - bx1 + qaT +abT +bqT +bbT b= a-b
                                                                              = Sw+ to SB = + E [x - N41)(x - M41) + 1 (00 - 60 - 00
               c) Show: $ = \( \tau \) (Swr4sB) $ = \( \tau \)
                                              ((Su = 1) w = a-b
                                     60 SWT-1 = SU + 4 SB
                                    a) t = sw pos. const
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