

PRECISION MEASUREMENTS OF ^{20}F BETA DECAY

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A DISSERTATION

Submitted to
Michigan State University
in partial fulfillment of the requirements
for the degree of

2019

ABSTRACT

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ACKNOWLEDGMENTS

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Chapter 1

Introduction

Precision measurements at low energy can compete with high energy measurements.

1.1 New Physics Searches

Direct detection Indirect detection

1.2 Beta Decay

Beta decay is one of the processes by which unstable nuclei lose energy. The general process is shown in equation 1.1

$${}^A_Z P \rightarrow {}^A_{Z\pm 1} D + e^\pm + \nu_e \quad (1.1)$$

with ${}^A_Z P$ being the parent nucleus, ${}^A_{Z\pm 1} D$ being the daughter nucleus, e^\pm is the outgoing electron or positron, and ν is an outgoing neutrino. The neutrino is an anti-electron neutrino in the case of beta⁻ decay, and an electron neutrino in the case of beta⁺ decay. There is also the process of electron capture, where a proton in the nucleus captures an inner electron and turns into a neutron.

The simplest type of nuclear beta decay is allowed beta decay. There are two types of allowed beta decay, which differ in angular momentum J and isospin T selection rules. The

two types are called Fermi and Gamow-Teller beta decay. Neither of these transitions change parity. The difference is that, in a Fermi transition, the change of the angular momentum J and the change of the isospin T is both zero. For a Gamow-Teller transition, the change in the angular moment J is 0 or ± 1 and the change of the isospin T is 0 or ± 1 . However, a Gamow-Teller transition cannot cause a transition between two states of $J = 0$. These are called superallowed beta decays. There are also mixed allowed transitions, where both matrix elements of Fermi decay and Gammow Teller decay contribute. In order to see what physics beyond the standard model beta decay measurements are sensitive to, a closer look at beta decay is needed.

1.2.1 Microscopic View of Beta Decay

At a microscopic level, the process of beta decay involves one of the quarks inside the nucleon emitting a W particle. This quark changes flavor, and the nucleon changes as well. The microscopic view of beta decay (for the β^- case) is shown in figure 1.1.

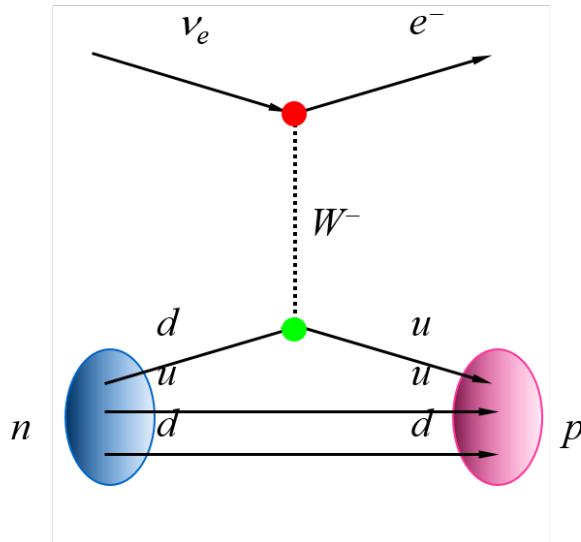


Figure 1.1: What β^- decay looks like microscopically

A down quark in a neutron goes to an up quark. This process emits a W^- boson that decays into an electron and an anti-electron neutrino. This means that any beta decay measurements are probing the weak sector. These measurements are complimentary to high energy measurements of weak interactions. For this work, a nucleon level treatment of beta decay will suffice.

1.2.2 Matrix elements of Beta Decay

In order to calculate the beta decay rate, Fermi's golden rule is needed. This is shown in equation 3.6.

$$\lambda = \frac{2\pi}{\hbar} \|M\|^2 \rho(E) \quad (1.2)$$

The density of states, $\rho(E)$, will be discussed further in the thesis.

This matrix element M , to first order, is shown in equation 1.3 [12]

$$|M|^2 = \xi [1 + a \frac{\vec{p}_e \cdot \vec{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} + \frac{\langle \vec{J} \rangle}{J} \cdot (A \frac{\vec{p}_e}{E_e} + B \frac{\vec{p}_\nu}{E_\nu} + D \frac{\vec{p}_e \times \vec{p}_\nu}{E_e E_\nu})] \quad (1.3)$$

ξ is written out in equation 1.4. This equation is written out to linear order.

$$\xi = \frac{1}{2} |M_F|^2 |C_V + C'_V|^2 (1 + |\rho|^2) \quad (1.4)$$

For equation 1.4, M_F is the Fermi matrix element, C_V and C'_V are vector coupling constants, and $|\rho|$ is the ratio of the Gamow-Teller matrix element to the Fermi matrix element. [12]

Going back to equation 1.3, $\langle \vec{J} \rangle$ is the average total angular momentum. The constants a , b , A , B , and D can be written in terms of the coupling constants as well. a depends on

the ratio of the Fermi and Gamow-Teller matrix elements ρ . This form of the observables informs the experimental design.

1.2.3 Types of Precision Measurements in Beta Decay

Given the form of equation 1.3, to get at different terms, different types of experiments are needed. A polarized nucleus is need to extract a . The nuclear spin points in one direction. Then, by angular momentum conservation, $\vec{p}_e \cdot \vec{p}_\nu$ can be found. Other correlations between energy and momenta have sensitivity to other terms in equation 1.3. Equation 1.3 is not complete, and many other terms exist.

For an unpolarized beam where only the energy of the electron is measured, the momenta are averaged over and all terms disappear except for b . This term is known as the Fierz term, and a measurement of the Fierz term was the ultimate goal of this experiment.

1.2.3.1 Fierz Term

The Fierz term, b , in equation 1.3, can be rewritten in terms of effective couplings. This is shown in equation 1.5

$$b = \pm \sqrt{1 - \alpha^2 Z^2} \frac{1}{1 + \rho} \text{Re} \left(\frac{C_S + C'_S}{C_V + C'_V} + |\rho|^2 \frac{C_T + C'_T}{C_A + C'_A} \right) \quad (1.5)$$

where ρ is the ratio of the Gamow-Teller matrix element to Fermi matrix element, α is the QED fine structure constant [12] The subscripts of C indicate which object the coupling corresponds to. Here, A means axial vector, V stands for polar vector, S stands for scalar, and T stands for tensor. The C coefficients correspond to parity conserving interactions, and the C' coefficients correspond to parity non-conserving coefficients [17] This means, that

in a pure Fermi decay, the Fierz term is sensitive to any non-standard scalar term, while in a pure Gamow-Teller decay, the Fierz term is sensitive to any non-standard Tensor terms.

The Fermi decays have been measured using super-allowed beta decays. For most of these measurements, however, decay of interest happens very rarely. The ft value was measured. ft values give the value of the Fierz term averaged over the beta decay energy spectrum. Several measurements of different decays are needed to get a good constraint. The other part of the Fierz term is the tensor coupling. In order to get a good measurement of tensor couplings, an allowed Gamow-Teller decay must be used. In this measurement, the nucleus of interest was ^{20}F .

Chapter 2

Description of ^{20}F

In order to get a measurement of the Fierz term, a nucleus that beta decays is needed. To put a limit on potential tensor terms, a Gamow-Teller transition is needed. To do a proper precision shape measurement, a simple decay relatively close to stability is needed. In this measurement, the nucleus used was ^{20}F .

2.1 ^{20}F Decay Characteristics

The decay scheme is given in figure 2.1.

As seen in the figure, ^{20}F decays 99.999% of the time to the first excited state of ^{20}Ne . The 2^+ state seen in the decay scheme is not the isobaric analogue state to the ground state of ^{20}F . That state is much higher in energy. The beta decay therefor has a isospin change of 1, and is a Gamow-Teller transition. The higher order matrix elements are very small. This means the Fierz term is sensitive to potential tensor couplings. The half-life of ^{20}F is about 11 seconds. This is an important consideration for the experimental design. The gamma ray and the end point energy of the electron are also important for the experimental design. In order to get at the Fierz term, the beta decay spectrum shape must be described precisely. The next chapter deals with the corrections to the beta decay spectrum.

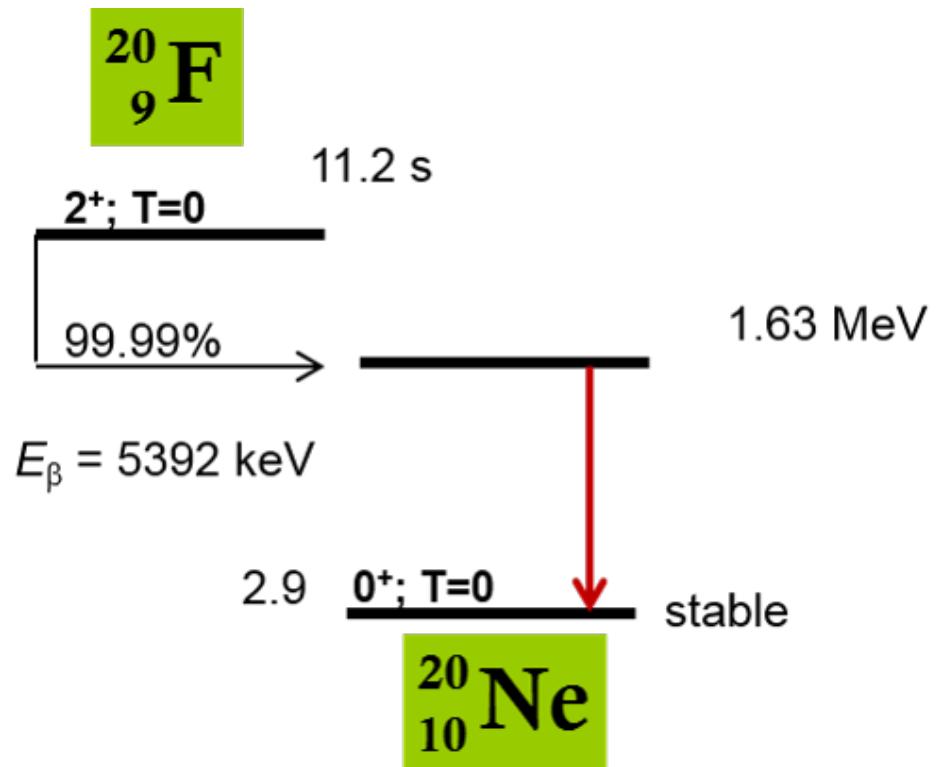


Figure 2.1: The decay scheme of ^{20}F .

2.2 Previous Measurements of ^{20}F

Chapter 3

Theoretical Description of Beta Decay Spectrum

To obtain a measure of the Fierz term, the beta decay spectrum must be precisely described. The description of the beta decay spectrum is written as a series of corrections on top of the main phase space factor. Through out this chapter, $\hbar = c = 1$.

The beta decay spectrum shape can be broken up in three different sections. The three terms are written out in equation 3.1

$$Q(E) = PS(E) * C(E) * \left(1 + b_{gt} \frac{m_e}{E}\right) \quad (3.1)$$

where $Q(E)$ is the total beta decay energy spectrum, $PS(E)$ is the phase space of the electron, $C(E)$ are all the hadronic and electromagnetic corrections multiplied together, and b_{gt} the Fierz term. This chapter will describe all that goes into the determining the beta decay spectrum.

3.1 Experimental Input to Describe Beta Decay

The corrections depend on several parameters of the decay. Some of them are just numbers, such as the atomic number of the daughter or mother nucleus or the mass number of the

system. However, there are two important parameters that are experimental measurements.

One is the q-value of the decay, which is defined in equation 3.2.

$$Q = m_{20F} - (m_{20Ne} + E_{level}) \quad (3.2)$$

where Q is the q-value, m_{20F} is the nuclear mass of ^{20}F , m_{20Ne} is the nuclear mass of ^{20}Ne , and E_{level} is the energy of the 1.6 MeV nuclear state in ^{20}Ne . Since it is difficult to measure bare nuclei, the atomic masses are used. For ^{20}F , $m_{20Ne} = 19.9924401762(17)\text{amu}$, $m_{20F} = 19.999981252(31)\text{amu}$ [24], and $E_{level} = 1.633674(15)\text{MeV}$ [22]. However, to get the total energy, m_e has to be added to the difference of atomic masses.

This mass difference is not quite the maximum electron energy. To get to the maximum electron energy, E_0 , the energy of the recoiling nucleus has to be taken into account. The formula is shown in equation 3.3

$$E_0 = Q \frac{1 + \frac{m_e^2}{2MQ}}{1 + \frac{Q}{2M}} \quad (3.3)$$

with m_e is the electron mass and M is the average nuclear mass [13].

The other parameter is the charge radius of the daughter nucleus. There are several ways to calculate the charge radius. In this work, the charge radius was taken from the measured root mean square (RMS) charge radius and converted. It was assumed that the ^{20}Ne nucleus was a sphere. From this, the radius was calculated using equation 3.4

$$r = \sqrt{\frac{5}{3}} r_{rms} \quad (3.4)$$

where r_{rms} is the root mean square charge radius, and r the charge radius. For this

work, $r_{rms} = 3.0055(21)$ [3]

With the two parameters, the q-value and the phase space, the shape of all beta decay spectra can be described.

