

# Determining the long term cost of vaccination schedules

A case study of measles in the United Kingdom

Max Goulding

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# Measles



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- ▶ Highly infectious viral illness
- ▶ Extremely unpleasant
- ▶ Cold like symptoms / red eyes / light sensitivity / fever / spots in the mouth and throat
- ▶ Complications such as pneumonia. In rare cases death
- ▶ Complications when pregnant women are infected. Low birth weight. Premature birth. Miscarriage

# Vaccination

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- ▶ Before vaccination 200,000-700,000 notified infections and 30-300 deaths annually
- ▶ Vaccine introduced in 1968. Replaced by MMR in 1988
- ▶ Between 1998-2008, 2000-5000 notified cases and 0-3 deaths annually
- ▶ 89% of infants vaccinated in 2010/2011
- ▶ Current HPA recommendation first dose at 13 months and follow up 3-5 years

# Maternal Antibodies

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- ▶ Mother transfers antibodies to infant in the womb
- ▶ Mothers with high antibody titre generally have infants with high antibody titre and vice versa
- ▶ Maternal antibodies protect infants from infection and from successful vaccination
- ▶ Maternal antibodies decay over time
- ▶ Vaccination is often successful when an infant is no longer protected by maternal antibodies
- ▶ Window of susceptibility

# Impact of vaccination of maternal antibodies

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- ▶ Since the introduction of vaccination there has been a decline in antibody titre within population
- ▶ Vaccinated individuals have lower antibody titre than those who gain immunity through infection
- ▶ Lack of natural boosting
- ▶ Infants have lower maternal antibody levels
- ▶ Infants lose immunity sooner than prior vaccination
- ▶ Increased window of susceptibility

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*Should vaccination schedules be altered to account for the increased window of susceptibility in infants?*

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*Should vaccination schedules be altered to account for the increased window of susceptibility in infants?*

- ▶ **Model** different vaccination schedules for measles
- ▶ Determine which offers **optimum** results



# Optimum?

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What different ways are there to determine optimum results?

- ▶ Minimise number of infections
- ▶ Minimise number of infections to particular age groups, as certain groups may have greater risks if infected
- ▶ Speed to eradication
- ▶ Minimise overall cost of measles

# How to model

There are two main possibilities to model diseases where the initial conditions are known.

- ▶ Stochastic
- ▶ Differential

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# General Methods

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I use some common methods throughout :

- ▶ Model using ODEs
- ▶ All ODEs are solved using a fourth order Runge-Kutta method, with time step  $h = \frac{1}{365}$
- ▶ Stable population of 60,000,000
- ▶ Initial values of  $S = 6,400,000$ ,  $I = 600,000$  and  $R = 53,000,000$

# SIR

## Assumptions

- ▶ The population is divided up into three group :
  - ▶ Susceptible
  - ▶ Infectious
  - ▶ Recovered
- ▶ Transitions from groups are exponential decays
- ▶ Homogeneous mixing
- ▶ Individuals born susceptible
- ▶ Recovered immunity lifelong
- ▶ Death applies equally to each group

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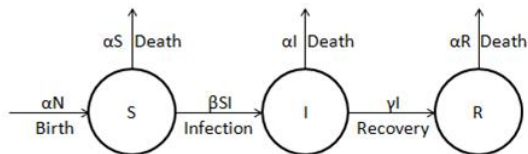
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## Model



$$N = S + I + R$$

$$\frac{dS}{dt} = \alpha N - \beta SI - \alpha S$$

$$\frac{dI}{dt} = \beta SI - \gamma I - \alpha I$$

$$\frac{dR}{dt} = \gamma I - \alpha R$$

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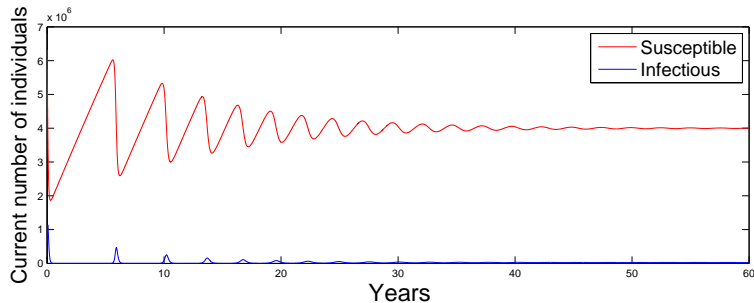
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**Figure:** The current number of infectious and susceptible individuals at each time step. Initial values of  $S = 6,400,000$ ,  $I = 600,000$  and  $R = 53,000,000$ .

