Ex: 12.1 Using Eq. (12.2), we obtain

$$V_{ICM\,\mathrm{min}} = -V_{SS} + V_{tn} + V_{OV3} - |V_{tp}|$$

$$= -1.65 + 0.5 + 0.3 - 0.5$$

$$= -1.35 \text{ V}$$

Using Eq. (12.3), we get

$$V_{ICM \max} = V_{DD} - |V_{OV3}| - |V_{tp}| - |V_{OV1}|$$

$$= 1.65 - 0.3 - 0.5 - 0.3$$

$$= +0.55 \text{ V}$$

Thus,

$$-1.35~\mathrm{V} \leq \mathit{V_{ICM}} \leq +0.55~\mathrm{V}$$

Using Eq. (12.5), we obtain

$$-V_{SS} + V_{OV6} \le v_O \le V_{DD} - |V_{OV7}|$$

Thus

$$-1.65 + 0.5 \le v_O \le 1.65 - 0.5$$

$$\Rightarrow$$
 -1.15 V  $\leq v_O \leq$  +1.15 V

Ex: 12.2 For all devices, we have

$$|V_A| = 20 \text{ V}$$

Using Eq. (12.13), we get

$$A_1 = -\frac{2}{|V_{OV1}|} / \left[ \frac{1}{|V_{42}|} + \frac{1}{|V_{44}|} \right]$$

$$=-\frac{2}{0.2}/\frac{2}{20}=-100 \text{ V/V}$$

Using Eq. (12.20), we obtain

$$A_2 = -\frac{2}{|V_{OV6}|} / \left[ \frac{1}{V_{A6}} + \frac{1}{|V_{A7}|} \right]$$

$$=-\frac{2}{0.5}/\frac{2}{20}=-40 \text{ V/V}$$

$$A = A_1 A_2$$

$$= -100 \times -40 = 4000 \text{ V/V}$$

$$r_{o6} = r_{o7} = \frac{|V_A|}{0.5 \text{ mA}} = \frac{20}{0.5} = 40 \text{ k}\Omega$$

$$R_o = r_{o6} \parallel r_{o7} = 40 \parallel 40 = 20 \text{ k}\Omega$$

Ex: 12.3 The feedback is of the voltage sampling type (i.e., the connection at the output is a shunt one), thus

$$R_{\text{out}} = R_{of} = \frac{R_o}{1 + A\beta}$$

where

$$R_o = r_{o6} \parallel r_{o7}$$

$$A = g_{m1}(r_{o2} \parallel r_{o4})g_{m6}(r_{o6} \parallel r_{o7})$$

$$\beta = 1$$

Thus,

$$R_{\text{out}} = \frac{r_{o6} \parallel r_{o7}}{1 + g_{m1}(r_{o2} \parallel r_{o4})g_{m6}(r_{o6} \parallel r_{o7})}$$

Usually,

$$A \gg 1$$

Thus,

$$R_{\text{out}} \simeq \frac{1}{g_{m6}[g_{m1}(r_{o2} \parallel r_{o4})]}$$

Ex: 12.4 Using Eq. (12.36), we get

$$f_t = \frac{G_{m1}}{2\pi C_C}$$

$$\Rightarrow C_C = \frac{G_{m1}}{2\pi f_c}$$

$$= \frac{0.3 \times 10^{-3}}{2\pi \times 10 \times 10^{6}}$$

$$= 4.8 \text{ pF}$$

From Eq. (12.31), we have

$$f_Z = \frac{G_{m2}}{2\pi C_C}$$

$$= \frac{0.6 \times 10^{-3}}{2\pi \times 4.8 \times 10^{-12}}$$

$$\simeq 20 \; MHz$$

From Eq. (12.35), we have

$$f_{P2} = \frac{G_{m2}}{2\pi C_2}$$

$$= \frac{0.6 \times 10^{-3}}{2\pi \times 2 \times 10^{-12}} = 48 \text{ MHz}$$

Thus,  $f_t$  is lower than  $f_Z$  and  $f_{P2}$ .

Ex: 12.5 (a) Using Eq. (12.36), we have

$$f_t = \frac{G_{m1}}{2\pi C_C}$$

$$\Rightarrow C_C = \frac{G_{m1}}{2\pi f_*}$$

$$= \frac{1 \times 10^{-3}}{2\pi \times 100 \times 10^6}$$

$$= 1.6 \, pF$$

$$A_0 = G_{m1}(r_{o2} \parallel r_{o4})G_{m2}(r_{o6} \parallel r_{o7})$$

$$= 1(100 \parallel 100) \times 2(40 \parallel 40)$$

$$= 50 \times 2 \times 20 = 2000 \text{ V/V}$$

$$f_{3dB} = \frac{f_t}{A_0} = \frac{100 \times 10^6}{2000} = 50 \text{ kHz}$$

$$R = \frac{1}{G_{m2}} = \frac{1}{2 \times 10^{-3}} = 500 \ \Omega$$

(c) From Eq. (12.35), we have

$$f_{P2} = \frac{G_{m2}}{2\pi C_2}$$
  
=  $\frac{2 \times 10^{-3}}{2\pi \times 1 \times 10^{-12}} = 318 \text{ MHz}$ 

$$\phi_{P2} = -\tan^{-1}\frac{f_t}{f_{P2}}$$

$$= -tan^{-1} \; \frac{100}{318}$$

$$= -17.4^{\circ}$$

$$PM = 90 - 17.4 = 72.6^{\circ}$$

Ex: 12.6 Using Eq. (12.47), we obtain

$$SR = V_{OV1}\omega_t$$

$$=0.2\times2\pi\times100\times10^6$$

$$= 126 \text{ V/}\mu\text{s}$$

Using Eq. (12.45),

$$SR = \frac{I}{C_C}$$

$$\Rightarrow I = 126 \times 10^6 \times 1.6 \times 10^{-12}$$

$$= 200 \mu A$$

$$R_B = \frac{2}{\sqrt{2\mu_n C_{ox}(W/L)_{12}I_{REF}}} \left( \sqrt{\frac{(W/L)_{12}}{(W/L)_{13}}} - 1 \right)$$

$$= \frac{2}{\sqrt{2 \times 90 \times 10^{-6} \times 80 \times 10 \times 10^{-6}}} \left( \sqrt{\frac{80}{20}} - 1 \right)$$

$$= 5.27 \text{ k}\Omega$$

Using Eq. (12.61), we obtain

$$g_{m12} = \frac{2}{R_B} \left( \sqrt{\frac{(W/L)_{12}}{(W/L)_{13}}} - 1 \right)$$

$$=\frac{2}{5.27}\left(\sqrt{\frac{80}{20}}-1\right)$$

$$= 0.379 \text{ mA/V}$$

Ex: 12.8 From Example 8.6,  $Q_8$  has

$$\left(\frac{W}{L}\right)_8 = \frac{40}{0.8}$$

$$g_{m8} = 0.6 \text{ mA/V}$$

$$g_{m13} = g_{m8} = 0.6 \text{ mA/V}$$

$$g_{m12} = \sqrt{2\mu_n C_{ox}(W/L)_{12} I_{\text{REF}}}$$

$$= \sqrt{2\mu_n C_{ox} \times 4(W/L)_{13} I_{REF}}$$

$$= 2g_{m13} = 1.2 \text{ mA/V}$$

Now,

$$R_B = \frac{2}{\sqrt{2\mu_n C_{ox}(W/L)_{12} I_{REF}}} \left( \sqrt{\frac{(W/L)_{12}}{(W/L)_{13}}} - 1 \right)$$

$$=\frac{2}{1.2\times10^{-3}}(\sqrt{4}-1)$$

$$= 1.67 \text{ k}\Omega$$

From Example 8.6, we have

$$V_{DD} = V_{SS} = 2.5 \text{ V}$$

$$I_{REF} = 90 \,\mu\text{A}$$

$$V_{tn} = 0.7 \text{ V}$$

$$|V_{tp}| = 0.8 \text{ V}$$

$$|V_{OV8}| = 0.3 \text{ V}$$

$$I_{\text{REF}}R_B = 0.09 \times 1.67$$

$$= 150 \text{ mV}$$

Since

$$g_{m13} = \frac{2I_{\text{REF}}}{V_{OV13}}$$

$$0.6 = \frac{2 \times 0.09}{V_{OV13}}$$

$$\Rightarrow V_{OV13} = 0.3 \text{ V}$$

$$V_{GS13} = 0.3 + 0.7 = 1 \text{ V}$$

$$V_{G13} = -V_{SS} + V_{GS13}$$

$$= -2.5 + 1 = -1.5 \text{ V}$$

$$V_{GS11} = V_{GS13} = 1 \text{ V}$$

$$V_{G11} = V_{G13} + V_{GS11}$$

$$= -1.5 + 1 = -0.5 \text{ V}$$

$$V_{SG8} = |V_{tp}| + |V_{OV8}|$$

$$= 0.8 + 0.3 = 1.1 \text{ V}$$

$$V_{G8} = V_{DD} - V_{SG8}$$

$$= 2.5 - 1.1 = +1.4 \text{ V}$$

Ex: 12.9 Total bias current =  $300 \mu A = 2I_B$ 

$$\Rightarrow I_B = 150 \,\mu\text{A}$$

$$I_B = I_{D1} + I_{D3}$$

$$150 = I_{D1} + 0.25I_{D1}$$

$$\Rightarrow I_{D1} = 120 \,\mu\text{A}$$

$$I = I_{D1} + I_{D2}$$
  
= 120 + 120 = 240  $\mu$ A  
 $I_{D3,4} = 0.25I_{D1,2} = 0.25 \times 120$   
= 30  $\mu$ A

Ex: 12.10 Using Eq. (12.64), we get

$$V_{ICM \text{ max}} = V_{DD} - |V_{OV9}| + V_{tn}$$
  
= 1.65 - 0.3 + 0.5 = +1.85 V

Using Eq. (12.65), we obtain

$$V_{ICM \min} = -V_{SS} + V_{OV11} + V_{OV1} + V_{Im}$$
$$V_{ICM \min} = -1.65 + 0.3 + 0.3 + 0.5$$

$$= -0.55 \text{ V}$$

Thus,

$$-0.55 \text{ V} \le V_{ICM} \le +1.85 \text{ V}$$

Using Eq. (12.68), we get

$$V_{Omax} = V_{DD} - |V_{OV10}| - |V_{OV4}|$$
  
= 1.65 - 0.3 - 0.3 = +1.05 V

Using Eq. (12.69), we obtain

$$V_{Omin} = -V_{SS} + V_{OV7} + V_{OV5} + V_{th}$$
$$= -1.65 + 0.3 + 0.3 + 0.5$$
$$= -0.55 \text{ V}$$

Thus,

$$-0.55 \text{ V} \le v_O \le +1.05 \text{ V}$$

Ex: 12.11 
$$G_m = g_{m1} = g_{m2}$$
  
 $G_m = \frac{2(I/2)}{V_{OV1}} = \frac{I}{V_{OV1}}$   
 $= \frac{0.24}{0.2} = 1.2 \text{ mA/V}$   
 $r_{o2} = \frac{|V_A|}{I/2} = \frac{20}{0.12} = 166.7 \text{ k}\Omega$   
 $r_{o4} = \frac{|V_A|}{I_{D4}} = \frac{|V_A|}{I_B - \frac{I}{2}} = \frac{20}{0.150 - 0.120}$ 

$$= \frac{20}{0.03} = 666.7 \text{ k}\Omega$$

$$r_{o10} = \frac{|V_A|}{I_B}$$
  
=  $\frac{20}{0.15} = 133.3 \text{ k}\Omega$ 

$$g_{m4} = \frac{2I_{D4}}{|V_{OV}|} = \frac{2 \times 0.03}{0.2} = 0.3 \text{ mA/V}$$

$$R_{o4} = (g_{m4}r_{o4})(r_{o2} \parallel r_{o10})$$

$$= (0.3 \times 666.7)(166.7 \parallel 133.3)$$

$$= 14.8 \text{ M}\Omega$$

$$g_{m6} = \frac{2I_{D6}}{V_{OV}} = \frac{2 \times 0.03}{0.2} = 0.3 \text{ mA/V}$$

$$r_{o6} = r_{o8} = \frac{|V_A|}{I_{D6,8}} = \frac{20}{0.03} = 666.7 \text{ k}\Omega$$

$$R_{o6} = g_{m6}r_{o6}r_{o8}$$

$$= 0.3 \times 666.7 \times 666.7 = 133.3 \text{ M}\Omega$$

$$R_o = R_{o4} \parallel R_{o6}$$

$$= 14.8 \parallel 133.3 = 13.3 \text{ M}\Omega$$

$$A_v = G_m R_o = 1.2 \times 13.3 \times 10^3 = 16,000 \text{ V/V}$$

Ex: 12.12 (a) The NMOS input stage operates over the following input common-mode range:

$$-V_{SS} + 2V_{OV} + V_m \le V_{ICM} \le V_{DD} - |V_{OV}| + V_m$$
  
that is,

$$(-2.5 + 0.6 + 0.7) \le V_{ICM} \le (2.5 - 0.3 + 0.7)$$
  
-1.2 V \le V<sub>ICM</sub> \le +2.9 V

(b) The PMOS input stage operates over the following input common-mode range:

$$-V_{SS} + V_{OV} - |V_{tp}| \le V_{ICM} \le V_{DD} - 2|V_{OV}| - |V_{tp}|$$
  
that is,

$$(-2.5 + 0.3 - 0.7) \le V_{ICM} \le (2.5 - 0.6 - 0.7)$$
  
-2.9 V <  $V_{ICM} < +1.2$  V

(c) The overlap range is

$$-1.2 \text{ V} \le V_{ICM} \le +1.2 \text{ V}$$

(d) The input common-mode range is

$$-2.9 \text{ V} \le V_{ICM} \le +2.9 \text{ V}$$

**Ex: 12.13** Denote the (W/L) of the transistors in the wide-swing mirror by  $(W/L)_M$ . Transistor  $Q_4$  has

$$(W/L)_5 = \frac{1}{4}(W/L)_M$$

$$I_{REF} = \frac{1}{2}\mu_n C_{ox} \left(\frac{W}{L}\right)_5 V_{OV5}^2$$

$$= \frac{1}{2}\mu_n C_{ox} \left(\frac{W}{L}\right)_M \times \frac{1}{4} V_{OV5}^2$$

$$= \frac{1}{2}\mu_n C_{ox} \left(\frac{W}{L}\right)_M (V_{OV5}/2)^2$$
Thus,
$$\frac{V_{OV5}}{2} = V_{OV}$$

where  $V_{OV}$  is the overdrive voltage for each of the mirror transistors. Thus,

$$V_5 = V_{tn} + 2V_{OV}$$

which is the value of  $V_{\text{BIAS}}$  needed in the circuit of Fig. 12.13(b).

**Ex: 12.14** At  $I_C = 0.1$  mA,

$$V_{BE} = 25 \ln \frac{0.1 \times 10^{-3}}{10^{-14}}$$

$$= 575.6 \text{ V}$$

$$g_m = \frac{I_C}{V_T} = \frac{0.1 \text{ mA}}{0.025 \text{ V}} = 4 \text{ mA/V}$$

$$r_e \simeq \frac{1}{g_m} = 250 \ \Omega$$

$$r_{\pi} = \frac{\beta}{g_{m}} = \frac{200}{4} = 50 \text{ k}\Omega$$

$$r_o = \frac{V_A}{I_C} = \frac{125 \text{ V}}{0.1 \text{ mA}} = 1.25 \text{ M}\Omega$$

Ex: 12.15 
$$V_T \ln \frac{I_{REF}}{I_{C10}} = I_{C10}R_4$$

$$25 \ln \frac{730}{I_{C10}} = 5I_{C10} \tag{1}$$

where  $I_{C10}$  is in  $\mu$ A, and both sides of Eq. (1) are in mV. Using iteration:

<i>I<sub>C</sub></i> (μ <b>A</b> )	LHS of Eq. (1) (mV)	RHS of Eq. (1) (mV)
100	49.5	500
50	67	250
20	89.9	100
19	91.2	95
18	92.6	90

Thus,

$$I_{C10} \simeq 19 \, \mu A$$

Ex: 12.16 Refer to Fig. 12.15. At node X,

$$I_{C10} = \frac{2I}{1 + \frac{2}{\beta_P}} + \frac{2I}{\beta_P}$$

$$I_{C10} = 2I \left[ \frac{\beta_P + 1 + \frac{2}{\beta_P}}{\beta_P \left( 1 + \frac{2}{\beta_P} \right)} \right]$$

$$\simeq 2I \frac{\beta_P + 1}{\beta_P + 2}$$

Thus,

$$I = \frac{I_{C10}}{2} = 9.5 \,\mu\text{A}$$

resulting in

$$I_{C1} = I_{C2} = I_{C3} = I_{C4} = 9.5 \,\mu\text{A}$$

Ex: 12.17 Figure 1 on next page shows the determination of the loop gain of the feedback circuit that stabilizes the bias currents of the first stage of the 741 op amp. Note that since  $I_{C10}$  is assumed to be constant, we have shown its incremental value at node X to be zero. Observe that this circuit shows only incremental quantities. The analysis shown provides the returned current signal as

$$I_r = -I_t \frac{\beta_P}{1 + \frac{2}{\beta_P}}$$

For  $\beta_P \gg 1$ , we have

$$I_r \simeq -\beta_P I_t$$

and the loop gain  $A\beta$  is

$$A\beta \equiv -\frac{I_r}{I_t} = \beta_P$$

**Ex: 12.18** 
$$V_{BE6} = V_T \ln \frac{I_{C6}}{I_S}$$

$$=25 \ln \frac{9.5 \times 10^{-6}}{10^{-14}} = 517 \text{ mV}$$

$$V_{R3} = V_{BE6} + IR_2$$

$$= 517 + 9.5 \times 10^{-6} \times 1 = 526.5 \text{ mV}$$

$$I_{C7}\simeq I_{E7}\simeq rac{V_{R3}}{R_3}$$

$$=\frac{526.5}{50}=10.5~\mu\text{A}$$

**Ex: 12.19** 
$$I_B = \frac{1}{2}(I_{B1} + I_{B2})$$

$$=\frac{1}{2}\left(\frac{I}{\beta_N+1}+\frac{I}{\beta_N+1}\right)$$

$$=\frac{I}{\beta_N+1}\simeq\frac{I}{\beta_N}$$

$$=\frac{9.5}{200}=47.5 \text{ nA}$$

$$I_{OS} = 0.1 \times I_B = 4.75 \text{ nA}$$

#### Ex: 12.20

$$V_{C1} = V_{CC} - V_{EB8} = 15 - 0.6 = 14.4 \text{ V}$$

 $Q_1$  and  $Q_2$  saturate when  $V_{ICM}$  exceeds  $V_{C1}$  by 0.3 V. Thus,

$$V_{ICM \, \text{max}} = +14.7 \, \text{V}$$

This figure belongs to Exercise 12.17.

