1 Introduction

1.1 Focal adhesion kinase

Focal adhesions (FA) are macromolecular protein complexes which act as a connection hub between the cell, i.e. the cytoskeleton, and the extracellular matrix (ECM). They enable the cell to performing tension forces, but can also trigger mechanical stimuli from the ECM. One important protein associated to FA is the focal adhesion kinase (FAK). FAK occurs in several signalling pathways and is a key player in integrating extracellular stimuli. It is of large interest not least because in cancer cells often an overexpression of FAK can be found and understanding the activation process of FAK could give rise to new cancer treatments [30].

1.1.1 Structure

FAK consists of four major domains (see **??**): a FERM domain as N-terminal, a tyrosine kinase, a proline rich region and a focal adhesion targeting (FAT) domain as C-terminal.

FERM (4.1 protein, ezrin, radixin and moesin) is a common protein domain, which targets proteins to membranes [8] and consists of three subdomains F1, F2 and F3. In the F2 subdomain there is the basic patch (^{216}KAKTLRK^{222}), which is a prominent binding site for phosphatidylinositol-4,5-bisphosphate (PI(4,5)P$_2$). This phospholipid is locally generated in FA due to integrin signaling [13].

The kinase domain of the C-lobe, the activation loop and the N-lobe. The catalytic activity of kinase is regulated by the phosphorylation of Y^{576} and Y^{577}, which are located in the activation loop [7]. The C-lobe also provides a binding site for PI(4,5)P$_2$ which is located next to the basic patch of the FERM domain [11].

The FERM domain and the kinase are connected by a linker region. Here the main autophosphorylation site Y^{397} can be found [13].

The FAT domain is linked to the kinase by a flexible proline rich region. FAT targets to FA by interacting with talin and paxillin, which are proteins associated with FA [2].

1.1.2 Activation

A maximum catalytic turnover requires Y^{576} and Y^{577} in the activation loop to be phosphorylated. In the inactive state this region is shielded by the FERM domain. Also the autophosphorylation site Y^{397} is isolated by the FERM domain. Therefore

an activation is only possible if the FERM domain dissociate at least partly from the kinase [20]. FAK triggers several stimuli, but in this thesis the main focus lies on the allosteric effect of PI(4,5)P$_2$ binding to the basic patch.

PI(4,5)P$_2$ is a has a net charge of -4, but in presence of K the deprotonated state gets promoted resulting in a net charge of -5. An electrostatic binding to the basic patch in the F2 subdomain results in long ranged configurational changes, which also influence the interface between the F1 subdomain and the N-lobe. Also the linker region gets less stronger bound so that an autophosphorylisation of Y^{397} is promoted. Phosphorylated Y^{397} is a suitable binding site for SH2, a subdomain of proteins from the Src kinase family. The presence of a kinase and the partial opening of the FERM kinase interface leads to a phosphorylisation of Y^{576} and Y^{577}. The resulting Src-FAK complex can act as an fully active kinase. In this state the FERM domain dissociates from the kinase [31, 13].

1.1.3 Dimerization and clustering

As explained above autophosphorylisation of Y^{397} is a crucial step for activation. It has been shown, that this autophosphorylisation occurs intermolecular, i.e. trans-phosphorylisation, in FAK dimers [28]. The main

This dimerisation can be found in several proteins containing a FERM domain. The interaction emerges around W^{266} and has an area of about 1350 Å^2. An additional interaction of the FAT domain and the FERM domain is required to stabilize the dimer [6]. Besides dimers larger clusters of FAK can emerge, which can contribute to additional signaling processes [18].

1.2 Molecular Dynamics simulations

Molecular dynamics (MD) simulations are an important tool to study biological systems on a microscopic scale. In the framework of MD simplifications are made, which enables simulations of several nanometres length scales for microseconds. Therefore MD is suitable for membranes, proteins and other biomolecules. Because in this thesis GROMACS (Groningen Machine for Chemical Simulations) [1, 3] was used as MD engine, the following part refers to GROMACS conventions and features.