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Does NOT account for vaccination!!!

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# SVIR

## Assumptions

- ▶ Inclusion of a Vaccinated group,  $V$
- ▶ Vaccination occurs at birth
- ▶ Vaccination is always successful
- ▶  $p$  proportion of the population are vaccinated
- ▶ Vaccinated immunity is lifelong

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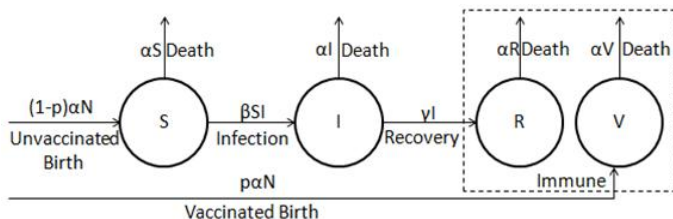
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# SVIR

## Model



$$N = S + V + I + R$$

$$\frac{dS}{dt} = (1-p)\alpha N - \beta SI - \alpha S$$

$$\frac{dV}{dt} = p\alpha N - \alpha V$$

$$\frac{dI}{dt} = \beta SI - \gamma I - \alpha I$$

$$\frac{dR}{dt} = \gamma I - \alpha R$$

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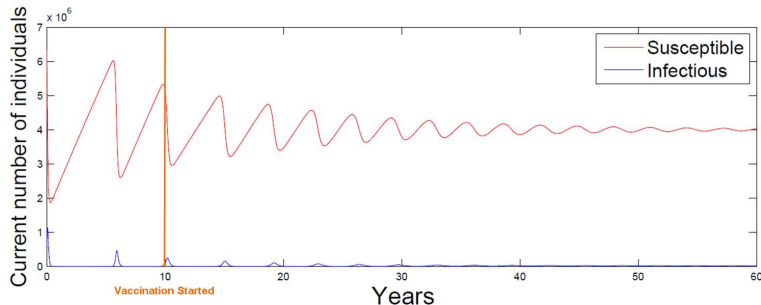
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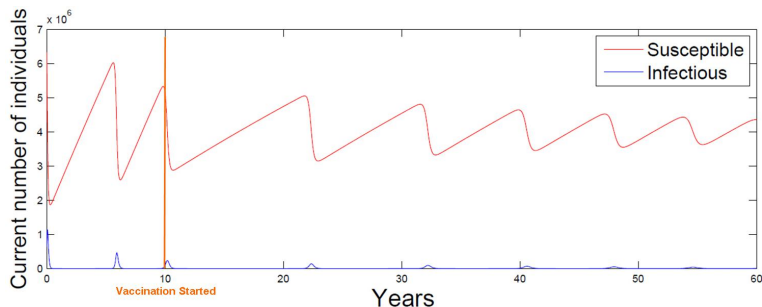
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**Figure:** The current number of infectious and susceptible individuals at each time step. 30% vaccination introduced in 10th year. Initial values of  $S = 6,400,000$ ,  $V = 0$ ,  $I = 600,000$  and  $R = 53,000,000$ .

# SVIR

## Results



**Figure:** The current number of infectious and susceptible individuals at each time step. 70% vaccination introduced in 10th year. Initial values of  $S = 6,400,000$ ,  $V = 0$ ,  $I = 600,000$  and  $R = 53,000,000$ .