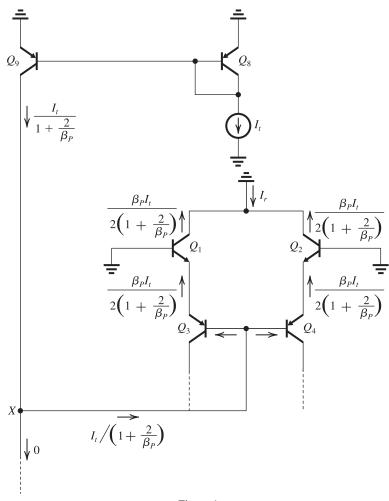


Figure 1

$$V_{C5} \simeq -V_{EE} + V_{BE5} + V_{BE7}$$

$$= -15 + 0.6 + 0.6 = -13.8 \text{ V}$$

$$Q_{3} \text{ (and } Q_{4} \text{) saturate when}$$

$$V_{B3} = V_{C5} - 0.3$$

$$= -13.8 - 0.3 = -14.1 \text{ V}$$
But,
$$V_{B3} = V_{ICM} - V_{BE1} - V_{EB3}$$

$$= V_{ICM} - 1.2 \text{ V}$$
Thus,
$$V_{ICM \min} = V_{B3} + 1.2 \text{ V}$$

$$= -14.1 + 1.2 = -12.9 \text{ V}$$
Thus,
$$I_{C17} = I_{C13B} = 550 \text{ μA}$$

$$V_{BE17} = V_{T} \ln \frac{I_{C17}}{I_{S}}$$

$$= 25 \ln \frac{550 \times 10^{-6}}{10^{-14}}$$

$$= 618 \text{ mV}$$

$$V_{R9} = V_{BE17} + I_{E17}R_{8}$$

$$\simeq 618 + 550 \times 0.1$$

$$= 673 \text{ mV}$$
Thus,
$$I_{R9} = \frac{673}{50} = 13.46 \text{ μA}$$

$$I_{B17} = \frac{550}{201} = 2.74 \,\mu\text{A}$$

$$I_{E16} = I_{R9} + I_{B17} = 16.30 \,\mu\text{A}$$

$$I_{C16} = \frac{200}{201} \times 16.3 = 16.2 \,\mu\text{A}$$

$$I_{B16} = \frac{16.2}{200} = 0.08 \,\mu\text{A}$$

Ex: 12.22 The two diode-connected transistors will carry a bias current of  $0.25I_{REF} = 180 \mu A$ . Since the output transistors have three times the values of  $I_S$  as that of the diode-connected transistors, the bias current in the output transistors will be

$$= 3 \times 180 = 540 \,\mu\text{A}$$

Ex: 12.23 
$$r_e = \frac{V_T}{I_E} \simeq \frac{25 \text{ mV}}{9.5 \text{ } \mu\text{A}} = 2.63 \text{ k}\Omega$$

$$g_{m1} \simeq \frac{1}{r_e} = 0.38 \text{ mA/V}$$

$$G_{m1} = \frac{1}{2}g_{m1} = 0.19 \text{ mA/V}$$

$$R_{id} = (\beta_N + 1) \times 4r_e$$

$$= 201 \times 4 \times 2.63$$

$$= 2.1 \text{ M}\Omega$$

Ex: 12.24 refer to Fig. 12.19.

(a) 
$$v_{b6} = i_{e6}(r_{e6} + R_2)$$
  
=  $i_e(r_{e6} + R_2)$ 

$$r_{e6} = \frac{V_T}{I_{E6}} \simeq \frac{25 \text{ mV}}{9.5 \text{ } \mu\text{A}} = 2.63 \text{ k}\Omega$$

$$v_{b6} = i_e(2.63 + 1) = 3.63 \text{ k}\Omega \times i_e$$

(b) 
$$i_{e7} = i_{R3} + i_{b5} + i_{b6}$$

$$= \frac{v_{b6}}{R_3} + \frac{2\alpha i_e}{\beta_N}$$
$$= \frac{3.63}{50}i_e + \frac{2}{201}i_e$$

$$= 0.08i_{e}$$

(c) 
$$i_{b7} = \frac{i_{e7}}{\beta_N + 1} = \frac{0.08}{201}i_e = 0.0004i_e$$

(d) 
$$v_{b7} = i_{e7}r_{e7} + v_{b6}$$

$$v_{b7} = 0.08 \times 2.63i_e + 3.63i_e$$

$$= 3.84 \text{ k}\Omega \times i_e$$

(e) 
$$R_{\rm in} = \frac{v_{b7}}{\alpha i_a} \simeq 3.84 \text{ k}\Omega$$

Ex: 12.25 
$$r_{o4} = \frac{|V_{Ap}|}{I} = \frac{50 \text{ V}}{9.5 \text{ µA}} = 5.26 \text{ M}\Omega$$

$$g_{m4} = 0.38 \text{ mA/V}$$

$$r_{e2} = 2.63 \text{ k}\Omega$$

$$r_{\pi 4} = \frac{\beta_P}{g_{m4}} = \frac{50}{0.38} = 131.6 \text{ k}\Omega$$

$$R_{o4} = r_{o4}[1 + g_{m4}(r_{e2} \parallel r_{\pi 4})]$$

$$= 5.26[1 + 0.38(2.63 \parallel 131.6)]$$

$$= 10.4 \text{ M}\Omega$$

(The answer in the book was obtained by neglecting  $r_{\pi 4}$ .)

$$r_{o6} = \frac{V_{An}}{I} = \frac{125 \text{ V}}{9.5 \text{ \mu A}} = 13.16 \text{ M}\Omega$$

$$g_{m6} = 0.38 \text{ mA/V}$$

$$R_6 = 1 \text{ k}\Omega$$

$$r_{\pi 6} = \frac{200}{0.38} = 526.3 \text{ k}\Omega$$

$$R_{o6} = r_{o6}[1 + g_{m6}(R_2 \parallel r_{\pi 6})]$$

$$= 13.16[1 + 0.38(1 \parallel 526.3)]$$

$$= 18.2 \text{ M}\Omega$$

$$R_{o1} = R_{o9} \parallel R_{o6}$$

$$= 10.4 \parallel 18.2 = 6.62 \text{ M}\Omega$$

**Ex: 12.26** 
$$|A_{vo}| = G_{m1}R_{o1}$$

Using  $G_{m1}$  given in the answer to Exercise 12.23,

$$G_{m1} = 0.19 \text{ mA/V}$$

and  $R_{o1}$  given in the answer to Exercise 12.25,

$$R_{o1} = 6.7 \text{ M}\Omega$$

we obtain

$$|A_{vo}| = G_{m1}R_{o1}$$

$$= 0.19 \times 6.7 = 1273 \text{ V/V}$$

**Ex: 12.27** Refer to Fig. 12.22, which shows the current mirror with an imbalance between  $R_1 = R$  and  $R_2 = R + \triangle R$ . Observe that the imbalance causes an error in the mirror transfer ratio of

$$\epsilon_m = \frac{\triangle I}{I}$$

where 
$$\frac{\Delta I}{I}$$
 is given by Eq. (12.94). Thus,

$$\epsilon_m = \frac{\triangle R}{R + \triangle R + r_c}$$

where 
$$r_e = r_{e5} = r_{e6}$$
,

$$\epsilon_m = \frac{\triangle R}{R + \triangle R + r_{e5}}$$
 Q.E.D.

For 
$$R = 1 \text{ k}\Omega$$
,  $\frac{\Delta R}{R} = 0.02 \text{ and } r_{e5} = 2.63 \text{ k}\Omega$ ,

$$\epsilon_m = \frac{0.02}{1 + 0.02 + 2.63} = 5.5 \times 10^{-3}$$

#### Ex. 12.28

Ex: 12.28
$$R_{o9} = r_{o9} = \frac{|V_{Ap}|}{I_{C9}} = \frac{50 \text{ V}}{19 \text{ }\mu\text{A}} = 2.63 \text{ M}\Omega$$

$$R_{o10} = r_{o10}[1 + g_{m10}(R_4 \parallel r_{\pi 10})]$$

where

$$r_{o10} = \frac{V_{An}}{I_{C10}} = \frac{125 \text{ V}}{19 \text{ }\mu\text{A}} = 6.58 \text{ M}\Omega$$

$$g_{m10} = \frac{I_{C10}}{V_T} = \frac{19 \text{ } \mu\text{A}}{0.025 \text{ V}} = 0.76 \text{ mA/V}$$

$$R_4 = 5 \text{ k}\Omega$$

$$r_{\pi 10} = \frac{\beta_N}{g_{m10}} = \frac{200}{0.76} = 263.2 \text{ k}\Omega$$

$$R_{o10} = 6.58[1 + 0.76(5 \parallel 263.2)]$$

$$= 31.1 \text{ M}\Omega$$

$$R_o = R_{o9} \parallel R_{o10}$$

$$= 2.63 \parallel 31.1 = 2.43 \text{ M}\Omega$$

# Ex: 12.29 Using Eq. (12.100), we obtain

$$G_{mcm} = \frac{\epsilon_m}{2R}$$

$$= \frac{5.5 \times 10^{-3}}{2 \times 2.43 \times 10^{6}} = 1.13 \times 10^{-6} \text{ mA/V}$$

CMRR = 
$$\frac{G_{m1}}{G_{mcm}} = \frac{0.19}{1.13 \times 10^{-6}} = 1.68 \times 10^5$$

or 104.5 dB

Without common-mode feedback, the CMRR is reduced by a factor equal to  $\beta_P$ . Equivalently,

$$CMRR = 104.5 - 20 \log \beta_P$$

$$= 104.5 - 20 \log 50$$

$$= 70.5 \text{ dB}$$

**Ex: 12.30** 
$$r_{e16} = \frac{V_T}{I_{E16}} \simeq \frac{25 \text{ mV}}{16.2 \text{ mA}} = 1.54 \text{ k}\Omega$$

$$r_{e17} = \frac{V_T}{I_{E17}} \simeq \frac{25 \text{ mV}}{0.55 \text{ mA}} = 45.5 \Omega$$

Using Eq. (12.103), we obtain

$$R_{i2} =$$

$$(200+1)\{1.54+[50 \parallel (200+1)(0.0455+0.1)]\}$$

$$\simeq 4~M\Omega$$

Ex: 12.31 Using Eq. (12.104), we get

$$i_{c17} = \frac{\alpha}{r_{e17} + R_8} v_{b17}$$

$$= \frac{200}{201} \frac{1}{0.0455 + 0.1} v_{b17} = 6.85 v_{b17} \tag{1}$$

Using Eq. (12.106), we obtain

$$R_{i17} = 201(0.0455 + 0.1) = 29.25 \text{ k}\Omega$$

Using Eq. (12.105), we get

$$v_{b17} = v_{i2} \frac{50 \parallel 29.25}{(50 \parallel 29.25) + 1.54} = 0.92 v_{i2}$$
 (2)

Combining Eqs. (1) and (2), we obtain

$$i_{c17} = 6.32v_{b17}$$

Thus,

$$G_{m2} = 6.32 \text{ mA/V}$$

This value is somewhat lower than the value generally published for  $G_{m2}$ , namely

$$G_{m2}=6.5 \text{ mA/V}$$

To conform with published literature, we shall use the latter value in future calculations.

Ex: 12.32 
$$R_{o13B} = r_{o13B} = \frac{|V_{Ap}|}{I_{C13B}}$$

$$=\frac{50}{0.55}=90.9 \text{ k}\Omega$$

$$R_{o17} = r_{o17}[1 + g_{m17}(R_8 \parallel r_{\pi 17})]$$

where

$$r_{o17} = \frac{125}{0.55} = 227.3 \text{ k}\Omega$$

$$g_{m17} = \frac{0.55}{0.025} = 22 \text{ mA/V}$$

$$R_8 = 0.1 \text{ k}\Omega$$

$$r_{\pi 17} = \frac{200}{22} = 9.09 \text{ k}\Omega$$

$$R_{o17} = 227.3[1 + 22(0.1 \parallel 9.09)]$$

$$=722 \text{ k}\Omega$$

$$R_{o2} = R_{o13B} \parallel R_{o17}$$

$$=90.9 \parallel 722 \simeq 81 \text{ k}\Omega$$

Ex: 12.33 Open-circuit voltage gain =  $-G_{m2}R_{o2}$ 

$$= -6.5 \times 81 = -526.5 \text{ V/V}$$

Ex: 12.34 
$$r_{e23} = \frac{V_T}{I_{E23}}$$

$$\simeq \frac{25 \text{ mV}}{0.18 \text{ mA}} = 138.9 \Omega$$

$$R_{o23} = \frac{R_{o2}}{\beta_{23} + 1} + r_{e23}$$

$$= \frac{81}{50 + 1} + 0.139$$

$$= 1.73 \text{ k}\Omega$$

$$r_{e20} = \frac{V_T}{I_{E20}}$$

$$= \frac{25 \text{ mV}}{5 \text{ mA}} = 5 \Omega$$

$$R_{out} = r_{e20} + \frac{R_{o23}}{\beta_{20} + 1}$$

$$= 5 + \frac{1730}{50 + 1} = 39 \Omega$$

Total output resistance =  $R_{\text{out}} + R_7$ = 39 + 27 = 66  $\Omega$ 

#### Ex: 12.35

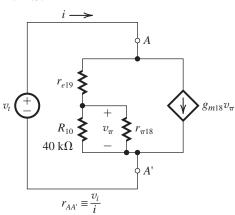


Figure 1 shows the equivalent circuit model of the circuit in Fig. E12.35. Note that the diode-connected transistors  $Q_{19}$  is replaced with  $r_{e19}$ ,

$$r_{e19} = \frac{V_T}{I_{E19}}$$

$$\simeq \frac{25 \text{ mA}}{16 \text{ μA}} = 1.56 \text{ k}\Omega$$

Transistor  $Q_{18}$  is replaced with its hybrid- $\pi$  model.

$$g_{m18} = \frac{I_{C18}}{V_T} = \frac{0.165 \text{ mA}}{0.025 \text{ V}}$$

= 6.6 mA/V

$$r_{\pi 18} = \frac{\beta_N}{g_{m18}} = \frac{200}{6.6} = 30.3 \text{ k}\Omega$$

Now,

$$v_{\pi} = v_{t} \frac{R_{10} \parallel r_{\pi}}{(R_{10} \parallel r_{\pi}) + r_{e19}}$$
$$= v_{t} \frac{40 \parallel 30.3}{(40 \parallel 30.3) + 1.56} = 0.917 v_{t}$$

$$i = \frac{v_t}{(40 \parallel 30.3) + 1.56} + g_{m18} \times 0.917 v_t$$
$$= 6.11 \times 10^{-3} v_t$$
$$r'_{AA} \equiv \frac{v_t}{i} \simeq 163 \ \Omega$$

**Ex:** 12.36 For  $v_0 = 10 \sin \omega t$ 

$$\frac{dv_O}{dt} = \omega \times 10 \cos \omega t$$

$$SR = \frac{dv_O}{dt} \Big|_{\text{max}} = \omega_M \times 10 = 2\pi f_M \times 10$$

$$f_M = \frac{SR}{20\pi} = \frac{0.63 \times 10^6}{20\pi} = 10 \text{ kHz}$$

Ex: 12.37  $I_{S2} = 2I_{S1}$ 

Using Eq. (12.127), we obtain

$$I = \frac{V_T}{R_2} \ln \frac{I_{S2}}{I_{S1}}$$

$$0.01 = \frac{0.025}{R_2} \ln 2$$

$$\Rightarrow R_2 = 1.73 \text{ k}\Omega$$

$$R_3 = R_4 = \frac{0.2 \text{ V}}{0.01 \text{ mA}} = 20 \text{ k}\Omega$$

Ex: 12.38 To obtain  $I_8 = 10 \mu A$ , transistor  $Q_8$  must have the same (ratio = 1) emitter area as  $Q_3$ , and

$$R_8 = R_3 = 20 \text{ k}\Omega$$

To obtain  $I_9 = 20 \mu A$ ,  $Q_9$  must have an EBJ area twice (ratio = 2) that of  $Q_3$  and

$$R_9 = \frac{1}{2}R_3 = 10 \text{ k}\Omega$$

To obtain  $I_{10}=5~\mu\text{A},~Q_{10}$  must have an EBJ area half (ratio = 0.5) that of  $Q_3$  and

$$R_{10} = 2R_3 = 40 \text{ k}\Omega$$

Ex: 12.39 Refer to the circuit in Fig. 12.42.

(a) Current gain from 
$$v_{IP}$$
 to output 
$$= (\beta_1 + 1)(\beta_2 + 1)\beta_P$$

$$\simeq \beta_1\beta_2\beta_P = \beta_N\beta_P^2$$
Current gain from  $v_{IN}$  to output 
$$= (\beta_3 + 1)\beta_N$$

$$\simeq \beta_3\beta_N = \beta_N^2$$
(b) For  $i_L = +10$  mA,
current needed at  $v_{IP}$  input

$$=\frac{10}{\beta_N \beta_R^2} = \frac{10}{40 \times 10^2} = 2.5 \,\mu\text{A}$$

### Exercise 12-9

For  $i_L = -10 \text{ mA}$ ,

current needed at  $v_{\mathit{IN}}$  input  $=\frac{10}{\beta_{\mathit{N}}^2}=\frac{10}{40^2}$ 

 $=6.25\;\mu A$ 

Ex: 12.40  $I_Q = 0.4 \text{ mA}, I = 10 \mu\text{A},$ 

 $\frac{I_{SN}}{I_{S10}} = 10, \ \frac{I_{S7}}{I_{S11}} = 2$ 

Using Eq. (12.136), we obtain

 $0.4 \times 10^3 = 2 \left( \frac{I_{\text{REF}}^2}{10} \right) \times 10 \times 2$ 

where  $I_{REF}$  is in  $\mu A$ . Thus,

 $I_{\rm REF}=10~\mu{\rm A}$ 

For  $i_L = -10$  mA, then

 $i_P = 10 + i_N$ 

Using Eq. (12.137), we get

$$\frac{i_N(10+i_N)}{i_N+10+i_N}=0.2$$

$$\Rightarrow i_N^2 - 9.6i_N + 2 = 0$$

$$\Rightarrow i_N = 0.2 \text{ mA}$$

$$i_P = 10.2 \text{ mA}$$

### 12.1 Using Eq. (12.2), we get

$$V_{ICM\,\mathrm{min}} = -V_{SS} + V_{tn} + V_{OV3} - |V_{tp}|$$

$$= -1 + 0.4 + 0.2 - 0.4 = -0.8 \text{ V}$$

Using Eq. (12.3), we obtain

$$V_{ICM \, \text{max}} = V_{DD} - |V_{OV5}| - |V_{tp}| - |V_{OV1}|$$

$$= 1 - 0.2 - 0.4 - 0.2 = +0.2 \text{ V}$$

Thus,

$$-0.8 \text{ V} \le V_{ICM} \le +0.2 \text{ V}$$

Using Eq. (12.5), we get

$$-V_{SS} + V_{OV6} \le v_O \le V_{DD} - |V_{OV7}|$$

Thus,

$$-0.8 \text{ V} < v_0 < +0.8 \text{ V}$$

### 12.2 For NMOS devices, we have

$$V_A = 25 \times 0.3 = 7.5 \text{ V}$$

For PMOS devices,

$$|V_A| = 20 \times 0.3 = 6 \text{ V}$$

Using Eq. (12.13),

$$A_1 = -\frac{2}{|V_{OV1}|} / \left[ \frac{1}{|V_{A2}|} + \frac{1}{V_{A4}} \right]$$

$$=-\frac{2}{0.15} / \left(\frac{1}{6} + \frac{1}{7.5}\right)$$

$$= -44.4 \text{ V/V}$$

Using Eq. (12.20), we obtain

$$A_2 = -\frac{2}{V_{OV6}} / \left[ \frac{1}{V_{A6}} + \frac{1}{|V_{A7}|} \right]$$

$$= -\frac{2}{0.2} / \left[ \frac{1}{7.5} + \frac{1}{6} \right]$$

$$= -33.3 \text{ V/V}$$

$$A = A_1 A_2 = 1478.5 \text{ V/V}$$

$$r_{o6} = \frac{7.5}{0.3} = 25 \text{ k}\Omega$$

$$r_{o7} = \frac{6}{0.3} = 20 \text{ k}\Omega$$

$$R_o = r_{o6} \parallel r_{o7} = 11.1 \text{ k}\Omega$$

For a unity-gain voltage amplifier using this op amp, we have

$$R_{\rm out} = R_{of} = \frac{R_o}{1 + A\beta}$$

$$=\frac{11.1~k\Omega}{1+1481.5\times1}$$

$$= 7.5 \Omega$$

**12.3** For the op amp to not have a systematic offset voltage, the condition in Eq. (12.1) must be satisfied, that is,

$$\frac{(W/L)_6}{(W/L)_4} = 2\frac{(W/L)_7}{(W/L)_5}$$

$$\frac{W/0.3}{6/0.3} = 2\frac{45/0.3}{30/0.3}$$

$$\Rightarrow W = 18 \,\mu\text{m}$$

Refer to Fig. 12.1:

$$I_{D8} = I_{REF} = 40 \,\mu\text{A}$$

$$I = I_{D5} = I_{REF} \frac{W_5}{W_8} = 40 \times \frac{30}{6} = 200 \ \mu A$$

$$I_{D7} = I_{REF} \frac{W_7}{W_0} = 40 \times \frac{45}{6} = 300 \ \mu A$$

$$I_{D6} = 300 \, \mu A$$

$$I_{D1} = I_{D2} = I_{D3} = I_{D4} = \frac{I}{2} = 100 \text{ } \mu\text{A}$$

The overdrive voltage at which each transistor is operating is determined from

$$I_D = \frac{1}{2}\mu C_{ox} \frac{W}{L} V_{OV}^2$$

Then  $V_{GS}$  is found from

$$|V_{GS}| = |V_t| + |V_{OV}|$$

The transconductance at which each transistor is operating is obtained from

$$g_m = \frac{2I_D}{V_{OV}}$$

The output resistance of each transistor is found from

$$r_o = \frac{|V_A|}{I_D}$$

$$A_1 = -g_{m1,2}(r_{o2} \parallel r_{o4})$$

$$= -1.33(150 \parallel 150) = -100 \text{ V/V}$$

$$A_2 = -g_{m6}(r_{o6} \parallel r_{o7})$$

$$= -3.16(50 \parallel 50) = -79 \text{ V/V}$$

$$A = A_1 A_2 = 7900 \text{ V/V}$$

Using Eq. (12.2), we obtain

$$V_{ICM\,\mathrm{min}} = -V_{SS} + V_{tn} + V_{OV3} - |V_{tp}|$$

$$V_{ICM\,\text{min}} = -1 + 0.45 + 0.19 - 0.45$$

$$= -0.81 \text{ V}$$

Using Eq. (12.3), we get

$$V_{ICM \max} = V_{DD} - |V_{OV5}| - |V_{tp}| - |V_{OV1}|$$

$$= 1 - 0.24 - 0.45 - 0.15$$

$$= +0.16 \text{ V}$$

The results are summarized in the following table:

