

ELEN20005 FOUNDATIONS OF ELECTRICAL NETWORKS

Semester 1 Exam, 2019

Numerical Answers

Question 1

(a).

$$\begin{aligned}0 &= \frac{v_1}{R_2} + \frac{v_1 - v_3}{R_1} + \frac{v_2 - v_3}{R_3} - i_s \\0 &= \frac{v_3 - v_1}{R_1} + \frac{v_3}{R_4} + \frac{v_3 - v_2}{R_3} \\0 &= -v_1 + \frac{v_x}{2} + v_2 \\v_x &= v_3 - v_1\end{aligned}$$

(b) Supplies 15 W (c) 332K

Question 2

(a) $v_C(0^-) = 50 \text{ V}$ (b) $v_C(0^+) = 50 \text{ V}$ (c) $v_C(t) = 25(1 + e^{-t}) \text{ V}$
(d) $v_C(\infty) = 25 \text{ V}$, after 4.6 s.

Question 4

(a) $\mathbf{V} = 2.17/\underline{77.5^\circ} \text{ V}$, $Z_T = 217/\underline{77.5^\circ} \Omega$.
(b) $i_C(t) = 1.1 \cos(1000t + 167^\circ) \text{ mA}$, $i_L(t) = 10.8 \cos(1000t - 12.5^\circ) \text{ mA}$
 $i_R(t) = 2.2 \cos(1000t + 77.5^\circ) \text{ mA}$, $v(t) = 2.17 \cos(1000t + 77.5^\circ) \text{ V}$

Question 5

(a) Load A: $P = 10 \text{ kW}$, $Q = 4.83 \text{ kVAR}$, $AP = 11.1 \text{ kVA}$, $\theta = 25.8^\circ$.
Load B: $P = 12 \text{ kW}$, $Q = -9.0 \text{ kVAR}$, $AP = 15 \text{ kVA}$, $\theta = -36.8^\circ$.
Source: $P = 22 \text{ kW}$, $Q = -4.2 \text{ kVAR}$, $AP = 22.4 \text{ kVA}$, $\theta = -10.8^\circ$.
 $I_{Arms} = 11.1 \text{ Arms}$, $I_{Brms} = 15 \text{ Arms}$.

(b) $R = 81.1 \Omega$, $X = 38.9 \Omega$.

Question 6

(b) $\mathbf{V}_1 = 791/\underline{18.4^\circ} \text{ V}$, $\mathbf{I}_1 = 0.354/\underline{-45^\circ} \text{ A}$.
(c) $\mathbf{V}_2 = 79.1/\underline{18.4^\circ} \text{ V}$, $\mathbf{I}_2 = 3.54/\underline{-45^\circ} \text{ A}$, $P = 62.7 \text{ W}$.

Question 7

$i = 0 \text{ A}$ as the diode is OFF.

Question 8

(a) $Z = ABC$
(b) X has 'No promises' from $t = 5 \text{ ns}$ to $t = 21 \text{ ns}$.
Y has 'No promises' from $t = 5 \text{ ns}$ to $t = 25 \text{ ns}$.
Z has 'No promises' from $t = 10 \text{ ns}$ to $t = 46 \text{ ns}$.
(c) contamination delay = 10 ns, propagation delay = 46 ns.

Question 9

(a) $\mathbf{V}_L = \frac{jV_t 2\pi f L}{R + j2\pi f L}$

(b) $H_L(f) = \frac{j2\pi^2 f}{5000 + j2\pi^2 f}$

(c) $V_L(t) = 98.7 \cos(10\pi t + 88.7^\circ) + 394 \cos(40\pi t + 85.5^\circ) \text{ mV}.$