1.2.1 The physics behind MD

In MD the system is simulated on an atomistic scale but with classical mechanics only. In order to do so atoms are only treated as spheres without distinction into electrons and nuclei. Quantum mechanical (QM) effects, such as excitation or electron transfer processes, are therefore not accessible and neglected in MD. However the atoms are parametrized by effective parameters, which can be motivated from QM [24, p. 127f].

Newtons equation of motion

$$\vec{F}_i = m_i \frac{\mathrm{d}^2 \vec{r}_i}{\mathrm{d}t^2} \tag{1.1}$$

where $\vec{F}_i$ is the force acting on particle i, m_i its mass and $\vec{r}_i$ its position, can be turned into two first-order differential equations

$$\frac{\mathrm{d}\vec{r}_i}{\mathrm{d}t} = \vec{v}_i \tag{1.2}$$

$$m_i \frac{\mathrm{d}\vec{v}_i}{\mathrm{d}t} = \vec{F}_i \tag{1.3}$$

They can be integrated numerically with e.g. Leapfrog- or Verlet integration scheme. Both are low order, i.e. the integration error is $\mathcal{O}(\Delta t^3)$, which saves computational cost. However they have the great advantage to be time reversible and symplectic. Later means, that it conserves the phase space volume, like the Hamiltonian operator would do as well. Therefore the long term error in energy conservation stays small [12, p. 72ff].

The force acting on particle i is given by the potential at its position.

$$\vec{F}_i = -\frac{\partial V}{\partial \vec{r}_i} \tag{1.4}$$

In MD bonded and non-bonded interactions contribute to the potential V, but it is also possible to apply external forces.

Bonded interactions

Bonded interactions act intra molecular and describe chemical bonds. They can occur between two, three or four particles.

An interaction between two bonded particles refers to their bond length. A deviation from the equilibrium bond length results in potential energy, which is usually described by an harmonic oscillator.

$$V_{\text{dist, bond }i} = \frac{k_{\text{dist}}}{2}(r - r_0)^2 \tag{1.5}$$

$k_{\text{dist,}}$ is the force constant and r_0 is the equilibrium bond length for the bond type of bond i. For larger deviations a Morse potential (exponential decaying potential for large deviations) is more precise, but has a much higher computational cost.

Also a deviation from an equilibrium angle between three bonded partners, i.e. the bond angle, results in potential energy. A common description is the harmonic oscillator as well.

$$V_{\text{angle}} = \frac{k_{\text{angle}}}{2}(\theta - \theta_0)^2 \tag{1.6}$$

The dihedral angle is the angle between two particles, which are separated by three bonds and can therefore be understood as the torsion angle of the intermediate two particles and bond. Besides a description of torsion this angle can also be used to preserve plane rings and the chirality of four particle groups. It is usually approximated with a periodic approach

$$V_{\text{dihedral, periodic}} = \frac{k_{\text{dihedral}}}{2}(1 + \cos(n\phi - \phi_0)) \tag{1.7}$$

where k_{dihedral} describes the energy barrier for turning the dihedral angle, n the number of minima in the energy function (multiplicity) and ϕ_0 a phase factor [1,

p. 71-83].

Non-bonded interactions

Non-bonded interactions are present between all atoms in the system and act pairwise. In MD Pauli repulsion, van der Waals (vdW) forces and electrostatic forces are taken into account. Because bonded interactions use effective parameters they are usually excluded from non-bonded interactions.

The Lennard-Jones potential combines Pauli repulsion (r^{-12} term) and the vdW force (r^{-6} term).

$$V_{\text{Lennard-Jones}} = \sum_{\text{non-bonded pairs i,j}} 4\epsilon \left(\left(\frac{\sigma}{r_{ij}} \right)^{12} - \left(\frac{\sigma}{r_{ij}} \right)^{6} \right) \tag{1.8}$$

ϵ is related to the potential depth and σ to the potential range.

The Coulomb potential is given by

$$V_{\text{Coulomb}} = \frac{q_1 q_2}{4\pi\epsilon_0\epsilon_r r} \tag{1.9}$$

where q_1, q_2 are the (partial) charges of the interacting particles, r their distance and ϵ_r the relative dielectric constant [1, p. 65-71].

