

Master Thesis M347
Modeling of Fast-Switching Transformers
for Voltage Stability Studies in Python

Author: Maximilian Markus Veit Köhler, B.Eng.
23176975

Supervisor: Ilya Burlakin, M.Sc.
Georg Kordowich, M.Sc.

Date of submission: 02nd May 2025



Contents

1	Introduction	1
1.1	Research Interests	2
1.2	Construction of the Thesis	3
2	Fundamentals	4
2.1	Power System Modeling	4
2.1.1	Transformer Electric Model and Behavior	5
2.1.2	Further Considerations of a Transformer Model	8
2.1.3	Open-Source Power System Simulation tools	8
2.2	Commonly Used On-Load Tap Changer Control	8
2.3	Voltage stability basics	9
2.3.1	Voltage stability definitions, classifications, and conditions	9
2.3.2	Analytical stability calculation of simple static power systems	10
2.3.3	Stability Limits of Complexer Systems: Continuation Power Flow	10
2.3.4	Stability Indices for Time Series Calculation	10
2.4	Summary in Short and Simple Terms	12
3	Methodical Modeling	13
3.1	Transformer Equipment Modeling	13
3.1.1	Implementing a Π -Representative Circuit with Variable Ratio	13
3.1.2	Tap Changer Control Modeling	16
3.1.3	Experimental: Extended Ideas and Improvements	20
3.2	Application of Voltage Stability	20
3.2.1	Influences of other device characteristics	20
3.2.2	Observing the current state of the system	20
3.3	Summary in Short and Simple Terms	21
4	Verification Setup and Results	22
4.1	Representative Electrical Networks	22
4.2	Validation Steps	24
4.2.1	Validation of the Π -Modeled Transformer with Variable Tap Position	24
4.2.2	Validation of the OLTC Control Schemes	24
4.2.3	Voltage Stability Rating Plausibility	24
4.3	Discussion of Model Limitations and Improvements	25
4.4	Summary in Short and Simple Terms	25

5	Case Study	26
5.1	Novel Control Strategy FSM	26
5.1.1	Scenario Setting	27
5.1.2	Simulation	27
5.1.3	Results	27
5.2	Influence of FSM on Voltage Angle Stability of Machines	27
5.3	Possible Extension for Power Flow Congruent Control	27
5.4	Summary in Short and Simple Terms	28
6	Discussion of the Results	29
6.1	Summary in Short and Simple Terms	29
7	Summary and Outlook	30
	Acronyms	XIII
	Symbols	XIII
	List of Figures	XV
	List of Tables	XVI
	List of Listings	XVII
	Bibliography	XVIII
	Appendix	a

1 Introduction

Some blibla as introduction. [1]

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, consectetur id, vulputate a, magna. Donec vehicula augue eu neque. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Mauris ut leo. Cras viverra metus rhoncus sem. Nulla et lectus vestibulum urna fringilla ultrices. Phasellus eu tellus sit amet tortor gravida placerat. Integer sapien est, iaculis in, pretium quis, viverra ac, nunc. Praesent eget sem vel leo ultrices bibendum. Aenean faucibus. Morbi dolor nulla, malesuada eu, pulvinar at, mollis ac, nulla. Curabitur auctor semper nulla. Donec varius orci eget risus. Duis nibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.

Nam dui ligula, fringilla a, euismod sodales, sollicitudin vel, wisi. Morbi auctor lorem non justo. Nam lacus libero, pretium at, lobortis vitae, ultricies et, tellus. Donec aliquet, tortor sed accumsan bibendum, erat ligula aliquet magna, vitae ornare odio metus a mi. Morbi ac orci et nisl hendrerit mollis. Suspendisse ut massa. Cras nec ante. Pellentesque a nulla. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Aliquam tincidunt urna. Nulla ullamcorper vestibulum turpis. Pellentesque cursus luctus mauris. Some more Text.

Nulla malesuada porttitor diam. Donec felis erat, congue non, volutpat at, tincidunt tristique, libero. Vivamus viverra fermentum felis. Donec nonummy pellentesque ante. Phasellus adipiscing semper elit. Proin fermentum massa ac quam. Sed diam turpis, molestie vitae, placerat a, molestie nec, leo. Maecenas lacinia. Nam ipsum ligula, eleifend at, accumsan nec, suscipit a, ipsum. Morbi blandit ligula feugiat magna. Nunc eleifend consequat lorem. Sed lacinia nulla vitae enim. Pellentesque tincidunt purus vel magna. Integer non enim. Praesent euismod nunc eu purus. Donec bibendum quam in tellus. Nullam cursus pulvinar lectus. Donec et mi. Nam vulputate metus eu enim. Vestibulum pellentesque felis eu massa. [MK]Write a nice introduction.

1.1 Research Interests

Here are gaps and possible extension of knowledge.

Here are the research objectives and questions.

- Influence of OLTC control on possible operational uses: Short-term voltage stability, long-term voltage stability;
- Can a increased dynamic regulation help machine recovery?
- Does the increased tap ratio gradient harm transient stability of machines? Does it help or harm CCT of machines or machine groups?
- Transformers act as big low-pass filters: Can this behavior be beneficial as well for the interactions of inverters in the grid on AC side (in the sense of Harmonic Stability)? [Quelle]

Research Question of this Thesis

How do different control types and characteristics of Tap Changing transformers influence the voltage stability of the given system?

Therefore following questions/steps can be imagined as supportive:

1. How can Voltage stability of a system be classified and be looked at? Which indices, measurements, etc.
2. Which transformer model has to be considered to show influences?
3. Which additional load models, source models, transmission model have to be modeled for an adequate assessment?
4. Which systems are useful to consider in showing effects? Which circumstances lead to a stability support, which to a decrease? Where can limits be drawn?

Additionally during the process of the thesis, the following question came up as an extension. Is is the second interest of this thesis, and shall be more focused in the later part. Therefore some assessments in the chapter 5 are conducted.

Additional Question of this Thesis

Can the already existing Tap Changer Control of the Fast Switching Module (FSM) be improved towards a more operation oriented control?

1.2 Construction of the Thesis

The afore stated research interests in combination with the yet not sufficient framework to use make demands on the structure of this work. Therefore it seems not sufficient trying to apply a completely standard sequence of chapter like „Introduction - Fundamentals - Methods - Results - Discussion“. Instead, the following structure is chosen to fulfill the research interests and to give a clear and understandable overview of the work.

Chapter 1: Introduction

Bibla

Chapter 2: Fundamentals

Bibla

Chapter 3: Methodical Modeling

Bibla

Chapter 4: Verification Setup and Results

Bibla

Chapter 5: Case study

Bibla

Chapter 6: Discussion of the Results

Bibla

Chapter 7: Summary and Outlook

Bibla

2 Fundamentals

Following chapter shall introduce the basics for implementing an OLTC equipped transformer into a existing PSS framework. This is considering the already existing surrounding, more detailed the electric behavior of the transformer itself and some control engineering theory for the corresponding OLTC. Thus its main goal is increasing voltage stability [1], main indices and assessment methods are considered as well.

Voltage stability:

- Definitions, classifications, conditions
- PV-curves / QV-curves
- Derivation of Indices: Practical application

Control engineering:

- State-of-the-art control mechanisms for OLTCs
- Chaos theory controllers

2.1 Power System Modeling

The simulation of power systems is a crucial tool, not only for stability studies, but for evaluating extensions or modifications in the planning process, the development of Assistance systems for operational management, and many other applications. [Quelle] Due to the complexity of the systems, simulations are often simplified. Not only with model constraints, but as well in the way of calculations. Mainly separating between Electromagnetic Transient (EMT) and Root Mean Square (RMS) simulations, the latter is used in this thesis. The section A.1 is giving more details, literature, and summarizing the processes behind the used tool *diffpssi*, if the reader is further interested in the topic.

