

# A regression Model

This is very quick look at what you can see in Jupyter notebooks. I haven't really included anything of much substance in here, rather just a look at what you can do and how it can be presented to you after I have done an analysis.

Importing all of the necessary modules for writing maths formulas, manipulating data and plotting.

```
In [1]: import pandas as pd
```

```
In [2]: import statsmodels.api as sm
```

```
In [3]: import numpy as np
```

```
In [4]: from sklearn import linear_model
```

```
In [5]: from matplotlib import pyplot as plt
```

```
In [6]: from scipy.stats import ttest_ind
```

```
In [7]: import matplotlib.cm as cm #latex module
```

Reading the data from the excel sheet (given by Carl)

```
In [8]: d = pd.read_excel("dataFromCarl.xlsx", sheet_name = 'Sheet2')
```

by calling 'd' which is the variable assigned to the data, you can see the table. 'Sheet2' of the sheet I moved MailingQty, Orders and marketing costs to run some tests.

```
In [9]: d
```

Out [9]:

|     | mailingQty | orders | marketingCosts |
|-----|------------|--------|----------------|
| 0   | 249500     | 8401   | 162501.19      |
| 1   | 102887     | 3514   | 0.00           |
| 2   | 881        | 71     | 0.00           |
| 3   | 110136     | 5114   | 0.00           |
| 4   | 67489      | 2506   | 0.00           |
| ... | ...        | ...    | ...            |
| 85  | 250000     | 8923   | 67850.00       |
| 86  | 60000      | 1394   | 21000.00       |
| 87  | 140000     | 6278   | 49000.00       |
| 88  | 229672     | 8280   | 80385.20       |
| 89  | 175000     | 3124   | 61250.00       |

90 rows × 3 columns

Setting the independant and dependant variables as x and y respectively to split out the table.

In [10]: `x = d.drop(["orders","marketingCosts"], axis=1)`

In [11]: `y = d.drop(["mailingQty","marketingCosts"], axis=1)`

By using the describe function below you can see some of the fundamental properties of the data such as mean, standard deviation and the quartile values.

In [12]: `d.describe()`

Out[12]:

|       | mailingQty    | orders      | marketingCosts |
|-------|---------------|-------------|----------------|
| count | 90.000000     | 90.000000   | 90.000000      |
| mean  | 80554.811111  | 3144.600000 | 25274.678770   |
| std   | 77325.020775  | 2992.850889 | 30107.264507   |
| min   | 0.000000      | 1.000000    | 0.000000       |
| 25%   | 2445.500000   | 350.500000  | 1394.325000    |
| 50%   | 57588.000000  | 2166.500000 | 12760.127200   |
| 75%   | 143750.000000 | 5596.500000 | 48400.458300   |
| max   | 250000.000000 | 9816.000000 | 162501.190000  |

This line just calls the function to initialize it from the module

In [13]: `regr = linear_model.LinearRegression()`

```
In [14]: regr.fit(x,y)
```

```
Out[14]: ▼ LinearRegression  
LinearRegression()
```