	$Q_1$	$Q_2$	$Q_3$	$Q_4$	$Q_5$	$Q_6$	$Q_7$	$Q_8$
$I_D$ ( $\mu$ A)	100	100	100	100	200	300	300	40
$ V_{OV} $ (V)	0.15	0.15	0.19	0.19	0.24	0.19	0.24	0.24
$ V_{GS} $ (V)	0.6	0.6	0.64	0.64	0.69	0.64	0.69	0.69
$g_m (mA/V)$	1.33	1.33	1.05	1.05	1.67	3.16	2.5	0.33
$r_o$ (k $\Omega$ )	150	150	150	150	75	50	50	375

Thus,

$$-0.8 \text{ V} \le V_{ICM} \le +0.16 \text{ V}$$

Using Eq. (12.5), we obtain

$$-V_{SS} + V_{OV6} \le v_O \le V_{DD} - |V_{OV7}|$$

Thus

$$-1 + 0.19 \le v_O \le 1 - 0.24$$

$$-0.81 \text{ V} \le v_O \le 0.76 \text{ V}$$

**12.4** For all transistors, we have

$$|V_A| = 20 \times 0.3 = 6 \text{ V}$$

Using Eq. (12.13), we get

$$A_1 = -\frac{2}{|V_{OV}|} / \frac{2}{|V_A|} = -\frac{6}{|V_{OV}|}$$

Using Eq. (12.20), we obtain

$$A_2 = -\frac{2}{|V_{OV}|} / \frac{2}{|V_A|} = -\frac{6}{|V_{OV}|}$$

$$A = A_1 A_2 = \frac{36}{|V_{OV}|^2}$$

$$1600 = \frac{36}{|V_{OV}|^2}$$

$$\Rightarrow |V_{OV}| = 0.15 \text{ V}$$

**12.5** From Eq. (12.24), we have

CMRR = 
$$[g_{m1}(r_{o2} \parallel r_{o4})] [2g_{m3}R_{SS}]$$

where

$$g_{m1} = \frac{I}{|V_{OV}|}$$

$$r_{o2} = r_{o4} = |V_A|/(I/2) = \frac{2|V_A|}{I}$$

$$g_{m3} = \frac{I}{|V_{OV}|}$$

$$R_{SS} = r_{o5} = \frac{|V_A|}{I}$$

Thus,

$$CMRR = \frac{I}{|V_{OV}|} \times \frac{1}{2} \times \frac{2|V_A|}{I} \times 2 \times \frac{I}{|V_{OV}|} \times \frac{|V_A|}{I}$$

$$=2\frac{|V_A|^2}{|V_{OV}|^2}$$

For CMRR = 72 dB = 4000, we have

$$4000 = 2 \times \frac{|V_A|^2}{0.15^2}$$

$$\Rightarrow |V_A| = 6.7 \text{ V}$$

Since  $|V_A| = |V'_A|L$ , we have

$$6.7 = 15L$$

$$\Rightarrow L = 0.45 \; \mu \text{m}$$

$$A_{\hat{v}} = \left| \frac{V_A}{V_{OV}} \right|^2 = \left( \frac{6.7}{0.15} \right)^2 = 2000 \text{ V/V}$$

**12.6** From Eq. (12.36), we obtain

$$f_t = \frac{G_{m1}}{2\pi C_C}$$

Thus

$$C_C = \frac{G_{m1}}{2\pi f_t} = \frac{0.8 \times 10^{-3}}{2\pi \times 120 \times 10^6} = 1.06 \text{ pF}$$

From Eq. (12.35), we get

$$f_{P2} = \frac{G_{m2}}{2\pi C_2}$$

$$= \frac{2.4 \times 10^{-3}}{2\pi \times 1.2 \times 10^{-12}} = 318.3 \text{ MHz}$$

From Eq. (12.31), we get

$$f_Z = \frac{G_{m2}}{2\pi C_C}$$

$$= \frac{2.4 \times 10^{-3}}{2\pi \times 1.06 \times 10^{-12}} = 360 \text{ MHz}$$

**12.7** (a) 
$$A = G_{m1}R_1G_{m2}R_2$$

$$= 1 \times 100 \times 2 \times 50 = 10,000 \text{ V/V}$$

(b) Without  $C_C$  connected:

$$\omega_{P1} = \frac{1}{C_1 R_1} = \frac{1}{0.1 \times 10^{-12} \times 100 \times 10^3}$$

$$= 10^8 \text{ rad/s}$$

This figure belongs to Problem 12.7, part (b).

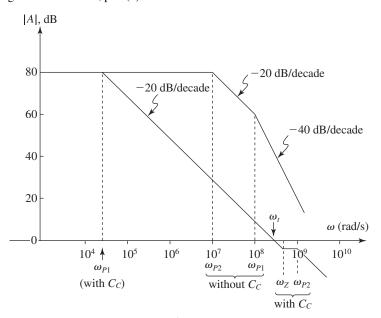


Figure 1

$$\omega_{P2} = \frac{1}{C_2 R_2} = \frac{1}{2 \times 10^{-12} \times 50 \times 10^3}$$

$$= 10^7 \text{ rad/s}$$

Figure 1 shows a Bode plot for the gain magnitude.

(c) With  $C_C$  connected:

Using Eq. (12.35), we obtain

$$\omega_{P2} = \frac{G_{m2}}{C_2}$$

$$= \frac{2 \times 10^{-3}}{2 \times 10^{-12}} = 10^9 \text{ rad/s}$$

For  $\omega_t$  two octaves below  $\omega_{P2}$ , we have

$$\omega_t = \frac{10^9}{4} \text{ rad/s}$$

Using Eq. (12.36), we get

$$\omega_t = \frac{G_{m2}}{C_C}$$

Thus

$$\frac{10^9}{4} = \frac{1 \times 10^{-3}}{C_C}$$

$$\Rightarrow C_C = 4 \text{ pF}$$

Now using Eq. (12.34), we obtain

$$\omega_{P1} = \frac{1}{R_1 C_C G_m r R_2}$$

$$= \frac{1}{100 \times 10^{3} \times 4 \times 10^{-12} \times 2 \times 10^{-3} \times 50 \times 10^{3}}$$

$$= \frac{10^{5}}{4} \text{ rad/s} = 25,000 \text{ rad/s}$$
Using Eq. (12.31), we get

$$\omega_Z = \frac{G_{m2}}{C_C}$$

$$= \frac{2 \times 10^{-3}}{4 \times 10^{-12}} = \frac{10^9}{2} \text{ rad/s} = 5 \times 10^8 \text{ rad/s}$$

The Bode plot for the gain magnitude with  $C_C$  connected is shown in Fig. 1.

**12.8** 
$$G_{m1} = 0.3 \text{ mA/V}$$

$$G_{m2}=0.6 \text{ mA/V}$$

$$r_{o2} = r_{o4} = 222 \text{ k}\Omega$$

$$r_{o6}=r_{o7}=111~\mathrm{k}\Omega$$

$$C_2 = 1 \text{ pF}$$

(a) 
$$A = G_{m1}(r_{o2} \parallel r_{o4})G_{m2}(r_{o6} \parallel r_{o7})$$

$$= 0.3(222 \parallel 222) \times 0.6(111 \parallel 111)$$

$$= 33.3 \times 33.3 = 1109 \text{ V/V}$$

(b) 
$$f_{P2} = \frac{G_{m2}}{2\pi C_2}$$

$$= \frac{0.6 \times 10^{-3}}{2\pi \times 1 \times 10^{-12}} = 95.5 \text{ MHz}$$

(c) 
$$R = \frac{1}{G_{m^2}} = \frac{1}{0.6 \times 10^{-3}} = 1.67 \text{ k}\Omega$$

(d) Phase margin = 
$$180 - 90 - \tan^{-1} \left( \frac{f_t}{f_{P2}} \right)$$

$$80^\circ = 90 - \tan^{-1}\left(\frac{f_t}{f_{P2}}\right)$$

$$f_t = f_{P2} \tan 10^\circ$$

$$= 95.5 \times 0.176 = 16.8 \text{ MHz}$$

Using Eq. (12.36), we obtain

$$C_C = \frac{G_{m1}}{2\pi f_t} = \frac{0.3 \times 10^{-3}}{2\pi \times 16.8 \times 10^6} = 2.84 \text{ pF}$$

The dominant pole will be at a frequency

$$f_{P1} = \frac{f_t}{\text{DC Gain}} = \frac{16.8 \times 10^6}{1109}$$

$$= 15.1 \text{ kHz}$$

(e) Since

$$f_t = \frac{G_{m1}}{2\pi C_C}$$

to double  $f_t$ ,  $C_C$  must be reduced by a factor of 2,

$$C_C = \frac{2.84}{2} = 1.42 \text{ pF}$$

At the new  $f_t = 2 \times 16.8 = 33.6$  MHz, we have

$$\phi_{P2} = -\tan^{-1}\frac{f_t}{f_{P2}}$$

$$= -\tan^{-1}\!\!\left(\frac{33.6}{95.5}\right) = -19.4^{\circ}$$

To reduce this phase lag to  $-10^{\circ}$ , we need to change R so that the zero moves to the negative real axis and introduces a phase lead of  $9.4^{\circ}$ . Thus,

$$\tan^{-1}\frac{f_t}{f_z} = 9.4^{\circ}$$

$$f_Z = \frac{f_t}{\tan 9.4} = \frac{33.6}{0.166} = 203 \text{ MHz}$$

$$f_Z = \frac{1}{2\pi C_C \left(R - \frac{1}{G_{m2}}\right)}$$

$$\Rightarrow R - \frac{1}{G_{m2}} = \frac{1}{2\pi \times 203 \times 10^6 \times 1.42 \times 10^{-12}}$$

$$=552 \Omega$$

$$R = 1670 + 552 = 2222 \Omega$$

$$= 2.22 \text{ k}\Omega$$

**12.9** (a) Using Eq. (12.36), we get

$$f_t = \frac{G_{m1}}{2\pi C_C}$$

$$C_C = \frac{G_{m1}}{2\pi f_t}$$

$$= \frac{1 \times 10^{-3}}{2\pi \times 100 \times 10^{6}} = 1.59 \text{ pF}$$

(b) 
$$f_{P2} = \frac{G_{m2}}{2\pi C_2}$$

$$= \frac{2 \times 10^{-3}}{2\pi \times 1 \times 10^{-12}} = 318 \text{ MHz}$$

$$f_Z = \frac{G_{m2}}{2\pi C_C} = \frac{2 \times 10^{-3}}{2\pi \times 1 \times 1.59 \times 10^{-12}}$$

$$= 200 \text{ MHz}$$

To obtain  $f_{P1}$ , we need to know the dc gain of the op amp,  $A_0$ , then

$$f_{P1} = \frac{f_t}{A_0}$$

The value of  $A_0$  is not specified in the problem statement!

(c) 
$$\phi_{P2} = -\tan^{-1}\left(\frac{f_t}{f_{P2}}\right)$$

$$= -\tan^{-1}\left(\frac{100}{318}\right) = -17.5^{\circ}$$

$$\phi_Z = -\tan^{-1}\left(\frac{f_t}{f_Z}\right)$$

$$\phi_Z = -\tan^{-1}\left(\frac{100}{200}\right) = -26.6^\circ$$

$$\phi_{\text{total}} = 90^{\circ} + 17.5 + 26.6 = 134^{\circ}$$

Phase margin = 
$$180 - 134 = 46^{\circ}$$

(d) From Eq. (12.44), for

$$f_Z = \infty$$

we select

$$R = \frac{1}{G_{m2}} = \frac{1}{2} = 0.5 \text{ k}\Omega = 500 \Omega$$

Phase margin = 
$$180^{\circ} - (90^{\circ} + 17.5^{\circ}) = 72.5^{\circ}$$

(e) To obtain a phase margin of  $85^{\circ}$ , we need the left-half plane zero to provide at  $f_t$  a phase angle of  $85^{\circ} - 72.5^{\circ} = 12.5^{\circ}$ . Thus,

$$12.5^{\circ} = \tan^{-1} \left( \frac{f_t}{f_Z} \right)$$

$$f_Z = \frac{f_t}{\tan 12.5^\circ} = \frac{100}{\tan 12.5^\circ} = 451 \text{ MHz}$$

From Eq. (12.44), we have

$$-f_Z = \frac{1}{2\pi C_C \left(\frac{1}{G_{m2}} - R\right)}$$

$$\Rightarrow R = 722 \Omega$$

**12.10** Using Eq. (12.46), we obtain

$$SR = 2\pi f_t V_{OV1,2}$$

$$= 2\pi \times 100 \times 10^6 \times 0.2$$

$$= 125.6 \text{ V/}\mu\text{s}$$

Using Eq. (12.45),

$$SR = \frac{I}{C_C}$$

$$\Rightarrow C_C = \frac{I}{SR} = \frac{100 \times 10^{-6}}{125.6 \times 10^6}$$

$$= 0.8 \text{ pF}$$

**12.11** 
$$G_{m1} = 1 \text{ mA}, G_{m2} = 5 \text{ mA/V}$$

(a) Using Eq. (12.36), we obtain

$$f_t = \frac{G_{m1}}{2\pi C_C}$$

$$\Rightarrow C_C = \frac{G_{m1}}{2\pi f_t} = \frac{1 \times 10^{-3}}{2\pi \times 80 \times 10^6}$$

$$= 2 pl$$

(b) Phase margin =

$$90^{\circ} - \tan^{-1} \left( \frac{\bar{f}_t}{f_{P2}} \right) - \tan^{-1} \left( \frac{f_t}{f_Z} \right)$$

where

$$f_{P2} = \frac{G_{m2}}{2\pi C_2}$$

and

$$f_Z = \frac{G_{m2}}{2\pi C_C}$$

For a PM of 70°, we have

$$\tan^{-1}\left(\frac{f_t}{f_{P2}}\right) + \tan^{-1}\left(\frac{f_t}{f_Z}\right) = 20^{\circ}$$

But.

$$f_Z = \frac{5 \times 10^{-3}}{2\pi \times 2 \times 10^{-12}} = 398 \text{ MHz}$$

and

$$\tan^{-1}\left(\frac{f_t}{f_Z}\right) = \tan^{-1}\left(\frac{80}{398}\right) = 11.4^{\circ}$$

Thus.

$$\tan^{-1}\left(\frac{f_t}{f_{P2}}\right) = 20 - 11.4^{\circ} = 8.6^{\circ}$$

$$\frac{f_t}{f_{P2}} = \tan 8.6^{\circ}$$

$$\Rightarrow f_{P2} = \frac{80}{\tan 8.6^{\circ}} = 529 \text{ MHz}$$

$$\frac{G_{m2}}{2\pi C_2} = 529 \times 10^6$$

$$C_2 = \frac{5 \times 10^{-3}}{2\pi \times 529 \times 10^6} = 1.51 \text{ pF}$$

This is the maximum value that  $C_2$  can have; if  $C_2$  is larger, then  $f_{P2}$  will be lower; and the phase it introduces at  $f_i$  will increase, causing the phase margin to drop below  $70^{\circ}$ .

**12.12** 
$$C_2 = 0.7 \text{ pF}.$$

For a phase margin of 72°, the phase due to  $f_{P2}$  at  $f_t$  must be 18°; thus,

$$\frac{f_t}{f_{P2}} = \tan 18^\circ$$

$$\Rightarrow f_{P2} = \frac{100}{\tan 18^{\circ}} = 307.8 \text{ MHz}$$

But

$$f_{P2} = \frac{G_{m2}}{2\pi C_2}$$

$$\Rightarrow G_{m2} = 2\pi f_{P2}C_2$$

$$= 2\pi \times 307.8 \times 10^6 \times 0.7 \times 10^{-12}$$

$$= 1.35 \text{ mA/V}$$

Thus,

$$g_{m6} = 1.35 \text{ mA/V}$$

For the transmission zero to be at  $\infty$ ,

$$R = \frac{1}{G_{m^2}} = \frac{1}{1.35 \times 10^{-3}} = 739 \ \Omega$$

$$SR = 2\pi f_t |V_{OV1,2}|$$

$$=2\pi\times100\times10^6\times0.15$$

$$= 94.2 \text{ V/}\mu\text{s}$$

$$SR = \frac{I}{C_C}$$

$$\Rightarrow C_C = \frac{I}{SR} = \frac{100 \times 10^{-6}}{94.2 \times 10^6} = 1.06 \text{ pF}$$

**12.13** SR = 
$$60 \text{ V/}\mu\text{s}$$
,  $f_t = 60 \text{ MHz}$ 

(a) Using Eq. (12.46), we obtain

$$SR = 2\pi f_t |V_{OV1}|$$

$$\Rightarrow |V_{OV1}| = \frac{60 \times 10^6}{2\pi \times 60 \times 10^6} = 0.16 \text{ V}$$

(b) Using Eq. (12.45), we get

$$SR = \frac{I}{C_C}$$

$$\Rightarrow C_C = \frac{I}{\text{SR}} = \frac{120 \times 10^{-6}}{60 \times 10^6} = 2 \text{ pF}$$

(c) For  $Q_1$  and  $Q_2$ , we have

$$I_{D1,2} = \frac{1}{2} \mu_p C_{ox} \left( \frac{W}{L} \right)_{1,2} |V_{OV1,2}|^2$$

$$60 = \frac{1}{2} \times 60 \times \left(\frac{W}{L}\right)_{1,2} \times 0.16^{2}$$

$$\Rightarrow \left(\frac{W}{L}\right)_{1} = \left(\frac{W}{L}\right)_{2} = 78.1$$

**12.14** 
$$G_{m1} = 0.8 \text{ mA/V}, G_{m2} = 2 \text{ mA/V}$$

(a) Using Eq. (12.36), we obtain

$$f_t = \frac{g_{m1}}{2\pi C_C}$$

$$\Rightarrow C_C = \frac{G_{m1}}{2\pi f_t} = \frac{0.8 \times 10^{-3}}{2\pi \times 100 \times 10^6} = 1.27 \text{ pF}$$

(b) Phase margin =
$$90^{\circ} - \tan^{-1} \left( \frac{f_t}{f_{P2}} \right) - \tan^{-1} \left( \frac{f_t}{f_Z} \right)$$

$$60^{\circ} = 90 - \tan^{-1} \left( \frac{f_t}{f_{P2}} \right) - \tan^{-1} \left( \frac{f_t}{f_Z} \right)$$

$$\tan^{-1}\left(\frac{f_t}{f_{P2}}\right) + \tan^{-1}\left(\frac{f_t}{f_Z}\right) = 30^{\circ}$$

$$f_{P2} = \frac{G_{m2}}{2\pi C_2}$$

$$f_Z = \frac{1}{2\pi C_C \left(\frac{1}{G_{m2}} - R\right)}$$
$$= \frac{1}{2\pi \times 1.27 \times 10^{-12} (0.5 - 0.5) \times 10^3} = \infty$$

$$\tan^{-1}\left(\frac{f_t}{f_{P2}}\right) = 30^\circ$$

$$f_{P2} = \frac{f_t}{\tan 30} = 173.2 \text{ MHz}$$

We now can obtain  $C_2$  from

$$173.2 \times 10^6 = \frac{2 \times 10^{-3}}{2\pi C_2}$$

$$\Rightarrow C_2 = \frac{2 \times 10^{-3}}{2\pi \times 173.2 \times 10^6} = 1.84 \text{ pF}$$

**12.15** (a) From Eq. (12.54), we have

$$PSRR^- = g_{m1}(r_{o2} \parallel r_{o4})g_{m6}r_{o6}$$

$$g_{m1} = \frac{2 \times \frac{I}{2}}{|V_{OV}|} = \frac{I}{|V_{OV}|}$$
$$r_{o2} = r_{o4} = \frac{|V_A|}{I/2} = \frac{2|V_A|}{I}$$

$$g_{m6} = \frac{2I_{D6}}{|V_{OV}|}$$

$$r_{o6} = \frac{|V_A|}{I_{D6}}$$

$$PSRR^{-} = \frac{I}{|V_{OV}|} \times \frac{1}{2} \times \frac{2|V_A|}{I} \times \frac{2I_{D6}}{|V_{OV}|} \times \frac{|V_A|}{I_{D6}}$$

$$=2\left|\frac{V_A}{V_{OV}}\right|^2$$
 Q.E.D.