3.2 Phase Space Beta Decay

The main part of the beta decay spectrum is the phase space factor. It is shown in equation 3.5

$$\frac{dN}{dE} = C * p_e W(Q - W)^2 \quad (3.5)$$

where C is a constant which includes the matrix element squared, p_e is the electron momentum, W the total electron energy, and Q the q-value of the beta decay. This is derived from the density of states of the particle. The constant is where the Fierz term enters. This comes in from Fermi's Golden Rule, which is shown in equation 3.6.

$$\lambda = \frac{2\pi}{\hbar} \|M\|^2 \rho \quad (3.6)$$

where λ is the transition probability, M the matrix element, and ρ the density of the states. The main effect on the spectrum shape originates from the density of states. The number of states for both the electron and the neutrino is show in equation 3.7

$$N = \frac{1}{(2\pi\hbar)^6} \int dr_e^3 \int dp_e^3 \int dr_{\nu_e}^3 \int dp_{\nu_e}^3 \quad (3.7)$$

where r and p corresponds to the position and momentum of the electron (e) and the neutrino (ν_e). Doing the integral over both r 's give two factors of the volume, which disappear

when the next factor is introduced. Since the neutrinos are unmeasured, the momentum of the neutrinos is integrated over. Assuming spherical symmetry, the new integral is shown in equation 3.8

$$dN = \frac{V^2}{4\pi^4 \hbar^6} p_e^2 dpe p_{\nu e}^2 dp_{\nu e} \quad (3.8)$$

This is simplified by approximating the neutrino as mass-less. The momentum of the neutrino is then equal to the energy of the neutrino. Then, the total energy E is written as a sum of the neutrino energy (or momentum) and the beta energy. Plugging that in gives equation 3.9 after integrating over the neutrino degrees of freedom.

$$dN = \frac{V^2}{4\pi^4 \hbar^6} (E - E_e)^2 p_e^2 dp_e \quad (3.9)$$

Then, the only thing left to do to recover equation 3.5 is to rewrite dp in terms of dE . The energy E_e has been replaced with W , which is the energy of the electron divided by the mass an electron, and E has been replaced by the Q-value. Since the measurement is not an absolute one, but only concerned with the shape of the spectrum, the normalization factor is arbitrary.

This is the main factor in describing the beta decay energy spectrum.

3.3 Variables of Correction Formula

For the rest of the discussion on beta decay corrections, everything is given without units. These corrections are largely electromagnetic in origin. All of the energies are divided by the electron mass. For this work, $m_e = 0.510998928 MeV$ The other important variables are

shown in table 3.1

Table 3.1: Variables used in the theory corrections

| Variable | Description | Equation or Value |
|-----------|--|---|
| A | Mass number | 20 |
| Z | Atomic number of daughter | 10 |
| α | Fine structure constant | $1/137.0359$ |
| R | Root mean square charge radius of daughter | 3.055 fm [3] |
| W | Total energy of beta electron | E/m_e |
| p | Electron momentum | $\sqrt{W^2 - 1}$ |
| W_0 | Maximum electron energy | E_0 |
| M_{ave} | Average nuclear mass | $\frac{M_{20}Ne + M_{20}F - 19m_e}{2m_e}$ |
| γ | Special relativity γ factor | $\sqrt{1 - (\alpha Z)^2}$ |

Before the theoretical corrections were fed into a Monte Carlo simulation, the uncertainties from the experimentally determined quantities was checked. Theoretical spectra were built with each value plus or minus it's uncertainty. Ratios between the spectra were taken and fit with a line. The results of those ratios are seen in figure 3.1.

Since the slopes of each line are much smaller than the shape factor values, the experimental uncertainties are negligible. The various theoretical corrections that are needed are now discussed below.

3.4 Electromagnetic Corrections and Hardonic Corrections

A graph of the various electromagnetic corrections are shown in figure 3.2, along with the hadronic shape factor.

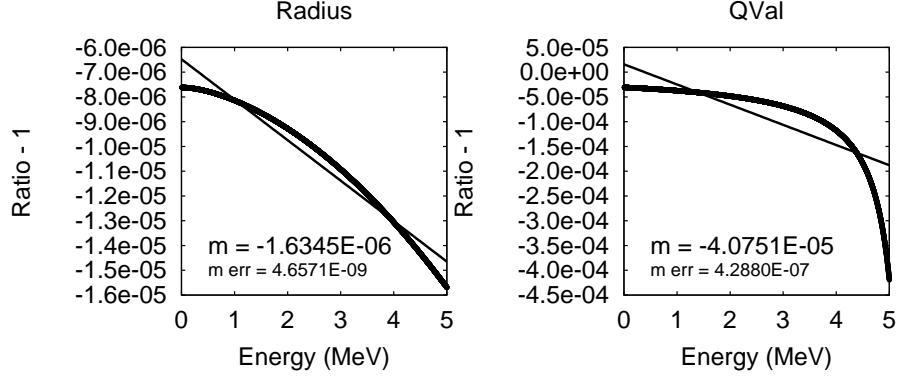


Figure 3.1: An estimate of the theory uncertainty due to the experimental parameter uncertainty. Shown are the slopes for each experimental parameter. They are orders of magnitude smaller than the $10^{-2}/\text{MeV}$ of the C_1 .

3.4.1 Fermi Function

The largest correction by over all size is the Fermi function. This accounts for the interaction of the charge of the outgoing electron and the charge of the nucleus. It is calculated by taking the Dirac equation wave functions and assuming the nucleus is a point charge of Ze . The Dirac wave functions are taken down to a nuclear radius R . This is since the wave functions diverge [28].

The Fermi function is printed in equation 3.10

$$F(Z, W) = 2 \frac{\gamma + 1}{\Gamma(2\gamma + 1)^2} (2pR)^{2(\gamma-1)} e^{\frac{\pi\alpha ZW}{p}} \left\| \Gamma(\gamma + i\frac{\alpha ZW}{p}) \right\|^2 \quad (3.10)$$

While this is the largest correction, it is the most understood one. The change of shape

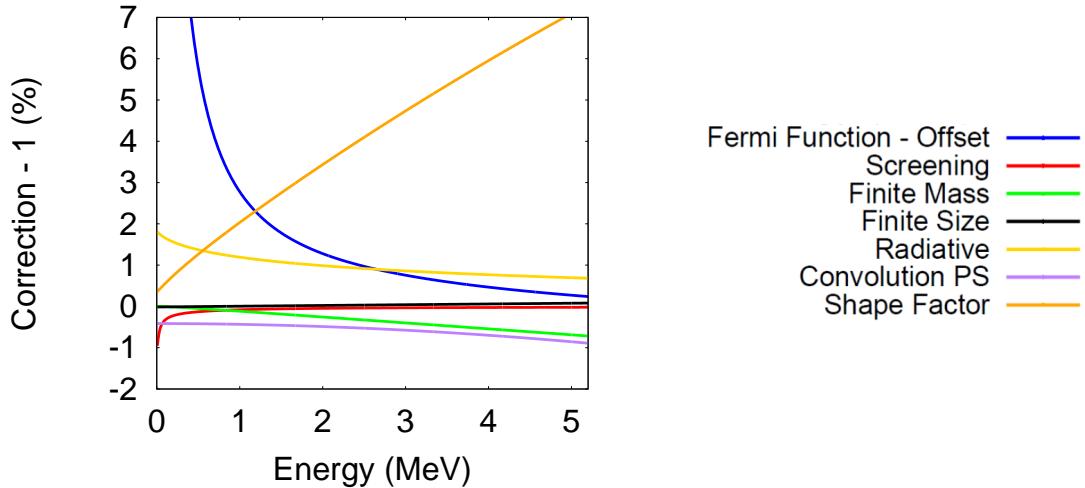


Figure 3.2: All the electromagnetic and hadronic corrections for ^{20}F plotted.

due the uncertainty in R is very small due to the functional form of the Fermi function.

3.4.2 Radiative Correction

The radiative correction was the next largest electromagnetic correction. For this measurement, the correction is only need to first order, which is on order α . The correction is a QED correction that stems from photons emitted from the beta particle. This photon can be absorbed by the nucleus of the daughter, which makes it a virtual photon. The photon can also be a real photon that propagates out off to infinity. The real photons are known as inner bremsstrahlung.

There are different descriptions of the radiative correction. The first is by Sirlin [21] and is shown in equation 3.11.

$$\begin{aligned}
R(W, W_0) = & 1 + \frac{\alpha}{2\pi} [3\ln(M) - \frac{3}{4} + 4(\frac{\operatorname{arctanh}(\beta)}{\beta} - 1) * (\frac{W_0 - W}{3W} - \frac{3}{2} + \ln(2(W_0 - W))) \\
& + \frac{4}{\beta} L(\frac{2\beta}{1+\beta}) + \frac{\operatorname{arctanh}(\beta)}{\beta} * (2 * (1 + \beta^2) + \frac{(W_0 - W)^2}{6W^2} - 4\operatorname{arctanh}(\beta))]
\end{aligned} \tag{3.11}$$

with $\beta = \frac{p}{W}$, M the proton mass, and $L(\frac{2\beta}{1+\beta})$ referencing to the Spence function, as seen in equation 3.12 [30]

$$L(x) = \int_0^x \frac{\ln(1-t)}{t} dt \tag{3.12}$$

The Sirlin formula assumes that the inner bremsstrahlung photons are not detected at all. This is mostly true if the source of the beta decay is centered outside of a detector. However, if the source is implanted inside of the detector, such as it is in this experiment, some of the inner bremsstrahlung is absorbed.

If all the inner bremsstrahlung is absorbed, a different form of the first order radiative correction is needed. There are many equivalent forms of this, but the one that was used for this experiment was by Fayans [7]. The form of this radiative correction is shown in equation 3.13

$$\begin{aligned}
R(W, W_0) = & 1 + \frac{\alpha}{\pi} [(\frac{2}{\beta} \ln(\frac{2\beta}{1+\beta}) + \frac{7}{8\beta} + \frac{3\beta}{8}) \ln(\frac{1+\beta}{1-\beta}) \\
& - 2\ln(\frac{4\beta^2}{1-\beta^2}) + \frac{4}{\beta} L(\frac{2\beta}{1+\beta}) + \frac{23}{8} + \frac{3}{2}\ln(M)]
\end{aligned} \tag{3.13}$$

With all the functions and variables meaning the same as in equation 3.11.

Unfortunately, the amount of inner bremsstrahlung absorbed depends on the geometry.

A more careful treatment of the radiative correction is needed.

3.4.2.1 Inner Bremsstrahlung

To first order, the energy spectrum of the inner bremsstrahlung photons is independent of Z . This is exactly like the two radiative corrections shown in equations 3.11 and 3.13. The spectrum is written out in equation 3.14 [16]

$$\Phi(k, W_e) = \frac{\alpha p}{\pi p_e k} \left(\frac{W_e^2 + W^2}{W_e p} \log(W + p) - 2 \right) \quad (3.14)$$

where $\Phi(k, W_e)$ is the probability density of seeing a photon of energy k from an electron of initial energy W_e . This equation was derived one way using outgoing waves from the Dirac equation in polar coordinates. This was calculated with the first order Born approximation. This means that at low energies, equation 3.14 is inaccurate. That can be seen, as the equation diverges as k goes to zero. If more orders of the approximation are added, this divergence can be controlled. These higher orders would correspond to emitting multiple photons. Each of these orders would have a probability reduced by a factor of α compared to equation 3.14. The higher orders would be less significant, except for at low energies. Since the probability density diverges, the higher orders could contribute. This would make the probability of emitting no photons finite.

However, another possibility is to add a cutoff. As long as the cutoff is high enough to be in the region where the first order Born approximation is valid, but low enough not to cut out gamma rays that are not fully absorbed, equation 3.14 is usable. The cutoff used was 50 keV. This cutoff was checked using Monte Carlo, and is within the region where the detector

and the source geometry absorbs all gamma rays.

To quantify the exact effect of the inner bremsstrahlung, a GEANT4 simulation was used. Electrons were generated using the phase space and the radiative correction in equation 3.13. Then, for each electron, equation 3.14 was sampled and a photon generated. No other physics process was looked at in this simulation. The ratio consisting of the energy absorbed over the initial energy was the output of the simulation. That ratio is the effective efficiency of absorbing the inner bremsstrahlung photons. Multiplying that ratio by equation 3.13 gives the effective radiative correction. Comparing all three radiative corrections can be seen in figure 3.3

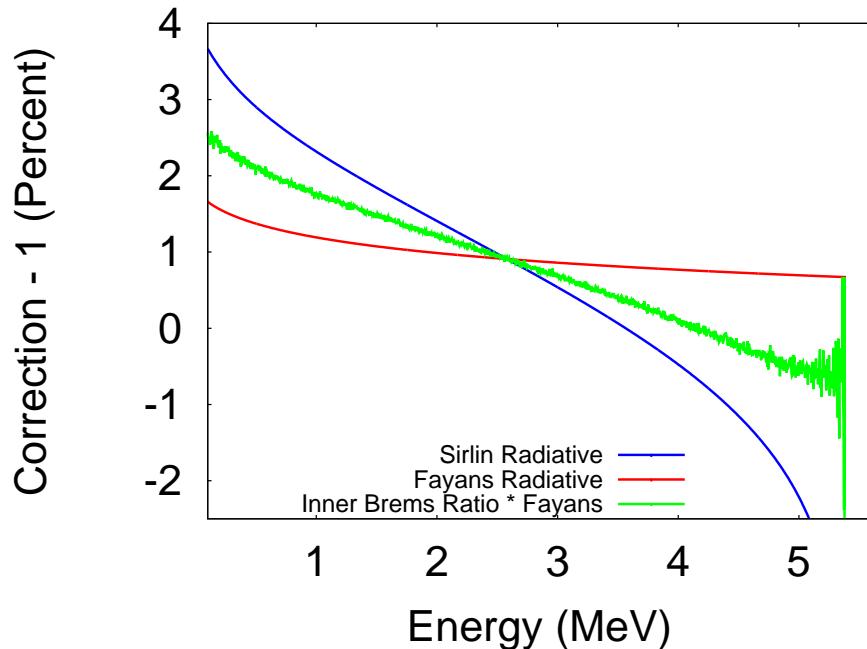


Figure 3.3: Comparing three different radiative corrections. The green line depends strongly on the detector geometry.

In order to see the effect of each correction on the slope, all three corrections offset in order to start from the same starting point. This is seen in figure 3.4. The effect of the inner

bremsstrahlung is to put the radiative correction halfway between the Sirlin and the Fayans formulas.