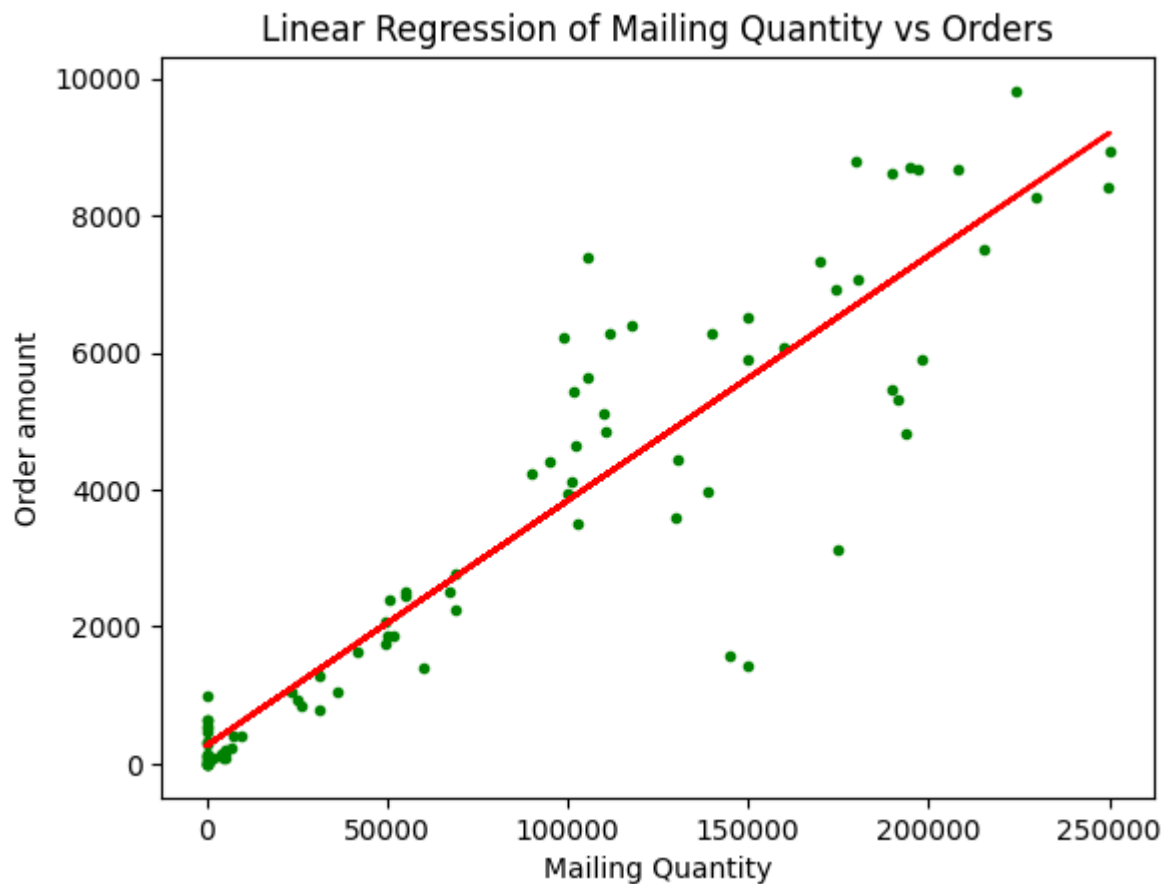
The predict function creates the regression line (best fit) by creating a simple  $y = mx + c$  function

```
In [15]: Y_pred = regr.predict(x)
```

Using the matplotlib library to plot the regression model

```
In [16]: plt.scatter(x, y, color = 'green', marker = '.')  
plt.plot(x, Y_pred, color='red')  
plt.xlabel("Mailing Quantity")  
plt.ylabel("Order amount")  
plt.title("Linear Regression of Mailing Quantity vs Orders")
```

```
Out[16]: Text(0.5, 1.0, 'Linear Regression of Mailing Quantity vs Orders')
```



```
In [17]: d.mean()
```

```
Out[17]: mailingQty      80554.811111
orders      3144.600000
marketingCosts 25274.678770
dtype: float64
```

```
In [18]: #coefficient of determination
r_sq = regr.score(x,y)
r_sq
```

```
Out[18]: 0.85318447280849
```

the  $R^2$  value determines how much of the dependant variable is explained by the shape of the independent. The value given of 0.853 means that 85.3% of the data can be explained by this regression model which is very good.  $0.7 <$  means a high level of correlation and  $0.4 >$  shows little correlation between the variables.

```
In [19]: res = ttest_ind(x,y).pvalue
res
```

```
Out[19]: array([1.52245875e-17])
```

T-tests determine how much of the data represents the null hypothesis, i.e. The percentage of data that demonstrate that the variables aren't related. This value is much smaller than 0.05 (5%) meaning that the null hypothesis is not true.

## Looking into Multivariable Linear Regression

For this test, there will be two independent variables and one dependant. This study will determine how the mailing quantity and the marketing costs will affect the total orders.