In general non-bonded interactions act between all atoms in the system, which come along with a very large computational cost.
The easiest solution is to use a cut-off radius r_c. Particles behind this radius are not taken into account. This can be implemented very efficiently with Verlet neighbour lists. For each particle a neighbour list is created, which contains all particles inside a second radius r_v with $r_v > r_c$. For a force calculation only the distances to the particles, which are part of the list, have to be calculated. The lists are updated, if the maximal displacement in the system is larger than $r_v - r_c$. This method is suitable especially for Lennard-Jones potential, because of its rapid decay r_c can be chosen very small [24, p. 144].
The electrostatic potential is proportional to $1/r$, that is why the use of a cut-off radius would lead to large jumps in the potential. Long range interactions have to be considered, which can be effectively done with Particle Mesh Ewald (PME) summation [9]. Particle mesh methods in general split the electrostatic potential

up into a short range and a long range part via a switching function. The short range part can be calculated with a small cut-off radius in real space. The long range part however is calculated by solving the Poisson equation of the actual charge distribution, for which a discrete grid (mesh) is used. In PME this grid is transformed to Fourier space, where the solution of the Poisson equation is a sum over the gridpoints. This requires of course periodic boundary conditions (see section 1.2.3) [24, p. 246-251].

External forces

In addition to bonded and non-bonded interactions external or artificial forces can be applied, such as pulling forces, restrains and constrains.

With GROMACS it is possible to perform pulling forces onto groups of atoms in the system. In this thesis pulling was used to bias distances between groups. For this GROMACS provides an option to apply an umbrella potential to two groups which yields in a force, which is proportional to the deviation of the distance between the groups from a reference distance. The force can be applied on one or two spatial dimensions only or along a predefined vector and the reference distance can change during in time [1, p. 154-159].
Restrains are artificial potentials applied to positions, distances, angles, dihedral angles or orientations of particle groups to conserve labile configurations or to take additional information from experimental data into account [1, p. 84f].
Constrains are set to keep properties, such as bond lengths constant. In order to do so, they get reset to the desired value after each time step [1, p. 44f].

1.2.2 Forcefields

The parameters for the potentials described above are provided by force fields. There is a wide range of force fields, which are optimized for different application fields. In this thesis tow different ones, CHARMM36 and Martini, are introduced.

Force fields define specific atomtypes, which allow a mapping of atoms (particles in physical system) onto beads (particles used in the simulation). This mapping can take the environment of the particle (binding partners, solvents, nearby charges a.o.) into account, but can also neglect details by f.e. mapping several

atoms to one bead (coarse-graining).

Force fields not only define the atomtypes and their properties, but also all parameters for the calculation of the potential, especially force constants, equilibrium distances a.o. Therefore they define the physics of the system.

All-atom and the CHARMM36 force field

CHARMM (*Chemistry at HARvard Macromolecular Mechanics*) is a MD engine, which uses its own force fields. They are bunched together as CHARMM force fields and are provided for other MD engines as well. The number of the force field corresponds to the version number of CHARMM, in which the force field was used first. The force field CHARMM36 [5, 19] (C36) was published in 2010.

In C36 all atoms are considered (all-atom force field). Parameters were mainly optimized to structural experimental data, such as nuclear magnetic resonance (NMR) or X-ray data, but also QM and semi empirical QM calculations were used (e.g. for dihedral angles of the sidechains of proteins [5] and partial charges of lipids [19]).

All simulations for optimizing have been done with a time step of 2fs. Therefore very detailed dynamics are still included in the simulations.

There are several models for water, which can be used with all-atom force fields. They differ mainly in intermolecular interactions of water atoms. For simulations in this thesis the TIPS3P water model was used. It is a modification of the TIP3P water model [17] used in parametrisation of C36, which allows also Lennard-Jones-interactions on the hydrogens and not only on the oxygen [5].

Coarse graining and the Martini 2.2 force field

The Martini 2.2 [21, 16] force field was introduced in 2013 and is one of the most famous coarse graining force fields. It maps usually four heavy atoms onto a single bead (ring-like structures need a higher resolution), which implicates of course a loss of chemical information, but also an enormous reduction of computational cost. With this approach much larger time- and spatial scales are accessible for MD simulations.