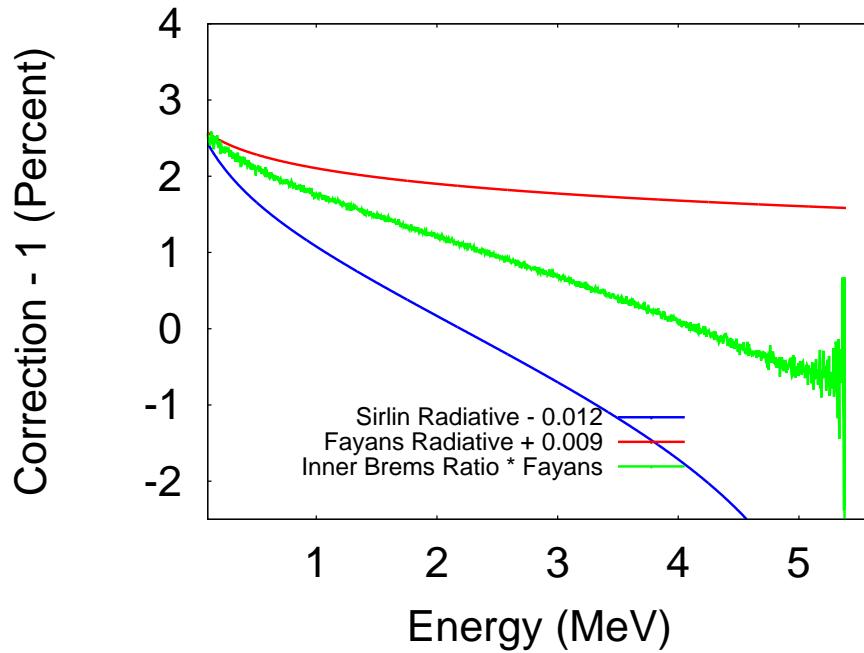


Figure 3.4: Starting all three radiative corrections from the same place. The green line is about halfway between the two others.

3.4.3 Screening

The screening correction is the next largest electromagnetic correction. It corresponds to the screening of the nuclear charge due to the electron cloud of the atom. The strongest effect of the screening correction is at low electron energies. This is a correction to the Fermi function.

3.4.3.1 Potentials Used in Screening Derivation

To calculate this correction, the Coulomb potential used to calculate the Fermi function is replaced with a Hulthén potential. This is shown in equation 3.15

$$V(r) = -\frac{\alpha Z \beta}{e^{\beta r} - 1} \quad (3.15)$$

Where r is the distance away from the center and β is a parameter characterizing the diffuseness of the electron cloud. The ratio of this new Fermi function to the old Fermi function is the screening correction. It multiplies the phase space.

The screening correction is negligible except for near the origin. Near the origin, equation 3.15 behaves as equation 3.16

$$V(r) = -\frac{\alpha Z}{r} + \frac{1}{2}\alpha Z \beta \quad (3.16)$$

and β is given by equation 3.17 [5].

$$\beta = 2C(Z)\alpha Z^{\frac{1}{3}}m_e \quad (3.17)$$

In the case of beta decay, the Z is number electrons of the mother atom. The assumption is that beta decay is occurring from neutral mother atoms. The only unknown is $C(Z)$.

To find the value of $C(Z)$, a comparison to another method of treating screening is needed. In another method of describing screening, the potential is described as a series of exponentials. This is shown in 3.18 [4].

$$V(r) = -\frac{\alpha Z}{r} \sum_n c_n e^{-b_n x} \quad (3.18)$$

where b_n and c_n are constants. The sum of all the c_n adds up to one. The value of x is shown in equation 3.19 [4]

$$x = 1.13\alpha Z^{\frac{1}{3}}rm_e \quad (3.19)$$

When equation 3.18 is expanded near the origin, the result is equation 3.20

$$V(r) = -\frac{\alpha Z}{r} + \alpha Z 1.13\alpha Z^{\frac{1}{3}}m_e \sum_n b_n c_n \quad (3.20)$$

By comparing equation 3.16, equation 3.17 and equation 3.20, the results in equation 3.21 are obtained.

$$C(Z) = 1.13 \sum_n c_n b_n \quad (3.21)$$

For fluorine, $n = 1$, $c = 1$, and $b = 0.907$ [4].

3.4.3.2 Screening Correction Formula

With all these factors out of the way, the screening correction can be written. $C(Z)$ in equation 3.17 is $0.907 * 1.13 = 1.02491$. The result is shown in equation 3.22 [5].

$$Q(Z, W) = X\left(\frac{W'}{W}\right) \left| \frac{\Gamma(\gamma + iy')}{\Gamma(\gamma + iy)} \right|^2 \left| \frac{\Gamma(\gamma + 2i\frac{p'}{\beta})}{\Gamma(\gamma + 2i\frac{p}{\beta})} \right|^2 e^{-\pi y} \left(\frac{2p}{\beta} \right)^{2(1-\gamma)} \quad (3.22)$$

with $y = \frac{\alpha Z W}{p}$, $y' = \frac{\alpha Z W'}{p'}$, γ is in table 3.1, $W' = W - \frac{1}{2}\alpha Z \beta$, and $p' = \frac{1}{2}p + \frac{1}{2}\sqrt{p^2 - 2\alpha Z W' \beta}$.

$X\left(\frac{W'}{W}\right)$ is in equation 3.23

$$X = \frac{1 + \frac{W' + \gamma m}{W'} \frac{\beta^2}{p} + \frac{1}{2} \gamma^2 [1 + (1 - \frac{\alpha Z}{\beta(W+m)})^{\frac{1}{2}}]^{-2} \frac{W-m}{W'} \frac{\beta^2}{p} [1 - \frac{1-\gamma}{8\gamma} \frac{\beta^2}{p}]}{(1 + \frac{\beta^2}{4p})} \quad (3.23)$$

The factor X in equation 3.23 is very close to 1. This correction matters most at low energy, and is very flat above 100 keV.

3.4.4 Finite Mass Correction

The finite mass correction corrects for the recoil movement of the ^{20}F nucleus. The form of finite mass corrections is given in equation 3.24 [29]

$$R(W, W_0, M) = 1 + r_0 + \frac{r_1}{W} + r_2 W + r_3 W^2 \quad (3.24)$$

With W being the total electron energy, W_0 the maximum electron energy, and M the nuclear mass of ^{20}Ne . The form of the r_i depends on if the decay is a vector decay or an axial decay. This is due to angular momentum conservation. Since ^{20}F is an axial decay, the form of the finite mass correction is shown in equations 3.25

$$\begin{aligned} r_0 &= -\frac{2W_0}{M} - \frac{W_0^2}{6M^2} - \frac{77}{18M^2} \\ r_1 &= -\frac{2}{3M} + \frac{7W_0}{9M^2} \\ r_2 &= \frac{10}{3M} - \frac{28W_0}{9M^2} \\ r_3 &= \frac{88}{9M} \end{aligned} \quad (3.25)$$

This effect is different than the hadronic shape factor.

3.4.5 Finite Size Correction

The finite size correction originates from treating the nucleus as a sphere uniformly charged sphere instead of a point particle. This sphere has a radius of R , as shown in equation 3.4. The form of the finite size correction is shown in equation 3.26 [29]

$$L_0(Z, W) = 1 + \frac{13(\alpha Z)^2}{60} - \alpha ZWR \frac{41 - 26\gamma}{15(2\gamma - 1)} - \alpha ZR\gamma \frac{17 - 2\gamma}{30W(2\gamma - 1)} + a_{-1} \frac{R}{W} + \sum_{n=0}^5 a_n (WR)^n + 0.41(R - 0.016) \quad (3.26)$$

Where the a_i coefficients are parameterized by equation 3.27

$$a = \sum_{x=1}^6 b_x (\alpha Z)^x \quad (3.27)$$

The b_x coefficients are numbers shown in table 3.2

Table 3.2: Coefficients for finite mass correction

| | b_1 | b_2 | b_3 | b_4 | b_5 | b_6 |
|----------|----------|----------|-----------|-----------|------------|-----------|
| a_{-1} | 0.115 | -1.8123 | 8.2498 | -11.223 | -14.854 | 32.086 |
| a_0 | -0.00062 | 0.007165 | 0.01841 | -0.053736 | 1.12691 | -1.5467 |
| a_1 | 0.02482 | -0.05975 | 4.84199 | -15.3374 | 23.9774 | -12.6534 |
| a_2 | -0.14038 | 3.64953 | -38.8143 | 172.1368 | -346.708 | 288.7873 |
| a_3 | 0.008152 | -1.15664 | 49.9663 | -273.711 | 657.6292 | -603.7033 |
| a_4 | 1.2145 | -23.9931 | 149.9718 | -471.2985 | 662.1909 | -305.6804 |
| a_5 | -1.5632 | 33.4192 | -255.1333 | 938.5297 | -1641.2845 | 1095.358 |

3.4.6 Convolution of Lepton and Nucleon Wavefunction

This is the last of the relevant electromagnetic corrections. In figure 3.2, the name given is, "convolution PS." This correction $C(Z, W)$ accounts for the interaction of the lepton

and nucleon wavefunctions. The radial part of the nucleon wavefunctions are modelled as a rectangle with width R . This is adequate for a shape measurement. Much like the finite size and mass corrections, this correction depends on the type of β decay. Since the decay of interest is an axial vector decay, the form of this correction is shown in equation 3.28

$$C(Z, W) = 1 + C_0 + C_1 W + C_2 W^2 \quad (3.28)$$

where the C coefficients are defined in equation 3.29 [29]

$$\begin{aligned} C_0 &= -\frac{-233(\alpha Z)^2}{630} - \frac{(W_0 R)^2}{5} + \frac{2\alpha Z RW_0}{35} \\ C_1 &= -\frac{21\alpha Z R}{35} + \frac{4W_0 R^2}{9} \\ C_2 &= -\frac{4R^2}{9} \end{aligned} \quad (3.29)$$

This correction depends on both the maximum energy of the outgoing electron and the charge radius. The shape contribution from this correction is minimal.

3.4.7 Hadronic Corrections

Nuclear form factors are one of the largest corrections to the beta spectrum. There are four relevant form factors that come together into a correction called here the nuclear shape factor. The form factors are described in table 3.3 [19] [6]

$$S(E) = 1 + C_0 + C_1 + \frac{C_{-1}}{E} + C_2 E^2 \quad (3.30)$$

where the C terms depend on the form factors and nuclear decay variables. How the

Table 3.3: Nuclear Form Factors

| Form Factor | Name | Value |
|-------------|---|----------------------|
| c_{1nuc} | Fermi matrix element | 0.253 |
| c_{2nuc} | Matrix element momentum transfer factor | 0.755 fm^2 |
| b_{wm} | Weak magnetism | 43.4 |
| d | Induced tensor term | 40.5 |

shape factor depends on the form factors is shown in equation 3.31 [6]

$$\begin{aligned}
 c_0 &= -\frac{2E_0}{M_{ave}} \left(1 + \frac{d}{c_{1nuc}} + \frac{b_{wm}}{c_{1nuc}} \right) + \frac{2c_{2nuc}}{9c_{2nuc}} 11m_e^2 \\
 c_{-1} &= -\frac{m_e^2}{3M_{ave}} \left(2 + \frac{2b_{wm}}{c_{1nuc}} + \frac{d}{c_{1nuc}} \right) - \frac{2c_{2nuc}}{9c_{1nuc}} 2m_e^2 E_0 \\
 c_1 &= \frac{2}{3M_{ave}} \left(5 + \frac{b_{wm}}{c_{1nuc}} \right) + \frac{2c_{2nuc}}{9c_{1nuc}} 20E_0 \\
 c_2 &= -\frac{40c_{2nuc}}{9c_{1nuc}}
 \end{aligned} \tag{3.31}$$

Two of the form factors, b_{wm} and c_{1nuc} are calculated from experimental data. d and c_{2nuc} are calculated from nuclear theory. The calculation of c_{1nuc} depends on the ft value. The calculation is shown in equation 3.32 [19]

$$c_{1nuc}^2 = \frac{2ft_0}{ft_{20}} \tag{3.32}$$

Where ft_0 is the ft value of the Fermi superallowed β decays, and ft_{20} the average of the ft values of the decays of ^{20}F and ^{20}Ne . This gives a value of 0.254 ± 0.004 [19]. The weak magnetism, b_{wm} , is of special theoretical interest.

3.4.7.1 The Weak Magnetism

The other form factor from the data is the weak magnetism form factor. It can be calculated from a $M1$ analog gamma-ray decay strength. This decay strength is from the 10.275 MeV analog state to the 1.634 MeV first excited state in ^{20}Ne . This is a 2^+ to 2^+ angular momentum transition, and a 1 to 0 isospin transition. The decay strength, Γ_{M1} , can be used to calculate b_{wm} as shown in equation 3.33

$$b_{wm} = \sqrt{\frac{6\Gamma_{M1}M^2}{\alpha E_\gamma^3}} \quad (3.33)$$

where M is the nuclear mass and E_γ the energy of that gamma ray. This gives a value of 43.4 ± 1.2 [19].

Getting a measurement of this value is of interest for two reasons. One, it tests the Conserved Vector Current (CVC) hypothesis. This hypothesis states that the weak interaction possesses a universal strength and a universal $V - A$ form [9]. This means that the quantity b_{wm} relates to difference of the magnetic moments of the neutron and the proton. In decays involving a $T = 1$ multiplet, the equation refeq:bwmcal is valid. This means the largest of the nuclear corrections can be determined from experimental data, which has a much smaller uncertainty than any theory calculations. The second reason is more experimental. It gives a parameter with which to benchmark analysis techniques. If the analysis produces a reasonable value of b_{wm} , the same procedure should give a good value for b_{gt} .

3.4.7.2 The Induced Tensor Form Factor

From equation 3.31, the induced tensor form factor d contributes to the corrections much in the same way as the Fierz term. The induced tensor form factor is calculated with theory.

Equation 3.34 gives the the tensor form factor [6]

$$d = Ag_AM_{\sigma L} \quad (3.34)$$

where A is the mass number (20 in this case), g_A the axial vector coupling constant, and $M_{\sigma L}$ a matrix element of the decay. This matrix element is shown in equation 3.35

$$M_{\sigma L} = < \beta | |\tau^+ i\vec{\sigma} \times \vec{l}| | \alpha > \quad (3.35)$$

where β is the final state, τ^+ the isospin raising operator, $\vec{\sigma}$ the spin operator, \vec{l} the angular momentum operator, and α the initial state. [6] In order to get the initial and final states α and β , shell model calculations have to be used. Different calculations have found d to equale 40.5 [6] and 20.5 [19]. Since d is divided by the aveage nuclear mass, this uncertainty in the form factor will not cause a large systematic effect.

3.5 Summary

With all these corrections, the experiment can be described to the required percision. The next chapter will describe details of the experimental set up and the detector configuration.