(b) A PSRR<sup>-</sup> of 72 dB means

$$PSRR^- = 4000$$

Thus,

$$4000 = 2 \frac{|V_A|^2}{0.15^2}$$

$$\Rightarrow |V_A| = 6.71 \text{ V}$$

Now,

$$|V_A| = |V_A'|L$$

$$6.71 = 15L$$

$$\Rightarrow L = 0.45 \,\mu\text{m}$$

**12.16** For  $Q_8$  and  $Q_9$ , we have

$$I_{\rm REF} = \frac{1}{2} \mu_p C_{ox} \left( \frac{W}{L} \right)_{8.9} |V_{OV8,9}|^2$$

$$225 = \frac{1}{2} \times 60 \times \frac{60}{0.5} \times |V_{OV8,9}|^2$$

$$\Rightarrow |V_{OV8,9}| = 0.25 \text{ V}$$

$$g_{m8} = g_{m9} = \frac{2I_D}{|V_{OV}|} = \frac{2 \times 0.225}{0.25}$$

$$= 1.8 \text{ mA/V}$$

For  $Q_{10}$ ,  $Q_{11}$  and  $Q_{12}$ , we have

$$g_m = g_{m8} = 1.8 \text{ mA/V}$$

$$\frac{2I_{\rm REF}}{V_{OV}} = 1.8$$

$$\Rightarrow V_{OV} = 0.25 \text{ V}$$

$$225 = \frac{1}{2} \times 180 \times \left(\frac{W}{L}\right) \times 0.25^2$$

$$\Rightarrow \left(\frac{W}{L}\right)_{10} = \left(\frac{W}{L}\right)_{11} = \left(\frac{W}{L}\right)_{12} = 40$$

Using Eq. (12.61), we obtain

$$R_B = \frac{2}{g_{m12}} \left( \sqrt{\frac{(W/L)_{12}}{(W/L)_{13}}} - 1 \right)$$

$$=\frac{2}{1.8\times 10^{-3}}\left(\sqrt{4}-1\right)$$

$$= 1.11 \text{ k}\Omega$$

Voltage drop across $R_B = I_{REF} \times 1.11$	$V_{ICM\mathrm{max}} = V_{DD} -  V_{OV9}  + V_{tn}$
$= 0.225 \times 1.11 = 0.25 \text{ V}$	= 1 - 0.15 + 0.4 = +1.25  V
The $\left(\frac{W}{L}\right)$ ratios of $Q_{10}$ , $Q_{11}$ and $Q_{12}$ are given	$V_{ICM\mathrm{min}} = -V_{SS} +  V_{OV11}  + V_{OV1} + V_{tn}$
above. For $Q_{13}$ , we have	= -1 + 0.15 + 0.15 + 0.4 = -0.3  V
$\left(\frac{W}{L}\right)_{12} = 4\left(\frac{W}{L}\right)_{12}$	Thus,
$\left(\frac{\overline{L}}{L}\right)_{13} = 4\left(\frac{\overline{L}}{L}\right)_{12}$	$-0.3 \text{ V} \le V_{ICM} \le +1.25 \text{ V}$
$\Rightarrow \left(\frac{W}{L}\right)_{12} = 160$	$v_{O\max} = V_{\rm BIAS1} +  V_{tp} $
\ /13	= 0.3 + 0.4 = +0.7  V
DC voltage at gate of $Q_{12}$	$v_{O\min} = -V_{SS} + V_{OV7} + V_{th} + V_{OV5}$
$= -V_{SS} + I_{REF}R_B + V_{th} + V_{OV12}$	= -1 + 0.15 + 0.4 + 0.15 = -0.3  V
= -1.5 + 0.25 + 0.5 + 0.25 = -0.5  V	Thus,
DC Voltage at gate of $Q_{10}$	$-0.3 \text{ V} \le v_O \le +0.7 \text{ V}$
$= V_{G12} + V_{tn} + V_{OV11}$	,
= -0.5 + 0.5 + 0.25 = +0.25  V	<b>12.19</b> $I_{D1} = I_{D2} = \frac{I}{2} = 0.2 \text{ mA}$
DC Voltage at gate of $Q_8$	$\begin{bmatrix} 1 \\ 0.2 \end{bmatrix}$
$=V_{DD}- V_{tp} - V_{OV8} $	$0.2 = \frac{1}{2} \times 0.4 \times \left(\frac{W}{L}\right)_{1,2} \times 0.04$
= 1.5 - 0.5 - 0.25 = +0.75  V	$\Rightarrow \left(\frac{W}{L}\right)_1 = \left(\frac{W}{L}\right)_2 = 25$
<b>12.17</b> $2I_B \times 2 = 1 \text{ mW}$	$I_{D3} = I_{D4} = I_B - \frac{I}{2} = 250 - 200 = 50 \mu\text{A}$
$I_B = \frac{10^{-3}}{4} = 0.25 \text{ mA} = 250 \mu\text{A}$	$50 = \frac{1}{2} \times 100 \times \left(\frac{W}{L}\right)_{\text{out}} \times 0.04$
$I_{D1}=4I_{D3}$	- (-/3,4
$I_{D1} + I_{D3} = I_B$	$\Rightarrow \left(\frac{W}{L}\right)_{1} = \left(\frac{W}{L}\right)_{1} = 25$
$5I_{D3}=250~\mu\text{A}$	$I_{D5} = I_{D6} = I_{D7} = I_{D8} = 50 \mu\text{A}$
$I_{D3} = 50 \ \mu\text{A}, \ I_{D4} = 50 \ \mu\text{A}$	
$I_{D1} = 200 \mu\text{A}, \; I_{D2} = 200 \mu\text{A}$	$50 = \frac{1}{2} \times 400 \times \left(\frac{W}{L}\right)_{5-8} \times 0.04$
$I = 400 \mu\text{A}$	$\Rightarrow \left(\frac{W}{L}\right)_5 = \left(\frac{W}{L}\right)_6 = \left(\frac{W}{L}\right)_7 = \left(\frac{W}{L}\right)_8$
<b>12.18</b> $V_{\text{BIAS1}} = V_{DD} -  V_{OV9}  -  V_{OV3}  -  V_{tp} $	= 6.25
= 1 - 0.15 - 0.15 - 0.4 = +0.3  V	$I_{D9} = I_{D10} = I_B = 250 \mu\text{A}$
$V_{\rm BIAS2} = V_{DD} -  V_{OV9}  -  V_{tp} $	$250 = \frac{1}{2} \times 100 \times \left(\frac{W}{L}\right)_{0.10} \times 0.04$
= 1 - 0.15 - 0.4 = +0.45  V	7 9,10
$V_{\text{BIAS3}} = -V_{SS} + V_{OV11} + V_m$	$\Rightarrow \left(\frac{W}{L}\right)_{0} = \left(\frac{W}{L}\right)_{10} = 125$
1 + 0.15 + 0.4 = 0.45 M	2/9 (2/10

This table belongs to Problem 12.19.

= -1 + 0.15 + 0.4 = -0.45 V

Transistor	$Q_1$	$Q_2$	$Q_3$	$Q_4$	$Q_5$	$Q_6$	$Q_7$	$Q_8$	$Q_9$	$Q_{10}$	$Q_{11}$
W/L	25	25	25	25	6.25	6.25	6.25	6.25	125	125	50

 $I_{D11} = I = 400 \,\mu\text{A}$ 

$$400 = \frac{1}{2} \times 400 \times \left(\frac{W}{L}\right)_{11} \times 0.04$$
$$\Rightarrow \left(\frac{W}{L}\right)_{11} = 50$$

Summary: See table on previous page.

12.20 
$$G_m = g_{m1} = g_{m2} = \frac{2(I/2)}{V_{OV}}$$
  
 $= \frac{I}{V_{OV}} = \frac{0.4}{0.2} = 2 \text{ mA/V}$   
 $I_{D4} = I_B - \frac{I}{2} = 0.25 - 0.2 = 0.05 \text{ mA}$   
 $g_{m4} = \frac{2I_{D4}}{|V_{OV}|} = \frac{2 \times 0.05}{0.2} = 0.5 \text{ mA/V}$   
 $r_{o4} = \frac{|V_A|}{I_{D4}} = \frac{10}{0.05} = 200 \text{ k}\Omega$   
 $r_{o2} = \frac{|V_A|}{I_{D2}} = \frac{|V_A|}{I/2} = \frac{10}{0.2} = 50 \text{ k}\Omega$   
 $r_{o10} = \frac{|V_A|}{I_{D10}} = \frac{|V_A|}{I_B} = \frac{10}{0.25} = 40 \text{ k}\Omega$   
 $R_{o4} = (g_{m4}r_{o4}) (r_{o2} \parallel r_{o10})$   
 $= 0.5 \times 200 (50 \parallel 40)$   
 $= 2.22 \text{ M}\Omega$   
 $I_{D6} = 50 \text{ \muA} = 0.05 \text{ mA}$   
 $g_{m6} = \frac{2 \times 0.05}{0.2} = 0.5 \text{ mA/V}$ 

$$g_{m6} = \frac{2 \times 0.05}{0.2} = 0.5 \text{ mA/V}$$

$$r_{o6} = \frac{|V_A|}{I_{D6}} = \frac{10}{0.05} = 200 \text{ k}\Omega$$

$$r_{o8} = \frac{|V_A|}{I_{D8}} = \frac{10}{0.05} = 200 \text{ k}\Omega$$

$$R_{o6} = g_{m6} r_{o6} r_{o8}$$

$$=0.5\times200\times200=20~\text{M}\Omega$$

$$R_o = R_{o4} \parallel R_{o6}$$

$$= 2.22 \parallel 20 = 2 \text{ M}\Omega$$

$$A_v = G_m R_o$$

$$= 2 \times 2000 = 4000 \text{ V/V}$$

For the closed-loop amplifier:

$$A = A_v = 4000$$

$$\beta = \frac{C}{C + 9C} = 0.1$$

$$\frac{V_o}{V_i} = A_f = \frac{A}{1 + A\beta} = \frac{4000}{1 + 4000 \times 0.1}$$

$$=\frac{4000}{401}=9.975 \text{ V/V}$$

$$R_{\text{out}} = R_{of} = \frac{R_o}{1 + A\beta} = \frac{2 \text{ M}\Omega}{401} \simeq 5 \text{ k}\Omega$$

**12.21** SR = 
$$\frac{I_B}{C_I}$$

$$10 \times 10^6 = \frac{I_B}{10 \times 10^{-12}}$$

$$\Rightarrow I_B = 10^{-4} \text{ A} = 0.1 \text{ mA} = 100 \text{ } \mu\text{A}$$

$$\frac{I}{2} = 3\left(I_B - \frac{I}{2}\right)$$

$$\frac{I}{2}(1+3) = 3I_B = 300$$

$$I = 150 \, \mu A$$

Now,

$$f_t = \frac{G_m}{2\pi C_t}$$

$$G_m = g_{m1,2} = \frac{2(I/2)}{V_{OV1,2}} = \frac{I}{V_{OV1,2}}$$

$$=\frac{0.15 \text{ mA}}{0.15 \text{ V}}=1 \text{ mA/V}$$

$$f_t = \frac{1 \times 10^{-3}}{2\pi \times 10^{-12}}$$

$$= 15.92 \text{ MHz}$$

Phase due to the two nondominant poles at  $f_t$ 

$$= -2 \tan^{-1} \left( \frac{15.92}{50} \right) = -35.3^{\circ}$$

Thus,

Phase margin = 
$$90 - 35.3 = 54.7^{\circ}$$

To increase the phase margin to 75°, the phase due to the two nondominant poles must be reduced to  $90 - 75 = 15^{\circ}$ , i.e. each should contribute 7.5°, thus we must reduce  $f_t$  to the value obtained as follows:

$$\tan^{-1}\left(\frac{f_t}{50 \text{ MHz}}\right) = 7.5^{\circ}$$

$$f_t = 50 \times \tan 7.5^{\circ} = 6.58 \text{ MHz}$$

This is achieved by increasing  $C_L$ ,

$$6.58 \times 10^6 = \frac{1 \times 10^{-3}}{2\pi C_L}$$

$$\Rightarrow C_L = \frac{10^{-3}}{2\pi \times 7.92 \times 10^6} = 24.2 \text{ pF}$$

The new value of slew-rate will be

$$SR = \frac{I_B}{C_I} = \frac{0.1 \times 10^{-3}}{24.2 \times 10^{-12}} = 4.13 \text{ V/}\mu\text{s}$$

**12.22** Refer to Fig. 12.9. When  $V_{id}$  is sufficiently large to cause  $Q_1$  to cut off and  $Q_2$  to conduct all of I,  $Q_3$  will carry a current  $I_B$ . However,  $Q_4$  will carry ( $I_B - I$ ). The current  $I_B$  in  $Q_3$  will be mirrored in the drain of  $Q_6$ . Thus, at the output node the current available to charge  $C_L$  will be

$$I_O = I_B - (I_B - I) = I$$

and the slew rate becomes

$$SR = \frac{I}{C_I}$$

**12.23** 
$$A = 80 \text{ dB} \equiv 10^4 \text{ V/V}$$

$$f_t = 20 \text{ MHz}, \ C_L = 10 \text{ pF}$$

$$I_B = I$$

$$|V_A| = 12 \text{ V}$$

Refer to Figs. 12.9 and 12.10. For  $I = I_B$ , the dc operating currents of the 11 transistors are as follows:

$$Q_1 - Q_8$$
:  $\frac{I}{2}$ 

 $Q_9$ ,  $Q_{10}$ , and  $Q_{11}$ : I

Thus, for  $Q_1 - Q_8$ , we have

$$g_m = \frac{I}{|V_{OV}|}$$

and

$$r_o = \frac{2|V_A|}{I}$$

while, for  $Q_9 - Q_{11}$ ,

$$r_o = \frac{|V_A|}{I}$$

Now

$$G_m = g_{m1,2} = \frac{I}{V_{OV}}$$

$$R_{o4} = (g_{m4}r_{o4}) \ (r_{o2} \parallel r_{o10})$$

$$= \frac{I}{|V_{OV}|} \times \frac{2|V_A|}{I} \left[ \frac{2|V_A|}{I} \parallel \frac{|V_A|}{I} \right]$$

$$= \frac{2|V_A|}{|V_{OV}|} \times \frac{2}{3} \frac{|V_A|}{I}$$

$$= \frac{4|V_A|^2}{3|V_{OV}|I}$$

$$R_{o6}=g_{m6}r_{o6}r_{o8}$$

$$= \frac{I}{|V_{OV}|} \frac{2|V_A|}{I} \frac{2|V_A|}{I}$$
$$= \frac{4|V_A|^2}{|V_{OV}|I}$$

$$R_o = R_{o4} \parallel R_{o6}$$

$$= \left[ \frac{4}{3} \frac{|V_A|^2}{|V_{OV}|I} \right] \parallel \left[ \frac{|V_A|^2}{|V_{OV}|I} \right]$$

$$= \frac{|V_A|^2}{|V_A|^2}$$

The voltage gain can now be found as

$$A = G_m R_o = g_{m1,2} R_o$$

$$= \frac{I}{|V_{OV}|} \; \frac{|V_A|^2}{|V_{OV}|I}$$

$$=\frac{|V_A|^2}{|V_{OV}|^2}$$

$$10,000 = \left| \frac{V_A}{V_{OV}} \right|^2$$

$$\Rightarrow \frac{|V_A|}{|V_{OV}|} = 100$$

$$\Rightarrow |V_{OV}| = \frac{12}{100} = 0.12 \text{ V}$$

To obtain  $f_t = 20$  MHz, we use

$$20 \times 10^6 = \frac{g_{m1,2}}{2\pi \times 10 \times 10^{-12}}$$

$$g_{m1,2} = 2\pi \times 10 \times 10^{-12} \times 20 \times 10^6$$

$$= 1.257 \times 10^{-3} \text{ A/V}$$

Thus,

$$\frac{I}{|V_{OV}|} = 1.257 \times 10^{-3}$$

$$\Rightarrow I = 1.257 \times 0.12 \times 10^{-3}$$

$$= 0.15 \text{ mA} = 150 \mu\text{A}$$

$$I_B = I = 150 \,\mu\text{A}$$

$$SR = \frac{I_B}{C_L} = \frac{150 \times 10^{-6}}{10 \times 10^{-12}}$$

$$= 15 \text{ V/}\mu\text{s}$$

For  $Q_1$  and  $Q_2$ , we have

$$I_D = \frac{I}{2} = 75 \ \mu A = \frac{1}{2} k'_n \left(\frac{W}{L}\right)_{1,2} V_{OV}^2$$

$$75 = \frac{1}{2} \times 400 \times \left(\frac{W}{L}\right)_{1.3} \times 0.12^2$$

$$\Rightarrow \left(\frac{W}{L}\right)_1 = \left(\frac{W}{L}\right)_2 = 26$$

For  $Q_3$  and  $Q_4$ , we have

$$I_D = I_B - \frac{I}{2} = 150 - 75 = 75 \,\mu\text{A}$$

Thus,

$$75 = \frac{1}{2} \times \frac{400}{2.5} \times \left(\frac{W}{L}\right)_{3.4} \times 0.12^2$$

Summary (Approximate Values):

Transistor	$Q_1$	$Q_2$	$Q_3$	$Q_4$	$Q_5$	$Q_6$	$Q_7$	$Q_8$	$Q_9$	$Q_{10}$	$Q_{11}$
W/L	26	26	65	65	26	26	26	26	130	130	52

$$\Rightarrow \left(\frac{W}{L}\right)_3 = \left(\frac{W}{L}\right)_4 = 65.1$$

For  $Q_5$ ,  $Q_6$ ,  $Q_7$ , and  $Q_8$ , we have

$$I_D = I_B = 75 \,\mu\text{A}$$

$$75 = \frac{1}{2} \times 400 \times \left(\frac{W}{L}\right)_{5.0} \times 0.12^{2}$$

$$\Rightarrow \left(\frac{W}{L}\right)_5 = \left(\frac{W}{L}\right)_6 = \left(\frac{W}{L}\right)_7 = \left(\frac{W}{L}\right)_8 = 26$$

For  $Q_9$  and  $Q_{10}$ , we have

$$I_D = I_B = 150 \,\mu\text{A}$$

$$150 = \frac{1}{2} \times \frac{400}{2.5} \times \left(\frac{W}{L}\right)_{9.10} \times 0.12^2$$

$$\Rightarrow \left(\frac{W}{L}\right)_9 = \left(\frac{W}{L}\right)_{10} = 130.2$$

For  $Q_{11}$ , we have

$$I_D = I = 150 \,\mu\text{A}$$

$$150 = \frac{1}{2} \times 400 \times \left(\frac{W}{L}\right)_{11} \times 0.12^{2}$$

$$\Rightarrow \left(\frac{W}{L}\right)_{11} = 52$$

See table above for a summary.

