

$$i$$

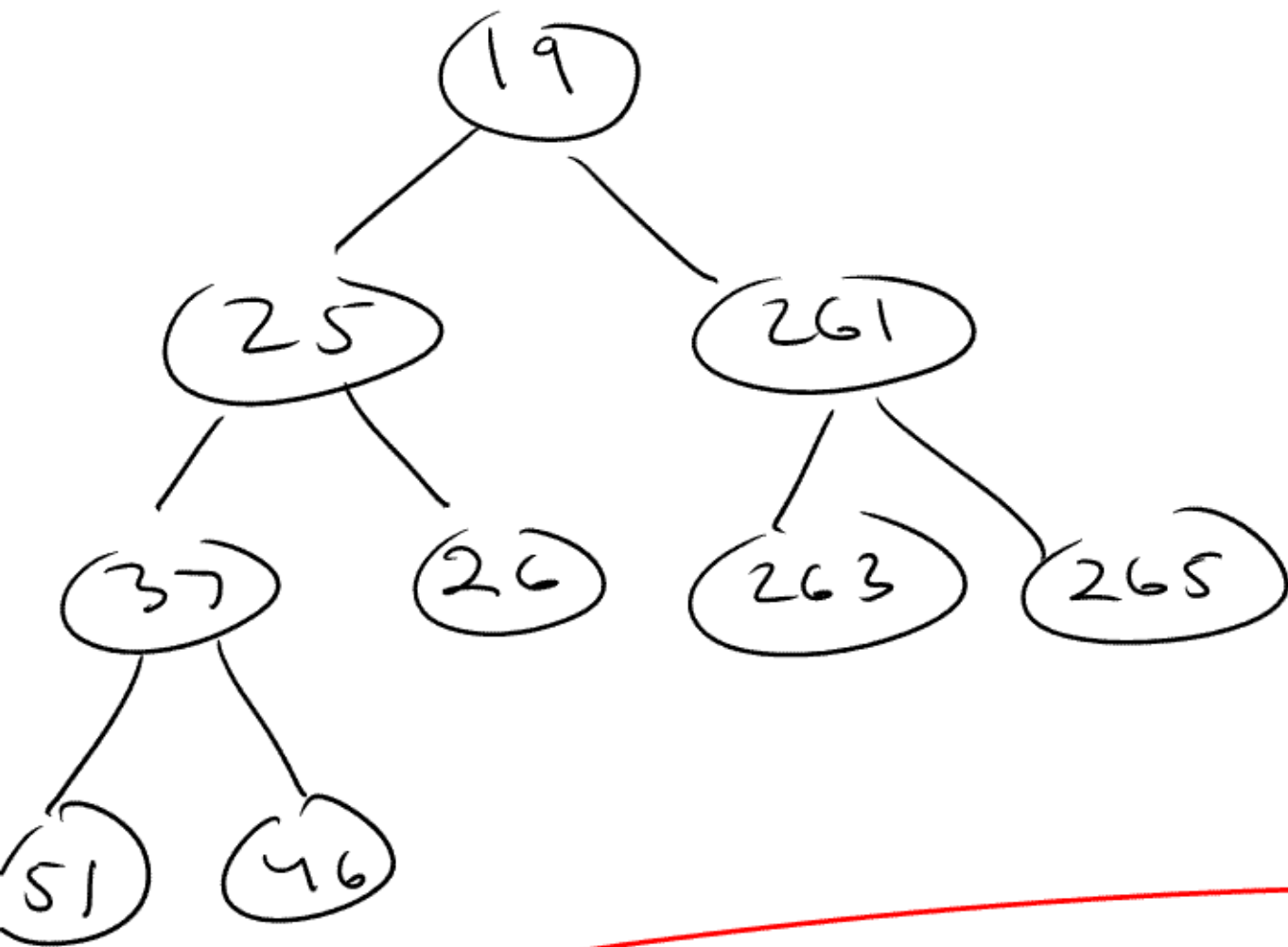
$$\text{LeftChild}(i) = 2i$$

$$\text{RightChild}(i) = 2i + 1$$

$$\text{Parent}(i) = \lfloor i/2 \rfloor$$