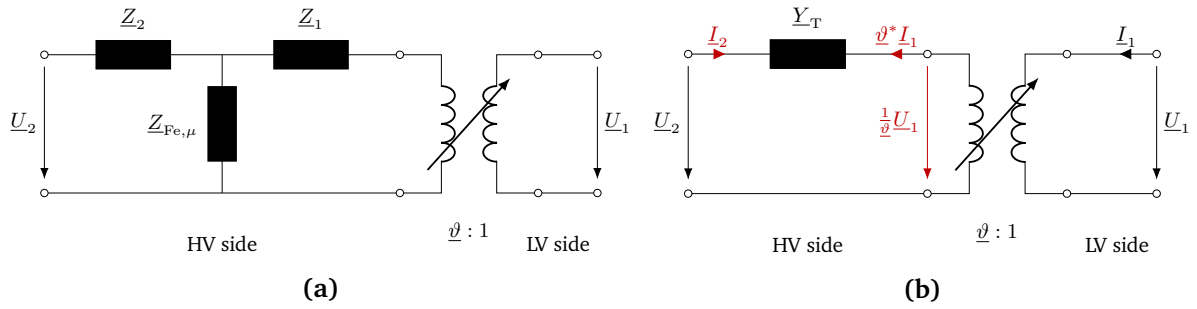


Figure 2.1: Two-Winding Transformer Circuit in the Positive Sequence; a) ideal representation with impedances on the HV side and b) simplified circuit with only the series impedance related on the HV side; own figure after [1]–[3]

2.1.1 Transformer Electric Model and Behavior

Typical for RMS-modeling is the usage of sequence components, especially the positive sequence for symmetrical grid operation and test cases. **[Quelle]** An equivalent circuit for the positive sequence is shown in Figure 2.1 part a), respectively reduced to the transformer ratio, the series impedances of the windings on the LV and HV side, and the shunt branch affected by iron and magnetization losses. [1]–[3]

The transformer ratio is typically noted as ϑ . Generally speaking it is the ratio between the number of windings of the secondary side to the primary side, as noted in Equation 2.1. With the typically used calculation unit „per unit“¹, the ratio becomes one in the standard case. A transformer ratio, which is only shifting current angles with the shifting angle ϕ , is represented through a complex number using the Euler Identity, as shown in Equation 2.2.

$$\vartheta = \frac{N_2}{N_1} \quad (2.1)$$

$$\underline{\vartheta} = \frac{N_2}{N_1} \cdot \exp\left(j \cdot \phi \cdot \frac{\pi}{180}\right) \quad (2.2)$$

The first simplification step is considering two assumptions. First, the iron and magnetization losses are neglectable. This can be illustrated with a short-circuit test of the transformer on the secondary side. During this test, one can obtain with the concept of a voltage divider, that

$$\underline{U}_{Fe,\mu} \ll \underline{U}_{T,rated},$$

¹means standardization to a reference value; further information on page XIV and Machowski, Lubosny, Bialek, *et al.* [1], Appendix A

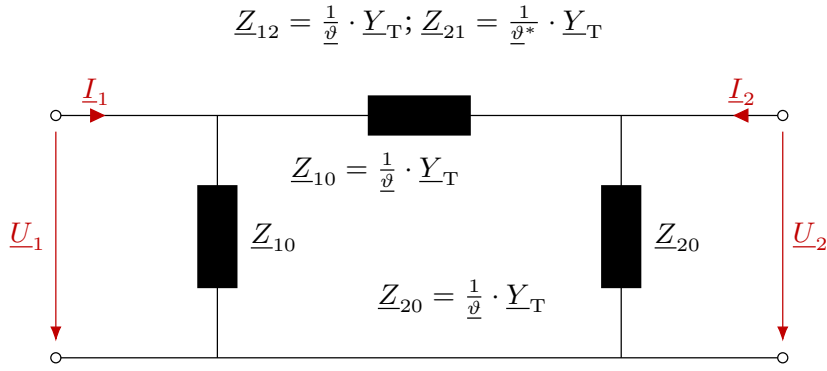


Figure 2.2: Π -representative circuit of an idealized transformer with a tap changer; own figure after [3], [4]

meaning that the shunt branch impedance is much greater than the series impedance of the transformer. Secondly, it is assumed, that the on the primary side related impedance of the secondary side, is equal to the impedance on the primary side. This leads to a symmetrical circuit of the transformer and the positive sequence equivalent circuit simplifies to Figure 2.1 part b). Mathematically this is shortly expressible as Equation 2.3, Equation 2.4, and Equation 2.5. [1]–[3]

$$\underline{Z}_1 = R_1 + jX_1; \quad \underline{Z}_2 = R_2\vartheta^2 + jX_2\vartheta^2 \quad (2.3)$$

$$\underline{Z}_1 = \underline{Z}_2 \quad (2.4)$$

$$\underline{Z}_T = \underline{Z}_1 + \underline{Z}_2 \quad (2.5)$$

The afore described simplification leads to only the necessity of considering the series impedance. Considering the afore mentioned normal ratio of $\vartheta = 1$ in the per unit system, the Python framework *diffpssi* has been using this model with only the series impedance and no variable ratio, meaning no shunt branches, before.

When one wants to look at variable transformer ratios, either with representing vector groups, or implementing On-Load Tap Changers (OLTCs), this model of only considering the series impedance has to be extended. Using shunt branches, the variable ratio behavior can be represented in a Π -model, as shown in Figure 2.2. [1]–[3]

Looking at the transformer as a black box two-port, with the index one being the LV side, the index two being the HV side, the admittance matrix for the variable ratio behavior can be expressed as in Equation 2.6. The voltages and current are defined as in Figure 2.1 part b). With rearranging the equation, one can obtain the admittance matrix of the Π -model with to the HV side related values as in Equation 2.7. [3], [4]

$$\begin{bmatrix} \underline{\vartheta}^* I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} \underline{Y}_T & -\underline{Y}_T \\ -\underline{Y}_T & \underline{Y}_T \end{bmatrix} \cdot \begin{bmatrix} \frac{1}{\underline{\vartheta}} \underline{U}_1 \\ \underline{U}_2 \end{bmatrix} \quad (2.6)$$

$$\underline{\mathbf{Y}}_{\Pi,T} = \underline{Y}_T \cdot \begin{bmatrix} \frac{1}{\underline{\vartheta}\underline{\vartheta}^*} & -\frac{1}{\underline{\vartheta}^*} \\ -\frac{1}{\underline{\vartheta}} & 1 \end{bmatrix} \quad (2.7)$$

For calculation of the individual shunt branches, one can apply the standard representation of two-ports consistent of a linear Π -circuit:

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} \underline{Y}_{10} + \underline{Y}_{12} & -\underline{Y}_{12} \\ -\underline{Y}_{21} & \underline{Y}_{20} + \underline{Y}_{21} \end{bmatrix} \cdot \begin{bmatrix} \underline{U}_1 \\ \underline{U}_2 \end{bmatrix}$$

When equating this with Equation 2.7, the shunt branches can be calculated respectively giving the admittances written down as Equation 2.8, Equation 2.9, and Equation 2.10, as they are noted in Figure 2.2 as well. [3], [4]

$$\underline{Y}_{12} = \frac{1}{\underline{\vartheta} \cdot \underline{a}_T^*} \cdot \underline{Y}_T, \text{ and}$$

$$\underline{Y}_{21} = \frac{1}{\underline{\vartheta} \cdot \underline{a}_T} \cdot \underline{Y}_T \quad (2.8)$$

$$\underline{Y}_{10} = \frac{1}{\underline{\vartheta}} \cdot \left(\frac{1}{\underline{\vartheta}} - \frac{1}{\underline{a}_T} \right) \cdot \underline{Y}_T \quad (2.9)$$

$$\underline{Y}_{20} = \left(1 - \frac{1}{\underline{\vartheta} \cdot \underline{a}_T} \right) \cdot \underline{Y}_T \quad (2.10)$$