The parametrisation in Martini is mainly based on fitting partitioning free energies of small molecules, such as amino acid side chain analogues, between a range of polar and non-polar solvents to results from all-atom simulations and experimental. For lipids also thermodynamic properties, such as area per lipid, have been considered. The parameters for membrane-protein interactions were optimized by fitting binding energies of small peptides and a membrane to experimental data and results from all-atom simulations data. In the simulations for optimization a time step of 20fs up to 30fs was used [16, 21].

Coarse graining brings a lot of side effects a long. First of all, the coarse graining is not unique, therefore important structural properties (e.g. the lipid tail length) are neglected. In proteins the simplifications also lead to problems, because the secondary structure become less stable in coarse grained models and has to be constrained by elastic networks (additional bonds between backbone beads) [22, p. 6812].
Further more coarse grained beads have a larger size, which leads a.o. to a smoothing of the energy profile. Because smaller local minima in the energy profile, which would slow down the evolving of the system, are smoothed out, coarse graining speeds up the dynamics in the system. The speed up factor is not constant, but can be relatively good approximated by factor four (obtained in most diffusion simulations) [22, p. 6810, 23, p. 7815].

Coarse graining also has an effect on the entropy and the temperature dependency of the system. In NpT ensembles the Gibbs free energy G is given by

$$G = H - TS \tag{1.10}$$

where S is the entropy and H the enthalpy. Due to a lower number of degrees of freedom in coarse grained systems the configurational entropy is reduced. Because Martini is tuned to free energy calculations, this implicates also a reduction of the enthalpy. Therefore a decomposition of G might not be realistic [22, p. 6811].

In Martini solvent beads represent four water molecules. Unfortunately the Martini water has a freezing temperature of up to 300 K and the freezing process is very sensitive to nucleation. To prevent this antifreeze beads were introduced, which have the same properties as the standard water beads except for a larger σ for the Lennard-Jones potential. By changing around 10% of the standard solvents to these antifreeze beads, the lattice conformation is disturbed and the freezing

temperature is increased [23, p. 7815].

The treatment of water as uncharged beads also implies, that the water phase is not polarizable in Martini. This problem is addressed by assuming a uniform relative dielectric constant, but at water phase interfaces the electrostatic interactions are systematically wrong and the interaction strength of polar beads is underestimated. To overcome this a polarizable water (PW) model was introduced to Martini. PW consists of three beads with equal mass. There is one positively charged bead and one negatively charged, both are bound to the central neutral bead. The charged beads acting only electrostatical with other charged beads, but not intramolecular. To control the distribution of the dipole momentum the binding angle between the three beads is constrained. The central bead interacts via the Lennard-Jones potential [29]. However PW comes with a higher computational cost and is not as well tested as the standard water model.

1.2.3 External constrains

Periodic boundary conditions

Because the simulation of an open system is not possible, boundary conditions have to be considered. Closed boundaries often lead to surface interaction artefacts and are therefore in most cases not suitable for MD simulation. That is why usually periodic boundary conditions (PBC) are used.

To use PBC the shape of the simulation box has to have a space filling geometry (e.g. rectangular or rhombic dodecahedron). With periodic boundary conditions images of the simulation box are repeated in every direction. If a particle leaves the simulation box, its periodic image is coming in from the opposite. So the number of particles is kept constant while surface interactions are avoided.

A particle interacts only with the nearest image of another particle, which means that particles near boundaries can interact with periodic images of other particles instead of the real particle. Nevertheless molecules can have long range interaction with their own periodic images, which leads to artefacts and has to be considered when choosing the systems size.

It is generally thought, that PBC only have small or no effects on equilibrium properties or structures of fluids, but known problems are the absence of long wavelength fluctuations (e.g. in phase transitions) or the violation of angular momentum conversation [24, p. 141f].

Thermostats

Integration schemes in MD are designed to conserve the energy of a system. This refers to a microcanonical ensemble, in which the number of particles N, the volume V and the energy E is constant (NVE). However in real biological systems not the energy but rather temperature is kept constant, which is the canonical ensemble (NVT). This can be achieved by thermostats. For the thermostats used in this thesis some characteristics are outlined below.