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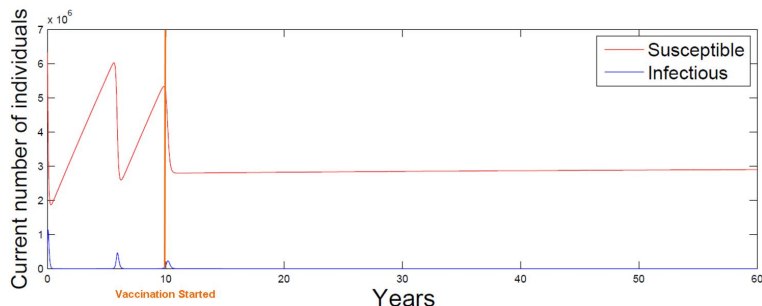
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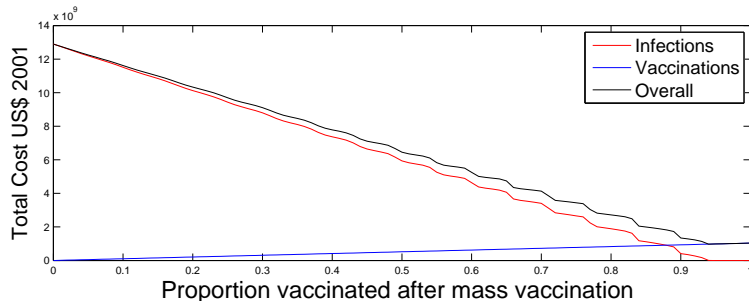
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**Figure:** The current number of infectious and susceptible individuals at each time step. 95% vaccination introduced in 10th year. Initial values of  $S = 6,400,000$ ,  $V = 0$ ,  $I = 600,000$  and  $R = 53,000,000$ .

# SVIR

## Overall cost results



**Figure:** Total cost of varying proportions of vaccination. The system is run for 50 years after mass vaccination. US \$307 (2001 levels) per measles case, US \$22.1 (2001 levels) per vaccination and US \$2.08 (2001 levels) per associated cost of vaccination.

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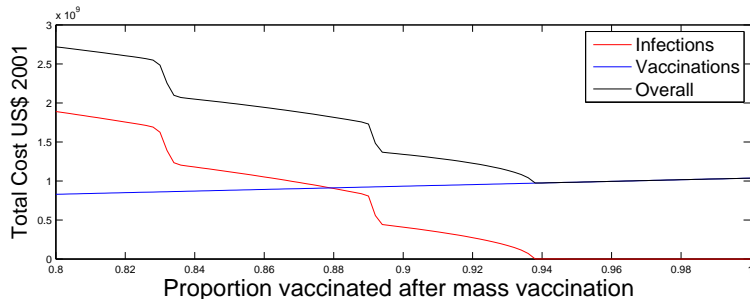
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## Challenges

Does NOT take account of protective maternal immunity!!!

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# Ideal BSVIR

## Assumptions

- ▶ Inclusion of birth immunity groups,  $B_R$  and  $B_V$  for infants of recovered and vaccinated mothers respectively
- ▶ Only individuals from  $S$ ,  $R$  and  $V$  groups give birth with infants entering  $S$ ,  $B_R$  and  $B_V$  groups respectively
- ▶ Births weighted to maintain stable population
- ▶ Birth recovered and vaccinated immunity exponentially decays at rate  $\sigma$  and  $\xi$  respectively
- ▶ Vaccination occurs when individuals become susceptible

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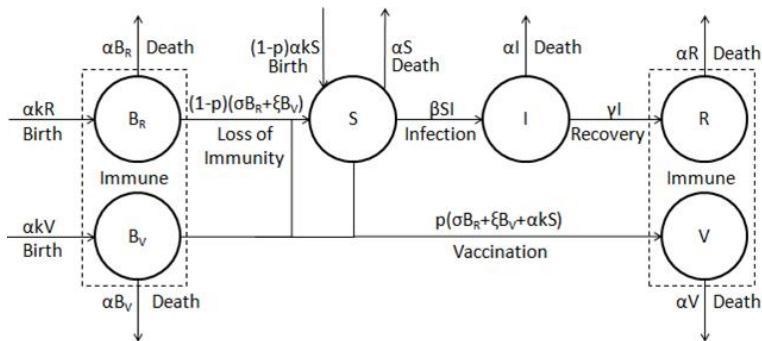
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$$N = B_R + B_V + S + V + I + R$$

$$\frac{dB_R}{dt} = \frac{\alpha NR}{(S + V + R)} - \sigma B_R - \alpha B_R$$

$$\frac{dB_V}{dt} = \frac{\alpha NV}{(S + V + R)} - \xi B_V - \alpha B_V$$

$$\frac{dS}{dt} = (1 - p) \left( \frac{\alpha NS}{(S + V + R)} + \sigma B_R + \xi B_V \right) - \beta SI - \alpha S$$