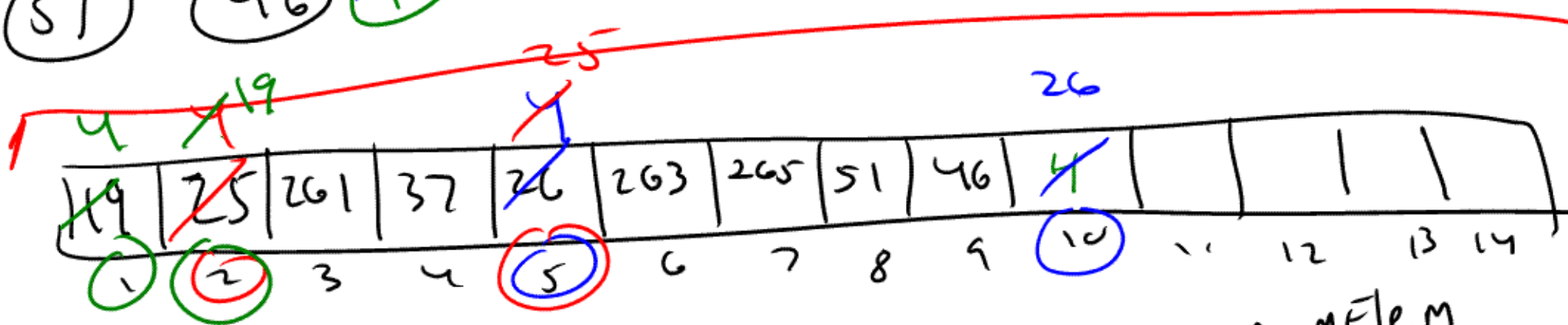
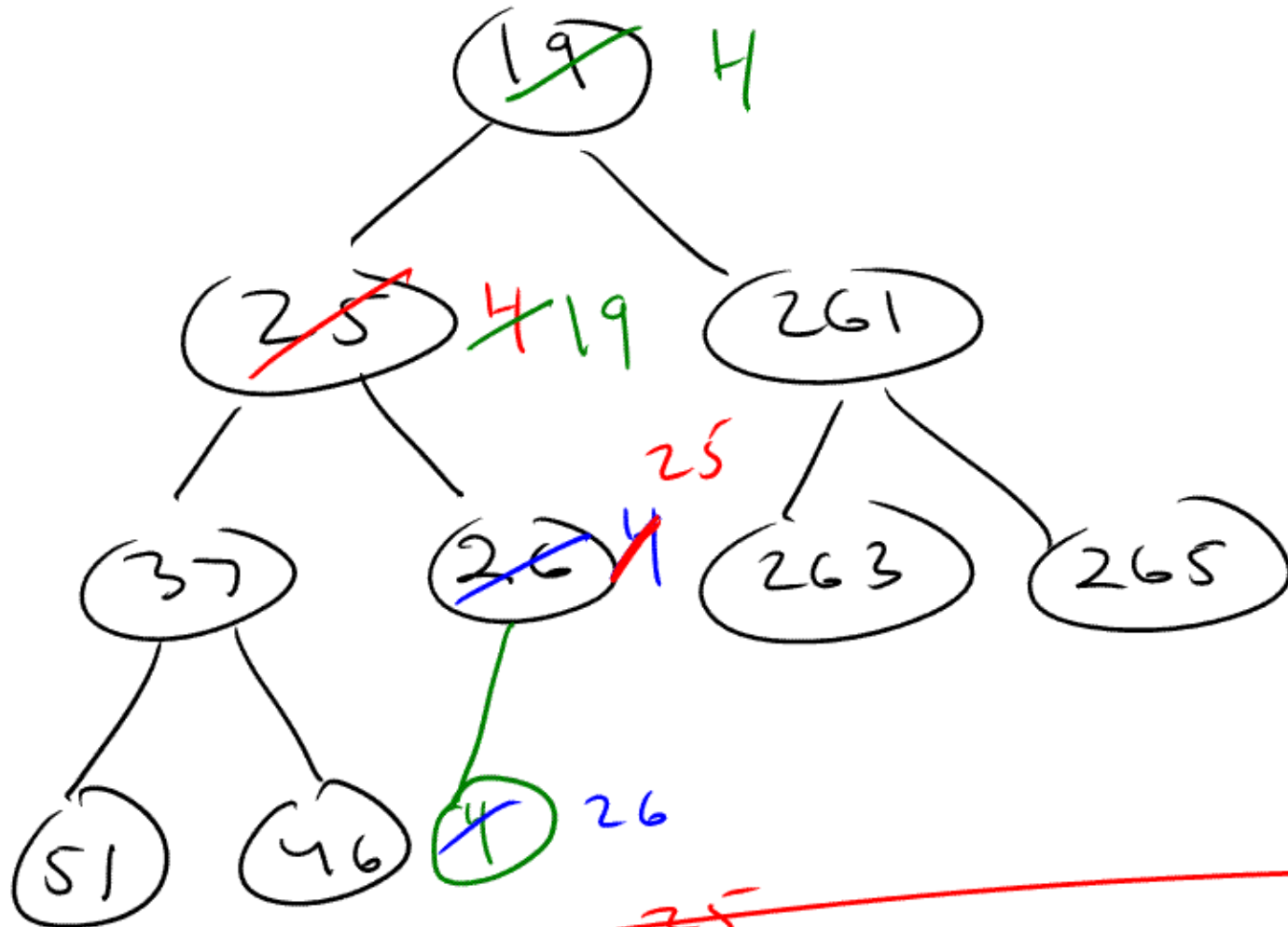
$110 \rightarrow 11$   
 $1100$   
 $1101$

