

$$\begin{aligned} \int_0^1 c(x+a) dx &= 1 \\ c \int_0^1 (x+a) dx &= c(\int_0^1 x dx + \int_0^1 a dx) \\ \int x dx &= \frac{x^2}{2} \quad \int a dx = ax \end{aligned}$$

$$c\left(\frac{x^2}{2} + ax\right)\Big|_0^1 = c\left(\left(\frac{1}{2} + a\right) - \left(\frac{0}{2} + 0\right)\right) = c\left(\frac{1}{2} + a\right)$$

$$c\left(\frac{1}{2} + a\right) = 1$$

$$c = \frac{1}{\frac{1}{2} + a}$$

$$a = 1.1; c = \frac{1}{\frac{1}{2} + 1.1} = 0.625$$

$$f(x) = \begin{cases} 0 & x < 0 \\ 0.625x + 0.6875 & 0 \leq x \leq 1 \\ 0 & 1 < x \end{cases}$$