# **12.24** (a) Refer to Fig. 12.12. For the NMOS input stage

$$V_{ICM\,\mathrm{max}} = V_{DD} - |V_{OV}| + V_{tn}$$

$$= 1 - 0.15 + 0.45 = +1.3 \text{ V}$$

$$V_{ICM\,\mathrm{min}} = -V_{SS} + V_{OV} + V_{OV} + V_{tn}$$

$$= -1 + 0.15 + 0.15 + 0.45$$

$$= -0.25 \text{ V}$$

Thus,

$$-0.25~\mathrm{V} \leq V_{ICM} \leq +1.3~\mathrm{V}$$

(b) For the PMOS input stage

$$V_{ICM\,\mathrm{max}} = V_{DD} - |V_{OV}| - |V_{tp}|$$

$$= 1 - 0.15 - 0.15 - 0.45 \text{ V}$$

$$= +0.25 \text{ V}$$

$$V_{ICM\,\mathrm{min}} = -V_{SS} + V_{OV} - |V_{tp}|$$

$$= -1 + 0.15 - 0.45$$

$$= -1.3 \text{ V}$$

Thus.

$$-1.3 \text{ V} \le V_{ICM} \le +0.25 \text{ V}$$

(c) The overlap range is

$$-0.25 \text{ V} \le V_{ICM} \le +0.25 \text{ V}$$

(d) 
$$-1.3 \text{ V} \le V_{ICM} \le +1.3 \text{ V}$$

#### **12.25** First we determine $V_{OV}$ :

$$90 = \frac{1}{2} \times 400 \times 20 \ V_{OV}^2$$

$$\Rightarrow V_{OV} = 0.15 \text{ V}$$

$$V_{\text{BIAS}} = V_t + 2V_{OV} = 0.45 + 2 \times 0.15$$

$$= 0.75 \text{ V}$$

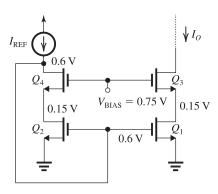


Figure 1

Figure 1 shows the voltages at the various nodes in the mirror circuit. The minimum voltage allowable at the output terminal is

$$v_{O\min} = V_{BIAS} - V_{tn}$$

$$= 0.75 - 0.45 = 0.3 \text{ V}$$

which is  $2V_{OV}$ .

The output resistance is

$$R_o \simeq g_{m3}r_{o3}r_{o1}$$

$$r_{o1} = r_{o3} = \frac{V_A}{I_D} = \frac{10}{0.09} = 111.1 \text{ k}\Omega$$

$$g_{m3} = \frac{2I_D}{V_{OV}} = \frac{2 \times 0.09}{0.15} = 1.2 \text{ mA/V}$$

$$R_o = 1.2 \times 111.1 \times 111.1 = 14.8 \text{ M}\Omega$$

12.26 Since  $Q_3$  is operating in the common-gate configuration and since the resistance in its drain is low, the input resistance at its source is  $1/g_{m3}$ . This resistance appears in parallel with  $r_{o1}$  which is much larger. Thus, the total resistance at this node is  $\simeq 1/g_{m3}$  and since the total capacitance is  $C_P$ , the pole introduced will have a frequency

$$f_P \simeq \frac{1}{2\pi C_P/g_{m3}} = \frac{g_{m3}}{2\pi C_P}$$
 Q.E.D.

Now.

$$f_t = \frac{g_{m1}}{2\pi C_L}$$

where  $g_{m1} = g_{m3}$  because all transistors are operating at the same values of  $I_D$  and  $|V_{OV}|$ .

For a phase margin of  $80^{\circ}$  the phase at  $f_t$  introduced by the pole at  $f_P$  must be only  $10^{\circ}$ ,

$$\tan^{-1}\left(\frac{f_t}{f_P}\right) = 10^{\circ}$$

$$f_P = \frac{f_t}{\tan 10^{\circ}} = \frac{f_t}{0.176}$$

$$\frac{g_{m3}}{2\pi C_P} = \frac{g_{m1}}{2\pi C_L \times 0.176}$$

$$\Rightarrow C_P = 0.176C_L$$

This is the largest value that  $C_P$  can have.

# 12.27 For each transistor we use

$$V_{BE} = V_T \ln \frac{I_C}{I_S}$$

$$= 25 \ln \left(\frac{I_C}{10^{-14}}\right)$$

$$g_m = \frac{I_C}{V_T} = \frac{I_C}{0.025 \text{ V}}$$

$$r_e \simeq \frac{1}{g_m}$$

$$r_{\pi} = \beta/g_m = 200/g_m$$

$$r_o = V_A/I_C = 125/I_C$$

We obtain the following results:

	$Q_1$	$Q_2$	$Q_5$	$Q_6$	$Q_{16}$	$Q_{17}$
$I_C$ ( $\mu$ A)	9.5	9.5	9.5	9.5	16.2	550
$V_{BE}$ (mV)	517	517	517	517	530	618
$g_m (mA/V)$	0.38	0.38	0.38	0.38	0.65	22
$r_e$ (k $\Omega$ )	2.63	2.63	2.63	2.63	1.54	0.045
$r_{\pi}$ (k $\Omega$ )	526	526	526	526	308	9.1
$r_o$ (M $\Omega$ )	13.2	13.2	13.2	13.2	7.72	0.227

12.28 
$$V_{BE1} = V_T \ln \frac{I_1}{I_{S1}}$$
  
 $V_{BE2} = V_T \ln \frac{I_1}{I_{S2}}$   
 $V_{BE3} = V_T \ln \frac{I_3}{I_{S3}}$   
 $V_{BE4} = V_T \ln \frac{I_3}{I_{S4}}$   
 $V_{BE3} + V_{BE4} = V_{BE1} + V_{BE2}$   
 $V_T \ln \frac{I_3}{I_{S3}} + V_T \ln \frac{I_3}{I_{S4}} = V_T \ln \frac{I_1}{I_{S1}} + V_T \ln \frac{I_1}{I_{S2}}$   
 $V_T \ln \frac{I_3^2}{I_{S3}I_{S4}} = V_T \ln \frac{I_1^2}{I_{S1}I_{S2}}$   
 $\Rightarrow \frac{I_3^2}{I_{S3}I_{S4}} = \frac{I_1^2}{I_{S1}I_{S2}}$   
 $\Rightarrow I_3 = I_1 \sqrt{\frac{I_{S3}I_{S4}}{I_{S1}I_{S2}}}$  Q.E.D.  
150 =  $I_1 \sqrt{3 \times 3} = 3I_1$   
 $\Rightarrow I_1 = 50 \text{ } \mu\text{A}$ 

#### 12.29 For the A and B devices, we have

$$V_{EB} = V_T \ln \frac{0.73 \times 10^{-3}}{10^{-14}}$$

=625 mV

For the A device, we have

$$g_{mA} = \frac{I_{CA}}{V_T} = \frac{0.25 \times 0.73}{0.025} = 7.3 \text{ mA/V}$$
 $r_{eA} \simeq \frac{1}{g_{mA}} = 137 \Omega$ 
 $r_{\pi A} = \frac{\beta}{g_{mA}} = \frac{50}{7.3} = 6.85 \text{ k}\Omega$ 
 $r_{oA} = \frac{|V_A|}{I_{CA}} = \frac{50}{0.18} = 278 \text{ k}\Omega$ 

For the B device, we have

$$g_{mB} = \frac{I_{CB}}{V_T} = \frac{0.75 \times 0.73}{0.025} = 21.9 \text{ mA/V}$$

$$r_{eB} \simeq \frac{1}{g_{mB}} = 46 \Omega$$

$$r_{\pi B} = \frac{\beta}{g_{mB}} = \frac{50}{21.9} = 2.28 \text{ k}\Omega$$

$$r_{oB} = \frac{|V_A|}{I_{CB}} = \frac{50}{0.55} = 90.9 \text{ k}\Omega$$

**12.30** 
$$V_{SG1} = |V_{tp}| + |V_{OV1}|$$

$$V_{GS2} = V_{tn} + V_{OV2}$$

$$V_{GS3} = V_{tn} + V_{OV3}$$

$$V_{SG4} = |V_{tp}| + |V_{OV4}|$$

But.

$$V_{SG1} + V_{GS2} = V_{GS3} + V_{SG4}$$

$$\Rightarrow |V_{OV1}| + V_{OV2} = V_{OV3} + |V_{OV4}|$$

Since

$$|V_{OV1}| = \sqrt{2I_1/k_1}$$

$$V_{OV2} = \sqrt{2I_1/k_2}$$

$$V_{OV3} = \sqrt{2I_3/k_3}$$

$$|V_{OV4}| = \sqrt{2I_3/k_4}$$

ther

$$\sqrt{2I_1}\left(\frac{1}{\sqrt{k_1}} + \frac{1}{\sqrt{k_2}}\right) = \sqrt{2I_3}\left(\frac{1}{\sqrt{k_3}} + \frac{1}{\sqrt{k_4}}\right)$$

$$\Rightarrow I_3 = I_1 \left[ \frac{\frac{1}{\sqrt{k_1}} + \frac{1}{\sqrt{k_2}}}{\frac{1}{\sqrt{k_3}} + \frac{1}{\sqrt{k_4}}} \right]^2$$

For  $k_1 = k_2$  and  $k_3 = k_4 = 16 k_1$ , we have

$$I_3 = I_1 \left[ \frac{2/\sqrt{k_1}}{2/\sqrt{k_3}} \right]^2 = 16 I_1$$

For  $I_3 = 1.6$  mA, we have

$$I_1 = 0.1 \text{ mA}$$

### 12.31 Differential input breakdown voltage

$$= 0.6 + 0.6 + 50 + 7$$

$$= 58.2 \text{ V}$$

where we have assumed that a forward conducting transistor exhibits  $|V_{BE}| = 0.6 \text{ V}$ .

# 12.32

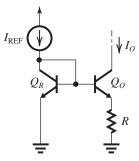


Figure 1

Refer to Fig. 1,

$$I_{REF} = 0.3 \text{ mA}, I_O = 10 \mu \text{A}$$

$$V_{BER} = V_T \ln \frac{I_{REF}}{I_S}$$

$$= 25 \ln \left( \frac{0.3 \times 10^{-3}}{10^{-14}} \right) = 603 \text{ mV}$$

$$V_{BEO} = V_T \ln \frac{I_O}{I_S}$$

$$=25\,\ln\!\left(\frac{10\times10^{-6}}{10^{-14}}\right)$$

$$= 518 \text{ mV}$$

$$V_{BER} - V_{BEO} = 603 - 518 = 85 \text{ mV}$$

$$R = \frac{85 \text{ mV}}{10 \mu \text{A}} = 8.5 \text{ k}\Omega$$

### 12.33 Refer to Fig. 12.15.

(a) A node equation at X yields

$$\frac{2I}{1 + 2/\beta_P} + \frac{2I}{\beta_P} = I_{C10}$$

$$2I \frac{\beta_P + 1 + \frac{2}{\beta_P}}{\beta_P \left(1 + \frac{2}{\beta_P}\right)} = I_{C10}$$

$$I = \frac{I_{C10}}{2} \left[ \frac{\beta_P (\beta_P + 2)}{\beta_P^2 + \beta_P + 2} \right]$$

For  $\beta_P = 50$ , we have

$$I = \frac{I_{C10}}{2} \times 1.019$$

For  $\beta_P = 20$ , we have

$$I = \frac{I_{C10}}{2} \times 1.043$$

Thus, I increases by  $\frac{I_{C10}}{2} \times 0.024$ , which is 2.4%.

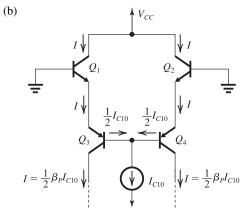


Figure 1

Figure 1 shows the suggested alternative design. As shown, here

$$I \simeq \frac{1}{2} \beta_P I_{C10}$$

For  $\beta_P = 50$ , we have

$$I = 25I_{C10}$$

For  $\beta_P = 20$ , we have

$$I = 10I_{C10}$$

Thus, I changes by  $-15I_{C10}$ , which is -60% change! This is a result of the absence of the desensitivity effect of negative feedback.

### **12.34** Refer to Fig. 12.15.

For  $I_{S9} = 2I_{S8}$ , the collector current of  $Q_9$  will be

$$I_{C9} = \frac{4I}{1 + \frac{2}{\beta_B}}$$

If  $\beta_P$  is large, a node equation at X yields

$$4I \simeq I_{C10}$$

$$\Rightarrow I = \frac{1}{4}I_{C10} = \frac{19}{4} = 4.75 \text{ } \mu\text{A}$$

To establish  $I_{C1} = I_{C2} = 9.5 \mu A$ , we need to redesign the Widlar source to provide

 $I_{C10} = 38 \,\mu\text{A}$ . From Eq. (12.86), we obtain

$$V_T \ln \frac{I_{\text{REF}}}{I_{C10}} = I_{C10} R_4$$

$$25 \times \ln \frac{730}{38} = 38R_4$$

$$\Rightarrow R_4 = 1.94 \text{ k}\Omega$$

**12.35** Refer to Fig. 12.15. For  $\beta_P$  large, a node equation at X yields

$$I_{C9} \simeq I_{C10}$$

If the ratio of the area of  $Q_9$  to that of  $Q_8$  is n, then

$$I_{C9} = n \times 2I$$

Thus,

$$2nI = I_{C10}$$

For  $I = 10 \mu A$  and  $I_{C10} = 40 \mu A$ , we have

$$n = 2$$

**12.36** Figure 1 shows the circuit when  $R_3$  is adjusted so that  $I_{C5} = I_{C6} = I_{C7}$ . Denoting the new value of these three currents  $I_1$ , we obtain the various currents indicated in Fig. 1. Now, at the input node X, we have

$$I_1\left(1+\frac{1}{\beta_N}\right) = 9.5 \,\mu\text{A}$$

$$\Rightarrow I_1 = \frac{9.5}{1 + (1/200)} = 9.45 \,\mu\text{A}$$

At this collector current, we have

$$V_{BE} = 25 \ln \frac{9.45 \times 10^{-6}}{10^{-14}} = 516.7 \,\mu\text{A}$$

The voltage drop across  $R_3$  becomes

$$V_{R3} = V_{BE5} + I_1 \left( 1 + \frac{1}{\beta_N} \right) R_1$$

$$= 516.7 + 9.5 \times 1$$

$$= 526.2 \text{ mV}$$

The value of  $R_3$  can now be found as

$$R_3 = \frac{V_{R3}}{I_1 \left(1 - \frac{1}{\beta_N}\right)} = \frac{526.2}{9.45 \left(1 - \frac{1}{200}\right)}$$

$$= 56 \text{ k}\Omega$$

**12.37** Refer to the circuit in Fig. 12.16. The current in  $Q_5$  remains equal to

$$I = 9.5 \, \mu A$$

This figure belongs to Problem 12.36.

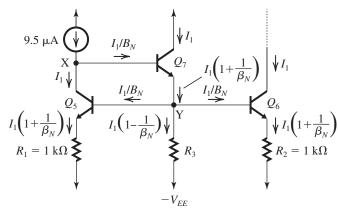


Figure 1

The voltage between the base of  $Q_5$  and  $-V_{EE}$  is

$$=V_{BE5}+IR_1$$

$$=25 \ln \left(\frac{9.5 \times 10^{-6}}{10^{-14}}\right) + 9.5 \times 1$$

$$= 517 + 9.5 = 526.5 \text{ mV}$$

With  $R_2$  shorted, this voltage appears across the BE junction of  $Q_6$ . Thus,

$$I_{C6} = I_S e^{V_{BE6}/V_T}$$

$$= 10^{-14} e^{526.5/25}$$

$$= 14 \mu A$$

**12.38** 
$$2I = 19 \,\mu\text{A}$$

Assuming

$$I_{C1} = I_{C2} = I = 9.5 \,\mu\text{A}$$

than

$$I_{B1} = \frac{9.5}{150} = 63.3 \text{ nA}$$

$$I_{B2} = \frac{9.5}{220} = 43.2 \text{ nA}$$

$$I_B = \frac{1}{2}(I_{B1} + I_{B2}) = 53.3 \text{ nA}$$

$$I_{OS} = |I_{B1} - I_{B2}| = 20.1 \text{ nA}$$

**12.39** Refer to Fig. 12.14 and to Exercise 12.21. From the answers to Exercise 12.21, we find that

$$V_{BE17} = 618 \text{ mV}$$

$$I_{E17} \simeq I_{C17} = 550 \,\mu\text{A}$$

$$I_{B17} = \frac{550}{200} = 2.75 \ \mu A$$

Voltage across  $R_9 = V_{BE17} + I_{E17} R_8$ 

$$= 618 + 550 \times 0.1$$

$$= 673 \text{ mV}$$

$$I_{E16} = I_{B17} + \frac{V_{R9}}{R_9}$$

For  $I_{C16} = 9.5 \mu A$ , we have

$$I_{E16} = 9.5 + \frac{9.5}{200} = 9.55 \,\mu\text{A}$$

Thus.

$$9.55 = 2.75 + \frac{673 \text{ (mV)}}{R_9 \text{ (k}\Omega)}$$

$$\Rightarrow R_9 = 98.9 \text{ k}\Omega$$

**12.40** 
$$V_{C1} = V_{CC} - V_{EB8} = 5 - 0.6 = 4.4 \text{ V}$$

 $Q_1$  and  $Q_2$  saturate when  $V_{ICM}$  exceeds  $V_{C1}$  by 0.4 V. Thus.

$$V_{ICM\,\text{max}} = +4.8\,\text{V}$$

$$V_{C5} \simeq -V_{EE} + V_{BE5} + V_{BE7}$$

$$= -5 + 0.6 + 0.6 = -3.8 \text{ V}$$

 $Q_3$  and  $Q_4$  saturate when

$$V_{R3} = V_{C5} - 0.4 = -4.2 \text{ V}$$

Rut

$$V_{B3} = V_{ICM} - V_{BE1} - V_{EB3}$$

$$= V_{ICM} - 1.2$$

Thus,

$$V_{ICM\,\mathrm{min}} = V_{B3} + 1.2$$

$$= -4.2 + 1.2 = -3.0 \text{ V}$$

Thus,

$$-3 \text{ V} \leq V_{ICM} \leq +4.8 \text{ V}$$

**12.41** 
$$I_{C18} + I_{C19} = 0.25 \times 0.73 = 180 \,\mu\text{A}$$

Require

$$I_{C18} = I_{C19} = 90 \,\mu\text{A}$$

$$V_{BE18} = 25 \ln \frac{90 \times 10^{-6}}{10^{-14}}$$

$$= 573 \text{ mV}$$

Current through  $R_{10} = I_{C19} + I_{B19} - I_{B18}$ 

$$\simeq I_{C19} = 90 \,\mu\text{A}$$

$$R_{10} = \frac{573}{90} = 6.4 \text{ k}\Omega$$

$$V_{BB} = V_{BE18} + V_{BE19}$$

$$= 2 \times 0.573 = 1.146 \text{ V}$$

Since  $V_{BB}$  appears across the series combination of  $Q_{14}$  and  $Q_{20}$ , we can write

$$V_{BB} = V_T \ln \frac{I_{C14}}{I_{S14}} + V_T \ln \frac{I_{C20}}{I_{S20}}$$

Substituting  $V_{BB} = 1.146$  V,  $I_{S14} = I_{S20} = 3 \times 10^{-14}$ , we obtain for the equal currents  $I_{C14}$  and  $I_{C20}$ 

$$1.146 = 2 \times 0.025 \ln \frac{I_{C14}}{3 \times 10^{-14}}$$

$$\Rightarrow I_{C14} = I_{C20} = 270 \,\mu\text{A}$$

### 12.42

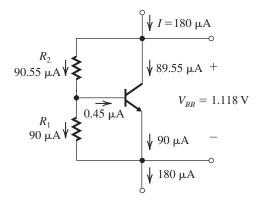


Figure 1

Refer to Fig. 1.