100	31	2019	62	7	4	26	18	31	79
1	2	3	4	5	6	7	8	9	10

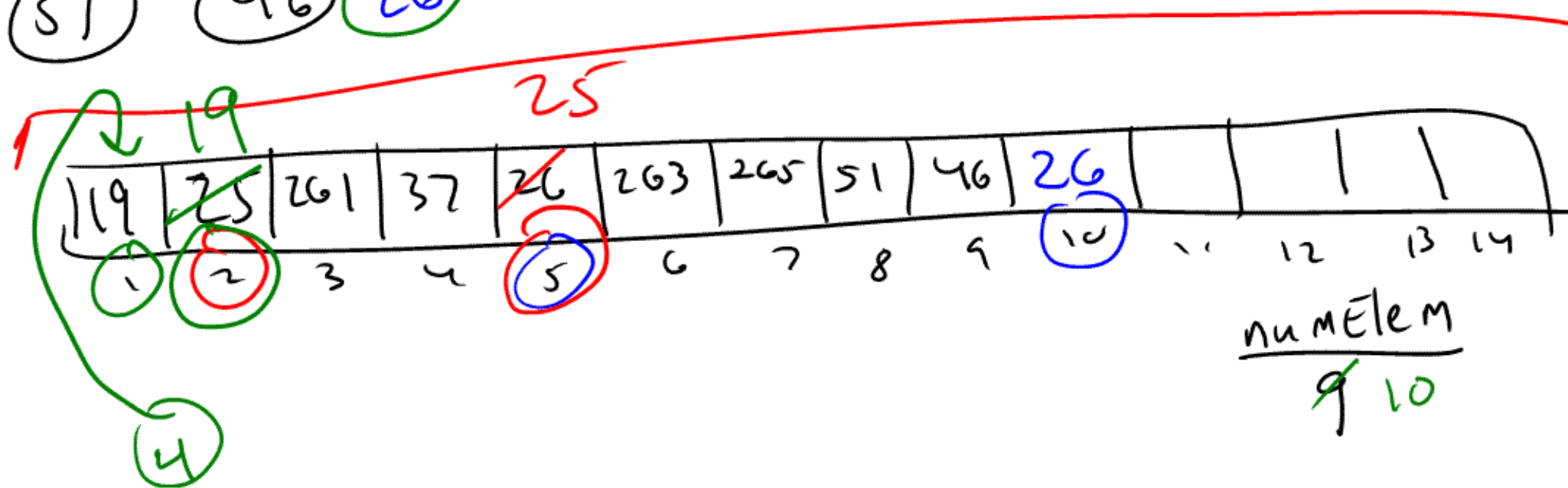
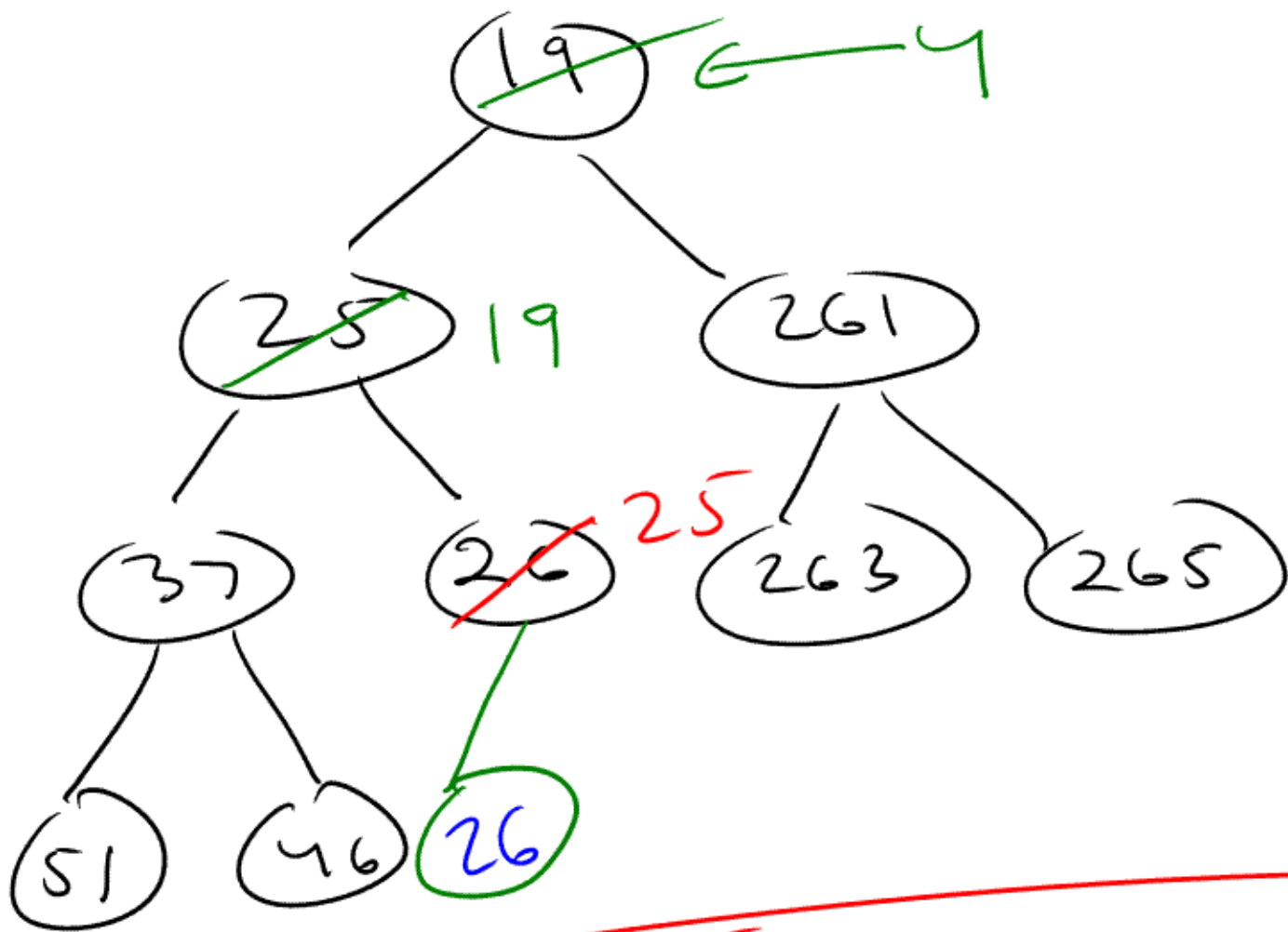