Berendsen thermostat The Berendsen thermostat [4] couples the system weakly to a heat bath with temperature T_0 by scaling the velocities of the particles. The temperature T, to which the system is set to, is given by

$$\frac{\mathrm{d}T}{\mathrm{d}t} = \frac{T_0 - T}{\tau_T} \tag{1.11}$$

Therefore an exponential relaxation can be observed. Weak coupling means, that the energy difference is not conducted in one rescaling, but over a given time scale τ_T, which allows a specification of the coupling strength.
It has been shown, that rescaling of velocities transfer kinetic energy from internal degrees of freedom, such as vibrations, to translational and rotational kinetic energy of the center of mass of the system [14, p. 738], which results in a wrong sampling of phase space. Therefore this thermostat is not suitable for production runs. Due to the exponential decay it adjusts quit fast, is stable against large deviations from the desired temperature and prevents oscillations. For these reasons it is often used in equilibration runs or non-equilibrium MD simulations [4, p. 3689].

Parinello-Bussi thermostat The Parrinello-Bussi thermostat [10] extends the Berendsen thermostat by a stochastic term, which leads to a more accurate sampling of phase space. The advantages of the Berendsen thermostat are still in place [1, p. 31].

Nosé-Hoover thermostat The Nosé-Hoover thermostat [25, 15] extends the Hamiltonian of the system by a friction representing a heat bath. The equations of motion are modified to

$$\frac{\mathrm{d}^2\vec{r}_i}{\mathrm{d}t^2} = \frac{\vec{F}_i}{m_i} - \frac{p_\xi}{Q(T_0, \tau_T)}\frac{\mathrm{d}\vec{r}_i}{\mathrm{d}t} \tag{1.12}$$

Here ξ represents the friction parameter with momentum p_ξ and a mass parameter $Q(T_0, \tau_T)$, which defines the coupling strength. Q depends on the target temperature T_0 and a coupling time scale τ_T. The evolution of ξ is defined as

$$\frac{\mathrm{d}p_\xi}{\mathrm{d}t} = T - T_0 \tag{1.13}$$

This leads to oscillations between the system and the heat bath with the period τ_T. The relaxation is about five times slower as by an exponential relaxation (see Berendsen or Parrinello–Bussi thermostats) with the same τ_T [1, p. 32f].

Often groups are coupled to independent thermostats. This is helpful, because the heat exchange between f.e. proteins and solvents is often not correct. Therefore proteins would cool down and the solvent would heat up [1, p. 34].

Barostats

In biological systems often not the volume but the pressure is constant. This refers to the isobaric isothermal ensemble (NpT). Below the characteristics of the barostats used in this thesis are outlined.

Berendsen barostat   Analogously to the Berendsen thermostat the Berendsen barostat [4] couples the systems pressure P weakly to an external pressure P_0 by rescaling the positions of the particles.

$$\frac{\mathrm{d}P}{\mathrm{d}t} = \frac{P_0 - T}{\tau_P} \tag{1.14}$$

τ_P is the time scale of coupling. Similar to the Berendsen thermostat this barostat does not sample the NpT ensemble and should therefore only be used in equilibration runs and non-equilibrium MD simulations [1, p. 36].

Parinello-Rahman barostat   In the Parinello-Rahman barostat [27, 26] the equations of motion of the particles change to

$$\frac{\mathrm{d}^2 \vec{r}_i}{\mathrm{d}t^2} = \frac{\vec{F}_i}{m_i} - \underline{M} \frac{\mathrm{d}\vec{r}_i}{\mathrm{d}t} \tag{1.15}$$

where $\underline{M}$ is a matrix is given by a differential equation depending on the current pressure, the target pressure, the volume and a time scale. The Parinello-Rahman barostat samples the full phase space and can be therefore used in production runs. Large deviations from the desired pressure however lead to oscillations in the box, therefore it should not be used for equilibration runs [1, p. 36].

GROMACS provides the possibility to couple the z-direction independently from the x- and y-direction, which is called semiisotropic pressure coupling. This feature is useful for membrane and pulling simulations, because the dynamics differ a lot between these axes.