$$I_E = I_{R1} = \frac{180}{2} = 90 \,\mu\text{A}$$

$$I_B = \frac{90}{201} = 0.45 \ \mu A$$

$$I_C = \frac{\beta_N}{\beta_N + 1} I_E$$

$$=\frac{200}{201}\times 90=89.55 \,\mu A$$

$$V_{BE} = V_T \ln \frac{I_C}{I_S}$$

$$=25 \ln \frac{89.55 \times 10^{-6}}{10^{-14}}$$

$$= 573 \text{ mV}$$

$$R_1 = \frac{573 \text{ mV}}{90 \text{ } \mu\text{A}} = 6.37 \text{ k}\Omega$$

$$I_{R2} = I_{R1} + I_B = 90 + 0.45 = 90.45 \,\mu\text{A}$$

$$V_{R2} = V_{BB} - V_{R1} = 1.118 - 0.573$$

$$= 0.545 \text{ V}$$

$$R_2 = \frac{545 \text{ mV}}{90.45 \text{ } \mu\text{A}} = 6.03 \text{ } \text{k}\Omega$$

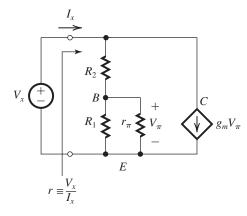


Figure 2

To determine the incremental resistance between the two terminals of the  $V_{BE}$  multiplier, we replace the transistor with its hybrid- $\pi$  model, as shown in Fig. 2. Here

$$g_m = \frac{I_C}{V_T} = \frac{89.55 \,\mu\text{A}}{25 \,\text{mV}} = 3.6 \,\text{mA/V}$$

$$r_{\pi} = \frac{\beta}{g_m} = \frac{200}{3.6} = 55.6 \text{ k}\Omega$$

$$R_1 \parallel r_\pi = 6.37 \parallel 55.6 = 5.7 \text{ k}\Omega$$

$$V_{\pi} = V_{x} \frac{R_{1} \parallel r_{\pi}}{(R_{1} \parallel r_{\pi}) + R_{2}}$$

$$=V_x \frac{5.7}{5.7 + 6.03} = 0.49 \ V_x$$

$$I_x = \frac{V_x}{5.7 + 6.03} + g_m \times 0.49 \ V_x$$

$$= V_x(0.085 + 1.764)$$

$$r \equiv \frac{V_x}{I_x} = \frac{1}{0.085 + 1.764} = 0.541 \text{ k}\Omega$$

$$= 541 \Omega$$

**12.43** Refer to Fig. 12.14 and Table 12.1. The current  $I_{CC}$  drawn from  $V_{CC}$  can be found as follows:

$$I_{CC} = I_{E12} + I_{E13} + I_{C14} + I_{E9} + I_{E8} + I_{C7} + I_{C16}$$

Assuming  $\beta_P$  and  $\beta_N \gg 1$ ,

$$I_{CC} = 730 + 730 + 154 + 19 + 19 + 10.5$$
  
+ 16.2

$$= 1678.7 \ \mu A = 1.68 \ mA$$

$$P_D = I_{CC}(V_{CC} + V_{EE})$$

$$= 1.68(15 + 15) = 50.4 \text{ mW}$$



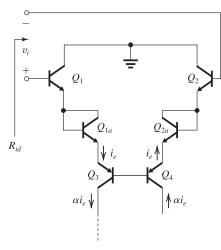


Figure 1

Figure 1 shows the input stage with the two extra diode-connected transistors  $Q_{1a}$  and  $Q_{2a}$ . Since these devices are simply in series with  $Q_1 - Q_4$ , they will have the same dc bias current, namely 9.5  $\mu$ A. Thus, each of  $Q_{1a}$  and  $Q_{2a}$  will have an incremental resistance equal to  $r_e$  of each of  $Q_1$  to  $Q_4$ ,

$$r_e = \frac{25 \text{ mV}}{9.5 \text{ } \mu\text{A}} = 2.63 \text{ } \text{k}\Omega$$

The input differential resistance  $R_{id}$  now becomes

$$R_{id} = (\beta_N + 1) \times 6r_e$$

$$= 201 \times 6 \times 2.63$$

$$= 3.2 \text{ M}\Omega$$

The effective transconductance of the input stage,  $G_{m1}$ , now becomes

$$G_{m1} \equiv \frac{2\alpha i_e}{v_{id}}$$

$$= \frac{2\alpha i_e}{6i_e r_e} = \frac{1}{3}g_{m1}$$

$$= \frac{1}{3} \frac{9.5 \text{ } \mu\text{A}}{25 \text{ } \text{mV}} = 0.13 \text{ } \text{mA/V}$$

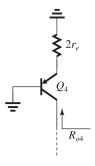


Figure 2

To find  $R_{o4}$ , refer to the circuit in Fig. 2.

$$R_{o4} = r_{o4}[1 + g_{m4}(2 r_e \parallel r_{\pi 4})]$$

where

$$r_{o4} = \frac{50 \text{ V}}{9.5 \text{ } \mu\text{A}} = 5.26 \text{ M}\Omega$$

$$g_{m4} = 0.38 \text{ mA/V}$$

$$r_{\pi 4} = \frac{50}{0.38} = 131.6 \text{ k}\Omega$$

$$R_{o4} = 5.26[1 + 0.38(5.26 \parallel 131.6)]$$

$$= 15.4 \text{ M}\Omega$$

$$R_{o1} = R_{o4} \parallel R_{o6}$$

$$= 15.4 \parallel 18.2 = 8.33 \text{ M}\Omega$$

Open-circuit voltage gain =  $G_{m1}R_{o1}$ 

$$= 0.13 \times 8.33 \times 10^3 = 1083 \text{ V/V}$$

Comparison

	Original Design	Modified Design
$R_{id}$ (k $\Omega$ )	2.1	3.2
$G_{m1}$ (mA/V)	0.19	0.13
$R_{o4} (\mathrm{M}\Omega)$	10.5	15.4
$R_{o1}$ (M $\Omega$ )	6.7	8.3
A <sub>vo</sub>   (V/V)	1273	1083

Thus the input resistance increases but the gain decreases: The additional diodes introduce negative feedback in the input stage; same effect as adding a resistance in the emitter of a common-emitter amplifier.

12.45 From Fig. 12.20(b) and Eq. (12.91), we get

$$R_{o6} = r_{o6}[1 + g_{m6}(R_2 \parallel r_{\pi 6})]$$

where

$$r_{o6} = \frac{125 \text{ V}}{9.5 \text{ } \mu\text{A}} = 13.6 \text{ M}\Omega$$

$$g_{m6} = \frac{9.5 \text{ } \mu\text{A}}{25 \text{ mV}} = 0.38 \text{ mA/V}$$

$$r_{\pi 6} = \frac{200}{0.38} = 526.3 \text{ k}\Omega$$

$$\frac{R_{o6}(\text{modified})}{R_{o6}(\text{original})} = \frac{1 + 0.38(R'_2 \parallel 526.3)}{1 + 0.38(1 \parallel 526.3)}$$

$$2 \simeq \ \frac{1 + 0.38 \ R_2'}{1 + 0.38}$$

$$\Rightarrow R'_2 = 4.63 \text{ k}\Omega$$

Thus,  $R_2$  must be increased by a factor of 4.63.

**12.46** Refer to Fig. 12.19.

(a) 
$$v_{b6} = i_{e6}(r_{e6} + R_2)$$

$$= i_e(r_{e6} + R_2)$$

where

$$r_{e6} = \frac{25 \text{ mV}}{9.5 \text{ } \mu\text{A}} = 2.63 \text{ } \text{k}\Omega$$

$$v_{b6} = i_e(2.63 + 2) = 4.63 \text{ k}\Omega \times i_e$$

(b) 
$$i_{e7} = i_{R3} + i_{b5} + i_{b6}$$

$$=\frac{v_{b6}}{R_3}+\frac{2\alpha i_e}{\beta}$$

$$=\frac{4.63}{50}i_e+\frac{2}{201}i_e$$

$$= 0.1i$$

(c) 
$$i_{b7} = \frac{i_{e7}}{\beta_N + 1} = \frac{0.1}{201}i_e = 0.0005i_e$$

(d) 
$$v_{b7} = i_{e7}r_{e7} + v_{b6}$$

$$= 0.1 \times 2.38i_e + 4.63i_e$$

$$= 4.89i_e$$

(e) 
$$R_{\rm in} \equiv \frac{v_{b7}}{\alpha i_e} \simeq 4.9 \text{ k}\Omega$$

**12.47** Output current of first stage = (1 - 0.8)I

$$= 0.2I$$

$$V_{OS} = \frac{0.2I}{G_{m1}}$$

where

$$G_{m1} = \frac{1}{2}g_{m1} = \frac{1}{2}\frac{I}{V_T}$$

Thus,

$$V_{OS} = \frac{0.2I}{0.5I/V_T}$$

$$= 0.4 \times V_T = 10 \text{ mV}$$

**12.48** Refer to Fig. 12.22 which shows the situation when  $R_1 = R$  and  $R_2 = R + \triangle R$ . The result of this mismatch is an output current  $\triangle I$  given by Eq. (12.94):

$$\Delta I = I \frac{\Delta R}{R + \Delta R + r_e} \tag{1}$$

If we have an input offset voltage  $V_{OS}$ , this offset results in an output current  $\Delta I$  given by

$$\Delta I = G_{m1} V_{OS} \tag{2}$$

The offset can be nulled by introducing a mismatch  $\triangle R$  that results in an equal magnitude and opposite polarity output current. The required  $\triangle R$  can be found by equating (1) and (2), thus

$$I\frac{\Delta R}{R + \Delta R + r_a} = G_{m1}V_{OS}$$

Substituting for  $G_{m1}$  by

$$G_{m1} = \frac{1}{2}g_{m1} = \frac{1}{2}\frac{I}{V_T}$$

we obtain

$$\begin{split} I \frac{\Delta R}{R + \Delta R + r_e} &= \frac{1}{2} \frac{I}{V_T} V_{OS} \\ \Rightarrow \frac{\Delta R}{R} &= \frac{V_{OS}}{2V_T} \frac{1 + r_e/R}{1 - V_{OS}/2V_T} \end{split} \quad \text{Q.E.D.}$$

(b) For 
$$V_{OS} = 3 \text{ mV}$$
 and recalling that

$$r_e = \frac{25 \text{ mV}}{9.5 \text{ } \mu\text{A}} = 2.63 \text{ k}\Omega \text{ and } R = 1 \text{ k}\Omega$$

ther

$$\frac{\Delta R}{R} = \frac{3}{2 \times 25} \, \frac{1 + (2.63/1)}{1 - (3/50)}$$

$$\frac{\triangle R}{R} = 0.23$$

or 23%

For 
$$V_{OS} = -3$$
 mV, we have

$$\frac{\triangle R}{R} = -0.205 \text{ or } -20.5\%$$

(c) The maximum offset voltage than can be trimmed this way corresponds to  $R_2$  completely shorted, that is,  $\triangle R = -R$ , thus

$$-1 = \frac{V_{OS}}{2V_T} \frac{1 + 2.63}{1 - \frac{V_{OS}}{2V_T}}$$

$$\Rightarrow V_{OS} = -\frac{2V_T}{2.63} = -19 \text{ mV}$$

# 12.49

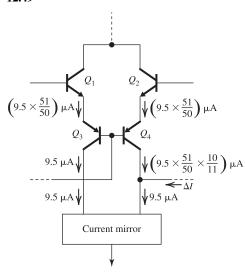


Figure 1

Figure 1 (see preceding page) shows the analysis when the  $\beta$  of  $Q_4$  is reduced to 10. The output current of the mirror is

$$\Delta I = 0.691 \,\mu\text{A}$$

which corresponds to an input offset voltage of

$$V_{OS} = \frac{\Delta I}{G_{m1}}$$
, where  $G_{m1} = \frac{1}{2}g_{m1} = 0.19 \text{ mA/V}$ 

Thus.

$$V_{OS} = \frac{0.691}{0.19} = 3.6 \text{ mV}$$

#### **12.50** From Eq. (12.102) we have

$$CMRR = g_{m1}(R_{o9} \parallel R_{o10})/\epsilon_m$$

where

$$g_{m1} = 0.38 \text{ mA/V}$$

$$R_{o9} = 2.63 \text{ M}\Omega$$

$$R_{o10} = 31.1 \text{ M}\Omega$$

$$\epsilon_m = 1 - 0.995 = 0.005$$

Thus,

CMRR = 
$$0.38(2.63 \parallel 31.3) \times 10^3 / 0.005$$

$$= 1.84 \times 10^5$$

or 105.3 dB

# **12.51** Refer to Fig. 12.19.

(a) If  $R_1$  is short-circuited, the incremental transfer ratio of the mirror can be found as follows:

$$i_{e5}r_{e5} = i_{e6}(r_{e6} + R_2)$$

Thus,

$$\frac{i_{c6}}{i_{c5}} = \frac{i_{e6}}{i_{e5}} = \frac{r_{e5}}{r_{e5} + R_2} = \frac{2.63}{2.63 + 1}$$

Thus, the output current of the mirror becomes

$$i_o = 1.72\alpha i_e$$

rather than  $2\alpha i_e$ . Thus, the gain of the 741 will be reduced by a factor of  $\frac{1.72}{2} = 0.86$ .

(b) If  $R_2$  is short-circuited, then

$$i_{e5}(r_{e5} + R_1) = i_{e6}r_{e6}$$
  

$$\Rightarrow \frac{i_{c6}}{i_{c5}} = \frac{i_{e6}}{i_{e5}} = \frac{r_{e5} + R_1}{r_{e6}}$$

$$=\frac{2.63+1}{2.63}=1.38$$

Thus,  $i_o$  of the mirror becomes

$$i_o = 2.38\alpha i_e$$

with the result that the gain of the 741 increases by a factor of  $\frac{2.38}{2} = 1.19$ .

(c) If both  $R_1$  and  $R_2$  are shorted, the gain remains unchanged.

**12.52** Please note that an error occurred in the first printing of the text:  $Q_9$  is biased at 19  $\mu$ A. With a resistance R in the emitter of  $Q_9$ ,  $R_{o9}$  becomes

$$R_{o9} = r_{o9}[1 + g_{m9}(R \parallel r_{\pi 9})]$$

where

$$r_{o9} = \frac{|V_{Ap}|}{I_{C9}} = \frac{50 \text{ V}}{19 \text{ }\mu\text{A}} = 2.63 \text{ M}\Omega$$

$$g_{m9} = \frac{I_{C9}}{V_T} = \frac{19 \,\mu\text{A}}{0.025 \,\text{V}} = 0.76 \,\text{mA/V}$$

$$r_{\pi 9} = \frac{\beta_P}{g_{m9}} = \frac{50}{0.76} = 65.8 \text{ k}\Omega$$

Thus, to obtain  $R_{o9} = R_{o10} = 31.1 \text{ M}\Omega$ , we use

$$31.1 = 2.63[1 + 0.76(R \parallel 65.8)]$$

$$\Rightarrow R = 18.2 \text{ k}\Omega$$

Thus,  $R_o$  to the left of node Y becomes

$$R_o = 31.1 \text{ M}\Omega \parallel 31.1 \text{ M}\Omega = 15.55 \text{ M}\Omega$$

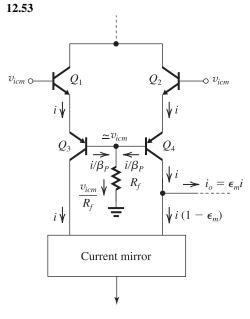


Figure 1

Figure 1 (see previous page) shows the input stage with the approach suggested for determining  $G_{ncm}$ . Here

$$R_f = R_o(1 + A\beta) = R_o(1 + \beta_P) \simeq \beta_P R_o$$

A node equation at the common bases of the  $Q_3$  and  $Q_4$  yields

$$\begin{split} &\frac{2i}{\beta_P} = \frac{v_{icm}}{R_f} \\ &\Rightarrow i = \frac{\beta_P}{2R_f} v_{icm} \\ &= \frac{\beta_P}{2\beta_P R_o} v_{icm} \\ &= \frac{v_{icm}}{2R_o} \end{split}$$

Thus,

$$i_o = \epsilon_m i = \frac{\epsilon_m}{2R_o} v_{icm}$$

and

$$G_{mcm} \equiv rac{i_o}{v_{icm}} = rac{\epsilon_m}{2R_o}$$

which is the same result [Eq. (12.100)] obtained by the alternative approach of Example 12.5.

**12.54** Refer to the results of Exercise 12.32. We need to raise  $r_{o13B}$  from 90.9 k $\Omega$  to 722 k $\Omega$  by inserting a resistance  $R_{13B}$  in the emitter of  $Q_{13B}$ . Since

$$R_{o13B} = r_{o13B}[1 + g_{m13B}(R_{13B} \parallel r_{\pi 13B})]$$

where

$$r_{o13B} = 90.9 \text{ k}\Omega$$
  
 $g_{m13B} = \frac{0.55 \text{ mA}}{0.025 \text{ V}} = 22 \text{ mA/V}$ 

$$r_{\pi 13B} = \frac{\beta_P}{g_{m13B}} = \frac{50}{22} = 2.27 \text{ k}\Omega$$

Thus,

$$722 = 90.9[1 + 22(R_{13B} \parallel 2.27)]$$

$$\Rightarrow R_{13B} = 366 \Omega$$

The resistors in the emitters of  $Q_{13A}$  and  $Q_{12}$  must be of values that will result in

$$I_{E13B}R_{13B} = I_{E12}R_{12} = I_{E13A}R_{13A}$$

Thus,

$$R_{13A} = \frac{I_{E13B}}{I_{E13A}} R_{13B}$$

$$= \frac{I_{C13B}}{I_{C13A}} R_{13B}$$

$$= \frac{550}{180} \times 366 = 1.12 \text{ k}\Omega$$

$$R_{12} = \frac{I_{E13B}}{I_{E12}} R_{13B}$$

$$= \frac{I_{C13B}}{I_{C12}} R_{13B}$$

$$= \frac{550}{730} \times 366 = 275 \Omega$$

12.55 Using Eq. (12.110), we obtain

$$v_{O\text{max}} = V_{CC} - |V_{CE\text{sat}}| - V_{BE14}$$
  
= 5 - 0.2 - 0.6 = +4.2 V  
Using Eq. (12.111), we get  
 $v_{O\text{min}} = -V_{EE} + |V_{CE\text{sat}}| + V_{EB23} + V_{BE20}$   
= -5 + 0.2 + 0.6 + 0.6 = -3.6 V

Thus,

$$-3.6 \text{ V} \le v_O \le +4.2 \text{ V}$$

12.56 Refer to Fig. P12.56.

$$R_{\text{out}} = r_{e14} + \frac{r_{AA} + r_{e23} + [R_{o2}/(\beta_P + 1)]}{\beta_{14} + 1}$$

where

$$r_{e14} = \frac{25 \text{ mV}}{5 \text{ mA}} = 5 \Omega$$

$$r_{AA} = 163 \Omega$$

$$r_{e23} = \frac{25 \text{ mV}}{0.18 \text{ mA}} = 139 \Omega$$

$$R_{o2} = 81 \text{ k}\Omega$$

$$\beta_{P} = 50$$

$$\beta_{14} = 200$$

Γhus

$$R_{\text{out}} = 5 + \frac{163 + 139 + (81000/51)}{201}$$
  
= 14.4 \Omega

**12.57** Refer to Fig. 12.25 and Example 12.6 with  $Q_{23}$  having its emitter and base shorted together. In such a situation the input resistance of the output stage becomes

$$R_{\text{in}3} = (\beta_{20}R_L) \parallel (r_{o13A} + r_{AA}) \tag{1}$$

where we have assumed the situation with  $v_O$  negative and  $Q_{20}$  supplying the load current.