1	19	2	25	3	261	4	37	5	26	6	263	7	265	8	51	9	46	10		11		12		13		14	
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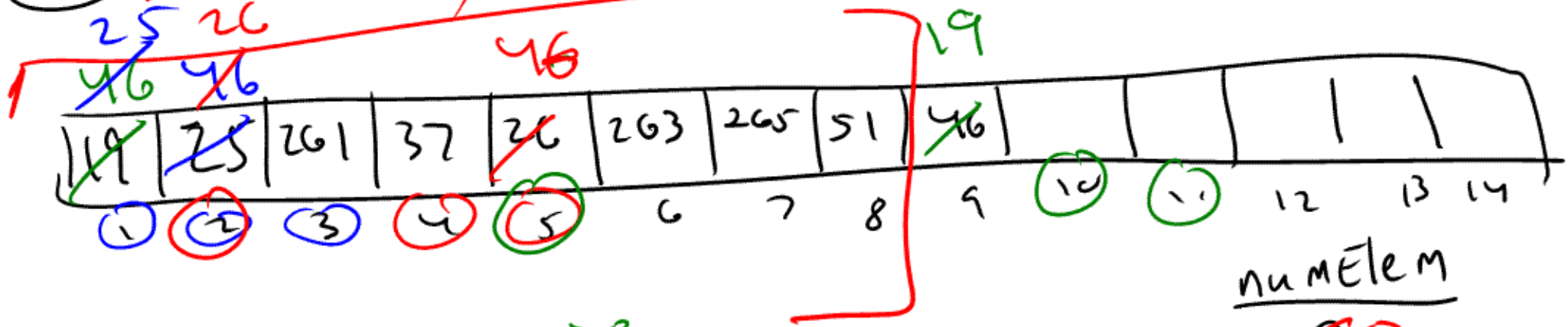
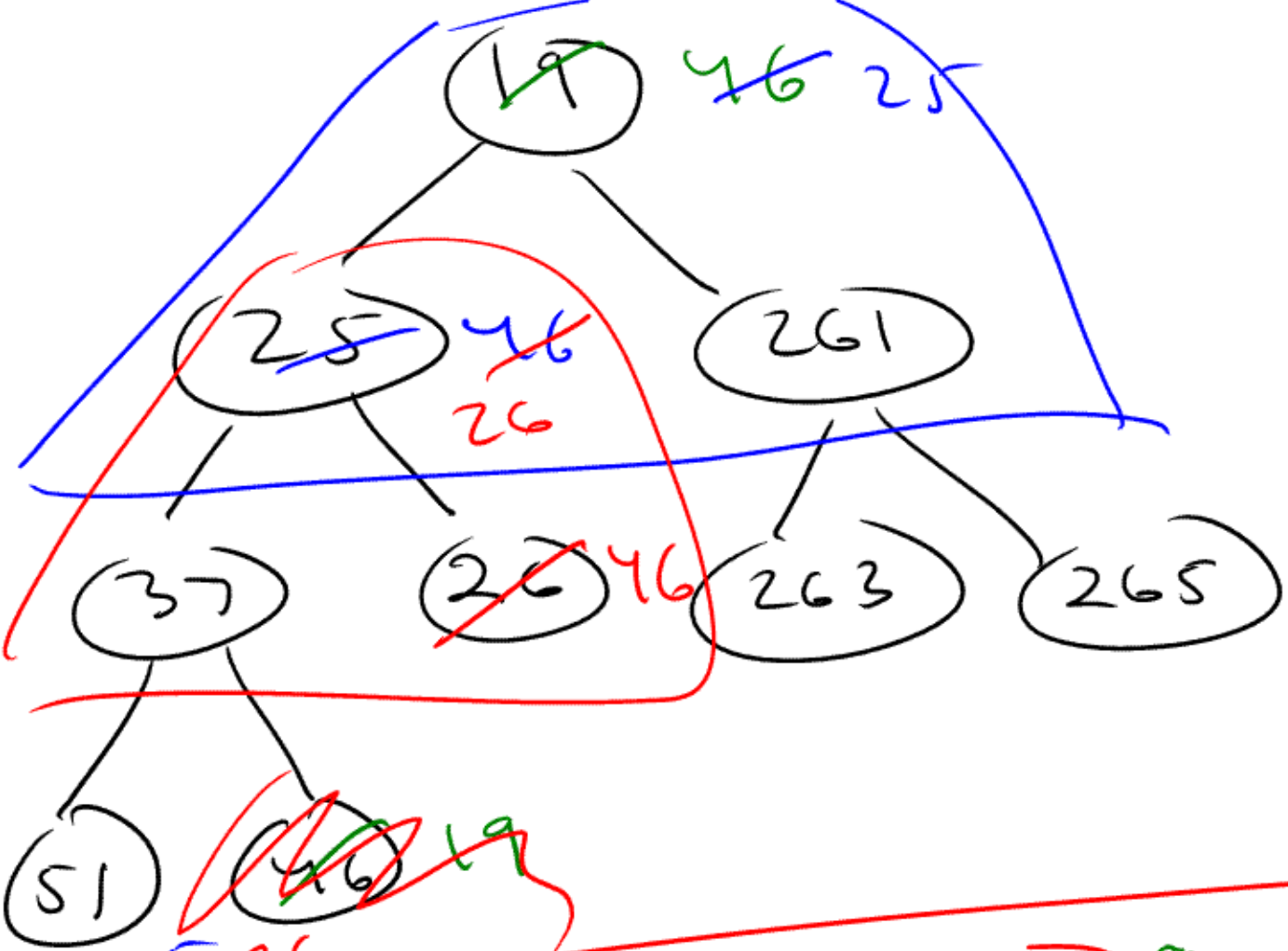
numElem  
9