Chapter 4

Experimental Description

The experiment was run at the National Superconducting Cyclotron Laboratory (NSCL) in East Lansing, Michigan. The experiment was run from September 1, 2015 to September 7, 2015.

4.1 Experimental technique

The technique used was a calorimetric technique, where the isotope of interest is implanted inside a detector. This reduced several effects could otherwise distort the beta decay spectrum. The largest of these is backscattering. If a beta decay source is placed outside a scintillator, there is a chance that the electrons will go into the detector material and bounce back out. This happens in the surface of the detector, and therefore the electron deposits very little energy into the detector. Backscattering causes the largest distortion at low energies. However, the description of backscattering using detector simulations varies too much to get a sufficient description for a precision shape measurement [14]. Beta decay electrons can scatter out of the sides of the detectors as well. This also distorts the beta spectrum in a different fashion. Lastly if there is a dead layer at the surface of the crystal, the energy deposited in that layer will not be absorbed.

With the calorimetric technique, the radioactive nucleus is surrounded by detector material. As long as the nuclei are implanted deep enough, the electrons will not have enough

energy to escape the detector. Even if the electron scatters several times, it still deposits all its energy. This range depends on the detector material. Since any dead layers are at the surface, the decays inside the detector do not see them. A 4π angular coverage is also obtained, as the detector material surrounds the source.

There are some caveats for a calorimetric technique. The first is that a large enough detector is needed. Otherwise the electrons could escape at high energies. This means that this technique works best with scintillator detectors, since it is hard to grow semi-conductor detectors large enough to absorb all the electron energy. A large effect is that electrons moving through the detector material will emit a lot of bremsstrahlung. Using a low-Z detector material will lessen this effect. However, Monte Carlo detector simulations can describe the production and absorption of bremsstrahlung to enough precision to allow for a precision beta decay measurement. Another issue is that accelerators used to generate the isotope of interest must be able to create them at high enough energy in order to implant the isotopes deep enough into your detector. This limits what nuclei can be used for this technique. The act of implanting the nuclei gives the detector a lot of energy. This means that an implant and decay cycle is need for this experimental technique.

For this experiment, a beam of ^{20}F , was implanted into two different detectors, which were used to cross-check different systematic effects. One was a CsI(Na) scintillator detector, and the other was a EJ-200 polyvinyltoluene scintillator detector. After an amount of ^{20}F was implanted, the beam was turned off by dephasing the RF that drove the cyclotrons. Then, the ^{20}F was allowed to decay inside the detector. Given the half-life of ^{20}F of 11 s, the measuring time was varied between 22 and 60 s.

4.2 Creating ^{20}F Beam

The beam of ^{20}F was created at the coupled cyclotron facility at the NSCL. The primary beam of ^{22}Ne was accelerated by the coupled cyclotrons to 150 MeV/A. A typical intensity of the primary beam was around $60 * 10^{-5}$ pnA. It was impinged on a 188 $\frac{\text{mg}}{\text{cm}^2}$ Be target and sent through the A1900 fragment separator. The resulting ^{20}F beam was at an energy of 130 MeV/A. The intensity of the ^{20}F was about $2 * 10^{-5}$ pnA. The beam was sent to the experimental vault where the detectors were sitting.

4.2.1 Beam Purity

The purity measured there was at 99.4%, with the main contaminates being ^{19}O . This was measured up stream of the detector set up. To double check the beam purity, two detectors were used. One was a thin Si PIN detector that was used as a sectionE detector. The other detector was a small CsI(Na) detector similar to the implant detector that was used during the steering and during the beam size measurement. It had a much lower voltage than the one used for the implantation measurement. Both of these in tandem were used to build a particle identification plot. From this, it was found that the beam is very clean.

4.2.2 Beam Size and Location

To test the size of the beam, a parallel plate avalanche counter (PPAC) was used. The size of the detector was 10 cm by 10 cm square. It was placed 65 cm upstream of the target. A horizontal and vertical grid was in the detector. Depending on where on each of the grids the particles hit, different charges were sent to either end of the PPAC. The signals were fed into a digital data acquisition system, and read out as an energy. The difference of the two

signals divided by the sum was interpreted as a position.

To calibrate the PPAC , a mask with several holes was used. This mask covered the front of the detector, and an alpha decay source in the vacuum was placed in front of the PPAC. Then, everything was left to run until an image of the mask was formed. The mask had holes in it every 1 cm. It also had a large L shaped hole so that the orientation of the mask could be seen. With this, the PPAC could be calibrated.

Before taking data for the beta decay spectrum measurement, the PPAC was inserted into the beam. After adjusting the parameters of the upstream beam optics, the final beam size at the PPAC was measured. The calibrated data of the signals was built into a 3-D histogram. There was some ringing in the PPAC, so the peak of the beam spot was fitted with a 3-D gaussian function. The average of the Gaussian and the sigma in the x and y direction was taken. From the sigmas, the half widths at half maximum (HWHM) in both directions were calculated. The distribution of the locations were sampled at eight different points. The points are shown as the black dots in Fig: 4.1. They are one HWHM away from the center.

After averaging the 8 points, the range on the z axis was taken from the average of those points to the top. The resulting beam was measured to be 8 mm by 6 mm large.

This is the size of the spot at the PPAC. Ion optics simulations were used to build the cross section of the beam at the PPAC and at the target. Using these cross sections, the magnification between the two locations was calculated. The magnification was different between the x and y directions.

For the depth of the implantation of the beam, ion simulations were used. The LISE++ program was fed the beam meagnets. It was given the energy of the beam and the detector set up. It then calculated the depth of the implantation of the detector and the range of

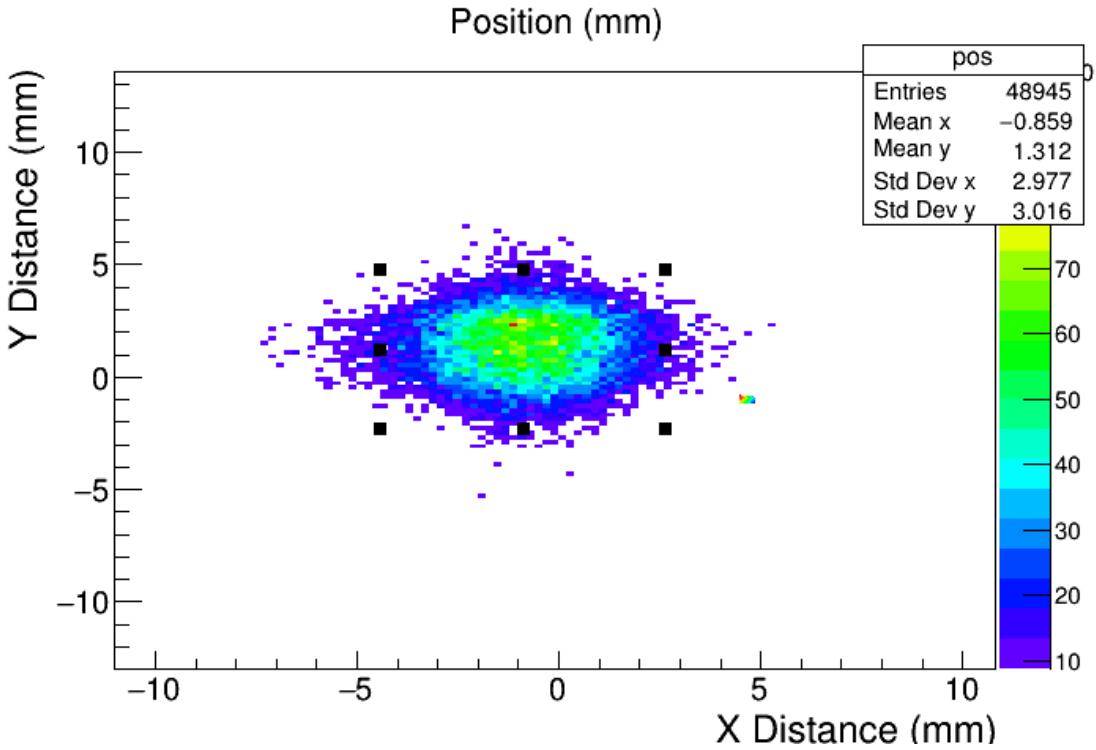


Figure 4.1: The beam spot of the calibrated PPAC spectrum. The samples of the spectrum that were averaged together are shown in the black dots. The center of the fit is not shown.

the depth inside the detector. This gave a depth of 3.02 cm in side the PVT detector and a depth of 1.156 cm in the CsI(Na) detector. The range of the depth was 1.2 mm in the PVT detector and 0.4 mm in the CsI(Na) detector.

4.2.2.1 Verification of Implant Depth

In order to verify the simulations for the beam implant depth, a degrader was inserted into the beam for a beam depth measurement. The degrader was made of aluminum and had two different thicknesses: 7.89 mm and 11.38 mm. The beam was caught by a CsI(Na) scintillator of a similar design to the one used for the implantation measurement. The angle of the degrader was changed to change the effective thickness of aluminum that the beam had to travel through. By varying this thickness to the one predicted to stop the beam outside

of the detector, the depth of implantation could be verified. This was done after the main run, and the simulations proved to be correct.

4.2.2.2 Spacers in Implant Detector

The actual CsI(Na) implant detector had PTFE spacers between the crystal wrapping and the aluminum housing. A spacer would be 2.4 mm thick. It was unknown if the spacer was in the path of the beam during an implant cycle. A similar crystal was taken apart for a repair. Pictures of that detector being taken apart showed where the spacer were on the side of the detector.

This is shown in figure 4.2



Figure 4.2: A CsI(Na) detector being taken apart. The red circle shows the side spacers

To see if the spacer was located in the path of the beam, the data with the degrader in front of the beam was used. The rates inside the implant detector was compared to the

effective thickness of aluminum. It was found took 14 mm of aluminum to bring the rate down to zero. This is shown in figure 4.3. If there were a PTFE spacer in the way of the beam, it would take 12 mm of aluminum to completely stop the beam. These results were calculated using LISE++ and are shown in figure ??.

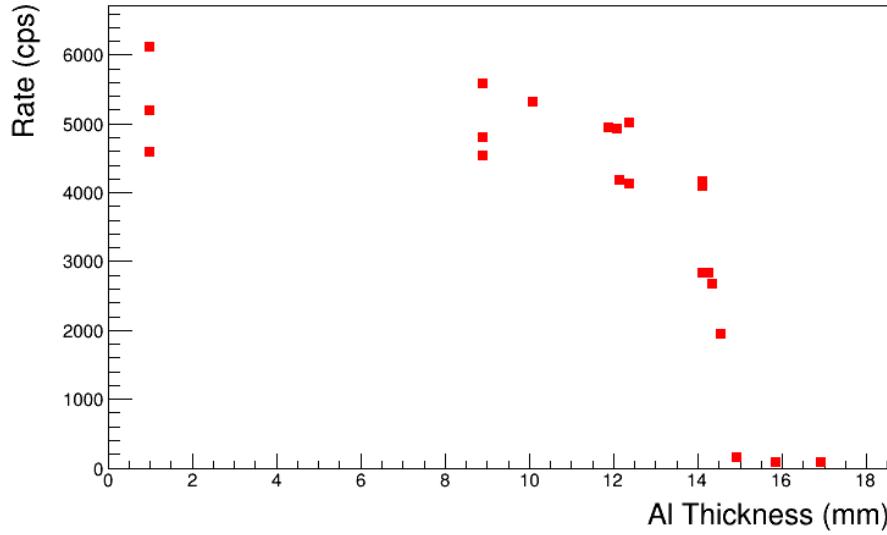


Figure 4.3: The experimental data from the degrader. All the fluorine is blocked after 14 mm of degrader

4.3 Detector Configuration

4.3.1 ^{20}F Decay Detectors

One implant detector was a scintillator 3 in diameter by 3 in long cylinder of EJ-200 polyvinyltoluene (PVT). It was attached to a clear plastic disk attached to a photomultiplier tube. The idea was to avoid a rate dependent gain effect that was seen in a previous experiment. The plastic detector signal is fast (around 100 ns) which makes pile-up a lesser concern. This detector was built by collaborators for this experiment. During the experiment the voltage on the PMT of this scintillator was varied. This was due do an observed

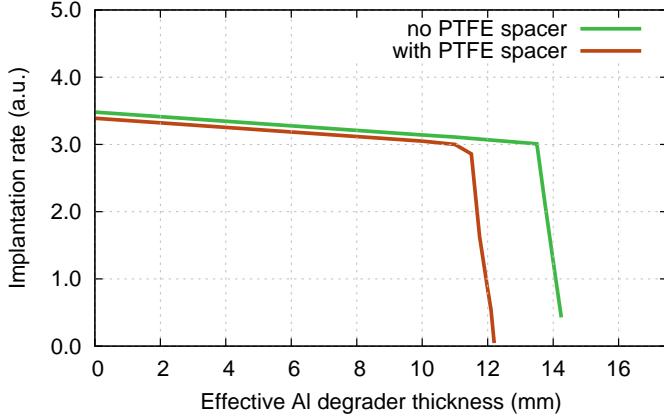


Figure 4.4: Calculating how thick an Al degrader would have to be to block the beam. A model with no spacer matches the data better.

distortion in the beta decay spectrum. A gain monitoring system was installed.

To monitor the gain of the plastic detector, a plastic disk containing an optical fiber was placed between the crystal and the photomultiplier tube. The other end of the fiber was fed into a box with an LED driven by a function generator, which ran at a trigger rate of 500 counts per second. The function generator produced two pulses separated by $136\ \mu\text{s}$. These two pulses had different amplitudes, so that the gain drift could be monitored by observing the drift from two different energies. The box was made light-tight with electrical tape and black paint. An additional optical fiber fed the light to a Si PIN diode. This was to monitor the light output of the LED.

To help check for systematics effects, another implant detector was used. It was a 2 in by 2 in by 4 in CsI(Na) detector. This detector was a module from the CAESAR array [26].