First the x variable must be overwritten to become a n x 2 array

```
In [20]: x = d[["mailingQty", "marketingCosts"]]
```

```
In [21]: y = d[["orders"]]
```

```
In [22]: regr = linear_model.LinearRegression()
```

```
In [23]: regr.fit(x,y)
```

```
Out[23]: ▼ LinearRegression
LinearRegression()
```

```
In [24]: print("Intercept: \n", regr.intercept_)
```

```
Intercept:
[267.30953125]
```

```
In [25]: print('Coefficients: \n', regr.coef_)
```

```
Coefficients:  
[[0.03532648 0.00124918]]
```

```
In [26]: x = sm.add_constant(x) # adding a constant
```

```
In [27]: model = sm.OLS(y, x).fit()
```

```
In [28]: predictions = model.predict(x)
```

```
In [29]: print_model = model.summary()
```

```
In [30]: print(model.params)
```

```
const          267.309531  
mailingQty      0.035326  
marketingCosts  0.001249  
dtype: float64
```

These values are the coefficients of the regression model; The amount that orders increases with every unit increase in mailing quantity or marketing price.

```
In [31]: print(print_model)
```

## OLS Regression Results

```

=====
===
Dep. Variable:          orders    R-squared:                0.
853
Model:                  OLS      Adj. R-squared:             0.
850
Method:                 Least Squares    F-statistic:              25
2.9
Date:                   Wed, 14 Dec 2022    Prob (F-statistic):       5.62e
-37
Time:                   13:49:35    Log-Likelihood:           -76
1.21
No. Observations:      90    AIC:                      15
28.
Df Residuals:          87    BIC:                      15
36.
Df Model:               2

```

Covariance Type: nonrobust

```

=====
=====
              coef      std err          t      P>|t|      [0.025
0.975]
-----
const          267.3095    177.904      1.503     0.137    -86.294
620.913
mailingQty      0.0353      0.003     10.856     0.000      0.029
0.042
marketingCosts  0.0012      0.008      0.149     0.882     -0.015
0.018
=====
=====

```

```

===
Omnibus:          19.772    Durbin-Watson:           2.
039
Prob(Omnibus):    0.000    Jarque-Bera (JB):        49.
248
Skew:             -0.701    Prob(JB):                2.02e
-11
Kurtosis:         6.342    Cond. No.                1.71e
+05
=====
=====

```

### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 1.71e+05. This might indicate that there are strong multicollinearity or other numerical problems.