Reactances and resistances are referred to the base voltage and apparent power of the operational unit, such as the transformer. The power system simulation uses its own base voltage and base apparent power, enabling the use of one single calculation domain. This is done to simplify the calculation and to make the results easily comparable to each other. Hence, the referred values have to be transformed from the equipment

based values to the simulation based values. The relations and conversions are defined as follows.

$$\underline{Y}_{T, \text{ sim}} = \underline{Y}_T \cdot \frac{S_n}{S_{n, \text{ sim}}} \quad (2.11)$$

Displayed like in Equation 2.11, the characteristic of the operational unit is referred to the simulation base value. Here, the admittance of the transformer is multiplied with its own rated apparent power, then divided by the apparent power of the simulation system. Similar, the voltages are calculated via ???. This specialities are considered in the tap changer modeling, thus further information is given in [1], Appendix A.

2.1.2 Further Considerations of a Transformer Model

Describe here the asymmetric and non-idealized transformer; phase shifting transformers; transformers, which can control longitudinal and transversal ratios; ...

2.1.3 Open-Source Power System Simulation tools

Some information about other open source python power system simulation tools, such as:

- Pandapower,
- TOPS,
-

Build up like a scan (see Georg's thesis).

BUT: As well including the there used implementation of transformers mathematical background and complexity.

2.2 Commonly Used On-Load Tap Changer Control

A few basics are in the interest, understanding differences between real world behavior, or possible ways of building up a OLTC transformer control. This control theory difference can be limiting as well for the results and objectives compared to the actual possible control in the field.

The target voltage is typically set from the control room of the grid operator, coming from pre-calculated load flow analysis. This can be set hours before, or even day-ahead with the estimated loads of the grid. This value is set locally for each operating unit subsequently. The control is then operating locally and without further involvement of the grid operator. [Quelle]

Typically the used controller in the field is a discrete controller, which can change tap positions under load within a time frame of around few seconds. Practical tap steps are around 2 % of the overall transforming ratio. The control is set up with a dead band, to avoid unnecessary tap changes. It is necessary to note here, that this control and its mathematical characteristics contains logical elements, blocks, and delays, which cannot be translated in a typical control theory transmission function. This leads to the missing possibility to easily obtain mathematical stability for the control of the overall considered power system. [Quelle]

2.3 Voltage stability basics

2.3.1 Voltage stability definitions, classifications, and conditions

A Practical introduction to voltage stability assessment, methods and indices is given in the standard and extending literature of Rueda-Torres, Annakage, Vournas, *et al.* [5], Danish [6], and Cutsem and Vournas [7].

Interesting to note/implement here: Basic classification, definitions, and the nature or conditions of voltage stability. Such as

- Short term vs. long term
- Static vs. dynamic
- Transmission driven vs. load driven vs. generation driven; stability/instability, and/or contributions
- Influence OLTC: Restoring voltage level, but not adding reactive capacities; hence adding risk of voltage collapses
- Load vs. transmission aspects
- Example mechanism: **Collapse effect of the nordic test system** [7], [8]

Table 2.1: Voltage instability types and different time frames with examples; after [Quelle]

No	Type	Cause of incident	Time frames
1	Long-term	Slowly use up of reactive reserves and no outage	Several minutes to several hours
2	Classical	Key outage leads to reactive power shortage	One to five minutes
3	Short-term	Induction motor stalling leads to reactive power shortage	Five to fifteen seconds

2.3.2 Analytical stability calculation of simple static power systems

2.3.3 Stability Limits of Complexer Systems: Continuation Power Flow

2.3.4 Stability Indices for Time Series Calculation

The idea behind stability indices is monitoring the current voltage stability state of the power system in relation to the critical point. This applies not only to static load flow cases, but for time series calculations of short circuits, load shedding or other disturbances. Therefore the dynamic contribution can be included as well. [Quelle]

Reviewing possible indices, either for online resp. real time monitoring or for subsequent analysis after a simulation, is out of the scope of this thesis. Danish [6] has already included an extensive review in his work, with reference to Doig Cardet [9], which is focussing on indices in interest for this thesis in particular. *Jacobian Matrix based interesting, because of the possible observability in diffpssi.*

One easy idea for obtaining a stable operation is looking at the Jacobian Matrix. Although it is mainly used in load flow calculations, it is possible to derive statements about the voltage stability as well. This can be realized through the relation of real power P , reactive power Q , voltage angle δ , and the voltage resp. voltage gradients

ΔV . If the Jacobian Matrix is getting singular, the System will not remain in a stable operation. Singularity of matrices is checked by following two hypothesis tests:

$$\det(\mathbf{J}) = 0 \quad (2.12)$$

$$J \times J^{-1} \uparrow \quad (2.13)$$

The Jacobian Matrix is defined as:

$$\mathbf{J} = \begin{bmatrix} \Delta \mathbf{P} \\ \Delta \mathbf{Q} \end{bmatrix} = \begin{bmatrix} \mathbf{H} & \mathbf{M}' \\ \mathbf{N} & \mathbf{K}' \end{bmatrix} \cdot \begin{bmatrix} \Delta \delta \\ \Delta V/V \end{bmatrix}$$

$$\begin{bmatrix} \Delta P_1 \\ \vdots \\ \Delta P_n \\ \Delta Q_1 \\ \vdots \\ \Delta Q_n \end{bmatrix} = \begin{bmatrix} \frac{\partial P_1}{\partial \delta_1} & \dots & \frac{\partial P_1}{\partial \delta_n} & V_1 \frac{\partial P_1}{\partial V_1} & \dots & V_n \frac{\partial P_1}{\partial V_n} \\ \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \frac{\partial P_n}{\partial \delta_1} & \dots & \frac{\partial P_n}{\partial \delta_n} & V_1 \frac{\partial P_n}{\partial V_1} & \dots & V_n \frac{\partial P_n}{\partial V_n} \\ \frac{\partial Q_1}{\partial \delta_1} & \dots & \frac{\partial Q_1}{\partial \delta_n} & V_1 \frac{\partial Q_1}{\partial V_1} & \dots & V_n \frac{\partial Q_1}{\partial V_n} \\ \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \frac{\partial Q_n}{\partial \delta_1} & \dots & \frac{\partial Q_n}{\partial \delta_n} & V_1 \frac{\partial Q_n}{\partial V_1} & \dots & V_n \frac{\partial Q_n}{\partial V_n} \end{bmatrix} \cdot \begin{bmatrix} \Delta \delta_1 \\ \vdots \\ \Delta \delta_n \\ \Delta V_1/V_1 \\ \vdots \\ \Delta V_n/V_n \end{bmatrix} \quad (2.14)$$

Although this method seems easy to implement, there are some numerical problems realted to that. Checking if a Matrix is singular with numerical methods, can only be realised as a probablilty expression. A result could be, that the determinant of the matrix is below a certain threshold. The algorithm would propose, that the matrix is probabilistic singular. **[Quelle]**

This problem leads to the necessity of applying other methods or indices for stability assessment. Further, the relation of the system state to the critical voltage collapse point is highly nonlinear in the Jacobian Matrix. This problem is adresssed by the indices in various ways, leading to a more or less linearized relation. **[Quelle]** Danish [6] is proposing a few other indices, that are based on the Jacobian Matrix, and shows comparative characteristics between Jacobian Matrix and system variable based voltage stability indices. These Jacobian Matrix based indices are listed and further described in section A.2, while the comparative characteristics are described in section A.3. The aforeside mentioned work of Doig Cardet [9] is focussing on these indices in particular.