In Eq. (1),

 $\beta_{20} = 50$ 

 $R_L = 2 \text{ k}\Omega$ 

$$r_{o13A} = \frac{|V_{Ap}|}{I_{C13A}} = \frac{50}{0.18} = 280 \text{ k}\Omega$$

and  $r_{AA}$  is the incremental resistance of the  $Q_{18}-Q_{19}$  bias network; very small ( $\simeq 160~\Omega$ ). Thus.

$$R_{\rm in3} \simeq (50 \times 2) \parallel 280$$

 $=74 \text{ k}\Omega$ 

The gain of the second stage becomes

$$A_2 = \frac{v_{i3}}{v_{i2}} = -G_{m2}R_{o2} \frac{R_{in3}}{R_{in3} + R_{o2}}$$
$$= -6.5 \times 81 \times \frac{74}{74 + 81}$$
$$= -215.4 \text{ V/V}$$

Compare to the value with  $Q_{23}$  included (-515 V/V).

## 12.58

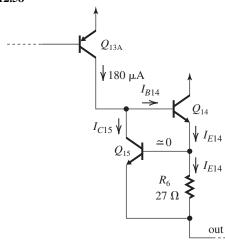


Figure 1

Refer to Fig. 1.

Iteration #1:

$$I_{C15} = 180 \, \mu A$$

$$V_{BE15} = 25 \ln \frac{180 \times 10^{-6}}{10^{-14}} = 590 \text{ mV}$$

$$I_{E14} = \frac{V_{BE15}}{R_6} = \frac{590 \text{ mV}}{27 \Omega} = 21.85 \text{ mA}$$

$$I_{B14} = \frac{I_{E14}}{\beta_N + 1} = \frac{21.85}{201} = 108.7 \,\mu\text{A}$$

Iteration #2:

$$I_{C15} = 180 - I_{B14} = 180 - 108.7 = 71.3 \,\mu\text{A}$$

$$V_{BE15} = 25 \ln \frac{71.3 \times 10^{-6}}{10^{-14}} = 567.2 \text{ mV}$$

$$I_{E14} = \frac{567.2}{27} = 21 \text{ mA}$$

$$I_{B14} = \frac{21 \text{ mA}}{201} = 104.5 \text{ } \mu\text{A}$$

Iteration #3:

$$I_{C15} = 180 - 104.5 = 75.5 \,\mu\text{A}$$

$$V_{BE15} = 25 \ln \frac{75.5 \times 10^{-6}}{10^{-14}} = 568.6$$

$$I_{E14} = \frac{568.6}{27} = 21.06 \text{ mA}$$

which is very close to the value found in Iteration #2; thus, no further iterations are necessary and

$$I_{E14} \simeq 21 \text{ mA}$$

## 12.59 Refer to Fig. 12.14.

Maximum current available from input stage =  $19 \mu A$ 

$$I_{C22} = 19 \,\mu\text{A}$$

$$V_{BE22} = 25 \ln \frac{19 \times 10^{-6}}{10^{-14}}$$

$$= 534 \text{ mV}$$

$$V_{BE24} = 534 \text{ mV}$$

$$I_{C24} = 19 \, \mu A$$

$$I_{R11} = \frac{534 \text{ mV}}{50 \text{ k}\Omega} = 10.7 \text{ } \mu\text{A}$$

$$I_{C21} = I_{C24} + I_{R11}$$

$$= 19 + 10.7 = 29.7 \mu A$$

$$V_{EB21} = 25 \ln \frac{29.7 \times 10^{-6}}{10^{-14}}$$

$$= 545.3 \text{ mV}$$

$$I_{R7} = \frac{545.3}{27} = 20.2 \text{ mA}$$

This is the maximum current that the 741 can sink. To reduce this current limit to 10 mA, we need to double the value of  $R_7$ .

**12.60** The factor 0.97 is simply

$$= \frac{R_L}{R_L + R_{\text{out}}}$$

Thus, for  $R_L = \infty$ ,

$$A_0 = 243, 147/0.97 = 250,667 \text{ V/V}$$

This is the open-circuit voltage gain. The output resistance is found from

$$\frac{2}{2 + R_{\text{out}}} = 0.97$$

$$\Rightarrow R_{\text{out}} = 62 \ \Omega$$

The gain with  $R_L = 500 \Omega$  is

$$A_0 = 250,667 \times \frac{500}{500 + 62}$$

$$= 223,013 \text{ V/V}$$

**12.61** If the phase margin is  $80^{\circ}$ , the phase due to the second pole  $f_{P2}$  at the unity gain frequency  $f_t$  must be  $10^{\circ}$ . Thus,

$$\tan^{-1}\frac{f_t}{f_{P2}} = 10^\circ$$

Since  $f_t = 1$  MHz,

$$f_{P2} = \frac{1 \text{ MHz}}{\tan 10^{\circ}} = 5.67 \text{ MHz}$$

**12.62** The phase introduced at  $f_t = 1$  MHz by each of the coincident second and third poles must be 5°. Thus,  $f_{P2} = f_{P3}$  can be obtained from

$$\tan^{-1}\frac{f_t}{f_{P2}} = 5^\circ$$

$$\Rightarrow f_{P2} = f_{P3} = \frac{1 \text{ MHz}}{\tan 5^{\circ}} = 11.4 \text{ MHz}$$

**12.63** 
$$f_P = \frac{f_t}{A_0} = \frac{5 \text{ MHz}}{10^6} = 5 \text{ Hz}$$

But,

$$f_P = \frac{1}{2\pi CR}$$

where

$$C = (1 + |A|)C_C$$

$$= (1 + 1000) \times 50$$

$$= 50.05 \; nF$$

$$5 = \frac{1}{2\pi \times 50.05 \times 10^{-9} \times R}$$

$$\Rightarrow R = 636 \text{ k}\Omega$$

12.64

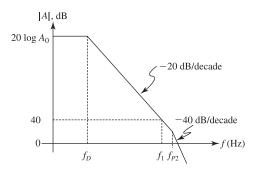


Figure 1

For a phase margin of  $85^{\circ}$  with a closed loop gain of 100, the phase at  $f_1$  due to the pole at 5 MHz must be at most  $5^{\circ}$ ; thus,

$$\tan^{-1}\frac{f_1}{5 \text{ MHz}} = 5^{\circ}$$

$$\Rightarrow f_1 = 5 \times \tan 5^\circ = 437 \text{ kHz}$$

Thus, the new dominant pole must be at  $f_D$ ,

$$f_D \times \frac{A_0}{100} = 437$$

$$f_D \times \frac{243,147}{100} = 437$$

$$\Rightarrow f_D = 180 \text{ Hz}$$

To find the required value of  $C_C$ , we use Eq. (12.116) to determine  $C_{in}$ :

$$C_{\rm in} = C_C(1 + |A_2|)$$

$$= C_C \times 516$$

Then,

$$f_D = \frac{1}{2\pi C_{\rm in} R_t}$$

$$R_t = 2.5 \text{ M}\Omega$$

$$180 = \frac{1}{2\pi \times 516C_C \times 2.5 \times 10^6}$$

$$\Rightarrow C_C = 0.7 \text{ pF}$$

**12.65** DC gain 
$$A_0 = G_{m1}R$$

$$= 2 \times 10^{-3} \times 2 \times 10^{7}$$

$$= 4 \times 10^4 \text{ V/V}$$

$$20 \log A_0 = 92 \text{ dB}$$

$$f_P = \frac{1}{2\pi C_C R}$$
=\frac{1}{2\pi \times 100 \times 10^{-12} \times 2 \times 10^7}
= 79.6 \text{ Hz} \simes 80 \text{ Hz}
$$f_t = A_0 f_P = 4 \times 10^4 \times 80$$
= 3.2 MHz

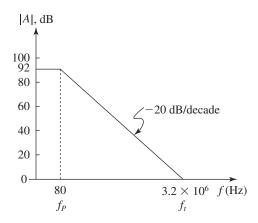


Figure 1

Figure 1 shows a sketch of the Bode plot for the magnitude of the open-loop gain of the op amp.

$$SR = \frac{I}{C_C}$$

But

$$G_{m1} = \frac{I}{2V_T}$$

Thus,

$$I = 2V_T G_{m1}$$

and

$$SR = 2V_T \frac{G_{m1}}{C_C}$$
  
=  $2 \times 25 \times 10^{-3} \times \frac{2 \times 10^{-3}}{100 \times 10^{-12}}$   
=  $1 \text{ V/}\mu\text{s}$ 

12.66 For a sine-wave output, we have

$$v_O = \hat{V}_o \sin \omega t$$

$$\frac{d v_O}{dt} = \omega \hat{V}_o \cos \omega t$$

$$\frac{d v_O}{dt} \bigg|_{\text{max}} = \omega \hat{V}_o$$

$$10 \times 10^6 = \omega_M \times 10$$

$$\omega_M = 10^6 \text{ rad/s}$$

$$f_M = \frac{10^6}{2\pi} = 159.2 \text{ kHz}$$

If the topology is similar to that of the 741, then we can use Eq. (12.126),

$$SR = 4V_T\omega_t$$

$$\Rightarrow \omega_t = \frac{SR}{4V_T} = \frac{10 \times 10^6}{4 \times 25 \times 10^{-3}}$$

$$=10^8$$
 rad/s

$$f_t = \frac{10^8}{2\pi} = 15.9 \text{ MHz}$$

**12.67** Including a resistance  $R_E$  in the emitter of each of  $Q_3$  and  $Q_4$  cause  $G_{m1}$  to become

$$G_{m1} = \frac{2}{4r_e + 2R_E}$$
$$= \frac{1}{2r_+ + R_-}$$

where  $r_e$  is the emitter resistance of each of  $Q_1 - Q_4$ ,

$$r_e = \frac{V_T}{I}$$

Thus

$$G_{m1} = \frac{I}{2V_T + IR_E} \tag{1}$$

The slew rate is still given by (12.125),

$$SR = \frac{2I}{C_C} \tag{2}$$

Also, the model in Fig. 12.30 still applies; thus,

$$\omega_t = \frac{G_{m1}}{C_C} \tag{3}$$

Equations (1)–(3) can be combined to obtain

$$SR = \frac{2I}{C_C} = \frac{2G_{m1}(2V_T + IR_E)}{C_C}$$

$$=2\omega_t(2V_T+IR_E)$$

$$=4(V_T+IR_E/2)\omega_t \qquad Q.E.D.$$

Since for the 741

$$SR = 4V_T \omega_t$$

to double SR while keeping  $\omega_t$  unchanged, we select

$$\frac{1}{2}IR_E = V_T$$

If we also keep I unchanged, then

$$R_E = \frac{2V_T}{I} = \frac{2 \times 25 \times 10^{-3}}{9.5 \times 10^{-6}}$$

$$= 5.26 \text{ k}\Omega$$

From Eq. (1), the new value of  $G_{m1}$  is

$$G_{m1} = \frac{I}{2V_T + IR_E}$$
$$= \frac{I}{2V_T + 2V_T} = \frac{I}{4V_T}$$

which is half the original value. From Eq. (3), we see that  $C_C$  will have to be one half the original value, thus

$$C_C = 15 \text{ pF}$$

This result could have been obtained also from  $SR = I/C_C$ ; doubling SR with I unchanged requires halving  $C_C$ . Now, with  $G_{m1}$  half the original value, the dc gain also will be half the original value,

$$A_0 = \frac{1}{2} \times 243,147 = 121,573 \text{ V/V}$$

or 101.7 dB

Finally, since

$$f_P = \frac{f_t}{A_0}$$

halving  $A_0$  with  $f_t$  unchanged means  $f_P$  is doubled,

$$f_P = 8.2 \text{ Hz}$$

This is a result of  $C_C$  in Eq. (12.116) being is halved and thus  $f_P$  in Eq. (12.118) is doubled.

**12.68** (a) Refer to Fig. P12.68.

$$I_{C1} = I_{C2} = I_{C3} = I_{C4} = 0.05 \text{ mA}$$

$$I_{C5} = 1 \text{ mA}$$

$$I_{C7} = I_{C6} = I_{C5} = 1 \text{ mA}$$

(b) For  $Q_1$  and  $Q_2$ , we have

$$g_m = \frac{0.05 \text{ mA}}{0.025 \text{ V}} = 2 \text{ mA/V}$$

$$r_{\pi} = \frac{\beta}{g_m} = \frac{100}{2} = 50 \text{ k}\Omega$$

$$R_{id} = 2r_{\pi} = 100 \text{ k}\Omega$$

(c) Figure 1 shows the small-signal analysis where

$$i_e = \frac{v_i}{2r_{e1,2}}$$

$$v_o = (\beta + 2)\beta\alpha i_e R_L$$

$$A_v = \frac{v_o}{v_i} = \frac{(\beta + 2)\beta\alpha R_L}{2r_{e1,2}}$$

$$A_v \simeq rac{1}{2} eta^2 rac{R_L}{r_{e1.2}}$$

where

$$r_{e1,2} = \frac{25 \text{ mV}}{0.05 \text{ mA}} = 0.5 \text{ k}\Omega$$

This figure belongs to Problem 12.68, part (c).

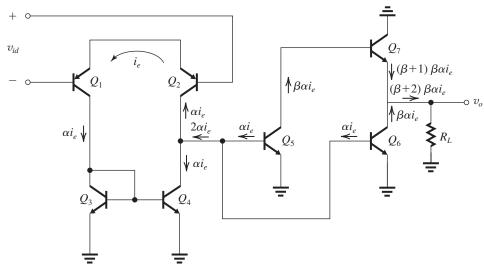


Figure 1

$$A_v = \frac{1}{2}100^2 \times \frac{5}{0.5} = 5 \times 10^4 \text{ V/V}$$

or 94 dB

(d)

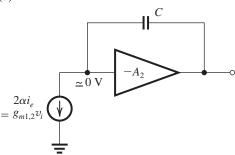


Figure 2

Replacing the second stage with an amplifier having a large negative gain, we obtain the equivalent circuit shown in Fig. 2. From this equivalent circuit we see that the gain is approximately given by

$$A(s) = \frac{g_{m1,2}}{sC}$$

Thus, the unity gain frequency  $\omega_t$  is given by

$$\omega_t = \frac{g_{m1,2}}{C}$$

and the 3-dB frequency  $\omega_P$  is

$$\omega_P = \frac{\omega_t}{A_0} = \frac{g_{m1,2}}{A_0 C}$$

$$f_P = \frac{g_{m1,2}}{2\pi A_0 C}$$

For  $f_P = 100$  Hz and substituting  $g_{m1,2} = 2$  mA/V and  $A_0 = 5 \times 10^4$ , we find

$$C = \frac{2 \times 10^{-3}}{2\pi \times 100 \times 5 \times 10^{4}}$$
$$= 63.7 \text{ pF}$$

**12.69** 
$$I = 5 \mu A$$

$$\frac{I_{S2}}{I_{S1}} = 4$$

Using Eq. (12.127), we obtain

$$I = \frac{V_T}{R_2} \ln \left( \frac{I_{S2}}{I_{S1}} \right)$$

$$5 \times 10^{-3} = \frac{0.025}{R_2} \ln 4$$

$$\Rightarrow R_2 = 6.93 \text{ k}\Omega$$

$$R_3 = R_4 = \frac{0.15 \text{ V}}{0.005 \text{ mA}} = 30 \text{ k}\Omega$$

**12.70** For 
$$I_5 = 10 \,\mu\text{A} = I$$
, then

$$\frac{Q_5 \text{ emitter area}}{Q_1 \text{ emitter area}} = 1$$

For 
$$I_6 = 40 \,\mu\text{A} = 4I$$
, then

$$\frac{Q_6 \text{ emitter area}}{Q_1 \text{ emitter area}} = 4$$

If we connect a resistance  $R_6$  in the emitter of  $Q_6$ , then  $I_6$  changes to a new value determined as follows:

$$V_{BE6} + I_6 R_6 = V_{BE1}$$

$$I_6R_6=V_{BE1}-V_{BE6}$$

$$= V_T \ln \frac{I}{I_{S1}} - V_T \ln \frac{I_6}{I_{S6}}$$

But  $I_6$  is to be equal to I, thus

$$IR_6 = V_T \ln \frac{I_{S6}}{I_{S1}}$$

$$R_6 = \frac{V_T}{I} \ln 4$$

$$\Rightarrow R_6 = \frac{0.025}{0.01} \ln 4 = 3.47 \text{ k}\Omega$$

If the  $V_{\rm BIAS1}$  line has a low incremental resistance to ground, then

$$R_{o5} = r_{o5} = \frac{V_{An}}{I_5} = \frac{30 \text{ V}}{10 \mu\text{A}} = 3 \text{ M}\Omega$$

$$R_{o6} = r_{o6} + (R_6 \parallel r_{\pi 6})(1 + g_{m6}r_{o6})$$

where

$$r_{o6} = \frac{30 \text{ V}}{10 \text{ } \mu\text{A}} = 3 \text{ M}\Omega$$

$$g_{m6} = \frac{10 \text{ } \mu\text{A}}{0.025 \text{ V}} = 0.4 \text{ mA/V}$$

$$r_{\pi 6} = \frac{\beta_N}{g_{m6}} = \frac{40}{0.4} = 100 \text{ k}\Omega$$

$$R_{o6} = 3 + (3.47 \parallel 100) \times 10^{-3} (1 + 1200)$$

$$R_{o6} = 3 + 4 = 7 \text{ M}\Omega$$

Thus, increasing the BEJ area by a factor of 4 and adding a resistance  $R_6$  to restore the current to the desired value of 10  $\mu$ A increases the output resistance by a factor of about 2.5!

**12.71** (a) The bias current I of the differential pair is given by Eq. (12.127),

$$I = \frac{V_T}{R_5} \ln \left( \frac{I_{S5}}{I_{S1}} \right) \tag{1}$$

The voltage gain of the differential pair is given by

$$A_d = g_m R_C$$

where  $g_m$  is the transconductance of each of the two transistors in the differential pair,

$$g_m = \frac{I/2}{V_T} = \frac{I}{2V_T}$$

Thus,

$$A_d = \frac{IR_C}{2V_T} \tag{3}$$

Substituting for I from Eq. (1) into Eq. (3), we obtain

$$A_d = \frac{1}{2} \frac{R_C}{R_5} \ln \left( \frac{I_{S5}}{I_{S2}} \right) \tag{4}$$

which indicates that  $A_d$  will be independent of temperature!

(b) 
$$I = 20 \text{ } \mu\text{A}, \ A_d = 10 \text{ V/V}, \ \frac{I_{S5}}{I_{S1}} = 4$$

Using Eq. (1), we obtain

$$20 \times 10^{-3} = \frac{0.025}{R_5} \ln 4$$

$$\Rightarrow R_5 = 1.73 \text{ k}\Omega$$

Using Eq. (4), we get

$$10 = \frac{1}{2} \frac{R_C}{1.73} \ln 4$$

$$\Rightarrow R_C = 25 \text{ k}\Omega$$

12.72 (a) Refer to Fig. 12.35(a).

$$V_{ICM\,\mathrm{min}} = V_{C1} - 0.6$$

$$= 0.7 - 0.6 = 0.1 \text{ V}$$

$$V_{ICM\,\text{max}} = V_{CC} - 0.1 - 0.7$$

$$= 3 - 0.8 = 2.2 \text{ V}$$

Thus,

$$0.1~\mathrm{V} \leq V_{ICM} \leq 2.2~\mathrm{V}$$

(b)

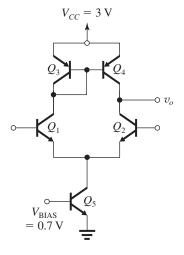


Figure 1

Figure 1 shows the complementary circuit to that in Fig. 12.33(a).

