Bios 6301: Assignment 1

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Create a Data Set

A data set in R is called a data frame. This particular data set is made of three categorical variables, or factors: gender, smoker, and exercise. In addition exercise is an ordered factor. age and los (length of stay) are continuous variables.

```
gender <- c('M','M','F','M','F','F','M','F','M')</pre>
age \leftarrow c(34, 64, 38, 63, 40, 73, 27, 51, 47)
smoker <- c('no','yes','no','no','yes','no','no','no','yes')</pre>
exercise <- factor(c('moderate','frequent','some','some','moderate','none','moderate','moderate'</pre>
                     levels=c('none','some','moderate','frequent'), ordered=TRUE
los \leftarrow c(4,8,1,10,6,3,9,4,8)
x <- data.frame(gender, age, smoker, exercise, los)
##
     gender age smoker exercise los
## 1
          М
             34
                     no moderate
## 2
          Μ
              64
                                     8
                    yes frequent
## 3
              38
                     no
                             some
## 4
          Μ
              63
                             some
                                    10
## 5
          F
              40
                    yes moderate
                                     6
          F
              73
## 6
                     no
                             none
                                     3
## 7
          М
              27
                     no
                             none
          F
## 8
              51
                                     4
                     no moderate
## 9
                    yes moderate
```

Create a Model

We can create a model using our data set. In this case I'd like to estimate the association between los and all remaining variables. This means los is our dependent variable. The other columns will be terms in our model.

The lm function will take two arguments, a formula and a data set. The formula is split into two parts, where the vector to the left of ~ is the dependent variable, and items on the right are terms.

```
lm(los ~ gender + age + smoker + exercise, dat=x)
##
## Call:
## lm(formula = los ~ gender + age + smoker + exercise, data = x)
##
## Coefficients:
##
   (Intercept)
                     genderM
                                              smokeryes
                                                           exercise.L
                                                                         exercise.Q
                                       age
##
      0.588144
                    4.508675
                                 0.033377
                                               2.966623
                                                            -2.749852
                                                                          -0.710942
##
    exercise.C
##
      0.002393
```

1. Looking at the output, which coefficient seems to have the highest effect on los? (2 points)

The gender coefficent seems to have the highest effect on `los` because the value is largest.

This can be tough because it also depends on the scale of the variable. If all the variables are standardized, then this is not the case.

Given that we only have nine observations, it's not really a good idea to include all of our variables in the model. In this case we'd be "over-fitting" our data. Let's only include one term, gender.

Warning When choosing terms for a model, use prior research, don't just select the variable with the highest coefficient.

2. Create a model using los and gender and assign it to the variable mod. Run the summary function with mod as its argument. (5 points)

```
mod <- lm(los ~ gender, dat=x)
summary(mod)
##
## Call:
## lm(formula = los ~ gender, data = x)
##
## Residuals:
##
      Min
              1Q Median
                             3Q
                                   Max
##
     -3.8
            -0.5
                    0.2
                            1.2
                                   2.5
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                  3.500
## (Intercept)
                              1.099
                                      3.186
                                              0.0154 *
## genderM
                  4.300
                              1.474
                                      2.917
                                              0.0224 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.197 on 7 degrees of freedom
```

The summary of our model reports the parameter estimates along with standard errors, test statistics, and p-values. This table of estimates can be extracted with the coef function.

Multiple R-squared: 0.5487, Adjusted R-squared: 0.4842
F-statistic: 8.51 on 1 and 7 DF, p-value: 0.02243

Estimates

3. What is the estimate for the intercept? What is the estimate for gender? Use the coef function. (3 points)

4. The second column of coef are standard errors. These can be calculated by taking the sqrt of the diag of the vcov of the summary of mod. Calculate the standard errors. (3 points)

```
summary(mod) %>% coef()
##
               Estimate Std. Error t value
                                               Pr(>|t|)
                          1.098701 3.185581 0.01537082
## (Intercept)
                    3.5
                          1.474061 2.917110 0.02243214
## genderM
                    4.3
summary(mod) %>% vcov %>% diag %>% sqrt
  (Intercept)
                   genderM
      1.098701
                  1.474061
##
# We see that the standard error computed with this method
# agrees with those given by the `coef()` function
```

The third column of coef are test statistics. These can be calculated by dividing the first column by the second column.

```
mod <- lm(los ~ gender, dat=x)
mod.c <- coef(summary(mod))
mod.c[,1]/mod.c[,2]
## (Intercept) genderM
## 3.185581 2.917110</pre>
```

The fourth column of coef are p values. This captures the probability of observing a more extreme test statistic. These can be calculated with the pt function, but you will need the degrees-of-freedom. For this model, there are 7 degrees-of-freedom.

5. Use the pt function to calculate the p value for gender. The first argument should be the test statistic for gender. The second argument is the degrees-of-freedom. Also, set the lower.tail argument to FALSE. Finally multiple this result by two. (4 points)

```
# Store the t-statistics for gender
t_stat_gender <- mod.c[,3][2]
pt(q=t_stat_gender, df=7, lower.tail = FALSE)*2

## genderM
## 0.02243214
# The calculated p-value of 0.02243214 agrees with the value in the table</pre>
```

Predicted Values

The estimates can be used to create predicted values.

```
3.5+(x$gender=='M')*4.3
```

```
## [1] 7.8 7.8 3.5 7.8 3.5 3.5 7.8 3.5 7.8
```

6. It is even easier to see the predicted values by passing the model mod to the predict or fitted functions. Try it out. (2 points)

```
predict(mod)
## 1 2 3 4 5 6 7 8 9
## 7.8 7.8 3.5 7.8 3.5 7.8 3.5 7.8
fitted(mod)
## 1 2 3 4 5 6 7 8 9
## 7.8 7.8 3.5 7.8 3.5 7.8 3.5 7.8
```

7. predict can also use a new data set. Pass newdat as the second argument to predict. (3 points)

```
newdat <- data.frame(gender=c('F','M','F'))
predict(mod, newdata = newdat)
## 1 2 3
## 3.5 7.8 3.5</pre>
```

Residuals

The difference between predicted values and observed values are residuals.

8. Use one of the methods to generate predicted values. Subtract the predicted value from the x\$los column. (5 points)

```
x$los - predict(mod)
```

```
## 1 2 3 4 5 6 7 8 9
## -3.8 0.2 -2.5 2.2 2.5 -0.5 1.2 0.5 0.2
```

9. Try passing mod to the residuals function. (2 points)

residuals (mod)

```
## 1 2 3 4 5 6 7 8 9
## -3.8 0.2 -2.5 2.2 2.5 -0.5 1.2 0.5 0.2
```

10. Square the residuals, and then sum these values. Compare this to the result of passing mod to the deviance function. (6 points)

```
residuals(mod)^2 %>% sum()
```

```
## [1] 33.8
```

deviance (mod)

```
## [1] 33.8
```

Remember that our model object has two items in the formula, los and gender. The residual degrees-of-freedom is the number of observations minus the number of items to account for in the model formula.

This can be seen by passing mod to the function df.residual.

```
df.residual(mod)
```

```
## [1] 7
```

11. Calculate standard error by dividing the deviance by the degrees-of-freedom, and then taking the square root. Verify that this matches the output labeled "Residual standard error" from summary(mod). (5 points)

```
(deviance(mod)/df.residual(mod)) %>% sqrt()
```

```
## [1] 2.197401
```

```
summary(mod)
```

```
##
## Call:
## lm(formula = los ~ gender, data = x)
##
## Residuals:
## Min 1Q Median 3Q Max
```

```
##
     -3.8
            -0.5
                    0.2
                           1.2
                                  2.5
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  3.500
                             1.099
                                     3.186
                                             0.0154 *
                  4.300
                                             0.0224 *
## genderM
                             1.474
                                     2.917
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.197 on 7 degrees of freedom
## Multiple R-squared: 0.5487, Adjusted R-squared: 0.4842
## F-statistic: 8.51 on 1 and 7 DF, p-value: 0.02243
# The Residual standard error is 2.197 using both methods
```

Note it will also match this output:

```
predict(mod, se.fit=TRUE)$residual.scale
```

```
## [1] 2.197401
```

T-test

Let's compare the results of our model to a two-sample t-test. We will compare los by men and women.

12. Create a subset of x by taking all records where gender is 'M' and assigning it to the variable men. Do the same for the variable women. (4 points)

```
dplyr::filter(x, gender=="M") -> men
dplyr::filter(x, gender=="F") -> women
```

13. By default a two-sampled t-test assumes that the two groups have unequal variances. You can calculate variance with the var function. Calculate variance for los for the men and women data sets. (3 points)

```
var_men <- var(men$los)
var_women <- var(women$los)
var_men</pre>
```

```
## [1] 5.2
var_women
```

```
## [1] 4.333333
```

14. Call the t.test function, where the first argument is los for women and the second argument is los for men. Call it a second time by adding the argument var.equal and setting it to TRUE. Does either produce output that matches the p value for gender from the model summary? (3 points)

```
t.test(women$los, men$los)
```

```
##
## Welch Two Sample t-test
##
## data: women$los and men$los
## t = -2.9509, df = 6.8146, p-value = 0.02205
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -7.7647486 -0.8352514
## sample estimates:
```

```
## mean of x mean of y
##
         3.5
                   7.8
t.test(women$los, men$los, var.equal = TRUE)
##
## Two Sample t-test
##
## data: women$los and men$los
## t = -2.9171, df = 7, p-value = 0.02243
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -7.7856014 -0.8143986
## sample estimates:
## mean of x mean of y
         3.5
# The t.test with var.equal=TRUE produces output that matches the p-value
# from the models summary
An alternative way to call t.test is to use a formula.
t.test(los ~ gender, dat=x, var.equal=TRUE)
##
##
   Two Sample t-test
##
## data: los by gender
## t = -2.9171, df = 7, p-value = 0.02243
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -7.7856014 -0.8143986
## sample estimates:
## mean in group F mean in group M
               3.5
                               7.8
##
# compare p-values
t.test(los ~ gender, dat=x, var.equal=TRUE)$p.value
## [1] 0.02243214
coef(summary(lm(los ~ gender, dat=x)))[2,4]
```

[1] 0.02243214