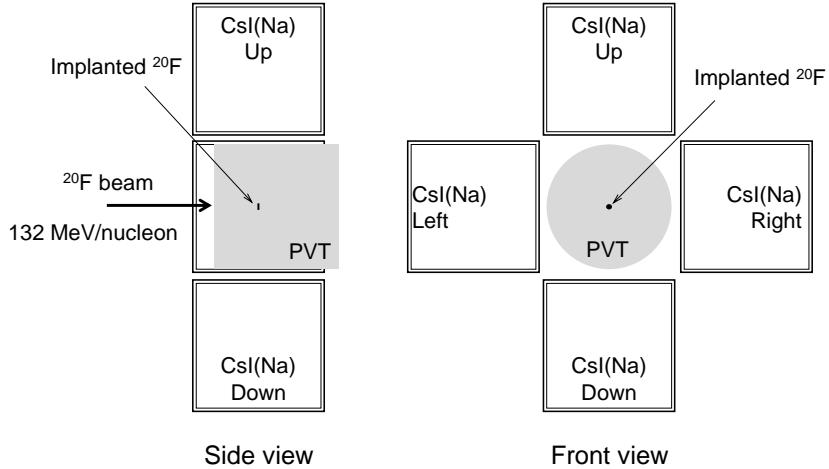


Figure 4.5: A sketch of the detector set up. Shown here is with the PVT detector implant. The CsI (Na) detector was centered in the middle of the the four gamma detectors and recessed by 1 inch. The bottom image shows a side of the detector set-up.

It does not have any gain monitoring like the PVT detector, but it is similar to a detector used in a different experiment. The other experiment was a similar measurement with ${}^6\text{He}$ instead of ${}^{20}\text{F}$.

In order to measure the gamma ray from the ${}^{20}\text{F}$ decay, a frame was built to hold four cubic 3 in CsI(Na) detectors. These were also part of the CAESAR array. The frame to hold the four detectors was designed to be able to move the four outer detectors around in various configurations. However, no other configurations were used during the experiment.

A sketch of both detector configurations is shown in Figure 4.5.

To switch between different implant detectors, the central detector in the frame was removed and put on the floor. The other detector was placed in the center of the four gamma detectors. The PVT detector was supported on a metal rail, while the CsI (Na) detector was supported on pile of scrap aluminum. The rail for the PVT detector, along with the four gamma detectors, can be see in figure 4.6.

A better view of the gamma detector cross can be seen in figure 4.7.

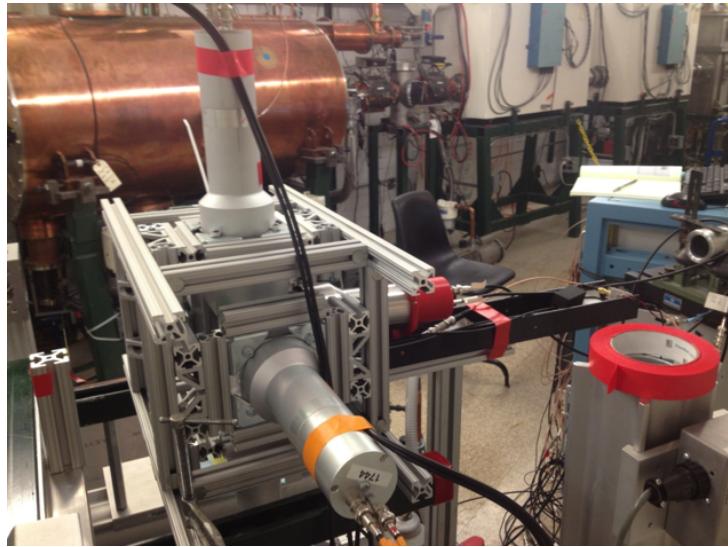


Figure 4.6: A picture of the PVT configuration. The colored tape on the PMTs of the gamma detectors was to keep track of what power and signal cable went to which detector. The rail the detector rested on can be seen. The optical fibers (the black cords) can be seen running into the black box with the LED.

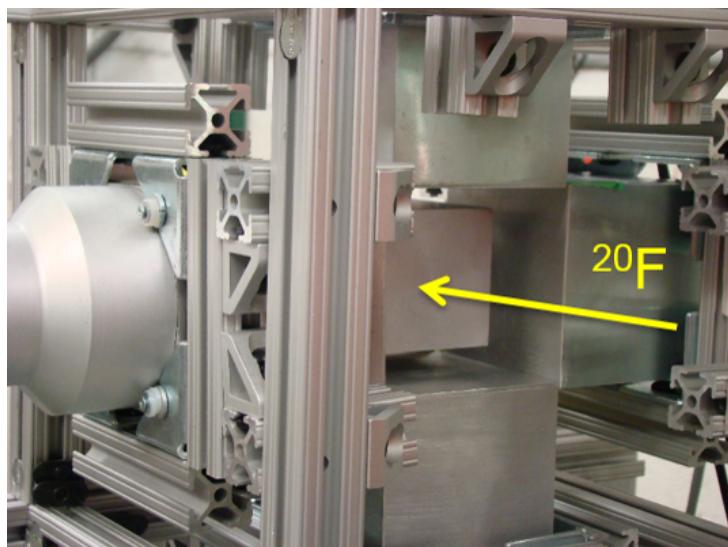


Figure 4.7: A picture of the CsI setup. The active crystal of the implant detector can be seen much better.

4.3.2 Detector Frame

The aluminum sheathing came with the detectors. However, the bars of aluminum in figure 4.6 were not part of the detector array. These bars made up the frame which was designed separately. In order to design the frame, the program FreeCAD was used. A CAD drawing of the gamma detectors was found and used. The PVT implant detector was modeled as a cylinder 3 inches in diameter and 3 inches long. The frame was made from extruded aluminum alloy bars from 80/20 Inc. Models of the bars were positioned in the program, and the frame built up from there. The frame was designed so that the gamma detectors could move around into a pin-wheel configuration. This configuration was not used during the experiment.

4.3.3 Powering the Detectors

To power the gamma and implant scintillators, 3 2-channel NHQ 212M ISEG power supplies were used. The Si detector was powered by a Tennelec TC248 amplifier. The PPAC was powered by an integrated power supply.

Each detector had a different voltage. The PVT implant detector was varied in voltage over the course of the experiment. This was due to concerns about saturation effects. Initially, the high voltage on the PVT detector was chosen to take advantage of the dynamic range of the detector. For the PPAC, The voltage for the four gamma detectors was chosen so that they had roughly the same gain. The voltages of the detectors is shown in table ??.

During the implantation cycle, a large amount of current was generated in the implant detectors. In order to counteract this, a limiter box was installed for the PVT detector for sets 3 to 6. The limiter box had several relays that cut the power to the PVT detector's

| Detector | Power Supply Setting (V) |
|------------------------|--------------------------|
| PVT Implant (Sets 1-4) | -975 |
| PVT Implant (Set 5) | -856 |
| PVT Implant (Set 6) | -780 |
| CsI (Na) Implant | 780 |
| CsI (Na) Gamma 1 | 930 |
| CsI (Na) Gamma 2 | 1000 |
| CsI (Na) Gamma 3 | 970 |
| CsI (Na) Gamma 4 | 1015 |
| Si Pin | 20 |
| Pin diode | 15 |
| PPAC | 560 |

photomultiplier tube during the beam on cycle. To accomplish this, the limiter box was given the same signal that fed the beam on/beam off for the cyclotrons. Due to concerns about the beta decay spectrum shape, the voltage on the PVT detector was changed as the experiment went on. For the CsI(Na) implant detector, the HV supply had the current limiter enabled. The power setting was not changed for the CsI(Na) implant detector.

4.4 Experimental Conditions

The data was taken in runs of roughly one hour. However, many runs were cut short when the DAQ stopped recording data for one of the detectors. This was usually the up gamma detector, and was correlated with the start of a new implant cycle. In order to properly measure the decay, the beam was pulsed with an implantation time of anywhere from 1 to 2 seconds, and a decay time ranging from 22 s to 32 s. The beam was turned off since the light from the implantation of the beam would drown out any signal obtained. A run with a decay time of 60 seconds was also taken for each implant detector.

To achieve the beam pulsing, two timer boxes were used. A CAEN N1145 quad scaler module was used to control the beam off time. This module had a digital control of time

down to 1 ms. Once the time finished counting down, a signal was sent to a second module. A CAEN N93B dual timer used the signal from the quad scaler as a start signal. The time period was set using a dial, which was less precise. Once the dual timer finished its time, it sent a signal back to the quad scaler to restart the cycle. The output of these two modules created a signal with one voltage level during the dual timer's time and another voltage condition during the quad scaler's time. This signal was fed into a box. The voltage level during the quad scaler's time dephased the cyclotron RF, turning the beam off. When the dual timer voltage level occurred, the RF returned to the tuned value, turning the beam on.

Chapter 5

Data Processing

The detectors were tested using an oscilloscope to check for their signals. The timing of each detector signal was recorded and used to tune the data acquisition. The signals were then inserted into a digital data acquisition system.

5.1 Data acquisition

All the signals for all the detectors were sent to digitizers. These digitizers were three 250 mega-samples per second 16 channel XIA PIXIE modules. They were run with the digital NSCL system. The first module had the implant detectors and the four gamma detectors. The second module had five signals from the PPAC and one signal for the Si detector. Both of these had the beam on signal, beam off signal, a 100 Hz pulser, and the signal from the PIN photo-diode. The third module only recorded the digitized wave-forms from the PVT detector.

Each of the channels on each of those modules outputted a time stamp and an energy calculated from a trapezoidal filter. The third module output the digitized waveform over 400 ns. The digitizers took samples every 8 ns. The clock used was a stable EPSON SGR-8002JC programmable crystal oscillator.

The first thing the PIXIE modules did was to digitize the wave forms of the signals. The digital wave forms of the signals were only saved for the PVT implant detector. The PIXIE

modules' software applied a trapezoidal energy filter to the digital wave-forms.

5.1.1 Trapezoidal Filter Description

The parameters of the trapezoidal filter needed to be set by hand. First, three sums of the digitized wave-forms were taken. The first sum was over a time known as $tPEAKING$. Then, a second sum was taken directly after the first over a time known as $tGAP$. Then, a third sum was taken directly after the second with over a period of $tPEAKING$ again. These three sums were added with equation 5.1

$$E = C_0 * S_0 + C_g * S_g + C_1 * S_1 \quad (5.1)$$

with S_0 being the first sum over $tPEAKING$ described above, S_G being the sum over $tGAP$, and S_1 being the second sum over $tPEAKING$. C_0 is described in equation 5.2

$$C_0 = \frac{-(1 - e^{\frac{tSPL}{\tau}})e^{\frac{tPEAKING}{\tau}}}{1 - e^{\frac{tPEAKING}{\tau}}} \quad (5.2)$$

where $tPEAKING$ is the time described above, $tSPL$ is the 8 ns sampling time, and τ an additional parameter.

C_g is described in 5.3

$$C_g = 1 - e^{\frac{tSPL}{\tau}} \quad (5.3)$$

with the same variables. Finally, C_1 is described in 5.4.

$$C_1 = \frac{1 - e^{\frac{tSPL}{\tau}}}{1 - e^{\frac{tPEAKING}{\tau}}} \quad (5.4)$$

With the same variables. This filter averaged the background before a pulse in C_0 over $tPEAKING$. It took a sample of the pulse, averaged over $tPEAKING$ again in C_1 . Then, it subtracted off C_0 from C_1 , after adjusting for the exponential decay of the pulse. The time constant of that decay is the τ parameter. When tuning the PIXIE system, the τ parameter has the most effect on the output energy.

For this experiment, the various filter parameters are summarized in table 5.1

Table 5.1: Energy Filter Parameters

| Detector | τ | $tPEAKING$ | $tGAP$ |
|------------------------|-----------|------------|--------|
| PVT implant | 60 ns | 208 ns | 128 ns |
| All CsI (Na) Detectors | 900 ns | 480 ns | 48 ns |
| PPAC Channels | 300000 ns | 1200 ns | 96 ns |

There was also a trigger filter in the PIXIE system. The filter was the same, but the times were much shorter, so that the trigger filter could work quicker. There was a threshold that the output of the trigger filter had to be above in order to be recorded. These values are shown in table 5.2

Table 5.2: Trigger Filter Parameters

| Detector | $tPEAKING$ | $tGAP$ | Threshold |
|------------------------|------------|--------|-----------|
| PVT implant | 104 ns | 104 ns | 30 |
| All CsI (Na) Detectors | 200 ns | 72 ns | 20 |
| PPAC Channels | 904 | 104 | 200 |

The peak of the trigger filter was used to calculate the time stamps of the events.

5.1.2 Data Acquisition Software

In order to set the parameters of the various filters, a program called NSCOPE was used [8]. The program GUI was used to set the rise time, the gap, and the threshold for both the energy filter and the trigger filter. These parameters were set differently for each detector type. The CsI(Na) detectors (the implant and the 4 gamma detectors) shared the rise time and gap time, while other detectors had different parameters. Sample spectra were taken with NSCOPE, and the parameters saved to a file.

This file was loaded with a program called ReadOut, which ran the data taking. The ReadOut program used a ringbuffer in order to record the output of the data. The program recorded data as an .evt binary file if the record option was selected.

The ringbuffer was also fed to a program called scalers. This gave the rates of the events coming into each channel. It gave an input rate to each channel, the recorded rate, and the total over each run. This was to check how each channel in each module was doing.

For online analysis, a program called SpecTcl was used. It took the evt files and processed them into histograms. These histograms could be put in coincidence. Displays of the implant detector energy and rate were displayed. The energy of the implant vs time was also displayed. Additionally, the implant energy vs time since last beam on was plotted as a 2-D spectra. The decay curves (time in implant minus last beam on) were also plotted. These histograms were used as diagnostics.

5.2 Data Taking and Processing

To take data, the ReadOutGUI program was activated. Data was taken in one hour intervals called runs, unless one of the detectors stopped counting early. If a detector stopped early, it

was the up detector. When that happened, the run was ended before one hour was up. The events built by Readout had a time interval of 8000 ns.

Each run generated one or more .evt files. The resulting .evt files of ReadOut were processed using a program called DDAS dumper. This converted the .evt files to ROOT files. One .evt was dumped to .root file. These ROOT files contained a TTree that had the energy and time stamps of each detector. The information was saved event by event. It was formatted in a C++ class called DDASEvent. This event class contained data for each channel from the data acquisition. The energy was given out in ADC units and was not calibrated. The time was given counts of DAQ clock. The digitized wave forms were also saved in this event.

From the ROOT files from the ddasdumper, another ROOT file was built. All the ROOT files from one run was built into one new ROOT file. These files were processed with a modified version of a program called *scan*. The original version was written by Stan Paulauskas. The TTree was looped over event by event. For each event, each channel was looped over. For the first event and first channel, the time integer was recorded. This first time was subtracted from all subsequent time stamps. The time differences were multiplied 8 ns to turn them into time in seconds. Then, the various energies and times for each detector were built into histograms for each channel. During looping through the events, the energy and times for the implant detectors, four gamma detectors, beam on signal, and beam off signals were saved to a variable. This information was used to build new events for a new TTree.

Each event started with a non-zero energy reading in any of the five detectors. Then, a 400 ns long time gate opened, during which all energies and times were saved into the event. The time signatures of the last beam on and beam off signals were also saved into

each event. The energies of the beam on or beam off signals were 0 or 1.

Chapter 6

Half Life Measurement

6.1 Motivation

During the experiment, it was noticed that there was a disagreement between different values of the half-life. As a side project and as a chance to thoroughly investigate the data, a half-life measurement was taken. The previous measurements of the half-life of ^{20}F are shown in Figure 6.1.

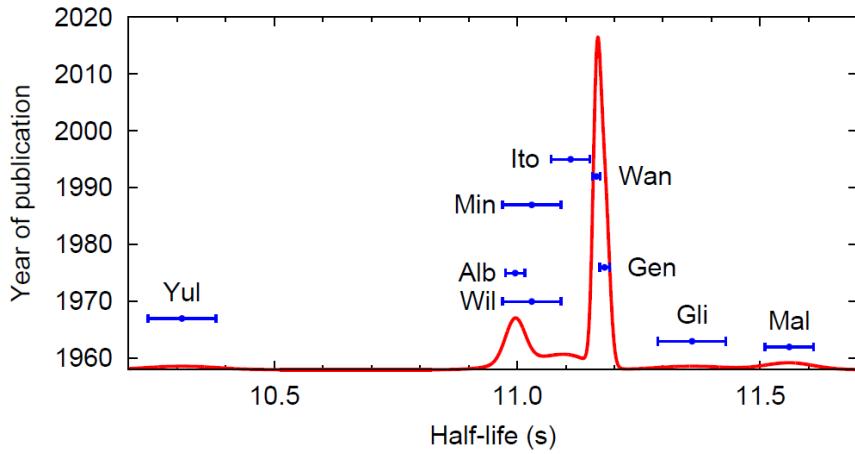


Figure 6.1: Previous measurements of the ^{20}F half-life. The labels correspond to: Mal [18], Gli [11], Yul [31], Wil [27], Alb [2], Gen [10], Min [20] and Wan [25] and Ito [15].

This ideogram has a red line which is a sum of Gaussian functions. The centroids of the Gaussians are the central values of the measurements. The sigmas are the errors, and each Gaussian is weighted by $\frac{1}{\sigma^2}$. This is to see that there are two different values that the half-lives are converging to.

It has been used in the past for searches of second-class currents and in astrophysics.

6.2 Half life data analysis

First, the data was processed as described in the previous chapter.

6.2.1 Data Selection

Only the data from the PVT implantation set was used for the half-life analysis. Afterglow was present in the CsI(Na) detector. This caused a slow pile-up effect, where a higher rate means more light. The extra light pushed events at higher rates towards higher energies. For the decay curve, it meant that at earlier times, the effective gain of the implant detector was higher. The beta cuts, however, stayed in the same position. Early in the decay cycle, events near the cuts could start out inside the window. As time went on and the gain changes, these cuts could move below the lower beta cut. Due to the shape of the beta spectrum, the higher the lower beta cut, the larger the effect. This effect is seen in Figure 6.2.

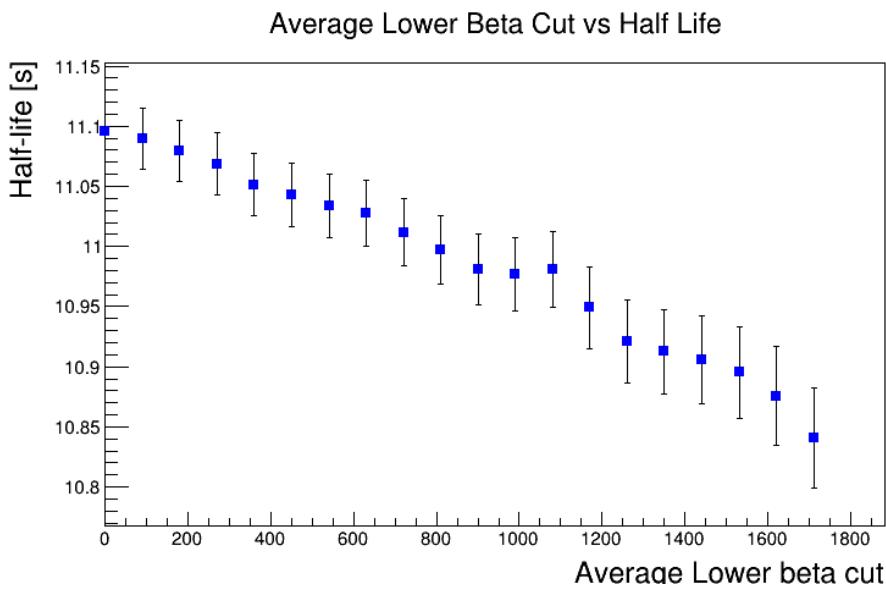


Figure 6.2: The effect of the lower beta cut vs the half-life in the CsI(Na) data

Attempts were made to counteract this effect with a more sophisticated analysis. The beta spectrum was built and fitted second by second in order to obtain a time-dependent calibration. The gain of the calibration was plotted as a function of time and fit with a line. The offset of the calibration was seen to be independent of time. The resulting time-dependent calibration was used to analyze the data. This reduced the effect seen in Figure 6.2, but did not entirely eliminate it. Since the CsI(Na) data has a small statistical impact, it was decided to eliminate that data from the analysis of the half-life.

The plastic scintillation did not have any afterglow, so the PVT implant detector was immune to this effect. The PVT data was separated into 7 sets. A summary of the set conditions is shown in Table 6.1 As shown in the table, the major conditions were the PVT high voltage, the inhibitor box, and the beam current.

Table 6.1: The PVT runs

| Set | Beam on Time [s] | Measuring Time [s] | PVT HV [v] | HV Inhibit Installed | Beam intensity [nA] | Runs |
|-----|------------------|--------------------|------------|----------------------|---------------------|------|
| 1 | 1.67 | 30 | -975 | No | 30 | 9 |
| 2 | 1.67 | 30 | -975 | No | 93 | 2 |
| 3 | 1.67 | 30 | -975 | Yes | 30 | 9 |
| 4 | 1.67 | 30 | -975 | Yes | 93 | 11 |
| 5 | 1.67 | 30 | -856 | Yes | 30 | 93 |
| 6 | 1.00 | 60 | -800 | Yes | 93 | 1 |
| 7 | 1.10 | 20 | -780 | Yes | 93 | 10 |

The inhibitor box was not installed until the third set of data. The inhibitor box shut off the high-voltage during the beam on period. Without the box, the current on the PMT was saturated during the beam on period. This caused a gain shift over time as the power supply recovered. This time-dependent gain shift caused large systematic errors when the beta cuts were moved. Thus, sets 1 and 2 where not used in the final analysis, but are listed here for completeness's sake. These gain shifts can be seen in Figure 6.3.

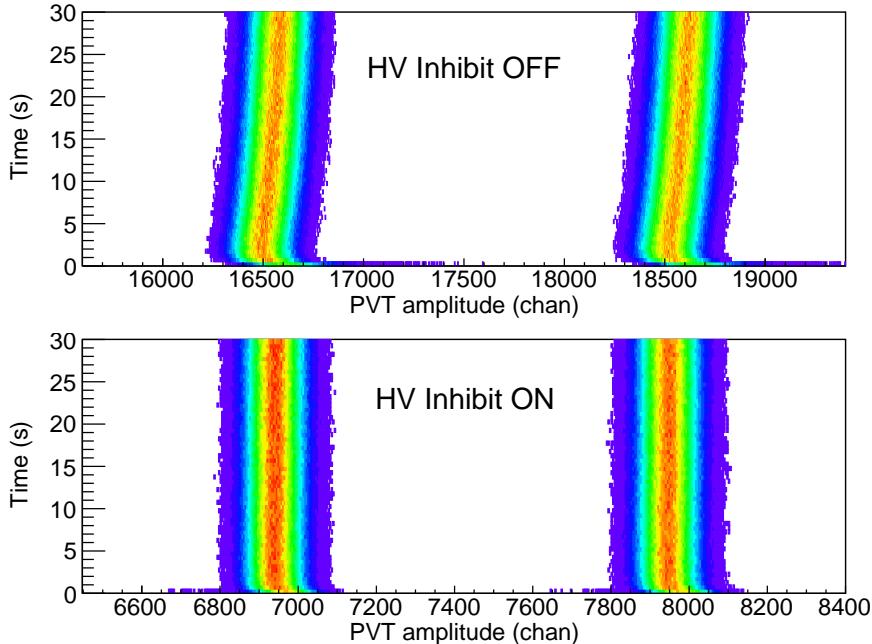


Figure 6.3: The light pulse as a function of time for set 1. The gain changes smoothly over time. This causes a large change in the half-life as the beta cuts are moved.

6.2.2 Cut Selection

In order to do the half-life analysis, software coincidences were imposed. Three conditions were set in total. Two conditions were on the energy in the implantation detector and one of the four CsI(Na) detectors. An additional condition on the time difference between the events recorded in the two detectors. A sample spectrum of all the gamma and beta energies is shown in Figure 6.4

Fixed energy gates were used for to select in the beta window for the PVT run sets. Each different data set had a different energy window due to the gain shifts. A sample spectrum with the gates can be seen in Figure 6.5. This spectrum was put in coincidence with the gamma spectra. The lower beta cut was selected to cut out the 511 beta spectrum as seen in Figure 6.4. When gated around that energies, the resulting gammas measured by the large CsI(Na) detectors are consistent with ^{10}C and ^{11}C . This comes from the break-up of the

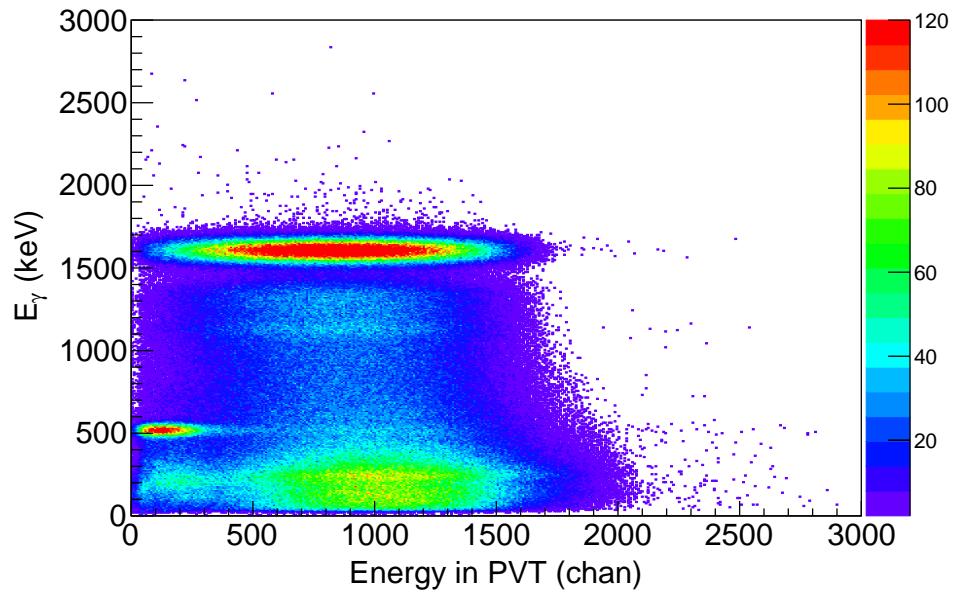


Figure 6.4: The 511 region can be seen in this graph

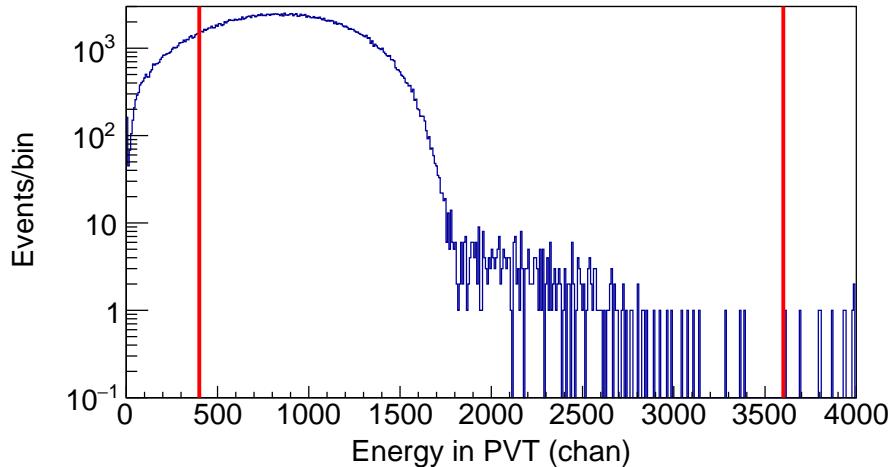


Figure 6.5: The lower beta cut was selected to be above the 511 region. The upper beta cut was selected to include all the pile up

plastic.

As described above, only the runs after the installation of the limiter box were used for the half-life analysis.