numElem  
9 10

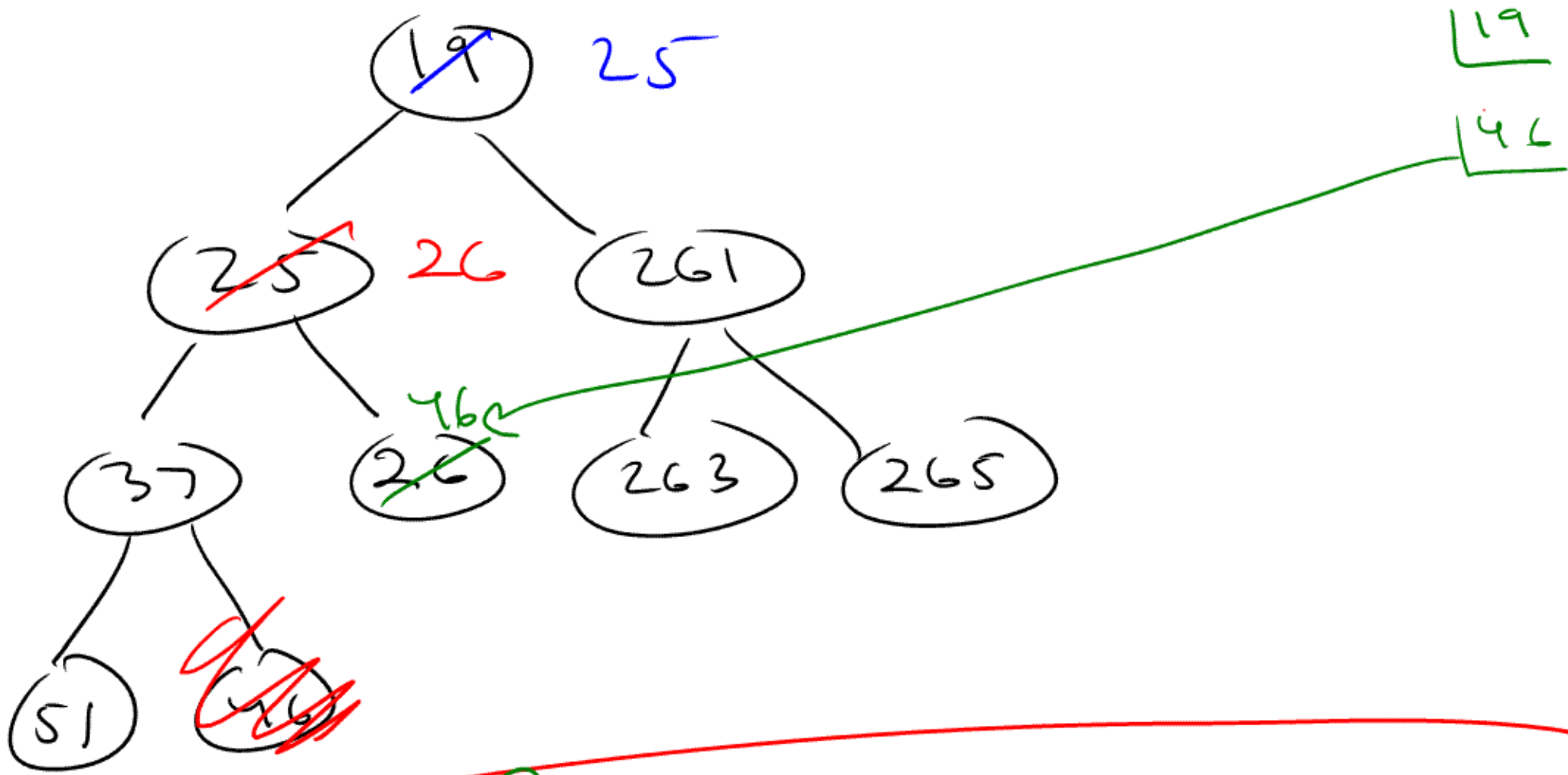


19



10 > 8  
11 > 8

numElem  
98



<del>19</del>	<del>25</del>	261	37	26	263	265	51	<del>46</del>						
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