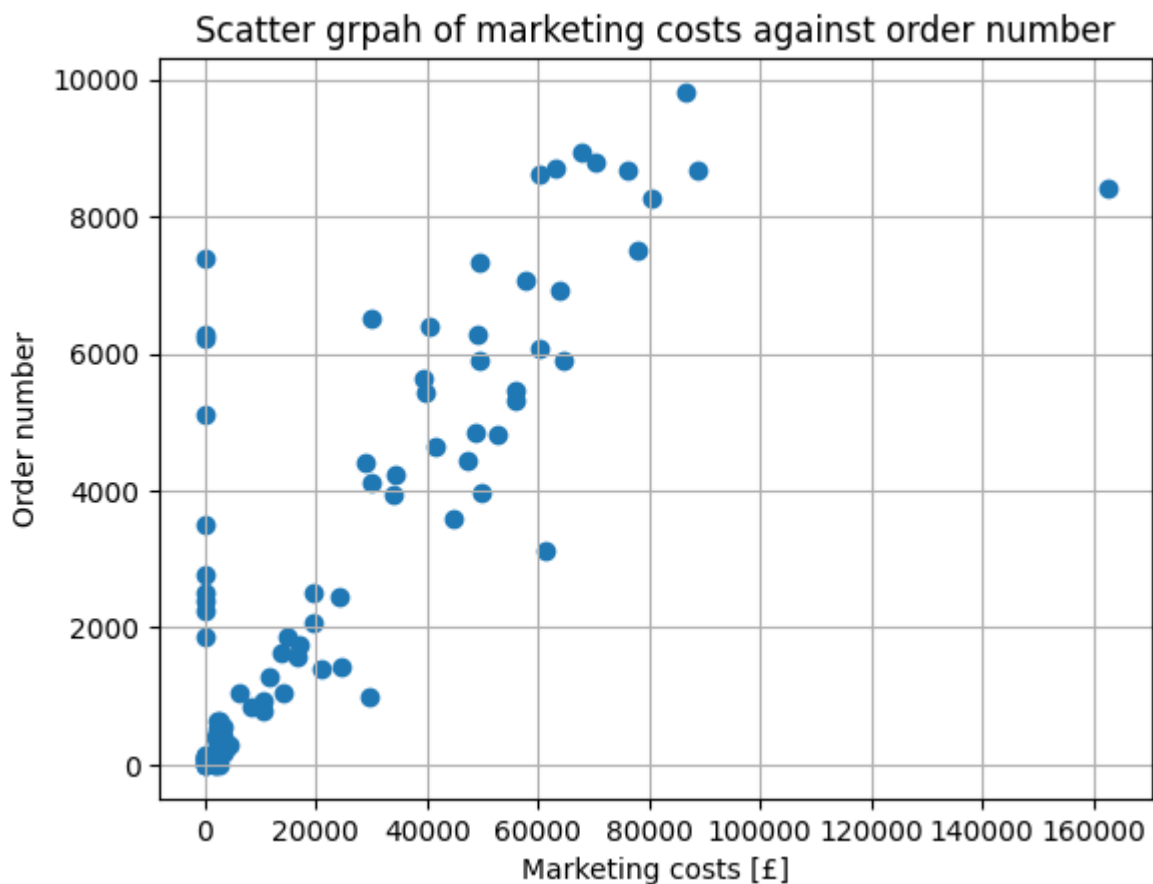
*The Summary Table Explained*

$P > |t|$  is the p-value. A p-value below 0.05 means that the variable is significant. This means that the mailingQty is significant but the marketing costs may not be.

The *Prob (F-statistic)* shows how the F-Statistic compares to the significance level. In other words, how true is the null hypothesis. In this case it is extremely low and therefore the null hypothesis can probably be ignored.

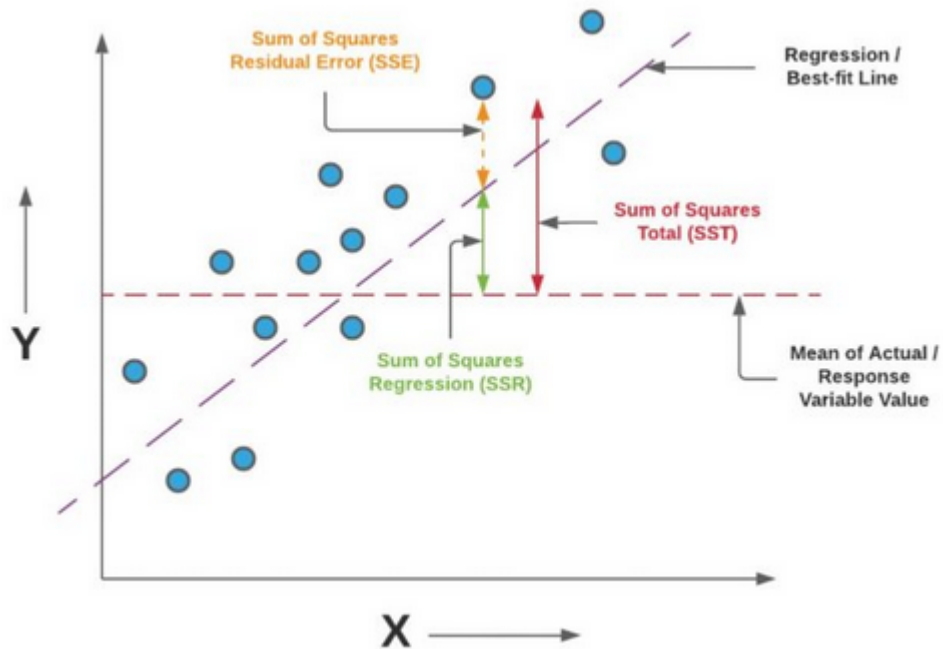
The  $R^2$  Value shows that 85.3% of the dependant variable's variation is explained by the independant variables.

```
In [32]: plt.scatter(d["marketingCosts"], d["orders"])
plt.title("Scatter grpah of marketing costs against order number")
plt.xlabel("Marketing costs [£]")
plt.ylabel("Order number")
plt.grid()
```



### Expalination of the t-test

The best way to explain the f-test is with the below diagram



## The F-Statistic

The f test of a regression model determines the significance of the trend. It tests the null hypothesis, which states that the model with no independent variables fits the data as well as the model

The F-statistic is required in conjunction with the p-value

f-tests test determines the significance of all the coefficients whereas the t-test determines the significance of the coefficients individually. It is useful to use a t-test as well to see the effect of the independent variables separately on the dependent.

In [ ]: