

# LSST-DESC Calibration Workshop '18

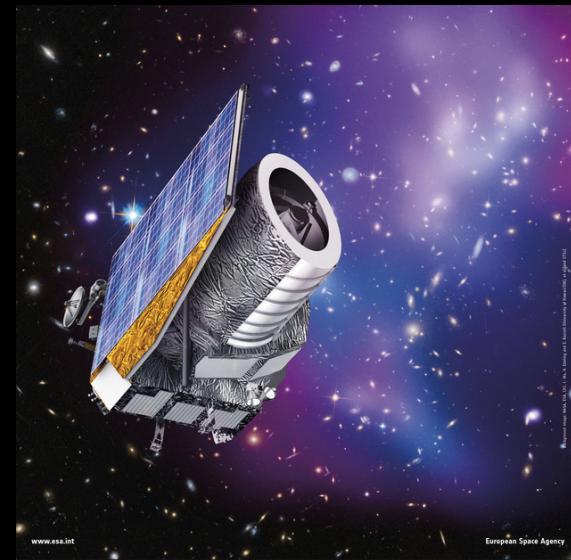
## Slitless spectro-photometry

# Disclaimer

- 1<sup>st</sup> time around, hi!
- No specific info. on AuxTel spectrograph properties nor observing modes
- Experience in ground-based *integral field* spectro-photometry (SNfactory/SNIFS) and space-born slitless spectrography (Euclid/NISP-S)



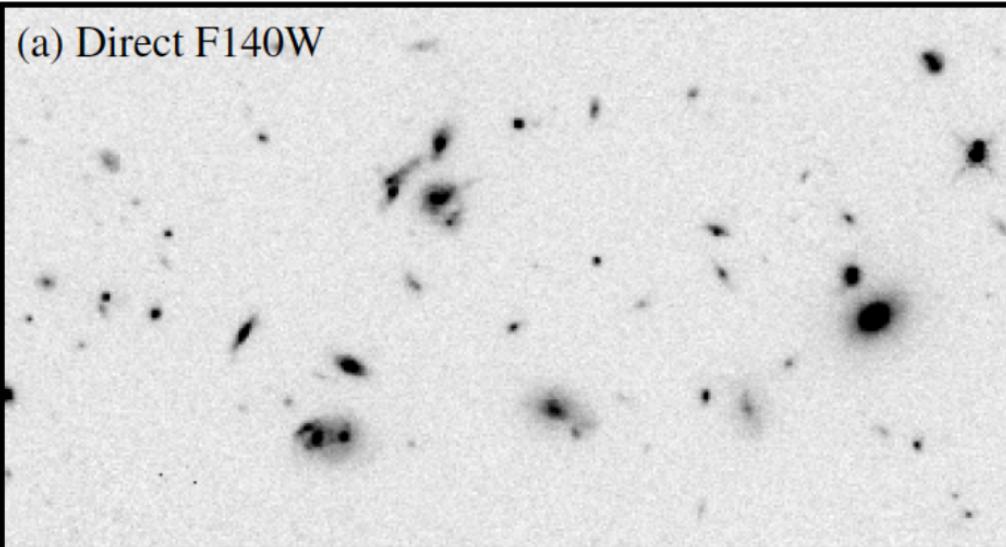
SNIFS on UH88



# Modeling slitless spectroscopy

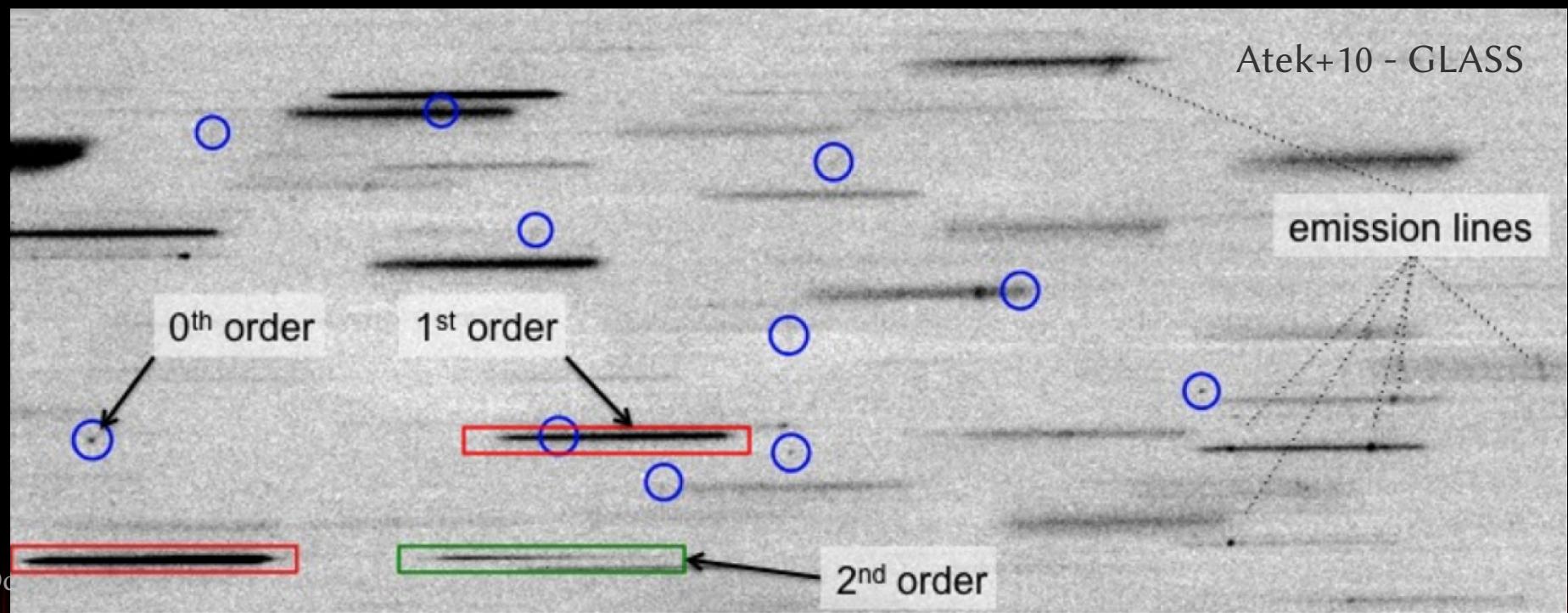
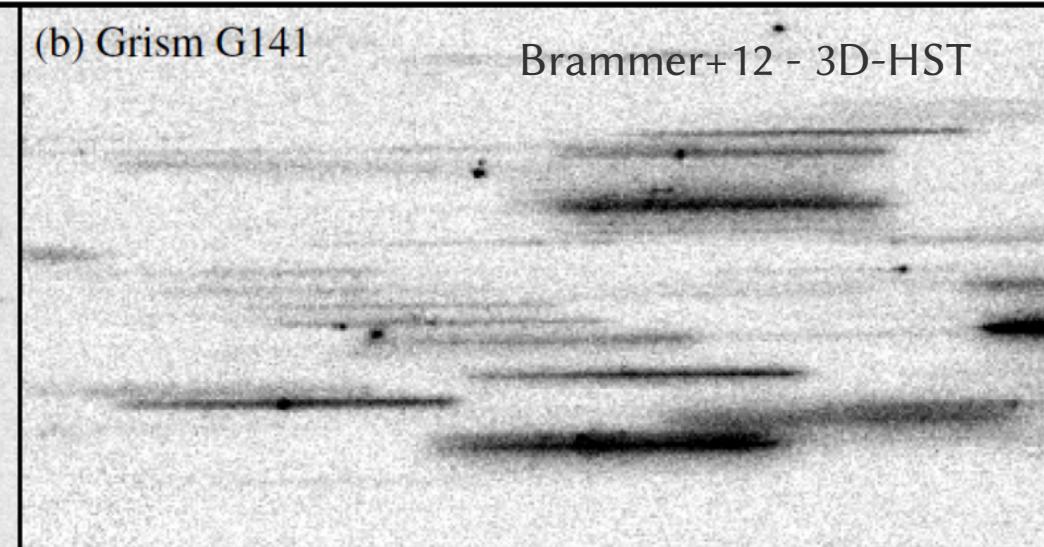
# Slitless spectroscopy

(a) Direct F140W



(b) Grism G141

Brammer+12 - 3D-HST



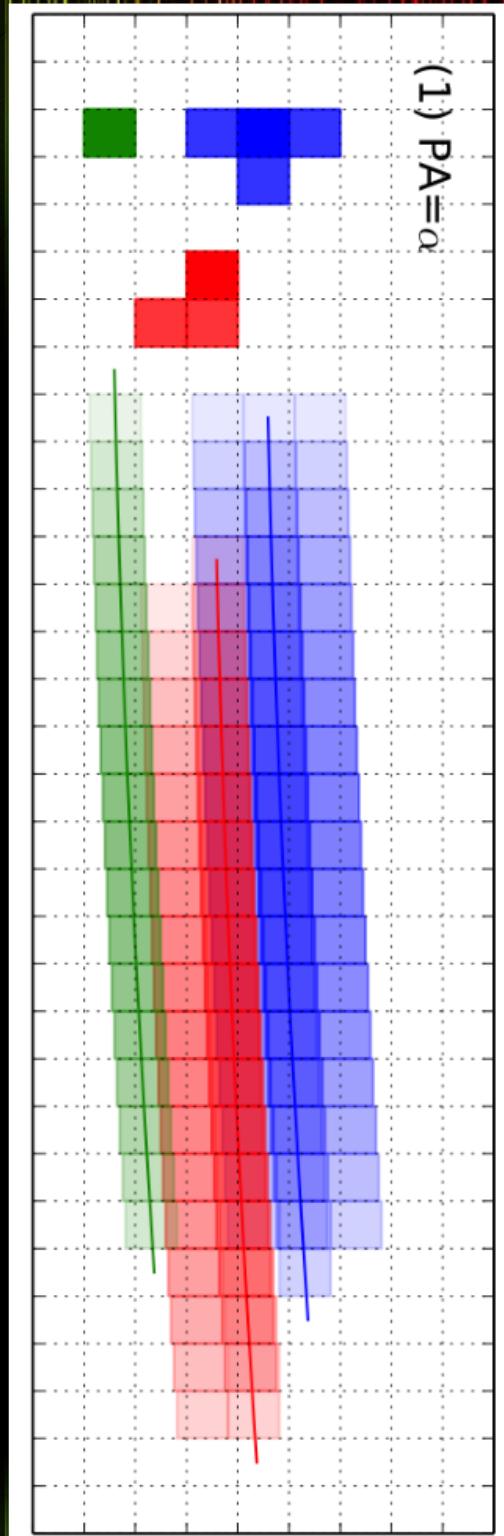
# Slitless spectroscopy

## ● Advantages

- ◆ Large FoV and high multiplexing
- ◆ Simple to build and to use

## ● Drawbacks

- ◆ Cross-contamination: overlap of different objects (potentially at different orders)
  - ▶ Mitigation: multi-PA observations & decont. model
- ◆ Self-contamination: mixing of spatial and spectral information
  - ▶ Spectral resolution is dependent of source size/seeing conditions
- ◆ High background level



# Traditional approach

- Standard “aXe-like” (Kümmel+09)
  - ◆ Empirical modeling of the spectral trace
    - ▶ Cross-dispersion: geometric distortions
    - ▶ Along dispersion: wavelength solution
  - ◆ Decontamination from neighbor sources
  - ◆ Cross-dispersion integration → 1D spectrum
    - ▶ Potentially x-disp. profile weighted (“optimal extraction”)
  - ◆ Multi-PA spectra are averaged *a posteriori*
    - ▶ But see LINEAR (Ryan+18) for 1<sup>st</sup> steps toward a forward model
- No handling of self-confusion
  - ◆ Spectral resolution is degenerate with source size (extent/PSF/seeing)
  - ◆ Correct for point sources observed in space, suboptimal otherwise

# Intrinsic & observable flux

- Source is characterized by intrinsic flux distribution  $C(\mathbf{r}, \lambda)$ 
  - ◆ E.g. a star:  $C(\mathbf{r}, \lambda) = S(\lambda) \times \delta(\mathbf{r} - \mathbf{r}_0)$
  - ◆ Separable source:  $C(\mathbf{r}, \lambda) = S(\lambda) \times F(\mathbf{r})$
- Atmosphere + Instrument is characterized by *Impulse Response Function* (supposed stationary)
  - ◆ mapping from intrinsic coords to obs. coords (astrometry,  $\lambda$ -calib)
  - ◆ spread around mean position
  - ◆ may include transmission
- *Observable* flux  $O(\mathbf{r}, \lambda) = (C \otimes P)(\mathbf{r}, \lambda)$ 
  - ◆ Only if you have an Integral Field Spectrograph!

# Direct imaging

- IRF can be decomposed in two components
  - ◆ a centered shape component  $P_0$  (aka PSF/LSF)
  - ◆ an offset component  $P_\Delta$ 
    - ▶ usually ignored by *ad hoc* registration of the PSF
- Direct imaging (photometry)
  - ◆  $P_0 = \text{PSF}$ ,  $P_\Delta \approx \delta(\mathbf{r})$ 
    - ▶ but chromatic aberrations & ADR correspond to a non-trivial  $P_\Delta$
  - ◆ Broadband image:  $I(\mathbf{r}) = \int d\lambda O(\mathbf{r}, \lambda)$ 
    - ▶  $\approx (\bar{C} \otimes \bar{P}_0)(\mathbf{r})$  for a weakly chromatic separable source

# Dispersed imaging

## ● Slitless spectroscopy

- ◆  $P_0$  = Point/Line Spread Function
- ◆  $P_\Delta(\mathbf{r}, \lambda) = \delta(\mathbf{r} - \Delta(\lambda))$  where  $\Delta(\lambda)$  is the dispersion law
- ◆ Dispersed image:  $I(\mathbf{r}) = \int d\lambda (C \otimes P_0)(\mathbf{r} - \Delta(\lambda), \lambda)$
- ◆ In spatial Fourier domain:

$$\hat{I}(\mathbf{k}) = \int d\lambda \hat{C}(\mathbf{k}, \lambda) {}^{\wedge}P_0(\mathbf{k}, \lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)}$$

- ◆ Under the separability assumption and a weakly chromatic PSF

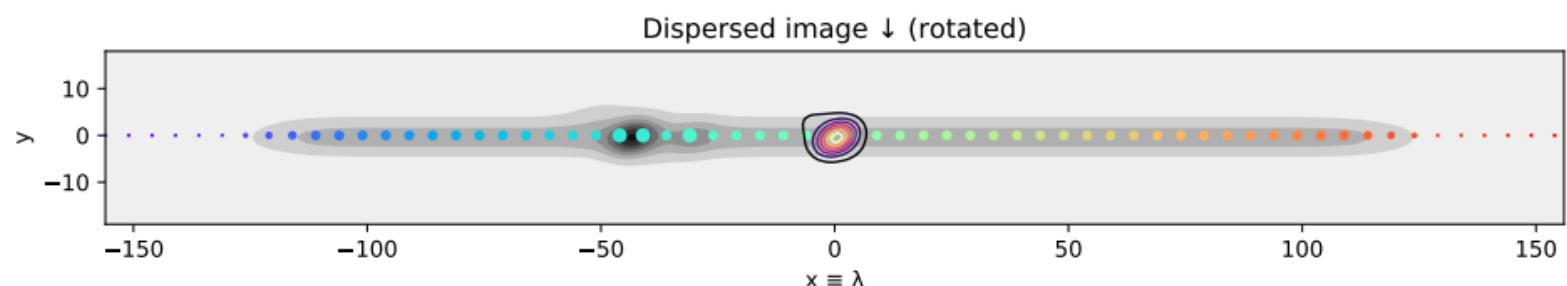
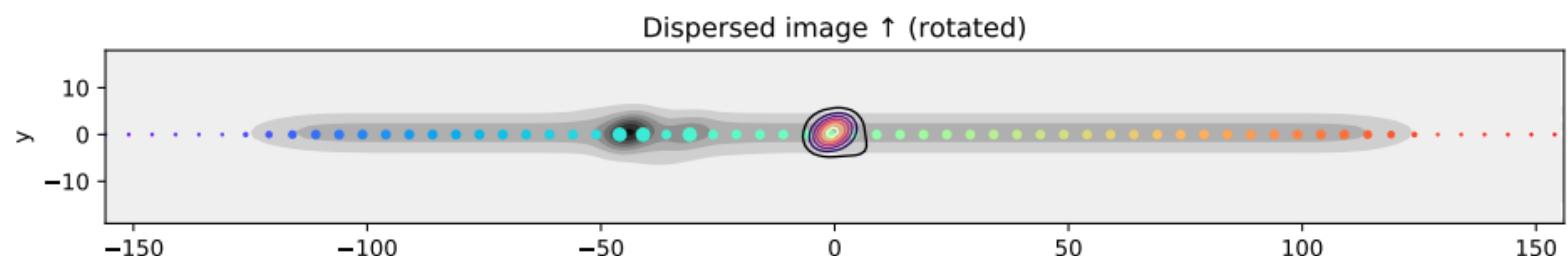
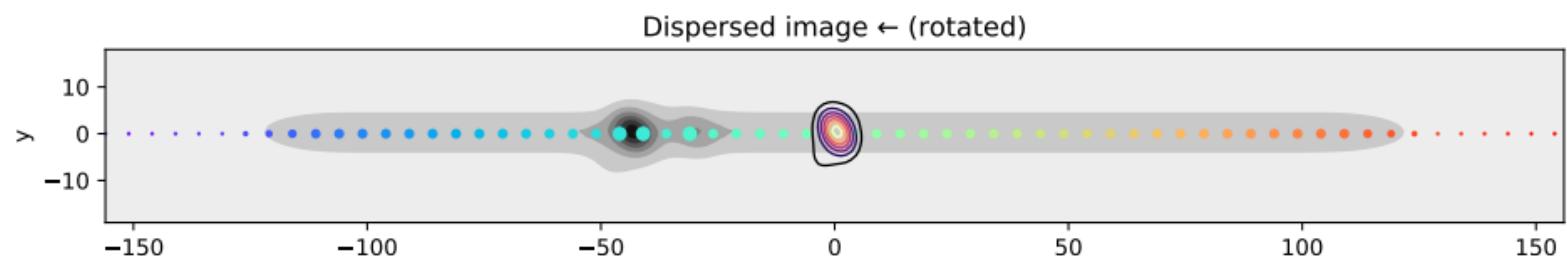
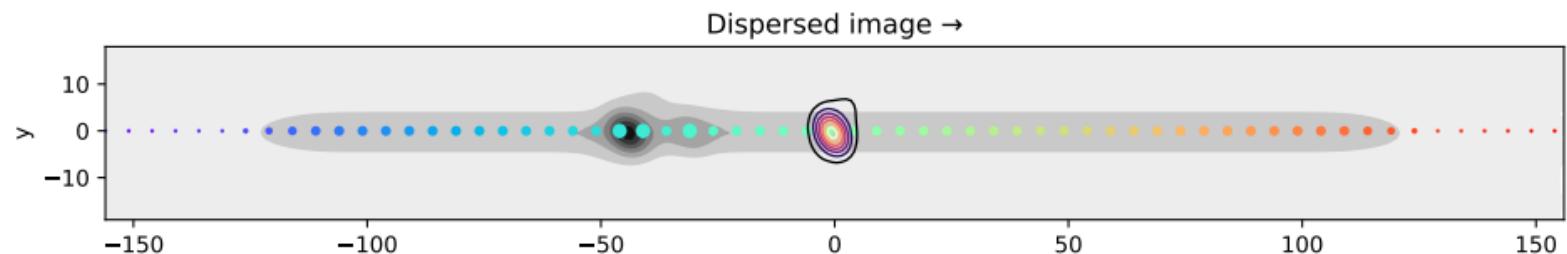
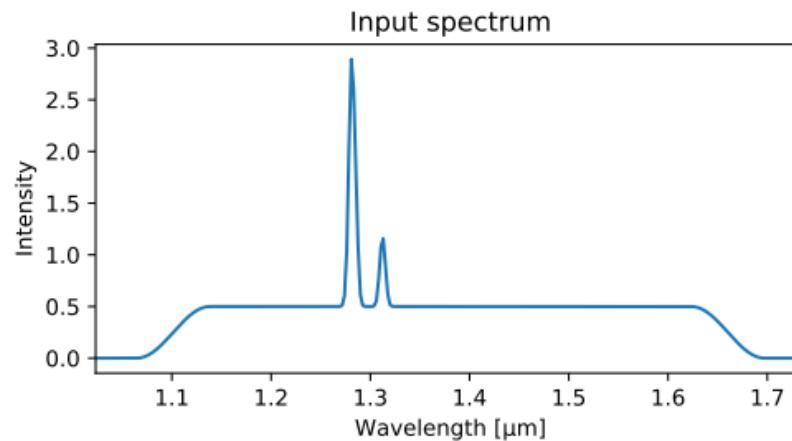
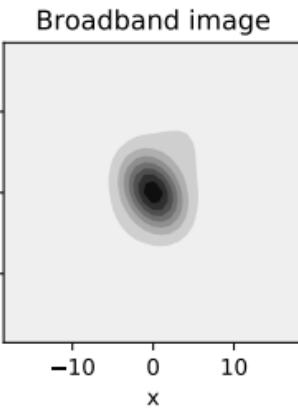
$$\hat{I}(\mathbf{k}) \approx {}^{\wedge}F(\mathbf{k}) {}^{\wedge}\bar{P}_0(\mathbf{k}) \int d\lambda S(\lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)}$$

- Almost the Fourier Transform of  $S(\lambda)$ !

# Dispersed image modeling

- $\hat{I}(\mathbf{k}) = \int d\lambda \hat{C}(\mathbf{k}, \lambda) \hat{P}_0(\mathbf{k}, \lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)} \approx \hat{F}(\mathbf{k}) \hat{\bar{P}}_0(\mathbf{k}) \int d\lambda S(\lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)}$ 
  - I = dispersed image,  $F \otimes \bar{P}_0 \approx$  broadband image
  - S = spectrum,  $\Delta$  = dispersion law
- Different approaches
  - ◆ Efficient simulation (for all dispersion orders)
  - ◆ Backward extraction of  $S(\lambda)$ 
    - ▶ Assume dispersion law  $\Delta(\lambda)$  and broadband image  $F \otimes \bar{P}_0$
    - ▶ Estimate  $S(\lambda)$  from Wiener-Hunt deconvolution
  - ◆ Forward model of dispersed image  $I(\mathbf{r})$ , e.g.
    - ▶ Calibration of dispersion law  $\Delta(\lambda)$ , of transmission  $T(\lambda)$
    - ▶ Simple galaxy model:  $S(\lambda) = \text{template} + \text{redshift}$
    - ▶ More complex model, e.g. galaxy kinematics (Outini+18, in prep.)

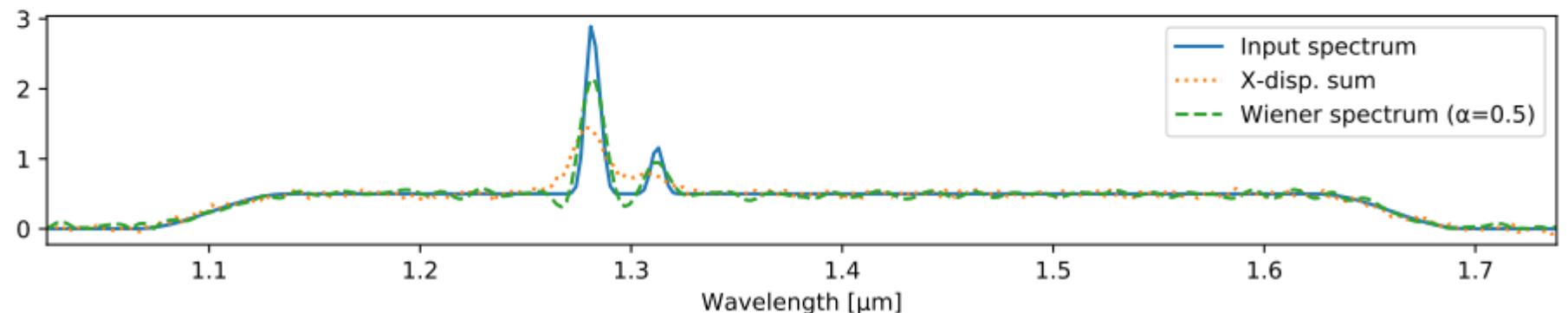
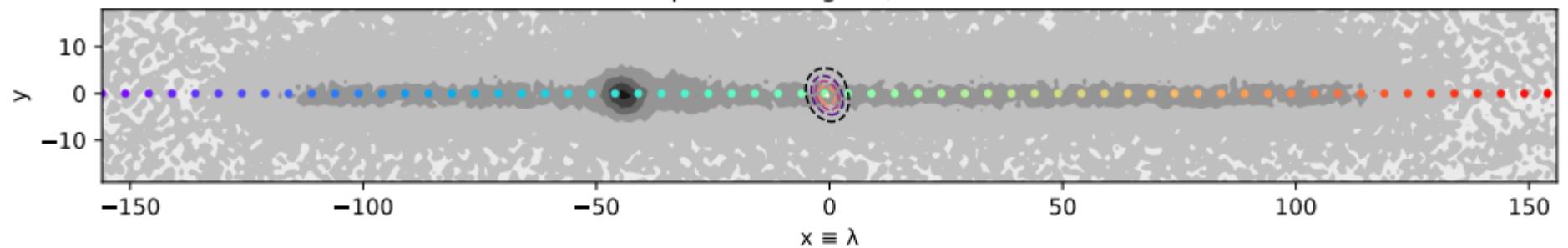
# WFC3/G141 (3D-HST) simulation



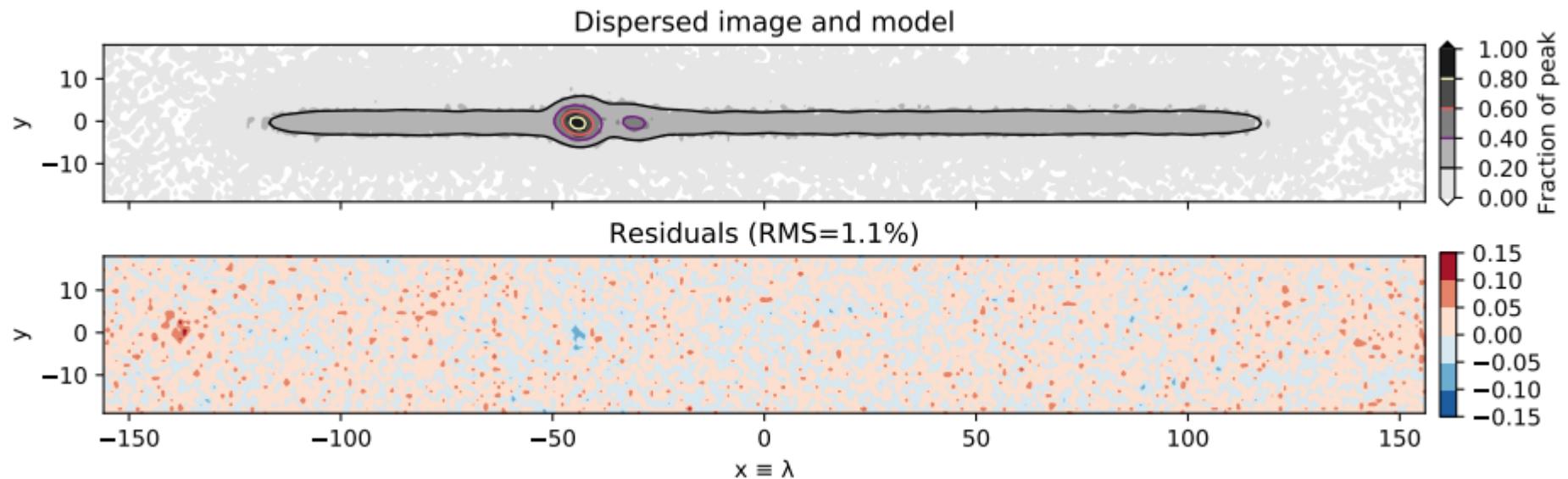
Copin 2018, in prep.

Oct. 2018

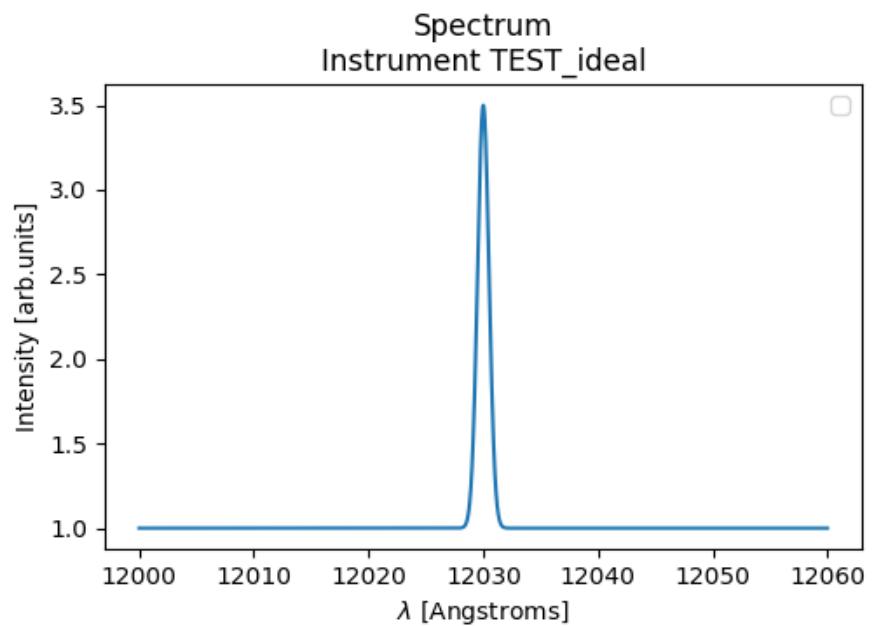
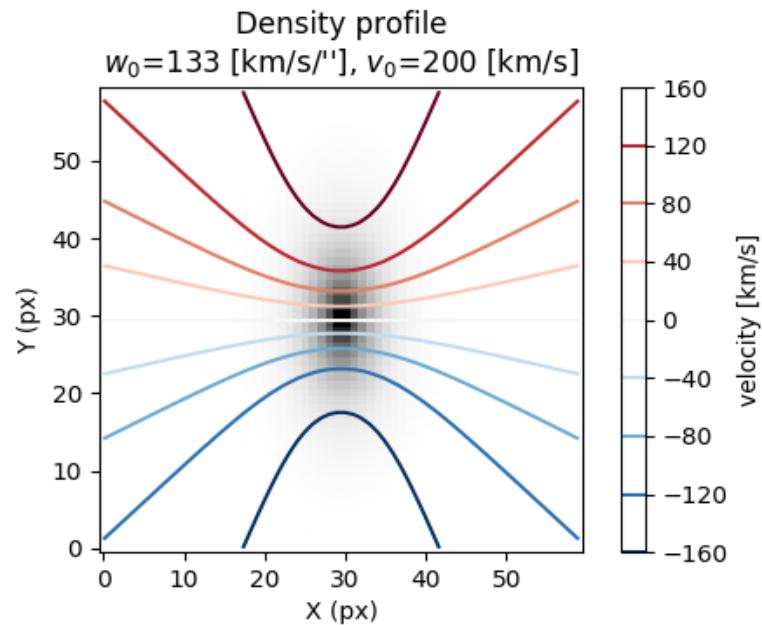
Dispersed image →, PSNR=30



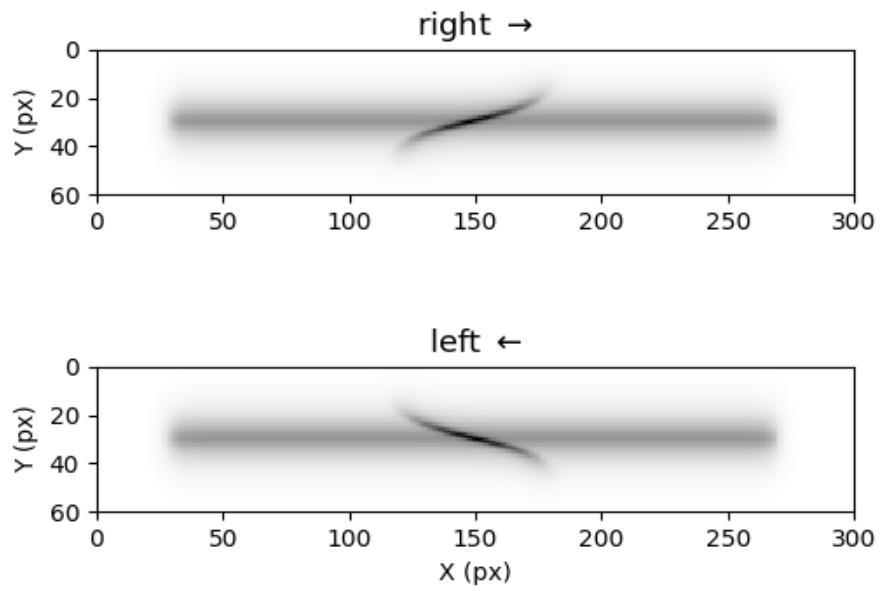
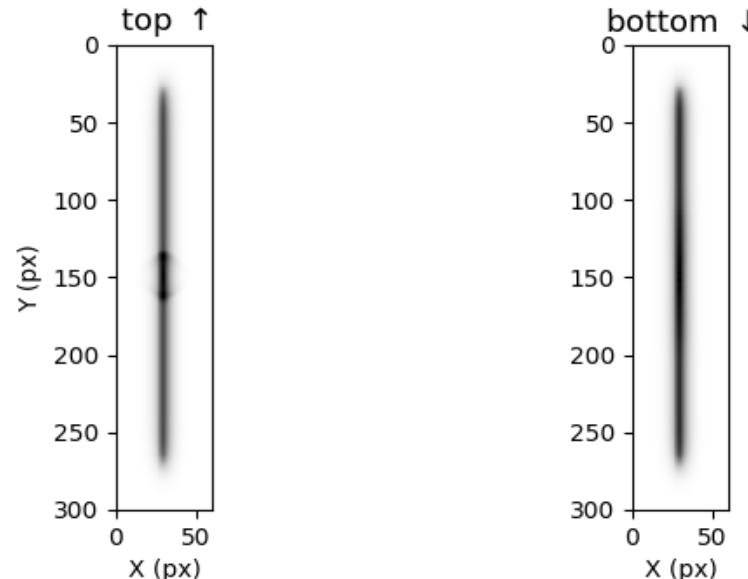
Copin 2018, in prep.



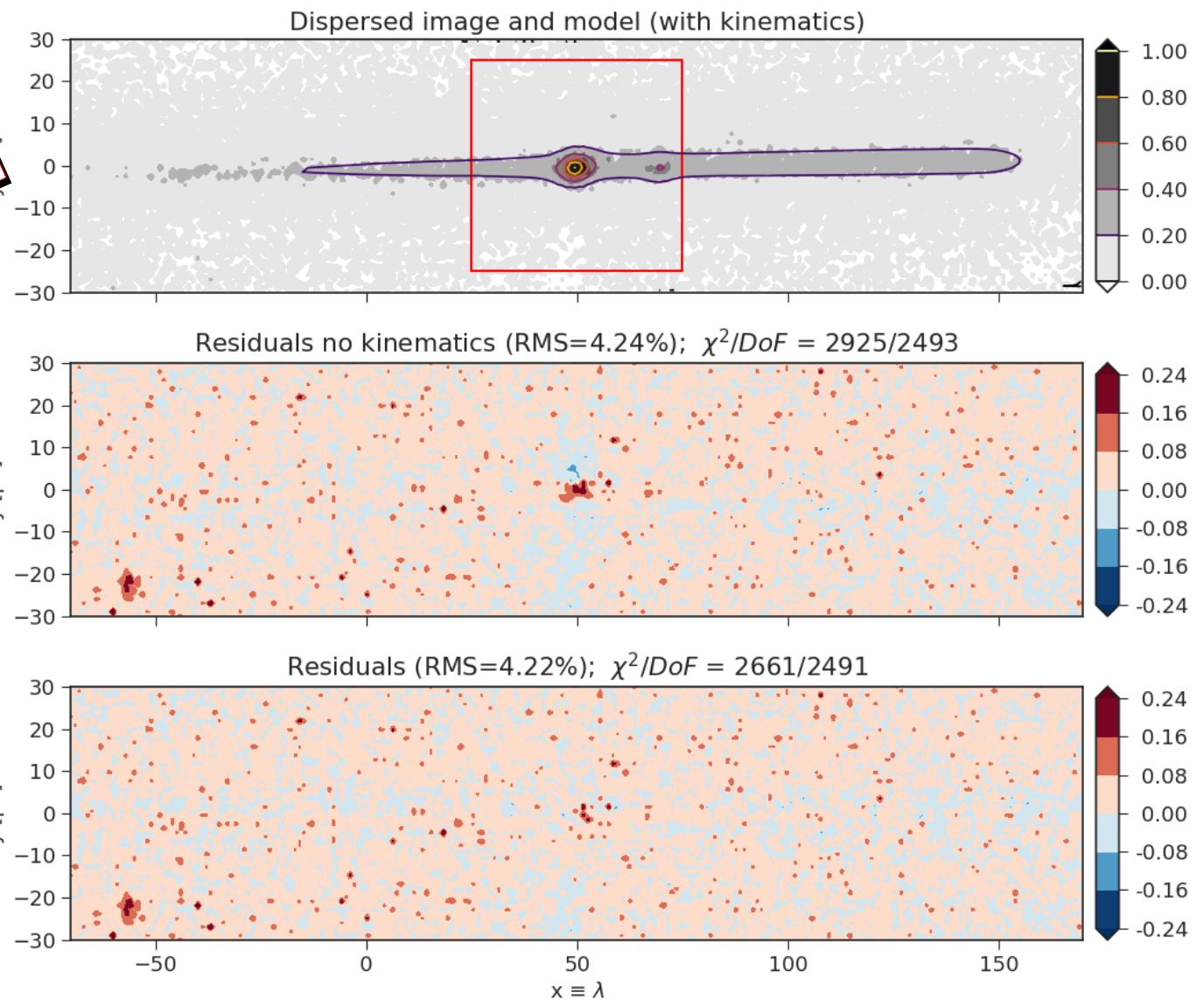
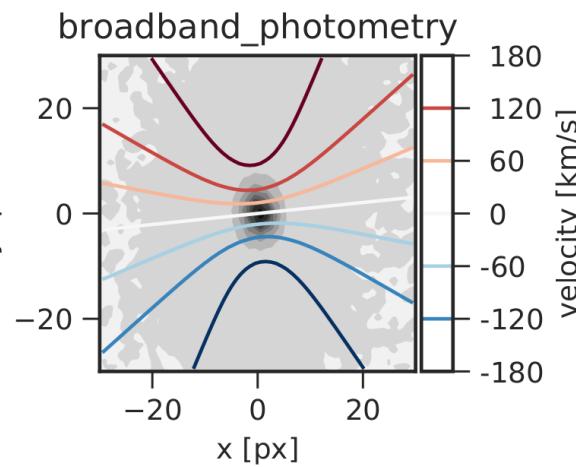
Galaxy  $r=1.0''$ ,  $i=60.0$  [deg],  $PA=0.0$  [deg]  
Instrument TEST\_ideal [ $D=0.2$  A/px]



emission line H $\alpha$ :  $\lambda_0=12030.0$  [Angstroms]  $\rightarrow z=0.83$



**PRELIMINARY**



Cold disk, velocity curve:  $v(r) = v_0 \tanh(w_0 r / v_0)$

$$v_0 \sin i = 205 \pm 24 \text{ km.s}^{-1}$$

$$w_0 \sin i = 232 \pm 25 \text{ km.s}^{-1}.\text{arcsec}^{-1}$$

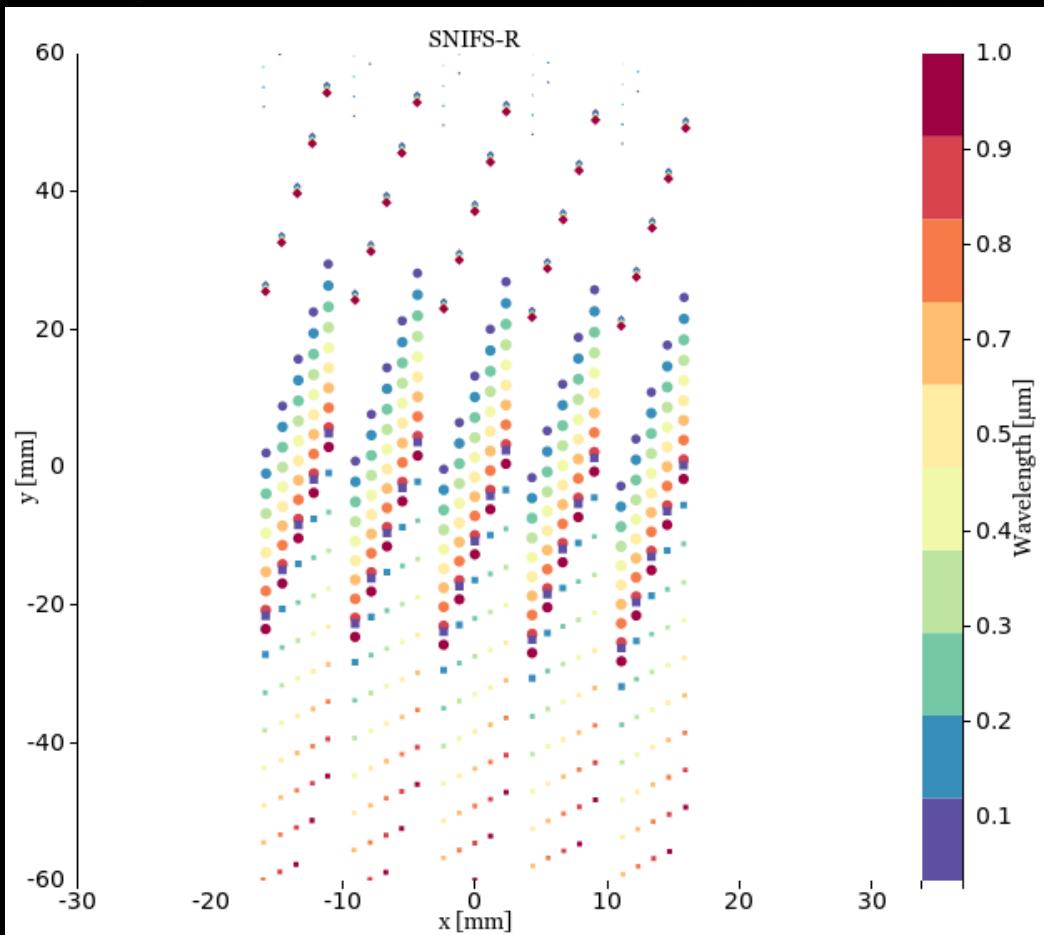
# Dispersed imaging of stars

- Point sources are easier:  $C(\mathbf{r}, \lambda) = \delta(\mathbf{r}) \times S(\lambda)$ 
  - ◆  $I(\mathbf{r}) = T F^{-1} \left( \int d\lambda \hat{P}_0(\mathbf{k}, \lambda) S(\lambda) e^{-i2\pi \mathbf{k} \cdot \Delta(\lambda)} \right)$
  - ◆ Simultaneous fit of dispersed image  $I(\mathbf{r})$ 
    - ▶ spectral trace: dispersion law  $\Delta(\lambda)$
    - ▶ spectral shape: instrumental PSF and seeing  $P_0$
    - ▶ flux:  $S = T \times S^*$  where  $T$  = transmission,  $S^*$  = ref. flux
  - ◆ Spectro-photometry will derive from proper modeling of these different components
    - ▶ Dispersed imaging is *closer* to “imaging” than “spectroscopy”
    - ▶ Most tools are readily available from photometry

# The (not so difficult?) path to slitless spectro-photometry

# Instrumental model

- Dispersion law  $\Delta(\lambda)$  as a function of position in FP
  - ◆ Effective geometrical model
- Instrumental PSF as a function of position in FP
  - ◆ Can be derived from 1<sup>st</sup> principles (WF propagation)
  - ◆ or adjusted empirically
  - ◆ More naturally expressed in Fourier domain



<http://spectrogrism.readthedocs.org>

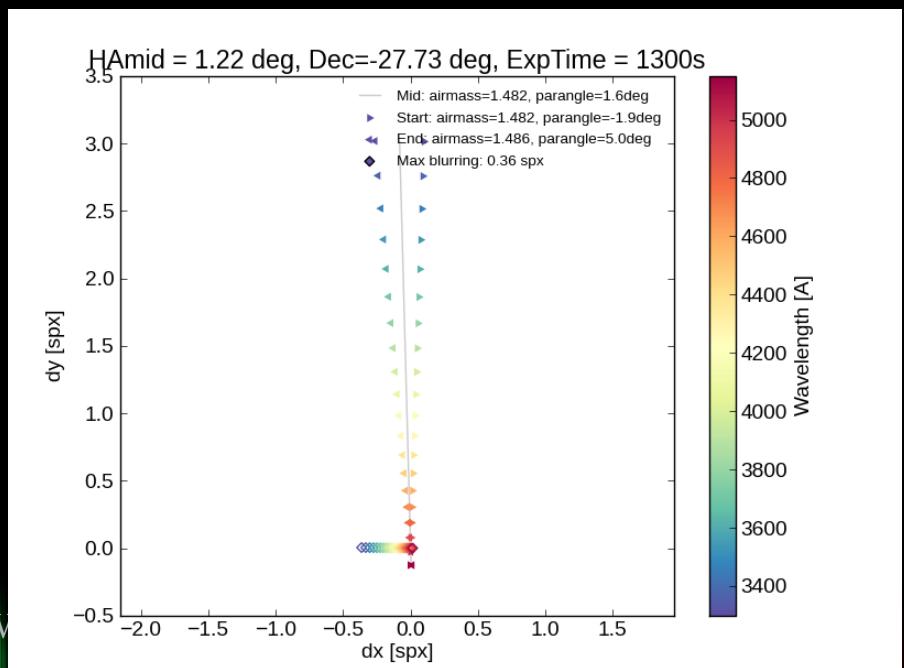
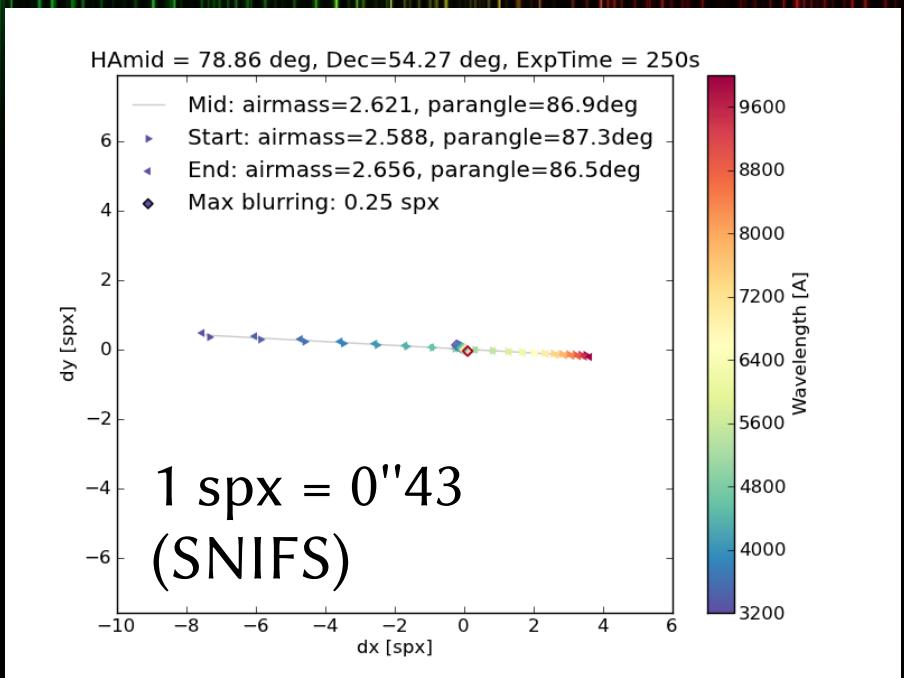
# Atmospheric Differential Refraction

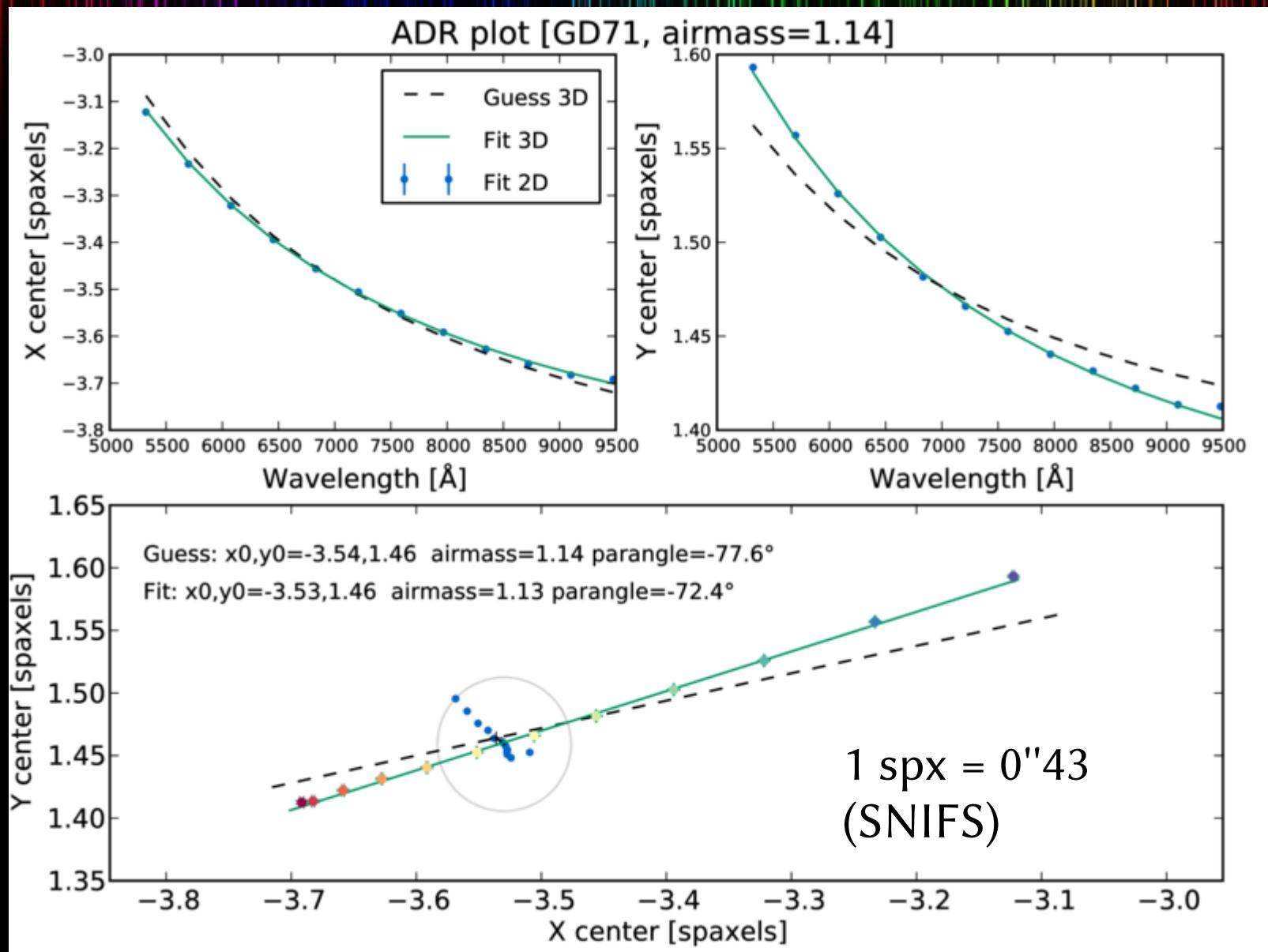
## ● Instantaneous ADR:

- ◆ distortion of spectral trace
- ◆ distortion of wave. solution
- ◆  $\Delta(\lambda) = \Delta_{\text{Disp}}(\lambda) + \Delta_{\text{ADR}}(\lambda)$

## ● Integrated ADR ( $t_{\text{exp}} > 0$ )

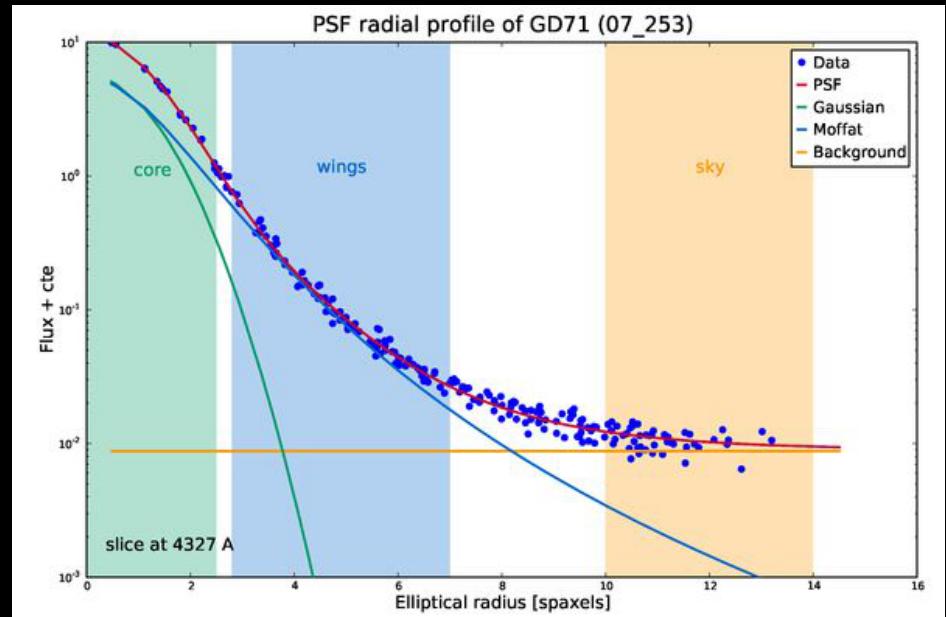
- ◆ widening of spectral trace
- ◆ spectral res. degradation
- ◆ flux-weighted time-average
- ◆ same formalism w/  $\Delta_{\text{ADR}}(\lambda, t)$





# Seeing (atmospheric PSF)

- Historical SNIFS PSF (Buton09)
  - ◆ Gaussian for the core
  - ◆ Moffat for the wings
  - ◆ Correlated parameters
- Observed PSF has more wings than plain Kolmogorov profile
  - ◆  $n_{\text{eff}} \sim 4.5/3$  rather than  $5/3$
  - ◆ Chrom. dependency is OK
- Current development (see also Xin+18):
  - ◆ Seeing: Kolmogorov/von Kármán profile
  - ◆ Instrument: eff. profile ( $K \otimes G$ )
  - ◆ Guiding: Gaussian



# Atmospheric transmission

- You know better than me
  - ◆ Multi-component expansion
  - ◆ Constraints from external probes
- What is a photometric night? At which level? Over which time-scale?

# Reference spectra

- Recalibration of the spectro-photometric standard stars ( $S^*$ )
  - ◆ Intrinsic consistency wrt/within Calspec: “standard star network”
  - ◆ Absolute flux/color calibration (e.g. StarDice, SCALA: Lombardo+17)
- Work in Progress in SNfactory
  - ◆ 14 years of repeated observations of 70 stars
  - ◆ spectro-photometry at mmag-scale

# Conclusions

- Slitless spectro-photometry is within reach
- Good understanding of dispersed image
  - ◆ Self-confusion is properly handled for punctual sources
  - ◆ **Assuming proper cross-contamination**
    - ▶ flexibility in dispersion orientation and/or multi-PA observations
    - ▶ multi-order decontamination
- Appropriate models of the different components
  - ◆ spectral trace: dispersion law  $\Delta(\lambda)$
  - ◆ spectral shape: instrumental PSF and seeing  $P_0$
  - ◆ flux:  $S = T \times S^*$  where  $T$  = transmission,  $S^*$  = ref. flux