A time difference condition was set by building a spectrum of the time differences between

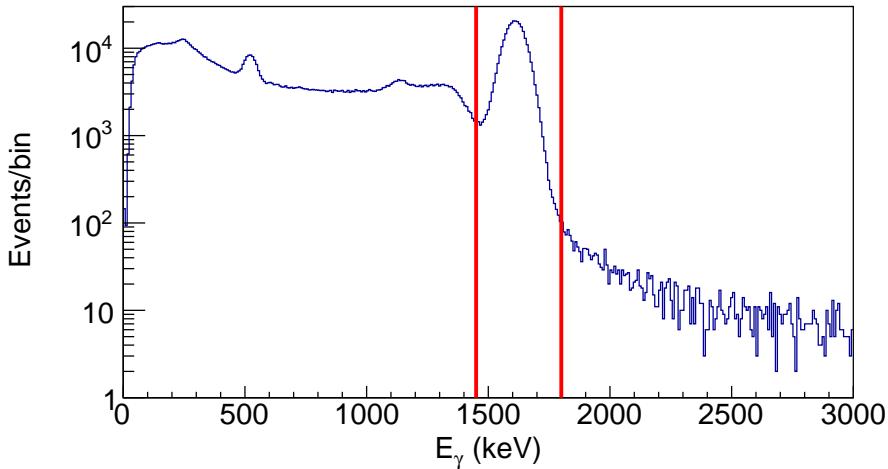


Figure 6.6: The wide cuts are to reduce the effect of the rate dependent gain.

the implant detector's event and one of the four gamma detector's events. The peak of this time difference spectrum was found, and an interval of ± 24 ns was used for this gate. A sample time difference spectrum can be seen in Figure 6.7

The time difference spectrum shows several features. First is the prompt peak, which are correlated gamma and beta events. To the right of the prompt peak, there is a pedestal of events. These come from pile-up events. What happens is that a ^{20}F event decays and the time stamp of the emitted beta is recorded. The corresponding gamma ray is not detected. Then, within the pile-up window, a second ^{20}F decays. The implant detector is dead and does not record the second time stamp. Due to pile-up, the time stamp of the second beta event is not recorded. The gamma ray is then detected at a later time compared to the first event. A cartoon sketch of this effect is shown in Figure 6.8. The pedestal can be seen in full in Figure 6.9.

The other events to the left of the prompt peak and to the right of the pile-up pedestal are accidental coincidences. These include the background coincidences.

The time signals for the outer four gamma detectors were used for the half-life analysis.

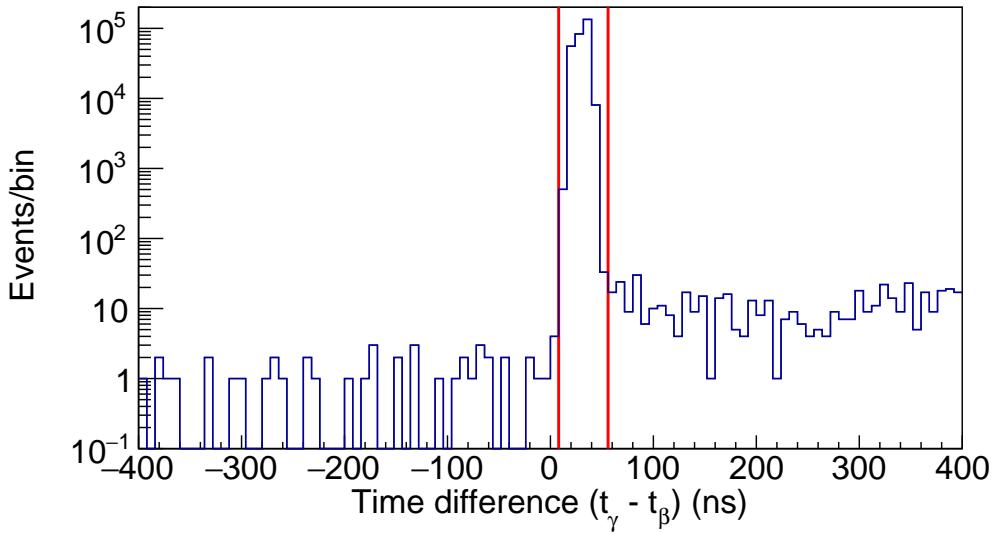


Figure 6.7: This is a gamma and beta energy filtered spectrum of the time difference between the up detector and the PVT implant detector. The tail on the right side of the large peak is due to pile up. The narrow time cuts are shown with a dotted line. The wide time cuts are shown with a solid line.

This gave 4 independent measurements of the half-life per run. Only full decay cycles were used. This was done by finding the last beam on and putting a condition on the run time of the events. The decays where the up detector stopped counting were ignored, as there were few enough that they did not make a difference.

The dead time was corrected using measured rates and a dead time of 464 ns for the implant detector and 656 ns for the gamma detectors. The dead time was measured by building a spectrum of the time difference between consecutive time stamps. The lowest time difference was taken as the dead time. This was checked using the light pulser in the PVT detector. For each gamma detector, a histogram of the energy-filtered rate was built. The unfiltered implantation detector rate and gamma rate was built. Using the uncorrected rates as an input, the gamma detector rate was corrected for bin by bin. The correction

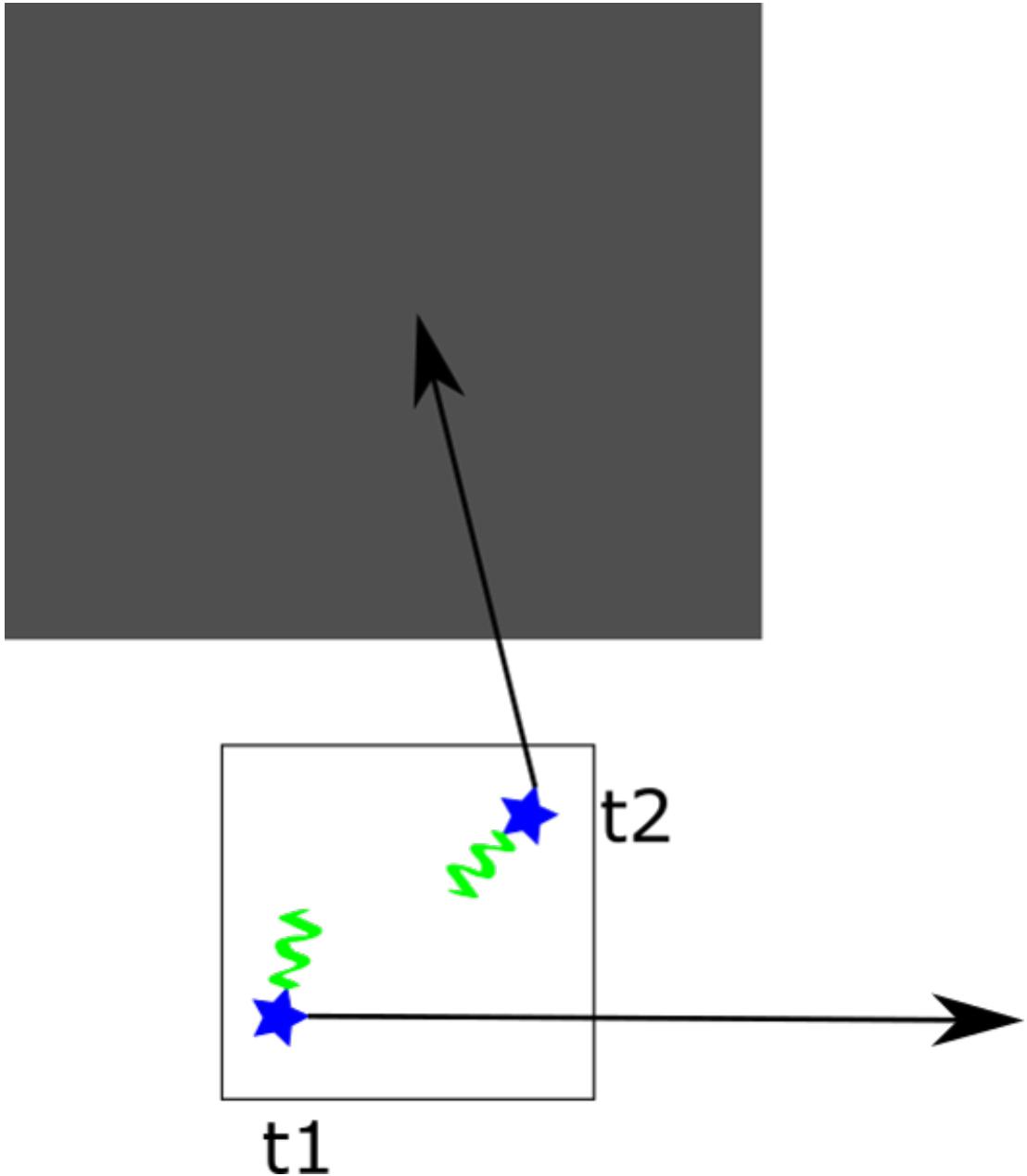


Figure 6.8: A sketch of the pile up events. A ^{20}F decay happens at time = t_1 . The green electron is detected in the implant detector. The black arrow (the gamma raw) is not. Then, later at time = t_2 , another ^{20}F decays. t_2 is within the pile-up window of t_1 . Both electrons energies pile-up and are added together. However, the time stamp recorded by the DAQ is still t_1 . The gamma ray from event t_2 can be detected in a gamma detector at time t_2 . This creates the uncorrelated event pedestal in the time difference graph.

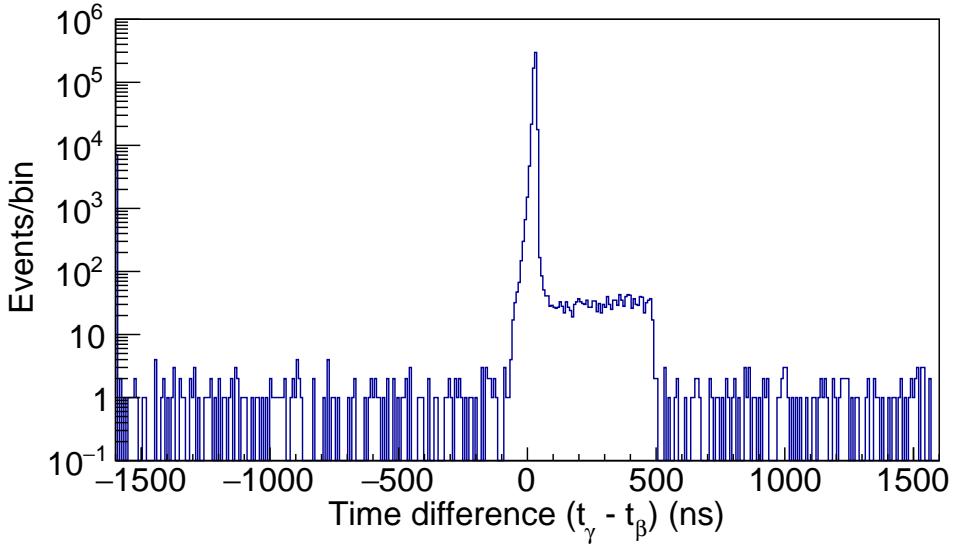


Figure 6.9: The time difference spectrum zoomed out. This figure is shown with energy coincidences.

used is shown in equation 6.1

$$r_{coincidence}^c = \frac{1}{1 - r_\beta \tau_\beta} \frac{1}{1 - r_\gamma \tau_\gamma} r_{coincidence}^m \quad (6.1)$$

where $r_{coincidence}^c$ is the corrected gamma-beta coincidence rate, r_β the raw measured implant rate, τ_β the dead time of the implant detector, r_γ and τ_γ the raw measured rate and dead time for the CsI(Na) detector, and $r_{coincidence}^m$ the measured coincidence rate. Then, after corrected for the dead time, each cycle was added together relative to the last beam off. These stacked cycles were used to find the half life.

For high beam intensity runs (i.e. sets 4,5 and 7), the dead-time corrections had a size of 31 to 36 ms. For low beam intensity runs, (i.e. set 3) the dead-time correction changed the half-life by 6 to 8 ms. The values shown in this chapter are those with the dead-time correction.

Once the decay spectra were put in coincidence and stacked up, it was fit with equation

$$f(t) = a \exp(-t * \ln 2 / T_{\frac{1}{2}}) \quad (6.2)$$

where a and $T_{\frac{1}{2}}$ are free parameters. a is the initial rate and $T_{\frac{1}{2}}$ the half-life. The decay curves were fit from 1.5 seconds past the beam on time to 1.5 second from the end of the decay time. The fitting method used was the log likelihood method. The 60 second decay run up detector result is shown in Figure 6.10. From this run, it is seen that the spectra does not decay back down to the background. The lack of background parameter in equation 6.2 comes from this observation.

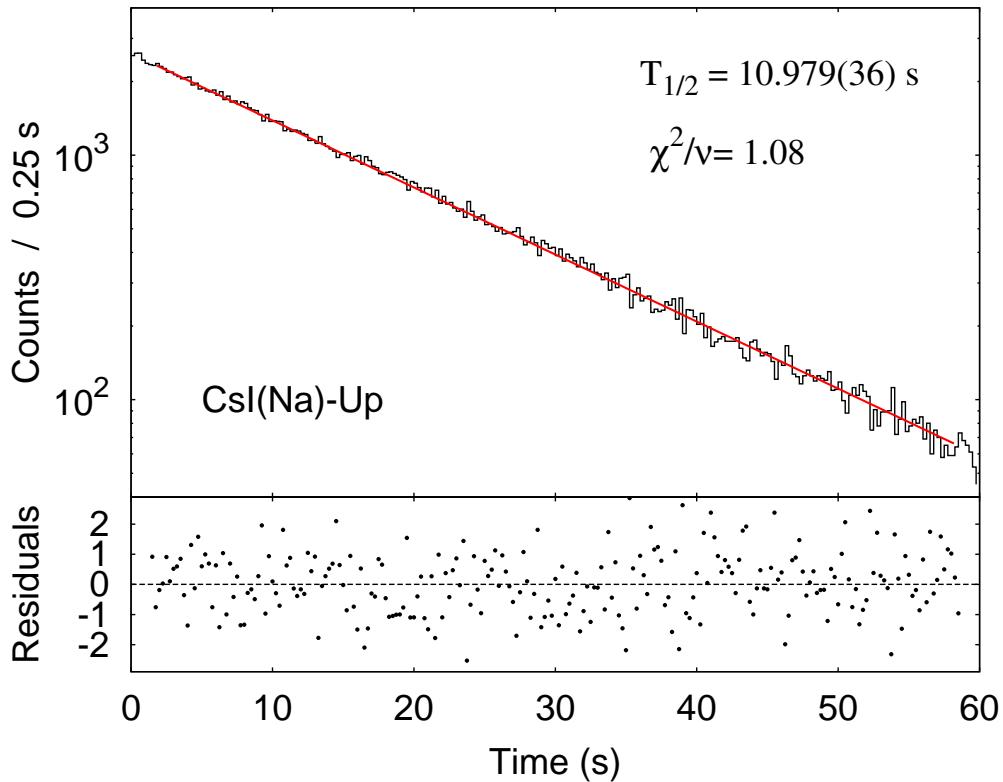


Figure 6.10: The decay spectrum from the up gamma detector is shown on the top graph. The red line is the exponential fit. The bottom graph shows the residuals from the fit.