Here,

$$0.8 \text{ V} \leq V_{ICM} \leq 2.9 \text{ V}$$

12.73 Refer to Fig. 12.35(b).

$$V_{ICM\,\text{max}} = V_{CC} - 0.1 - 0.7 = 3 - 0.8$$

$$= +2.2 \text{ V}$$

$$V_{ICM\,\text{min}} = \frac{1}{2}I_{RC} - 0.6$$

$$= \frac{1}{2} \times 0.02 \times 25 - 0.6$$

$$= -0.35 \text{ V}$$

Thus,

$$-0.35 \text{ V} \le V_{ICM} \le +2.2 \text{ V}$$

$$A_v = g_m R_C$$

$$g_m = \frac{I_C}{V_T} = \frac{10 \times 10^{-6}}{25 \times 10^{-3}} = 0.4 \text{ mA/V}$$

$$A_v = 0.4 \times 25 = 10 \text{ V/V}$$

12.74 
$$g_m = \frac{I/2}{V_T} = \frac{20 \text{ }\mu\text{A}}{25 \text{ mV}} = 0.8 \text{ mA/V}$$

For 
$$A_d = 10$$
 V/V, we have

$$10 = g_m R_C$$

$$\Rightarrow R_C = 12.5 \text{ k}\Omega$$

$$\frac{I}{2}R_C = 20 \times 10^{-3} \times 12.5 = 0.25 \text{ V}$$

 $V_{ICM \min} = 0.8 \text{ V}$ 

$$V_{ICM\,\text{max}} = V_{CC} - \frac{I}{2}R_C + 0.6$$

$$= 3 - 0.25 + 0.6 = 3.35 \text{ V}$$

Thus,

$$0.8 \text{ V} \le V_{ICM} \le 3.35 \text{ V}$$

$$R_{id} = 2r_{\pi} = 2\frac{\beta_N}{g_m}$$

$$=2\frac{40}{0.8}=100 \text{ k}\Omega$$

To increase  $R_{id}$  by a factor of 4,  $g_m$  and hence I must be reduced by a factor of 4, thus  $I_{C6}$  becomes

$$I_{C6} = 10 \, \mu A$$

To keep the gain and the permissable range of  $V_{ICM}$  unchanged,  $R_C$  must be increased by a factor of 4, thus  $R_C$  becomes

$$R_C = 50 \text{ k}\Omega$$

**12.75** Refer to Fig. 12.38, which shows the differential half-circuit of the differential amplifier of Fig. 12.37.

$$R_{id} = 2r_{\pi 1} = 2\frac{\beta_P}{q_{m1}}$$

where

$$g_{m1} = \frac{I_{C1}}{V_T} = \frac{4 \times 10^{-6}}{25 \times 10^{-3}} = 0.16 \text{ mA/V}$$

Thus,

$$R_{id} = \frac{2 \times 10}{0.16} = 125 \text{ k}\Omega$$

The short-circuit transconductance  $G_{m1}$  can be found from Fig. 12.38(b):

$$G_{m1} = \frac{i_o}{v_{id}/2}$$

At node X we have four resistances to ground:

$$r_{o1} = \frac{|V_{Ap}|}{I_{C1}} = \frac{20 \text{ V}}{4 \mu \text{A}} = 5 \text{ M}\Omega$$

$$R_7 = 22 \text{ k}\Omega$$

$$r_{o7} = \frac{|V_{An}|}{I_{C7}} = \frac{30 \text{ V}}{8 \text{ } \mu\text{A}} = 3.75 \text{ M}\Omega$$

$$r_{e7} \simeq \frac{1}{g_{m7}} = \frac{V_T}{I_{C7}} = \frac{25 \text{ mV}}{8 \mu \text{A}} = 3.125 \text{ k}\Omega$$

Obviously,  $r_{o1}$  and  $r_{o7}$  are much larger than  $r_{e7}$  and  $R_7$ . Then, the portion of  $g_{m1}(v_{id}/2)$  that flows into the emitter proper of  $Q_7$  can be found from

$$i_{e7} \simeq g_{m1} \left( \frac{V_{id}}{2} \right) \frac{R_7}{R_7 + r_{e7}}$$

$$=g_{m1}\left(\frac{V_{id}}{2}\right)\frac{22}{22+3.125}$$

$$=0.876g_{m1}\left(\frac{V_{id}}{2}\right)$$

Thus,

$$G_{m1}\equiv rac{i_o}{V_{id}/2}=rac{lpha i_{e7}}{V_{id}/2}$$

$$= 0.876g_{m1} = 0.137 \text{ mA/V}$$

The total resistance between the output node and ground for the circuit in Fig. 12.38(a) is

$$R = R_{o9} \parallel R_{o7} \parallel (R_L/2)$$

The resistances  $R_{o9}$  is the output resistance of  $Q_9$ , which has an emitter-degeneration resistance  $R_9$ . Thus,

$$R_{o9} = r_{o9} + (R_9 \parallel r_{\pi 9})(1 + g_{m9}r_{o9})$$

where

$$r_{o9} = \frac{|V_{Ap}|}{I_{C9}} = \frac{20 \text{ V}}{8 \mu \text{A}} = 2.5 \text{ M}\Omega$$

$$g_{m9} = \frac{I_{C9}}{V_T} = \frac{8 \mu A}{25 \text{ mV}} = 0.32 \text{ mA/V}$$

$$r_{\pi 9} = \frac{\beta_P}{g_{m9}} = \frac{10}{0.32} = 31.25 \text{ k}\Omega$$

Thus

$$R_{o9} = 12.5 + (33 \parallel 31.25)$$

$$\times 10^{-3} (1 + 0.32 \times 2.5 \times 10^{3})$$

$$= 15.3 \text{ M}\Omega$$

The resistance  $R_{o7}$  is the output resistance of  $Q_7$ , which has an emitter-degeneration resistance  $(R_7 \parallel r_{o1}) \simeq R_7$ . Thus,

$$R_{o7} = r_{o7} + (R_7 \parallel r_{\pi7})(1 + g_{m7}r_{o7})$$

$$r_{o7} = \frac{|V_{An}|}{I_{C7}} = \frac{30 \text{ V}}{8 \mu \text{A}} = 3.75 \text{ M}\Omega$$

$$g_{m7} = \frac{I_{C7}}{V_T} = \frac{8 \mu A}{25 \text{ mV}} = 0.32 \text{ mA/V}$$

$$r_{\pi 7} = \frac{\beta_N}{g_{m7}} = \frac{40}{0.32} = 125 \text{ k}\Omega$$

Thus,

$$R_{o7} = 3.75 + (22 \parallel 125) \times 10^{-3} (1 + 0.32 \times 3.75 \times 10^{3})$$

$$= 26.2 M\Omega$$

$$\frac{R_L}{2} = \frac{1.5}{2} = 0.75 \text{ M}\Omega$$

The load resistance R can now be found as

$$R = 15.3 \parallel 26.2 \parallel 0.75 = 0.696 \text{ M}\Omega$$

Finally, we can find the voltage gain as

$$A_v = \frac{v_{od}/2}{v_{id}/2} = G_{m1}R$$

$$= 0.137 \times 0.696 \times 10^3 = 95.4 \text{ V/V}$$

**12.76** 
$$I_{C1} = I$$

$$I_{C7} = I_{C9} = 2I$$

From Fig. 12.37 we see that the current through  $R_7$  is approximately  $(I_{C1} + I_{C7})$ , that is, 3*I*. Thus,

$$R_7 = \frac{0.2}{3I}$$

Since  $Q_3$  and  $Q_4$  are cut off, the current through  $R_9$  is equal to  $I_{E9}$  or approximately  $I_{C9}$ , thus

$$R_9 = \frac{0.3}{2I}$$

To determine the short-circuit transconductance  $G_{m1}$ , refer to Fig. 12.38(b).

$$g_{m1} = \frac{I_{C1}}{V_T} = \frac{I}{V_T}$$

$$G_{m1} = \frac{i_o}{v_{id}/2}$$

At node X we have four resistances in parallel, namely,  $r_{o1}$ ,  $R_7$ ,  $r_{o7}$ , and  $r_{e7}$ :

$$r_{o1} = \frac{|V_{Ap}|}{I_{C1}} = \frac{20}{I}$$

$$R_7 = \frac{0.2}{3I} = \frac{0.067}{I}$$

$$r_{o7} = \frac{V_{An}}{I_{C7}} = \frac{30}{2I} = \frac{15}{I}$$

$$r_{e7} \simeq \frac{V_T}{I_{C7}} = \frac{0.025}{2I} = \frac{0.0125}{I}$$

Thus,  $r_{o1}$  and  $r_{o7}$  are much greater than  $r_{e7}$  and  $R_7$ , and the portion of  $g_{m1}\left(\frac{v_{id}}{2}\right)$  that flows into the emitter proper of  $Q_7$  is given by

$$i_{e7} \simeq g_{m1} \left(\frac{v_{id}}{2}\right) \frac{R_7}{R_7 + r_{e7}}$$

$$= \left(\frac{I}{V_T}\right) \left(\frac{v_{id}}{2}\right) \frac{0.067}{0.067 + 0.0125}$$

$$=0.84\left(\frac{I}{V_T}\right)\left(\frac{v_{id}}{2}\right)$$

The output short-circuit current  $i_o$  will be

$$i_o \simeq i_{e7} = 0.84 \left(\frac{I}{V_T}\right) \left(\frac{v_{id}}{2}\right)$$

Thus,

$$G_{m1} = 0.84 \frac{I}{V_T} \simeq 33.6I$$

To obtain the output resistance R,

$$R = R_{o9} \parallel R_{o7}$$

we determine  $R_{o9}$  as follows:

$$R_{o9} = r_{o9} + (R_9 \parallel r_{\pi 9})(1 + g_{m9}r_{o9})$$

where

$$r_{o9} = \frac{|V_{Ap}|}{I_{C9}} = \frac{20}{2I} = \frac{10}{I}$$

$$g_{m9} = \frac{I_{C9}}{V_T} = \frac{2I}{0.025} = 80I$$

$$g_{m9}r_{o9} = 800$$

$$r_{\pi 9} = \frac{\beta_P}{g_{m9}} = \frac{10}{80I} = \frac{0.125}{I}$$

Thus,

$$R_{o9} = \frac{10}{I} + \left(\frac{0.15}{I} \parallel \frac{0.125}{I}\right) \times 801$$

$$=\frac{64.6}{I}$$

We next determine  $R_{o7}$  as follows:

$$R_{o7} = r_{o7} + (R_7 \parallel r_{\pi7})(1 + g_{m7}r_{o7})$$

$$r_{o7} = \frac{15}{I}$$

$$R_7 = \frac{0.067}{I}$$

$$g_{m7} = \frac{I_{C7}}{V_T} = \frac{2I}{V_T}$$

$$g_{m7}r_{o7} = 1200$$

$$r_{\pi 7} = \frac{\beta_N}{g_{m7}} = \frac{40}{2I/V_T} = \frac{0.5}{I}$$

Thus,

$$R_{o7} = \frac{15}{I} + \left(\frac{0.067}{I} \parallel \frac{0.5}{I}\right) \times 1201$$

$$=\frac{80}{I}$$

We now can determine the output resistance R as

$$R = R_{o9} \parallel R_{o7} = \frac{64.6}{I} \parallel \frac{86}{I} = \frac{36.9}{I}$$

The open-circuit voltage gain can be obtained as

$$A_{vo} = G_{m1}R$$

$$= 0.84 \left(\frac{I}{V_T}\right) \left(\frac{36.9}{I}\right)$$

$$= 1240 \text{ V/V}$$

With a load resistance  $R_L$ , we have

$$A_{v} = A_{vo} \frac{R_{L}}{R_{L} + R}$$

$$= 1240 \frac{R_{L}}{R_{L} + \frac{36.9}{I}}$$

$$= 1240 \frac{IR_{L}}{IR_{L} + 36.9}$$

For  $R_L = 1 \text{ M}\Omega$  and I in  $\mu A$ , we have

$$A_v = 1240 \frac{I}{I + 36.9}$$

From this equation we can obtain

$$I = \frac{36.9}{\frac{1240}{A_v} - 1}$$

Thus, for  $A_v = 150$  V/V, the required value of I is

$$I = \frac{36.9}{\frac{1240}{150} - 1} = 5.1 \,\mu\text{A}$$

and for  $A_v = 300 \text{ V/V}$ , we require

$$I = \frac{36.9}{\frac{1240}{300} - 1} = 11.8 \ \mu\text{A}$$

**12.77** (a) Refer to Fig. 12.39. Break the loop at the input of the CMF circuit and apply a common-mode input signal  $\triangle V_{CM}$ . The CMF circuit will respond by causing a change  $\triangle V_B$  in its output voltage that can be found from its transfer characteristic as

$$\triangle V_B = \triangle V_{CM}$$

Now, a change  $\triangle V_B$  in the base voltage of  $Q_7$  and  $Q_8$  results in

$$\Delta I_{E8} = \Delta I_{E7} = \frac{\Delta V_B}{r_{e7} + R_7}$$

The corresponding change in the collector voltages of  $Q_7$  and  $Q_8$  will be

$$\Delta v_{O2} = \Delta v_{O1} = -\Delta I_{C7} R_o$$

Now,

$$\triangle I_{C7} \simeq \triangle I_{E7}$$

and

$$R_o = R_{o7} \parallel R_{o9}$$

thus

$$\Delta v_{O1} = -\frac{\Delta V_B}{r_{e7} + R_7} (R_{o7} \parallel R_{o9})$$

This is the returned voltage, thus

$$A\beta \equiv -\frac{\Delta v_{O1}}{\Delta V_{CM}}$$

$$= \frac{R_{o7} \parallel R_{o9}}{r_{e7} + R_7} \qquad \text{Q.E.D.}$$
(1)

(b) From Example 12.8, we have

$$R_{o7} = 23 \text{ M}\Omega, R_{o9} = 12.9 \text{ M}\Omega,$$

$$r_{e7} \simeq \frac{V_T}{I_{C7}} = \frac{25 \text{ mV}}{10 \mu \text{A}} = 2.5 \text{ k}\Omega,$$

$$R_7 = 20 \text{ k}\Omega$$

thus

$$A\beta = \frac{(23 \parallel 12.9) \times 10^3}{2.5 + 20}$$

$$= 367.3$$

For a change  $\Delta I = 0.3 \,\mu\text{A}$ , the corresponding change in  $V_{CM}$  without feedback is

$$\triangle V_{CM} = \triangle I(R_{o7} \parallel R_{o9})$$

The negative feedback reduces this change by the amount of negative feedback  $1+A\beta \simeq A\beta$ , thus the actual  $\triangle V_{CM}$  becomes

$$\triangle V_{CM} \simeq rac{\triangle I(R_{o7} \parallel R_{o9})}{A\beta}$$

Substituting for  $A\beta$  from Eq. (1), we obtain

$$\triangle V_{CM} = \triangle I(r_{e7} + R_7)$$

$$= 0.3 \times 10^{-6} (2.5 + 20)$$

$$= 6.75 \text{ mV}$$

which is identical to the value found in Example 12.8.

**12.78** (a)  $v_O$  can range to within 0.1 V (the saturation voltage) of ground and  $V_{CC}$ , thus

$$0.1 \text{ V} \le v_O \le 2.9 \text{ V}$$

(b) For  $i_L = 0$ , the output resistance is

$$R_o = r_{oN} \parallel r_{oP}$$

where

$$r_{oN} = \frac{V_{An}}{I_Q} = \frac{30 \text{ V}}{0.6 \text{ mA}} = 50 \text{ k}\Omega$$

$$r_{oP} = \frac{|V_{Ap}|}{I_O} = \frac{20 \text{ V}}{0.6 \text{ mA}} = 33.3 \text{ k}\Omega$$

Thus

$$R_o = 50 \parallel 33.3 = 20 \text{ k}\Omega$$

(c) 
$$R_{\text{out}} = R_{of} = \frac{R_o}{1 + A\beta}$$

$$=\frac{20 \text{ k}\Omega}{1+10^5} \simeq 0.2 \Omega$$

(d) For  $i_L = 12$  mA, we have

$$i_N = \frac{I_Q}{2} = 0.3 \text{ mA}$$

$$i_P = 12 + 0.3 = 12.3 \text{ mA}$$

$$r_{oN} = \frac{30 \text{ V}}{0.3 \text{ mA}} = 100 \text{ k}\Omega$$

$$r_{oP} = \frac{20 \text{ V}}{12.3} = 1.63 \text{ k}\Omega$$

$$R_o = 100 \parallel 1.63 = 1.6 \text{ k}\Omega$$

(e) For  $i_L = -12$  mA, we have

$$i_P = 0.3 \text{ mA}$$

$$i_N = 12.3 \text{ mA}$$

$$r_{oN} = \frac{30 \text{ V}}{12.3 \text{ mA}} = 2.44 \text{ k}\Omega$$

$$r_{oP} = \frac{20 \text{ V}}{0.3 \text{ mA}} = 66.7 \text{ k}\Omega$$

$$R_o = 2.44 \parallel 66.7 = 2.4 \text{ k}\Omega$$

**12.79** Refer to Fig. 12.43.

$$v_{B7} = v_{BEN} = V_T \ln \left( \frac{i_N}{I_{SN}} \right) \tag{1}$$

$$i_4 = \frac{v_{EBP} - v_{EB4}}{R_4} \tag{2}$$

$$v_{B6}=v_{BE5}+i_5R_5$$

But,

$$i_5 = i_4$$
 and  $R_5 = R_4$ 

thus

$$v_{B6} = v_{BE5} + i_4 R_4$$

Using Eq. (2), we obtain

$$v_{B6} = v_{BE5} + v_{EBP} - v_{EB4}$$

$$= (v_{BE5} - v_{EB4}) + v_{EBP}$$

$$= V_T \ln \left( \frac{I_{S4}}{I_{S5}} \right) + V_T \ln \left( \frac{i_P}{I_{SP}} \right)$$

$$=V_T \ln \left(\frac{I_{S4} i_P}{I_{S5} I_{SP}}\right) \tag{3}$$

Now, using the given relationship

$$\frac{I_{SP}}{I_{S4}} = \frac{I_{SN}}{I_{S5}}$$

in Eq. (3), we get

$$v_{B6} = V_T \ln \left( \frac{i_P}{I_{SN}} \right) \tag{4}$$

Using Eqs. (1) and (4), we obtain

$$v_{B6} - v_{B7} = V_T \ln \left(\frac{i_P}{i_N}\right)$$

This is the differential voltage input for the differential amplifier  $Q_6 - Q_7$ . Thus,

$$i_{C6} = \frac{I}{1 + e^{(v_{B6} - v_{B7})/V_T}}$$

$$=\frac{I}{1+\frac{i_P}{i_N}}$$

$$=\frac{i_N}{i_P+i_N}I$$
 Q.E.D.

Similarly.

$$i_{C7} = \frac{I}{1 + e^{(v_{B7} - v_{B6})/V_T}}$$

$$=\frac{I}{1+\frac{i_N}{i_N}}$$

$$=\frac{i_P}{i_P+i_N}I$$
 Q.E.D.

**12.80** 
$$v_E = v_{EB7} + v_{BEN}$$

Since  $Q_7$  conducts a current  $i_{C7}$  given by Eq. (12.131),

$$i_{C7} = I \frac{i_P}{i_P + i_N}$$

and  $Q_N$  conducts a current  $i_N$ , then

$$v_E = V_T \ln \left( \frac{I \ i_P}{i_P + i_N} \ \frac{1}{I_{S7}} \right) + V_T \ln \left( \frac{i_N}{I_{SN}} \right)$$

$$= V_T \ln \left[ \frac{i_P \ i_N}{i_P + i_N} \ \frac{I}{I_{SN} \ I_{S7}} \right] \qquad \text{Q.E.D.}$$

**12.81** 
$$I_Q = 0.6 \text{ mA} = 600 \mu\text{A}$$

$$I = 12 \mu A$$

$$\frac{I_{SN}}{I_{S10}} = 8$$

$$\frac{I_{S7}}{I_{S11}} = 4$$

Using Eq. (12.136), we have

$$600 = 2\left(\frac{I_{\text{REF}}^2}{12}\right) \times 8 \times 4$$

$$\Rightarrow I_{REF} = 10.6 \ \mu A$$

The minimum current in each transistor is about  $0.3\,\mathrm{mA}.$