For this thesis, the indices in Table 2.2 are chosen on the basis of the work of Danish [6] and Doig Cardet [9]. They will be implemented in the Python framework in section 3.2, and used for with the theoretical calculated limits of subsection 2.3.2 and subsection 2.3.3.

Table 2.2: Voltage stability indices for the assessment of the power system stability in this thesis; after [Quelle]

Index	Basis	Description
VCPI	Jacobian Matrix	The index is based on the Jacobian Matrix, and is showing the proximity of the current system state to the critical voltage collapse point.
VSI	System Variables	The index is based on the system variables, and is showing the proximity of the current system state to the critical voltage collapse point.

2.4 Summary in Short and Simple Terms

3 Methodical Modeling

3.1 Transformer Equipment Modeling

Some literature and fundamentals about transformers, control, stability assessment, fast-switching modules, and analysis in Python.

Things to mention:

- First model: Admittance Matrix manipulations
- Second model: Current Injection Model

3.1.1 Implementing a Π -Representative Circuit with Variable Ratio

Mathematical Description and Definitions

Describe the Transformer circuit, the Π -model, simplification of impedances, relation to the specific side, ...

1. Show the admittance matrix deduction process for placing the impedances on one side
2. How to interpret \underline{v} ; especially if complex and a mixture of longitudinal and angle ratio
 - > e.g. Asymmetrical shifter, vector groups, or only tapping on the current-voltage angle ϕ
3. Illustrate differences if the impedance relation is switching sides (Machowski vs. Kundur / Milano)
 - > refer the admittances to the lv or hv side: different definition of \underline{v} , different admittance matrix of the transformer
4. Dependency of connections? (which side, step-up, step-down transformer?)

Important note on indices: 1 always LV side, 2 always HV side; ϑ is always on the HV side, meaning when relating the impedances to another side, the admittance matrix is differing. This is the difference between the Machowski and the Kundur / Milano approach. In the simulation tool, this has to be understood and implemented towards the correct side.

Mathematical for MACHOWSKI / SIMULATION

Similar to the mentioned typical assumptions from [1]

- Neglecting (normally big) shunt branches in the circuit,
- Assuming the impedances on the HV and LV side are symmetrical (the same), and
- (...more?),

these are considered in this paper as well.

Procedure for accounting the Admittance Matrix:

1. Set constraints as Ohms law for the admittance matrix and the tap ratio,
2. Re-arrange equation to set currents and voltages independent of the transformer ratio,
3. calculate the series admittance and the shunt admittances after the given standard formula.

$$\begin{bmatrix} \underline{I}_1 \\ \underline{I}_2 \end{bmatrix} = \begin{bmatrix} \underline{Y}_{12} + \underline{Y}_{10} & -\underline{Y}_{12} \\ -\underline{Y}_{21} & \underline{Y}_{21} + \underline{Y}_{20} \end{bmatrix} \cdot \begin{bmatrix} \underline{U}_1 \\ \underline{U}_2 \end{bmatrix} \quad (3.1)$$

OLTC tap ratio definition:

$$\underline{\vartheta} = 1 + k \cdot \Delta v \quad (3.2)$$

$$\text{with } k \in [k_{\min}; k_{\max}]; k_{\min} \equiv -k_{\max} \quad (3.3)$$

Angle definition as multiplication to the tap ratio:

$$\underline{a}_T = \exp\left(j \cdot \phi \cdot \frac{\pi}{180}\right) \quad (3.4)$$

Mathematical for Paper ILYA and KUNDUR / MILANO

Relavant points for the definition of the OLTC ratio:

- Complex vs. Rational number: Angle or Asymetric shifter
- How can angles and logitudinal ratios be mathematically expressed?
- How to understand when Relation to hv or lv side?

The OLTC ratio \underline{v} when placing the replacement impedance \underline{Z}_T , respectively the replacement admittance \underline{Y}_T , on the high voltage side is defined as:

$$\underline{v} = 1 + k \cdot \Delta v \quad (3.5)$$

$$\text{with } k \in [k_{\min}; k_{\max}]; k_{\min} \equiv -k_{\max} \quad (3.6)$$

Within this definition, k_{\min} defines the minimum tap position, k_{\max} the maximum OLTC postition. When relating the replacement impedance to the low voltage side, the tap ratio is defined differently, while looking at the tap position in Equation 3.6 in the same manner.

$$\underline{v} = \frac{1}{1 + k \cdot \Delta v} \quad (3.7)$$

Voltage angle shifting through the influence of vector groups, meaning a different wiring and thus magnetic coupling of the transformer can be expressed within the transformer model. By mathematically applying a turning vector with the length of one to the overall tap ratio, this can be included in the model. Mathematical, this is expressed by the following equation. The characteristic number n_T is relating to to angle, with one step being equal to 30° angle ratio.

$$\underline{a}_T = \exp\left(j \cdot n_T \cdot \frac{\pi}{6}\right) \quad (3.8)$$

Just briefly describe the influence of an asymetric vs. an ideal transformer. Why the difference and how the representation could work.

Additional Algorithmics

- How to automatically determine switching direction?
-> switchin direction dependent on what? (load-flow direction?)

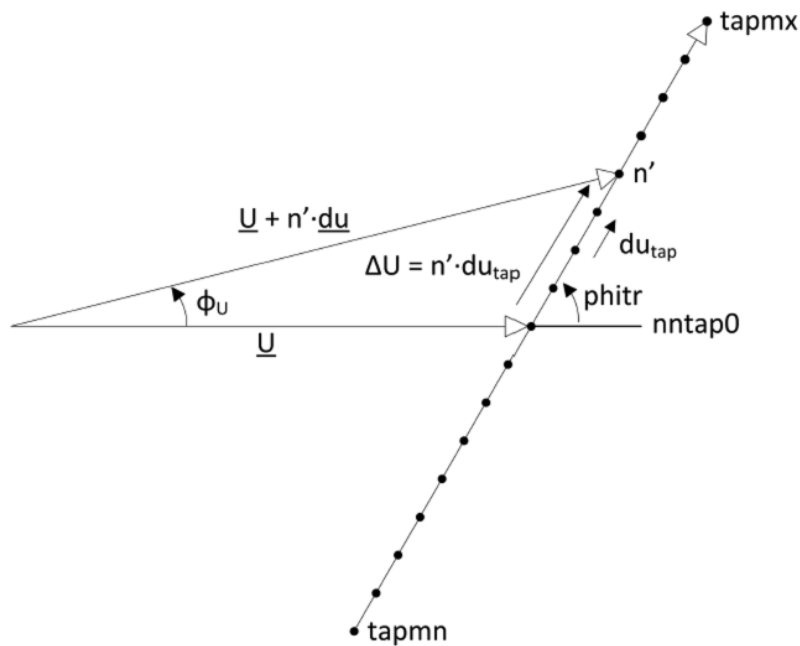


Figure 3.1: Illustration of the tap ratio vector for an ideal and an asymmetric transformer; from the **DigSILENT Technical Reference Manual** ... [Quelle]

- Controller set points: also dependent on load flow?
- How can I change the transformer control setpoints to be load flow dependent?
- How can I ensure, utilization of the transformer is not $> S_n$?

3.1.2 Tap Changer Control Modeling

This is the description of the ideas, development, and implementation of a OLTC control scheme.

Discrete Control Loop

- Describe implementation
- Describe benefits / drawbacks
- Control scheme
- Switching logic and behavior (voltage tracking)

This control method represents the currently most used and thus representative control scheme for OLTCs. With the mechanic nature of the switching mechanism, the control look can only access discrete ratios within time frames of around a few seconds. Such

a discrete control loop is described by Milano [3], [10]. A scheme of this control loop is shown in Figure 3.2.