The decay spectra were built run by run, and the resulting fitting results were averaged together. Runs with a p-value less than 0.05 were considered statistically insignificant and thrown out. After all the significant half-lives were collected, the average of them all was taken.

6.3 Systematic Effects

Several systematic effects were looked at. The dead time correction was applied before any other systematics were investigated.

6.3.1 Dead Time

The timing resolution of the clock is 8 ns. Due to this, there is an uncertainty on the dead times of at least 8 ns. The dead times were varied ± 4 ns and the half lives calculated. Half the difference of those half lives is the systematic uncertainty.

6.3.2 Pile Up Effects

The dead time is over-corrected. Due to pile up, some of the pile up events are not totally lost. Some of the events thought to be missing just got shuffled around. This is a problem due to the fact that energy gates are imposed. The pile-up events also have a different time structure than the regular events. Due to the fact that the pile-up goes as the singles rate squared, the half-life of the pile-up events is half that of the non-piled-up events. This creates a background with a different time signature, and causes a change in half-life.

The 48 ns time cut around the peak, shown in Figure 6.7, was compared to several other, larger time cuts. The narrow time cut still have some uncorrelated background and pile-up

events in them.

To account for this effect, several other time cuts were taken. These cuts were plotted vs half-life. This graph was fit with a quadratic function. This function was extrapolated to zero, which was the correction due to the pile-up. This graph is shown in Figure 6.11.

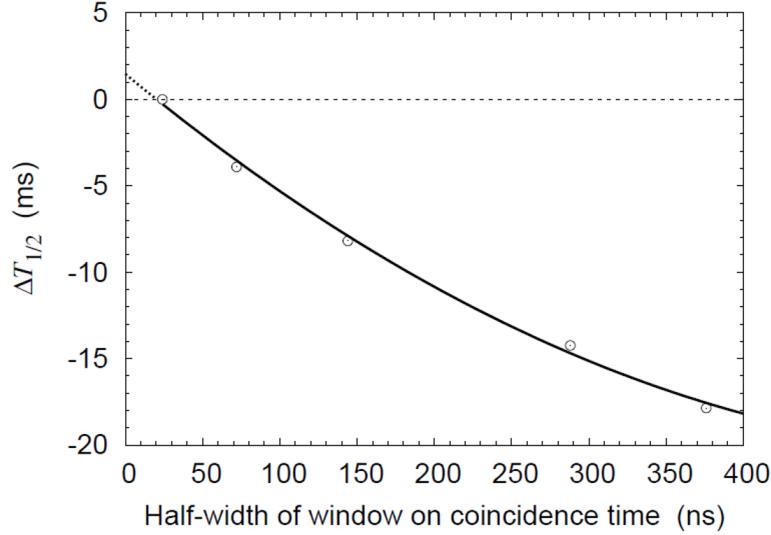


Figure 6.11: Time difference vs the resulting half-life. The line is a quadratic fit which was extrapolated to zero.

The extrapolation line is shown. The half-life was corrected to the zero value of the window. The difference between this extrapolated value and the previously measured value was taken as a correction and as an error bar.

6.3.3 Background

The first systematic effect is the effect of background. Due to the low decay time, directly fitting a background is impossible. There is no background region for the fitting function to anchor to, which induces a large correlation between the background and the half life. Several techniques were used to estimate the background.

6.3.3.1 Simultaneous vs Seperate Fitting

The first attempt was by simultaneously fitting each run with a different fitting function.

The equation used was equation 6.3.

$$f(t) = a(\exp -t * \ln 2 / T_{\frac{1}{2}} + b) \quad (6.3)$$

with a and $T_{\frac{1}{2}}$ the same as in equation 6.2 and b the relative background level. The half-life of the four detectors was set to be a common parameter. The relative background level and initial rate, however, were assumed to be independent for each spectrum. The resulting half life was compared to the value found with fitting each detector seperately without a background.

The effect of adding a background was investigated using Monte Carlo. Exponential functions were generated and an amount of background added. The resulting function was fit with a decay curve without a background parameter. The amount of background added was varied, and the resulting half lives plotted. It was found that increasing the background decreased the value of the half life, and that the background level and the half life value were strongly correlated.

A similar Monte Carlo was written to check the simultaneous fit method. Four decay curves were fitting and simultaneously fitted the same way was the data. They were also fitted separately with only an exponential decay. The background was varied and the difference between the two values was taken. The method shows a trend similar to the one seen in the previous Monte Carlo.

In the data, it was discovered that the results of the simultaneous vs separate fitting depended on the size of the dead time correction. If the dead time was over-corrected, it

induced an effect that was similar to having a larger background. If more dead time was imposed, the effect was as if there was a negative background. A dead time correction was added to the Monte Carlo, and a similar trend was seen. As long as the dead time is known exactly, the background can be extracted with this technique. However, as it is somewhat uncertain of what the exact dead time should be, this technique cannot be used to determine the background.

6.3.3.2 Spectra Arguments

The other way to try and gauge the background size is to look at the spectra. Looking at Figure 6.7, it can be seen that on the left side of the large peak, there are very few counts. It can also be seen that the prompt peak in the center contains most of the counts, while there is a long tail on the right side of the peak. This tail is due to pile up. An event in the beta window piles up with another event later in time. The second event is read by a gamma detector, but is correlated with the first event, causing the large time difference. The time spectrum changes if the beta spectrum is cut in different ways.

In the gamma beta spectrum, it can be seen that there is no background events aside from the 511 region. This is due to the presence of ^{10}C and ^{11}C . When the detectors are put into triple and quadruple coincidence, the gamma rays of those isotopes appear. There are no gamma rays in the 1620 keV window which was filtered on.. The only coincidence possible is if there is pile up into that window along with a beta event. The estimate of those events is shown on the left side of the peak in the time difference figure shown in Fig. 6.7 These events are accounted for when extrapolating the different time difference cuts, as shown in Figure 6.11

6.3.4 Cut Sensitivity

For each pair of detectors, there were four conditions: two for each the implant and gamma detectors. For the gamma cuts, the edges of the gates were varied ± 5 keV in each direction for each cut. The results is insensitive to the upper beta cut. The lower beta cut was scanned with 6 different values going evenly from the initial lower beta cut to the peak of the spectrum. Moving the lower beta cut also effects the dead time correction. In order to disentangle the two, the lower beta cut was varied with two different time difference conditions. The location where the difference between the two calculations blows up is where the effect of the lower beta cut starts being swamped by the effect of the pile up. This is limit of where the lower beta cut was scanned. All four of these conditions were varied independently, and the procedure of generation the spectrum and fitting the decay curves was done. Half the resulting range of half-life values was taken to be a systematic uncertainty.

The fitting range of the decay spectra was varied. The start of the fit was varied bin by bin up to 6.5 seconds into the decay spectrum. The end of the fit was varied the other way to cut out the end of the decay spectrum. Since there was no noticeable systematic effect, there was no increase in error associated with this effect.

6.3.5 Oscillator Stability

The oscillator of the PIXE board has a stability of $\pm 5 * 10^{-5}$. All times in the analysis were stretched by this value, and the half life calculated. Have the difference between the stretched value and the original value is another systematic error.

6.3.6 Binning and Fitting

In order to check the sensitivity of the result to binning, the decay curves were rebinned by a factor of two. Half the difference between the rebinned half life and the original half life is considered the correction and the uncertainty.

For the fitting method, log-likelihood estimators were used to fit the summed data. This was done with two different packages which gave identical results. This was compared to analytic results, which gave the same results, so the half life is insensitive to the fitting method.

6.4 Result and discussion

The PVT runs are shown in Figure 6.12

The results for the PVT runs are shown in table 6.2 for the PVT runs.

Table 6.2: The PVT runs

| Detector | Half-Life | Error |
|----------|-----------|--------|
| Up | 11.0195 | 0.0088 |
| Left | 10.9944 | 0.0087 |
| Down | 10.9980 | 0.0085 |
| Right | 10.9987 | 0.0095 |
| Mean | 10.9999 | 0.0044 |

The size of the systematic errors investigated are shown in table 6.3

After the dead time correction, the value of the half-life from the CsI(Na) implant detector runs was found to be 11.0011 ± 0.0069 (stat) ± 0.0030 (syst) s.

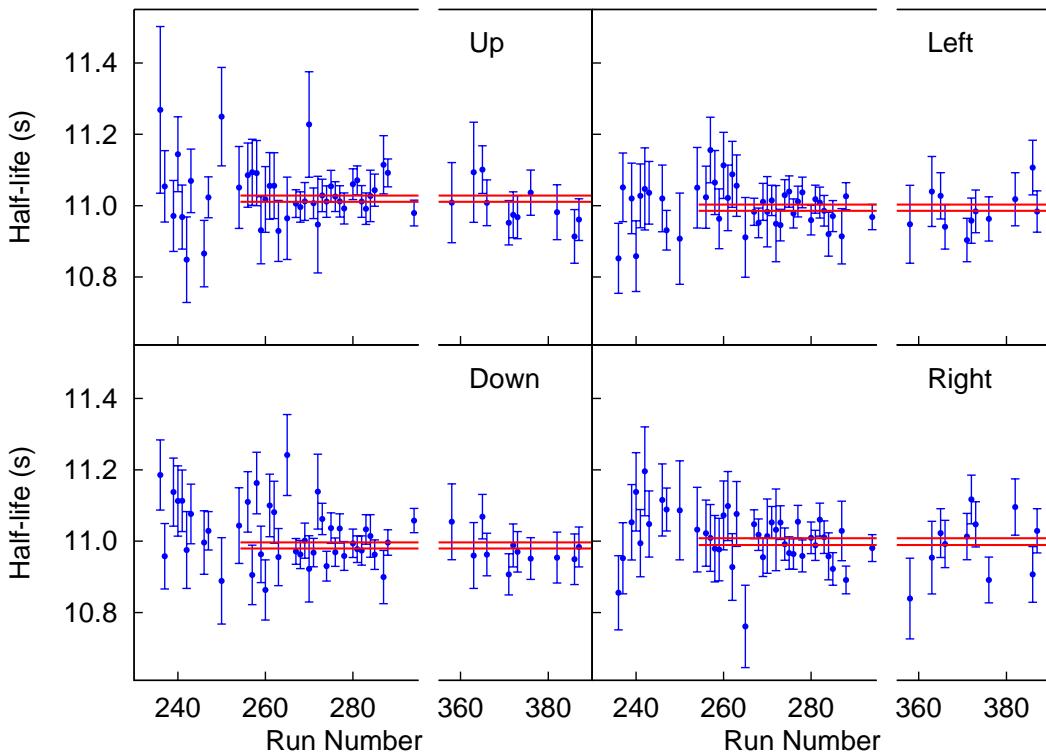


Figure 6.12: The red lines show the results of the fits over the runs that were used. The additional half-lives shown are excluded to reasons discussed previously.

Table 6.3: Systematics

| Source | Correction [ms] | Uncertainty [ms] |
|----------------------|-----------------|------------------|
| Dead-time | 0.00 | 0.24 |
| Oscillator stability | 0.00 | 0.80 |
| Lower PVT cut | 0.00 | 2.32 |
| Lower gamma cut | 0.00 | 0.15 |
| Upper gamma cut | 0.00 | 0.05 |
| Uncorrelated events | 1.47 | 1.47 |
| Binning | -0.30 | 0.30 |
| Total systematic | 1.17 | 2.89 |

6.5 Conclusion

The half-life measured is most consistent with some previous measurements of a half-life of about 11 s. This can be seen in Figure 6.13. This measure disagrees with the most recent

measurements.

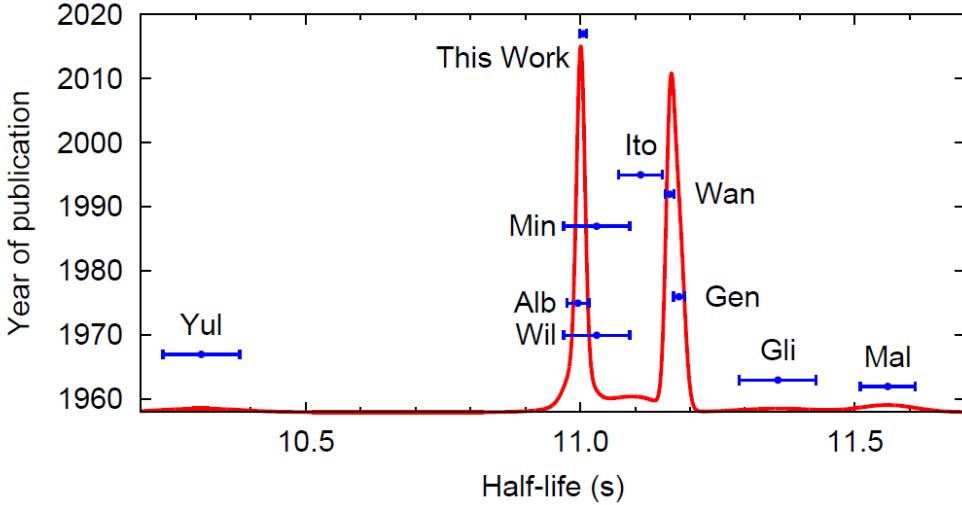


Figure 6.13: A scatter plot of (a) previous values with this work added. The labels correspond to: Mal [18], Gli [11], Yul [31], