

Question 1

Say whether the following is true or false and support your answer by a proof.

$$(\exists m \in \mathbb{N})(\exists n \in \mathbb{N})(3m + 5n = 12)$$

The statement is false. When n is larger or equal to 2 we have: $3m + 5n \geq 13$ for any m . This is because when $n = 2$ we have $3m + 10$, which means the sum is at least 13 since m is part of the natural numbers. Thus n must be equal to 1. From this we get: $3m + 5$. This means $3m$ needs to be equal to $12 - 5 = 7$ in order for the equality to hold. Since $\neg(3 \mid 7)$ there is no natural number m for which the statement is true.