numElem  
98

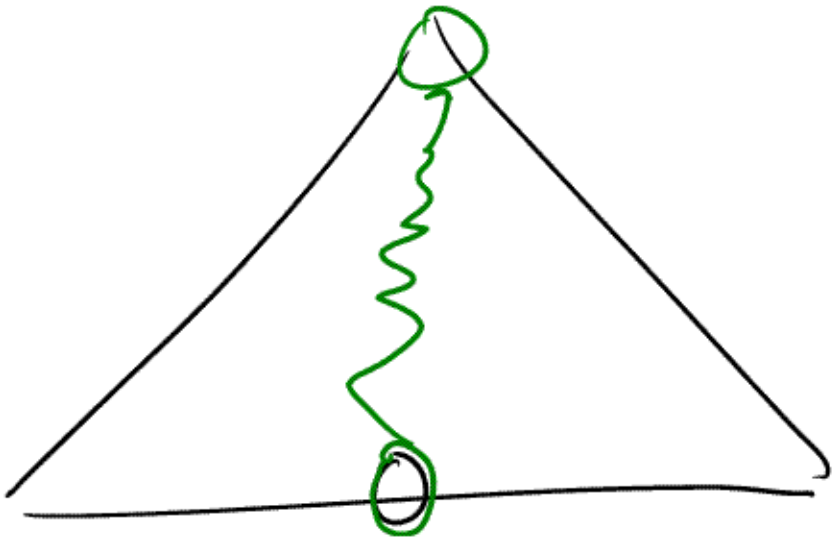
# Analysis

IsEmpty :  $O(1)$

FindMin :  $O(1)$

insert worst case

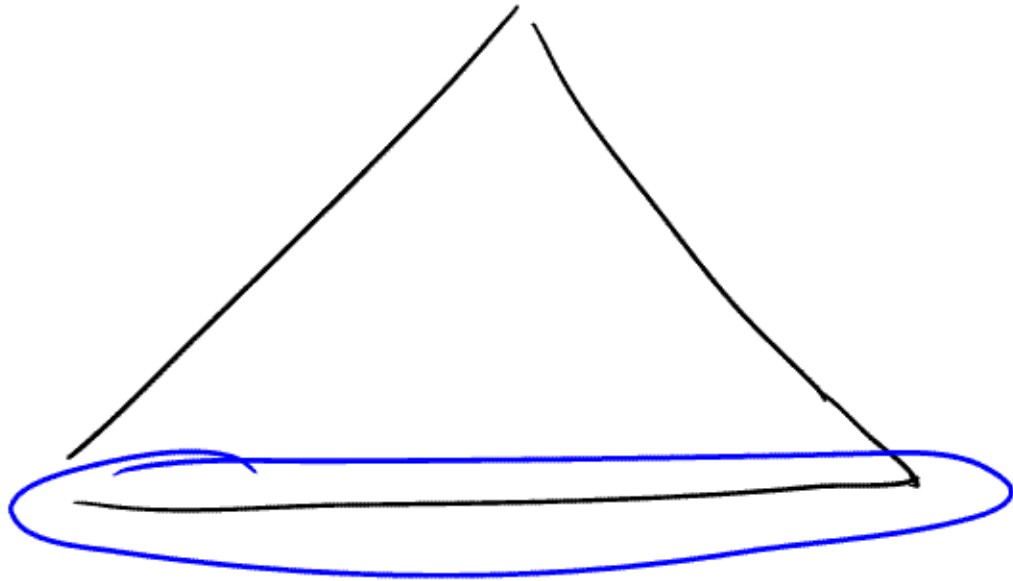
wc  $O(\lg n)$



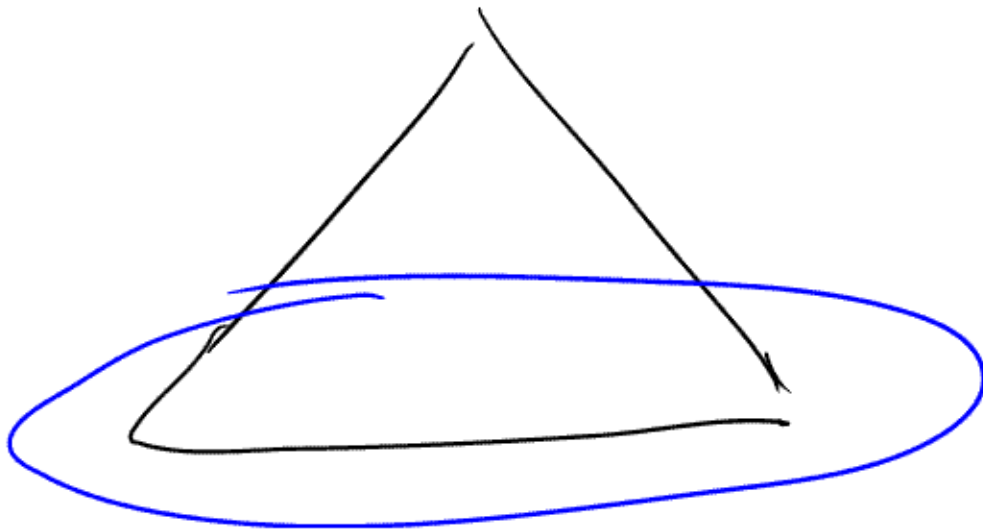
insert

avg case

avg:  $O(1)$

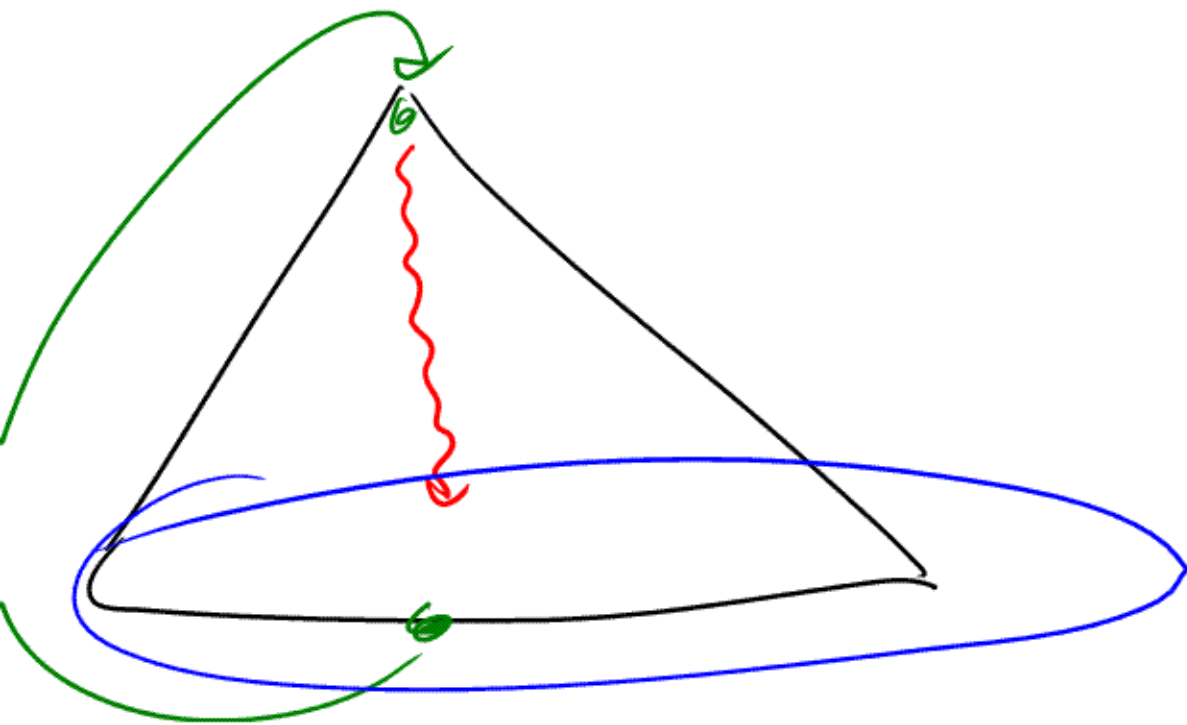


perfect tree  
> 50% of  
values in  
bottom level



complete tree  
> 50% of  
values in  
bottom two  
levels





delete min

wc a avg case

$O(\lg n)$

# Disjoint Sets

$\equiv 0$	$\equiv 3$
$\equiv 1$	$\equiv 4$
$\equiv 2$	$\equiv 5$

$$S_1 \cup S_2 \cup S_3 \cup S_4 \cup \dots \cup S_n = \bigcup$$

$$S_i \cap S_j = \emptyset$$

if  $i \neq j$

a b c

d e f

aRa aRb aRc  
bRa bRb bRc  
cRa cRb cRc

add aRd

↳ dRa

cRd, dRa → eRa  
aRe  
etc.

abc  
def

void Union (Set A, Set B)

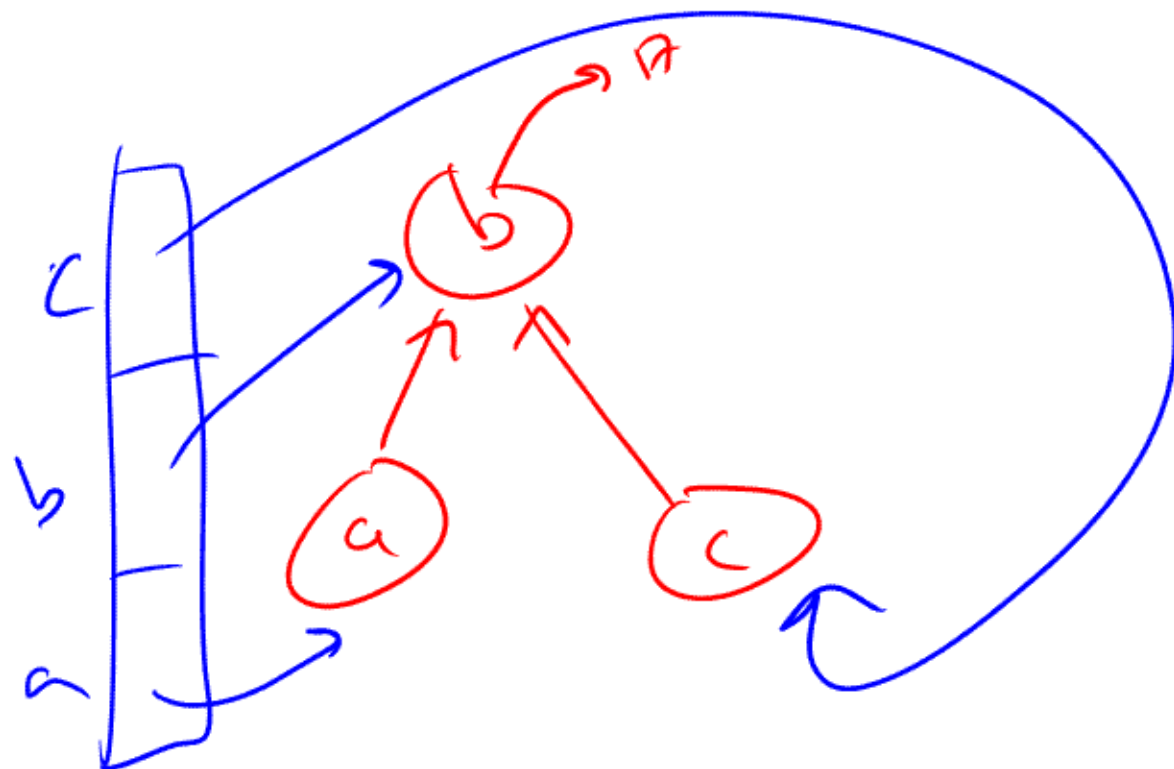
Set Find (element x)

↳ to see if  $a R b$ ,

$\text{Find}(a) == \text{Find}(b)$

→ add  $a R b$

↳  $\text{Union}(\text{Find}(a), \text{Find}(b))$ ;



up-tree