

1. Evaluate the following integrals using the method of substitution.

(a)  $\int \frac{1}{\ln(x^x)} dx.$

(b)  $\int \frac{e^{2x}}{\sqrt{3-4e^{2x}}} dx.$

(c)  $\int \frac{1}{\sqrt{4-(x+3)^2}} dx.$

2. Suppose that  $y = f(x)$  and  $y = g(x)$  are both continuous functions on the interval  $[a, b]$ . Determine if each statement below is always true or sometimes false.

(a) Suppose that  $f(c) > g(c)$  for some number  $c \in (a, b)$ . Then the area bounded by  $f, g, x = a$ , and  $x = b$  can be found by evaluating the integral  $\int_a^b (f(x) - g(x)) dx$ .

(b) If  $\int_a^b (f(x) - g(x)) dx$ , evaluates to -5, then the area bounded by  $f, g, x = a$ , and  $x = b$  is 5.

(c) If  $f(x) > g(x)$  for every  $x \in [a, b]$ , then  $\int_a^b |f(x) - g(x)| dx = \int_a^b (f(x) - g(x)) dx$

3. Find the area bounded by the region between the curves  $f(x) = x^3 + 2x^2$  and  $g(x) = x^2 + 2x$ .

4. Find the area bounded by the region enclosed by the three curves  $y = x^3$ ,  $y = -x$ , and  $y = -1$ .

5. Find the area bounded by the curves  $y = \cos(x)$  and  $y = \sin(2x)$  on the interval  $[0, \frac{\pi}{2}]$ .

6. Find the area of the triangle with vertices at the points  $(0, 1)$ ,  $(3, 4)$ , and  $(4, 2)$ . USE CALCULUS.

7. For each function below: (i) determine which method to use to evaluate the function (formula, u-substitution, or integration by parts, and (ii) evaluate the integral.

(a)  $\int \frac{\sqrt{\ln(x)}}{x}.$

(b)  $\int (\ln(x))^2.$