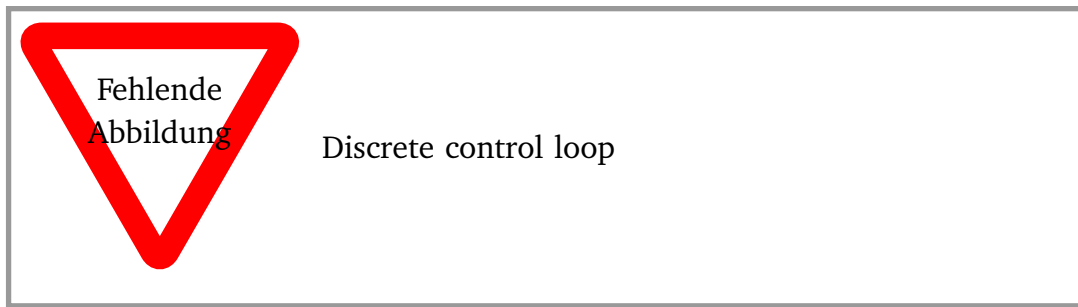


Figure 3.2: Discrete control loop of an OLTC; scheme based on Milano [10]

This control loop type is beneficial due to its accurate representability of current OLTC abilities. It gains access to assess stability within simulation environments, as analytical methods are not suited.

A negative aspect of a discrete control loop is the missing opportunity of generating a transfer function. This blocks the stability assessment with standard control engineering methods. Further, popular analysis methods like eigenvalue analysis is not possible, due to the lack of possibility to form derivatives.

The structure of the implementation is illustrated in the block diagram of Figure 3.3. The controller is actively changing the algebraic functions of the simulation environment, therefore it is quasi dynamic. The controller output logic is called, when updating the admittance matrix of the transformer. Additionally, the differential functions of the connected simple controllers, like integrators, PT1-blocks, etc., are called by the solver and are thus part of the differential equations. The logic determines the physical interpretation of the OLTC, and therefore

1. If the OLTC has to switch,
2. When the switching operation is finished, and
3. What the current, or in case after a switching the new, tap ratio is.

It is important to note, that this structure relies on the calculation of the dynamic admittance matrix on each time step.

The output of the controller is based on the following logic.

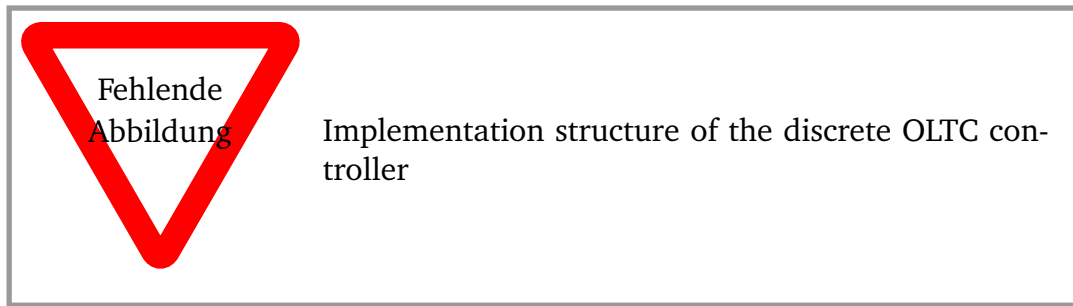


Figure 3.3: Implementation structure of the discrete OLTC controller

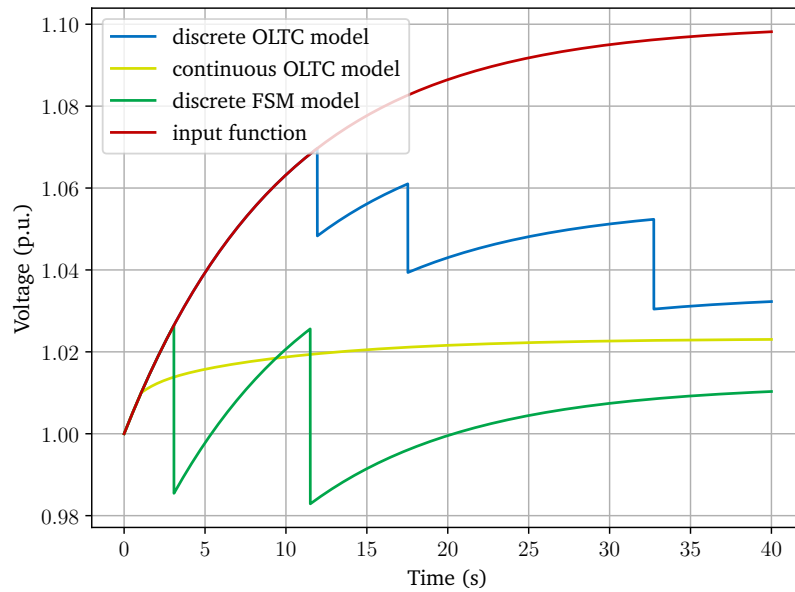


Figure 3.4: Characterization of the OLTC control loop; the input function simulates the to be regulated voltage, the output functions are characterized by $o(t) = i(t) \cdot \underline{v}_{\text{trafo}}$

Continuous Control Loop

Control Schemes for the Fast Switching module

- Describe implementation
- Describe benefits / drawbacks
- Control scheme
- Switching logic and behavior (voltage tracking)

Describe the operational logic and structure of the Fast Switching Module (FSM) first.

A control logic for a so called FSM has been presented from Burlakin, Scheiner, Mehlmann, *et al.* [4], and illustrated in Figure 3.5.

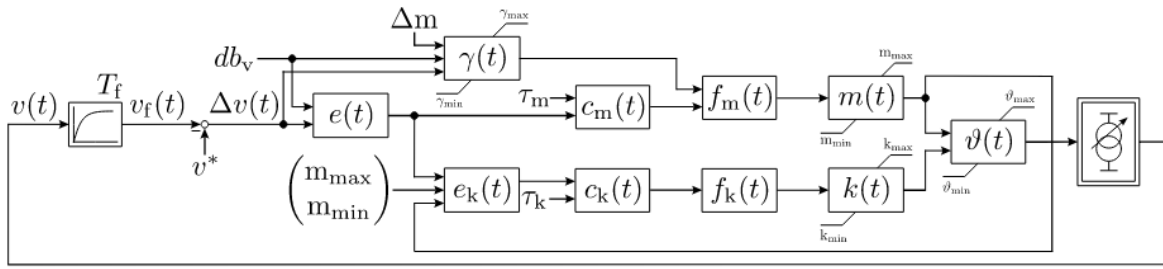


Figure 3.5: Control loop of a FSM; scheme based on Burlakin, Scheiner, Mehlmann, *et al.* [4]

However, the implementation logic in Python is slightly differing from the presented scheme in [4], simply for not overcomplication of the code and therefore debugging. The implementation is similar to the afore discussed one of a standard OLTC controller.

Discrete Control Loop as most Representative

A continuous control loop for a FSM is presented within Burlakin, Scheiner, Mehlmann, *et al.* [4], [11]. Similar to the solely OLTC loop, it represents the real behavior best, but is obstructive for stability assessments. The scheme of the logic is shown in Figure 3.6.

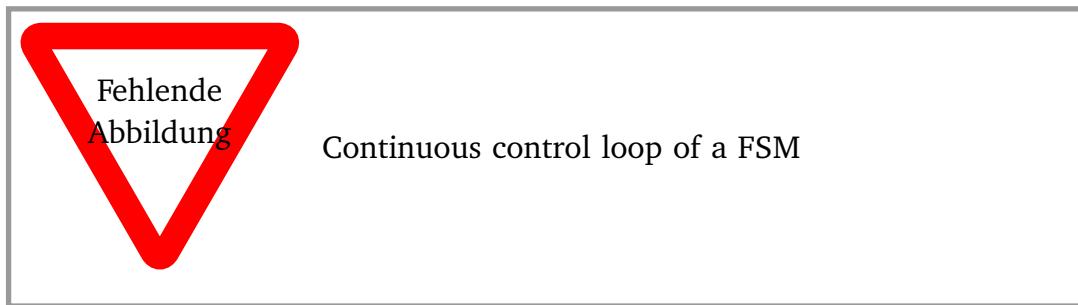


Figure 3.6: Continuous control loop of a FSM; scheme based on Burlakin, Scheiner, Mehlmann, *et al.* [4]

Continuous Control Loop for best Stability Assessment

3.1.3 Experimental: Extended Ideas and Improvements

Operational Oriented FSM Control

Alternative Tap Skipping Logic

Varying the Voltage Setpoint and Target Calculation

Here, another idea of control target creation shall be mentioned. Instead of a fixed bus voltage reference, the difference of both bus voltages is considered. Further, the sign of that difference is used to determine the direction of the tap change.

3.2 Application of Voltage Stability

3.2.1 Influences of other device characteristics

Just look on other mutual influences in the power system (simulation), such as:

- Load characteristics and types of modeling
- Maximum thermal currents of cables and operating components
- Asynchronous machines (or called „induction motors“?)

3.2.2 Observing the current state of the system

Static and Dynamic Indices

- Which indices can be implemented?
- Which make sense?
- Implementation and calculation of them?

Stability Monitoring

- Index combination and „traffic light“ monitoring
- Restauration options and opportunities
- Local mapping
- Weak point identification

3.3 Summary in Short and Simple Terms

4 Verification Setup and Results

4.1 Representative Electrical Networks

The following section shall introduce the used power systems in the simulation with the Python framework, considering verification, and also extension meaning the performed case studies in chapter 5. The models are chosen to represent different network sizes and complexities, thus allowing the objective of graded interaction levels of the developed (transformer) model. The models are based on the work of Machowski, Lubosny, Bialek, *et al.* [1], Kundur and Malik [2], *IEEE Guide for Load Modeling and Simulations for Power Systems* [12], and Van Cutsem, Glavic, Rosehart, *et al.* [8].

Single Machine Infinite Bus (SMIB) Model

One very popular and thus powerful electrical network for the verification of power system stability is the SMIB model. It is a compact and simplified model of a power system, allowing easy analytical calculation, verification and development. Mutual influences are comparably simple to understand and calculate, as the infinite bus bus is acting as a fixed grid connection point with a large adjoining grid. The generator is connected to the bus bar via a transmission line and a transformer. The model was largely discussed by Kundur and Malik [2], and is shown in Figure 4.1. The generator and the IBB are represented by synchronous machines, developed and discussed by Kordowich and Jaeger [13]. The specific model details are included in ??, additionally the simulation setup for verification is described in Table 4.1.

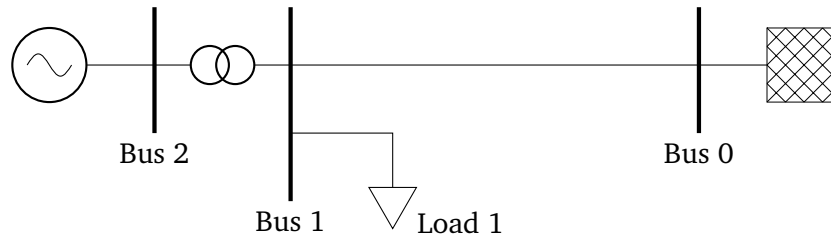


Figure 4.1: Single Machine Infinite Bus (SMIB) model for verification and validation of the Python framework; own figure after [1], [2]

Table 4.1: Simulation Setup for validation of the Π -modeled transformer; considering a transforming ratio $\underline{v} \neq 1$ and $\underline{v} \in \mathbb{C}$

Parameter	Value
Generator inertia H	3.5 s
Generator damping D	0.1 p.u.
Generator resistance R	0.01 p.u.
Generator reactance X	0.1 p.u.
Transformer resistance R	0.01 p.u.
Transformer reactance X	0.1 p.u.
Transmission line resistance R	0.01 p.u.
Transmission line reactance X	0.1 p.u.

Further, this model shall be slightly modified according to Figure 4.2. A load is added at the secondary bus of the transformer, the rest of the system is kept. Table 4.1 already contains this modification.

**Figure 4.2:** Modified Single Machine Infinite Bus (SMIB) model with additional load

Simple Single Machine Load Model

Following model is often recommended [Quelle] for easy voltage control studies, in explicit for OLTCs. Similar to the SMIB model, it consists from one synchronous generator, busses, and lines in a single branch. The IBB is thus removed and changed to a load. This two element type o configuration allows for an easy analytical calculation of voltage stability and control. Although this thesis is focussing on OLTC transformers, the model is extended with one in between. A single line representation is depicted in Figure 4.3.

Further details about its configuration and simulation setup are included in ???. It should be noted, that simple load models are not useful for simulation of this example

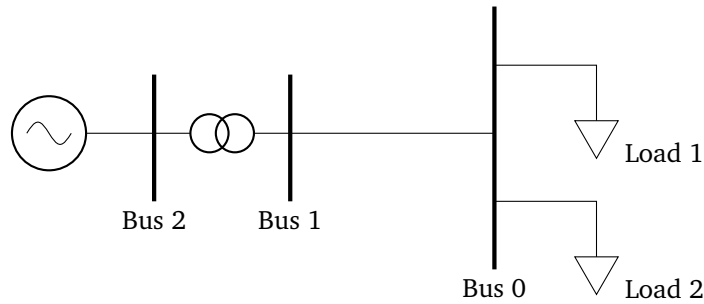


Figure 4.3: Single line representation of a simple single machine load model; own illustration with characteristics from **[Quelle]**

network. Usually constant Z models are used as loads, therefore simulation results can be misleading and not showing desired effects or voltage instability mechanisms **[Quelle]**. The simulation framework is extended with XX types of load models, to satisfy the requirements of the single machine load model, and a connected stability assessment.

IEEE Nine-Bus System

Nordic Test System

4.2 Validation Steps

4.2.1 Validation of the Π -Modeled Transformer with Variable Tap Position

4.2.2 Validation of the OLTC Control Schemes

Standard Discrete OLTC Control

Fast Switching OLTC Control

4.2.3 Voltage Stability Rating Plausibility

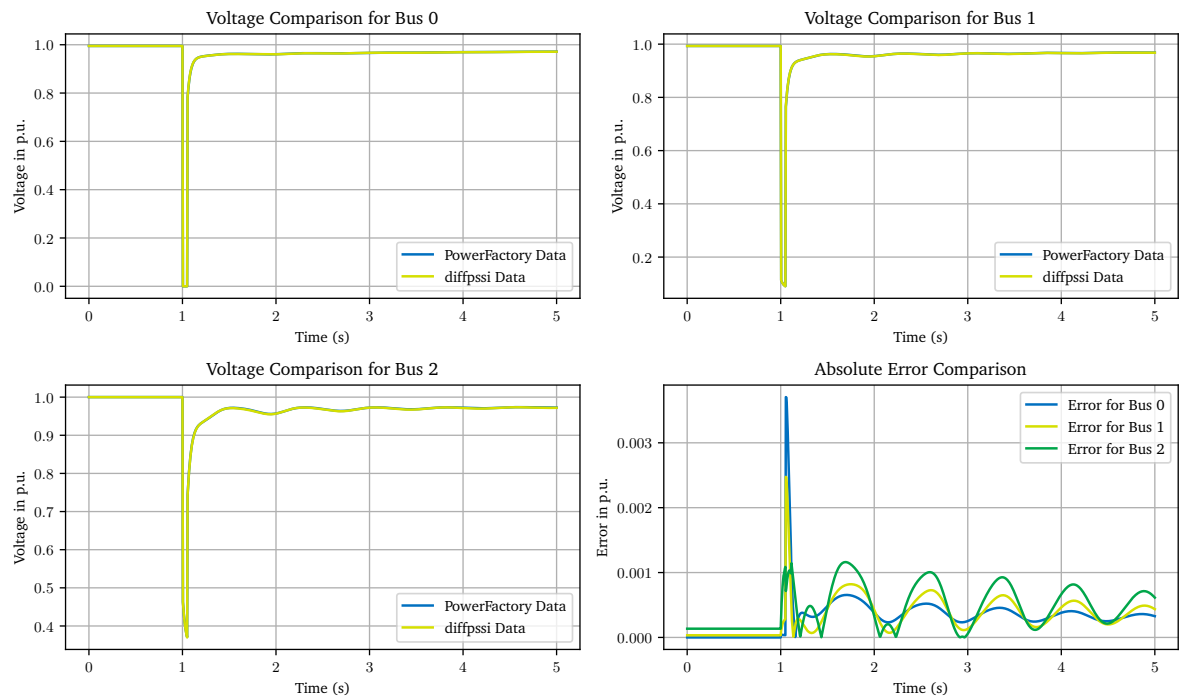


Figure 4.4: Comparison of the II-modeled transformer in the SMIB model between PowerFactory and the Python framework

Place results here, looking at: off nominal tap ratio, and with off nominal phase shifting (e.g. 110°)

4.3 Discussion of Model Limitations and Improvements

4.4 Summary in Short and Simple Terms

5 Case Study

In the interest of investigation / the Case Study are:

- Influence of switching times on stability margin/begin of destabilization,
- Influence of max. ratio change per switching event, and
- Influence on different test systems (destabilization mechanisms).

Does it make sense to structure like that? (Scenarios - Simulation - Results)

Or is it a better idea thinking in terms of specific „use cases“ as sections:

- What happens under strong grid conditions? -> Section: Strong grid condition behavior
- What happens under weak grid conditions? -> Section: Weak grid condition behavior
- Strongly interconnected grids
- Widely extended linear string grids

5.1 Novel Control Strategy FSM

Thinking of fast and slow voltage gradients: fast gradients are compensated by the FSM, slow gradients are compensated by the OLTC. Therefore optimal utilisation of injected damping moment of the FSM.

Also thinking of different presets of the OLTC and FSM, which are tried to keep constant. Different grid operators can utilize for typical grid conditions of over- or under-voltage at PCC.

Following contains:

- Implementation of different logic
- Testing of presets and switching logic
- Damping moment beneficial?

5.1.1 Scenario Setting

5.1.2 Simulation

5.1.3 Results

5.2 Influence of FSM on Voltage Angle Stability of Machines

Thinking of Rotor Angle Stability, maybe considered by an EAC implementation?

What does the fast Switching, esp. at up to 8% of the nominal voltage, do to the machines?

Comparison between standard Transformer / OLTC and FSM control.

5.3 Possible Extension for Power Flow Congruent Control

Extension in the Control Algorithm to decide which Bus has to be regulated, to avoid contrary actions of the OLTC and FSM against the power flow. Therefore not decrease of stability, but increase. Possible Application: Grid coupling Transformers, Battery Storage assisted Virtual powerplants, etc.

For this thinking maybe another control strategy is relevant:

- No setpoint from a load flow day-ahead or similar time frame; but rather current load and bus voltages are considered
- Not the deviation of one transformer bus voltage from a setpoint, but the deviation between the two bus voltages is relevant
- Maybe the absolute deviation to the optimal bus voltages at the current load situation is relevant

Big general problem: In which direction does the OLTC / the FSM have to switch? In some cases, the direction is not correct, in some it is correct.

5.4 Summary in Short and Simple Terms

6 Discussion of the Results

6.1 Summary in Short and Simple Terms

7 Summary and Outlook

Some conclusion.

Some outlook and nice blibla.

Acronyms

EMT	Electromagnetic Transient
FSM	Fast Switching Module
HV	High Voltage
IBB	Infinite Bus Bar
LV	Low Voltage
OLTC	On-Load Tap Changer
PCC	Point of Common Coupling
PSS	Power System Simulation
RMS	Root Mean Square
SG	Synchronous Generator
SMIB	Single Machine Infinite Bus

Symbols

δ	$^{\circ} / \text{deg}$	power angle (or power angle difference)
$\Delta\omega$	$\frac{1}{s}$	change of rotor angular speed
$\underline{\theta}$	-	transformer ratio; complex if phase shifting
A	-	acceleration or deceleration area
\underline{E}	V	voltage of SG or IBB
H_{gen}	s	inertia constant of a Synchronous Generator (SG)
\underline{I}	A	current
P	W	effective power; electrical or mechanical
Q	var	reactive power
R	Ω	ohmic resistance
\underline{S}	VA	apparent power
\underline{V}	V	voltage
\underline{X}	Ω	reactance
\underline{Y}	$\frac{1}{\Omega} / S$	admittance
\underline{Z}	Ω	impedance

The different symbols are used with different indices, these are semantic and explained in the surrounding context. Following notation is commonly used for mathematical and physical symbols:

- Phasors or complex quantities are underlined (e.g. \underline{I})
- Arrows on top mark a spatial vector (e.g. \vec{F})
- Boldface denotes matrices or vectors (e.g. **F**)
- Roman typed symbols are units (e.g. s)
- Lower case symbols denote instantaneous values (e.g. i)
- Upper case symbols denote RMS or peak values (e.g. I)
- Subscripts relating to physical quantities or numerical variables are written italic (e.g. I_1)

In the simulations and calculations the per unit system (p.u.) is preferred, thus normalizing all values with a base value. Where necessary, absolute units are added to indicate the explicit use of the normal unit system. For more information about this per-unit system please refer to Machowski, Lubosny, Bialek, *et al.* [1], specifically Appendix A.1 provides a detailed description and explanation.

List of Figures

2.1	Two-Winding Transformer Circuit in the Positive Sequence	5
2.2	Π -representative circuit of an idealized transformer with a tap changer .	6
3.1	Illustration of the tap ratio vector for an ideal and an asymmetric transformer	16
3.2	Discrete control loop of an OLTC; scheme based on Milano [10]	17
3.3	Implementation structure of the discrete OLTC controller	18
3.4	Characterization of the OLTC control loops	18
3.5	Control loop of a Fast Switching Module (FSM)	19
3.6	Continuous control loop of a FSM; scheme based on Burlakin, Scheiner, Mehlmann, <i>et al.</i> [4]	19
4.3	Single line representation of a simple single machine load model; own illustration with characteristics from [Quelle]	24
4.4	Comparison of the Π -modeled transformer in the SMIB model between PowerFactory and the Python framework	25

List of Tables

2.1	Voltage instability types and different time frames	10
2.2	Voltage stability indices for the assessment in this thesis	12
4.1	Simulation Setup for validation of the Π -modeled transformer	23

List of Listings

Bibliography

- [1] J. Machowski, Z. Lubosny, J. W. Bialek, and J. R. Bumby, *Power System Dynamics: Stability and Control*, Third edition. Hoboken, NJ, USA: John Wiley, 2020, 1 p., ISBN: 978-1-119-52636-0 978-1-119-52638-4.
- [2] P. S. Kundur and O. P. Malik, *Power System Stability and Control*, Second edition. New York Chicago San Francisco Athens London Madrid Mexico City Milan New Delhi Singapore Sydney Toronto: McGraw Hill, 2022, 948 pp., ISBN: 978-1-260-47354-4.
- [3] F. Milano, *Power System Modelling and Scripting* (Power Systems), 1. ed. Heidelberg: Springer, 2010, 556 pp., ISBN: 978-3-642-13668-9.
- [4] I. Burlakin, E. Scheiner, G. Mehlmann, *et al.*, “Enhanced Voltage Control in Off-shore Wind Farms with Fast-Tapping on-Load Tap-Changers,” presented at the 23rd Wind & Solar Integration Workshop, Helsinki, Finland, Oct. 11, 2024.
- [5] J. L. Rueda-Torres, U. Annakage, C. Vournas, *et al.*, “Evaluation of Voltage Stability Assessment Methodologies in Modern Power Systems with Increased Penetration of Inverter-Based Resources (TR 126),” 2024. DOI: 10.17023/SA3K-AZ76. [Online]. Available: https://resourcecenter.ieee-pes.org/publications/technical-reports/pes_tr_126_psdp_110724 (visited on 12/02/2024).
- [6] M. S. S. Danish, *Voltage Stability in Electric Power System: A Practical Introduction*. Berlin: Logos-Verl, 2015, 219 pp., ISBN: 978-3-8325-3878-1.
- [7] T. Cutsem and C. Vournas, *Voltage Stability of Electric Power Systems*. Boston, MA: Springer US, 1998, ISBN: 978-0-387-75535-9 978-0-387-75536-6. DOI: 10.1007/978-0-387-75536-6. [Online]. Available: <http://link.springer.com/10.1007/978-0-387-75536-6> (visited on 10/24/2024).
- [8] T. Van Cutsem, M. Glavic, W. Rosehart, *et al.*, “Test Systems for Voltage Stability Studies,” *IEEE Transactions on Power Systems*, vol. 35, no. 5, pp. 4078–4087, Sep. 2020, ISSN: 0885-8950, 1558-0679. DOI: 10.1109/TPWRS.2020.2976834. [Online]. Available: <https://ieeexplore.ieee.org/document/9018172/> (visited on 11/08/2024).
- [9] C. E. Doig Cardet, “Analysis on Voltage Stability Indices,” M.S. thesis, RWTH Aachen, 2010, 107 pp. [Online]. Available: <http://hdl.handle.net/2099.1/14636> (visited on 02/04/2025).

- [10] F. Milano, “Hybrid Control Model of Under Load Tap Changers,” *IEEE Transactions on Power Delivery*, vol. 26, no. 4, pp. 2837–2844, Oct. 2011, ISSN: 0885-8977, 1937-4208. DOI: 10.1109/TPWRD.2011.2167521. [Online]. Available: <http://ieeexplore.ieee.org/document/6029301/> (visited on 09/02/2024).
- [11] I. Burlakin, E. Scheiner, G. Mehlmann, *et al.*, “Enhancing Variable Shunt Reactors with a Power Electronic Fast-Switching Module,” in *Power Transformers and Reactors (A2)*, Paris: CIGRE, Aug. 2024.
- [12] *IEEE Guide for Load Modeling and Simulations for Power Systems*, 2022. DOI: 10.1109/IEEESTD.2022.9905546. [Online]. Available: <https://ieeexplore.ieee.org/document/9905546/> (visited on 11/08/2024).
- [13] G. Kordowich and J. Jaeger. “A Physics Informed Machine Learning Method for Power System Model Parameter Optimization.” arXiv: 2309.16579 [cs, eess]. (Sep. 28, 2023), [Online]. Available: <http://arxiv.org/abs/2309.16579> (visited on 09/02/2024), pre-published.

Appendix

A	Fundamentals	b
A.1	Description of the Power System Simulation process	b
A.2	Jacobian based voltage stability criteria	c
A.3	Comparison of System based and Jacobian based indices	c

A Fundamentals

A.1 Description of the Power System Simulation process

In this appendix section, the general process of power system simulation is described. As this thesis is aiming to understand voltage stability and processes in longer periods of time, these explanations apply to pointer-based simulations, called RMS simulations. Meaning that the considered effects are slower electromechanical nature instead of faster electromagnetic ones. The in this thesis used Python framework „*diffpssi*“ is based on this type of simulation, and due to its open-source based nature traceable.

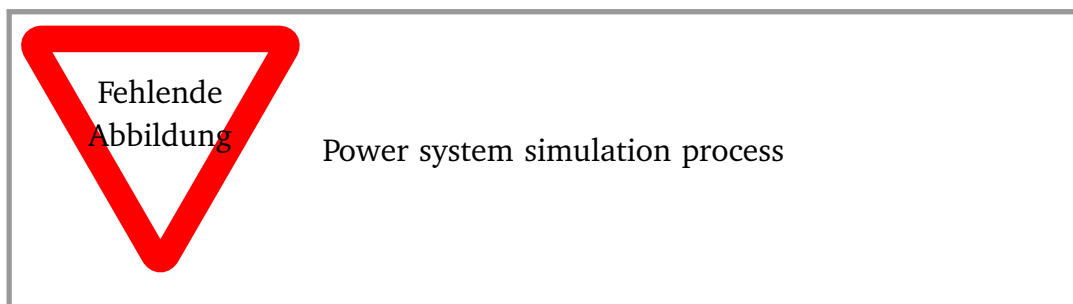


Figure A.1: Power system simulation process; own illustration

Really basic: (?)

- RMS vs EMT simulation (-> meaning one cannot simulate other faults than 3ph w/o ground)
- Phasor description
- Basic formulation: Static (algebraic) and dynamic (differential) equations
- Using of solvers (Integrators) for time domain simulation
- Using of different optimization algorithms for steady state (load flow) simulation -> initial values

Less basic and more advanced:

- routines in the framework

- two types: Algebraic and Differential equations have to be solved at each time step -> What is which? Which operational equipment is typically described with which type of equation?
- per unit system applying for easier simulation (different voltage levels)
- ...

A.2 Jacobian based voltage stability criterions

Danish [6] is showing, describing, and referencing some voltage stability indices based on the Jacobian matrix. The following table is a collection of these indices.

A.3 Comparison of System based and Jacobian based indices

Table A.1: Jacobian based voltage stability criteria; after Danish [6]

Index	Abbreviation	Calculation	Stability Threshold	Reference
Tangent Vector Index	TVI	$TVI_i = \left \frac{dV_i}{d\lambda} \right ^{-1}$	depending on load increase	
Test Function		$t_{cc} = \left e_c^T \cdot \mathbf{J} \times \mathbf{J}_{cc}^{-1} \cdot e_c \right $	details are given in reference	
	i	$i = \frac{1}{i_0} \cdot \sigma_{\max} \cdot \left(\frac{d\sigma_{\max}}{d\lambda_{\text{total}}} \right)^{-1}$	$i > 0$	
Minimum Eigenvalue		$\Delta V = \sum_i \xi_i^{i\eta_i} \Delta Q$	all eigenvalues should be positive	
Minimum Singular Value		$\begin{bmatrix} \Delta \vartheta \\ \Delta V \end{bmatrix} = \mathbf{V} \Sigma^{-1} \mathbf{U}^T \begin{bmatrix} \Delta F \\ \Delta G \end{bmatrix}$	details are given in reference	
Predicting Voltage Collapse		$\frac{V}{V_0}$	the smallest index value	
Impedance Ratio		$\frac{Z_i^i}{Z_i}$	$\frac{Z_i^i}{Z_i} \leq 1$	