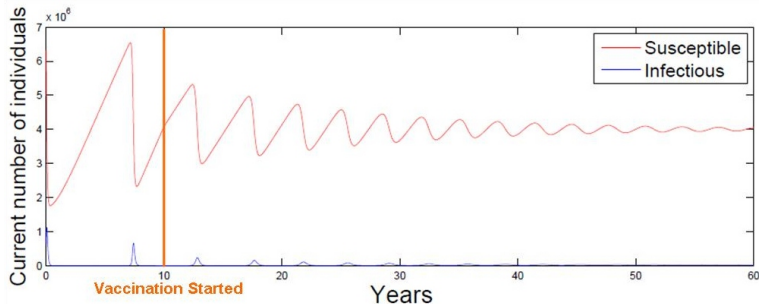
$$\frac{dV}{dt} = p \left( \frac{\alpha NS}{(S + V + R)} + \sigma B_R + \xi B_V \right) - \alpha V$$

$$\frac{dI}{dt} = \beta SI - \gamma I - \alpha I$$

$$\frac{dR}{dt} = \gamma I - \alpha R$$

# Ideal BS VIR

## Results



**Figure:** The current number of infectious and susceptible individuals at each time step. 30% vaccination introduced in 10th year. Initial values of  $B_R = 0$ ,  $B_V = 0$ ,  $S = 6,400,000$ ,  $V = 0$ ,  $I = 600,000$  and  $R = 53,000,000$ .

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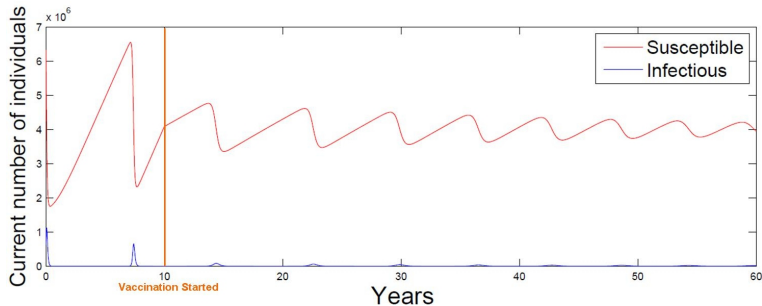
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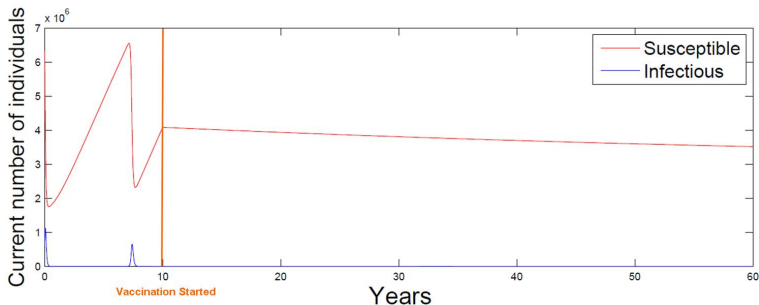
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**Figure:** The current number of infectious and susceptible individuals at each time step. 95% vaccination introduced in 10th year. Initial values of  $B_R = 0$ ,  $B_V = 0$ ,  $S = 6,400,000$ ,  $V = 0$ ,  $I = 600,000$  and  $R = 53,000,000$ .

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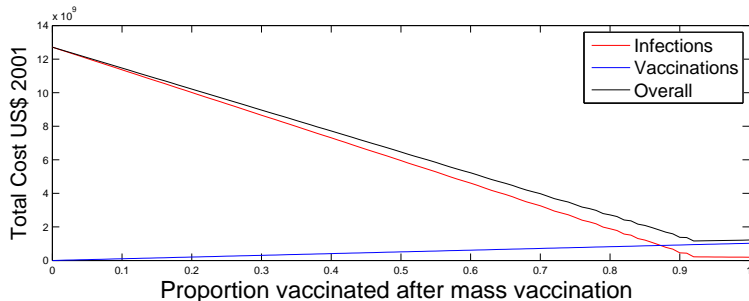
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## Overall cost results



**Figure:** Total cost of varying proportions of vaccination. The system is run for 50 years after mass vaccination. US \$307 (2001 levels) per measles case, US \$22.1 (2001 levels) per vaccination and US \$2.08 (2001 levels) per associated cost of vaccination.

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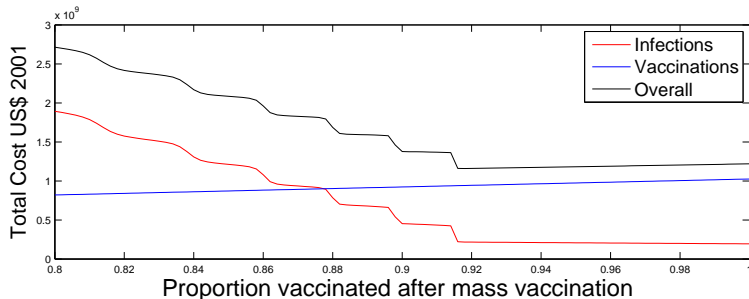
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## Challenges

Vaccination schedules are NOT realistic.  
Loss of maternal immunity NOT realistic.

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# Realistic BSVIR

## Assumptions

- ▶ Have an age-stratified model
- ▶ Store population as a matrix, with rows as immunity statuses and columns as age groups
- ▶ Age groups the same size as the time step
- ▶ Discretely apply vaccination to the appropriate age group(s). Only those susceptible have successful vaccination
- ▶ Only those in certain age groups give birth
- ▶ For double vaccination schedules, assume second vaccination is independent
- ▶ For computational reasons use a 'partially' age-stratified model, with those  $> 4$  years in a single group

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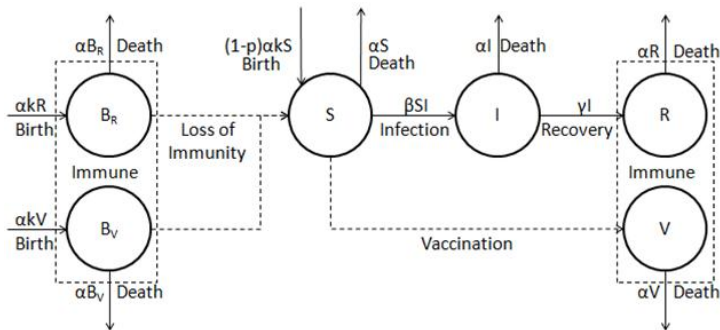
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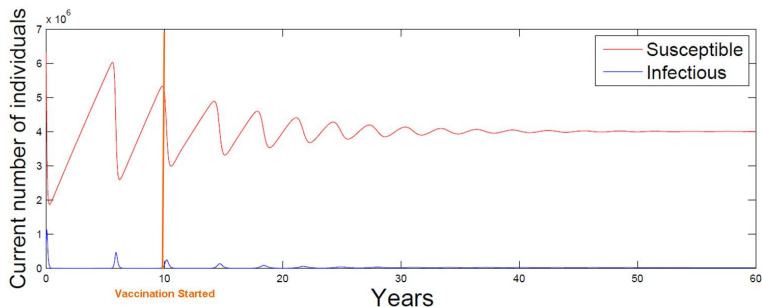
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**Figure:** The current number of infectious and susceptible individuals at each time step. 30% vaccination introduced in 10th year. Initial values of  $S(n) = 6,400,000$ ,  $I(n) = 600,000$ ,  $R(n) = 53,000,000$  and  $B_V(n) = B_R(n) = V(n) = 0$ , where  $n$  is  $> 4$  age group.

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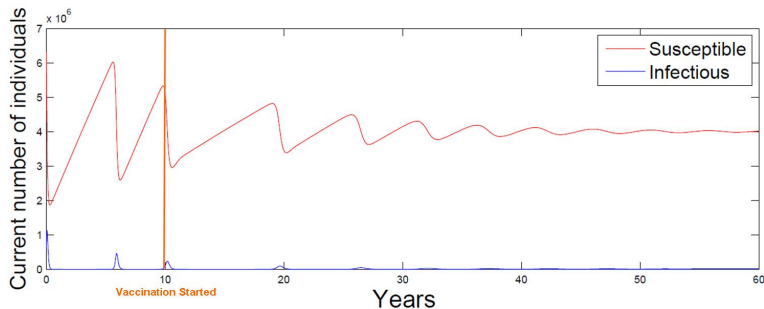
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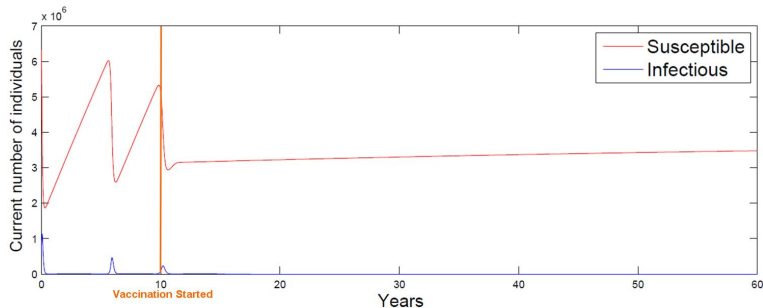
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**Figure:** The current number of infectious and susceptible individuals at each time step. 95% vaccination introduced in 10th year. Initial values of  $S(n) = 6,400,000$ ,  $I(n) = 600,000$ ,  $R(n) = 53,000,000$  and  $B_V(n) = B_R(n) = V(n) = 0$ , where  $n$  is  $> 4$  age group.

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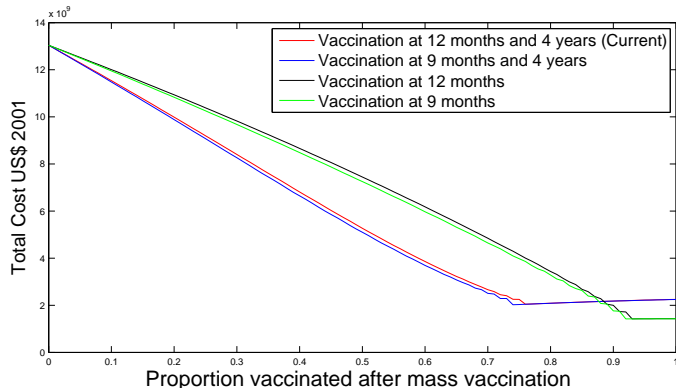
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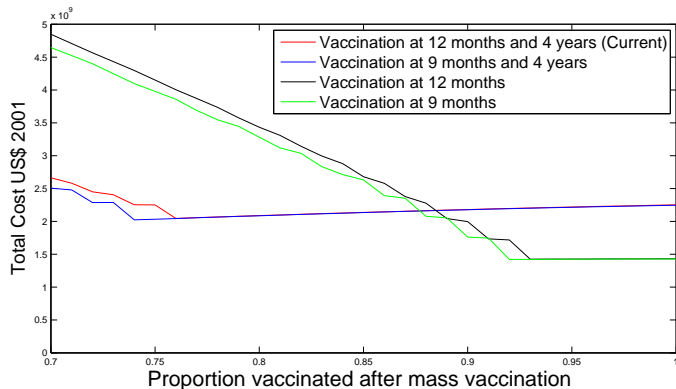
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## Challenges

- ▶ Not fully age-stratified
- ▶ Serological data not up to date
- ▶ Double vaccination schemes independent
- ▶ Population assumptions over simplistic
- ▶ Economic factors not accounted for
- ▶ Lifelong immunity not guaranteed

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These models show some general trends :

- ▶ It is cheaper in terms of overall cost to over-vaccinated a population than to under-vaccinated a population
- ▶ Eradication is possible if over 95% is vaccinated
- ▶ Reduction of the initial vaccination to 9 months may have potential cost savings
- ▶ Changing to a single vaccination schedule may bring a cost reduction if a high enough proportion of infants are vaccinated

# Future Developments

- ▶ Age-Stratified Models
- ▶ Up to date serological data
- ▶ Model mumps and rubella

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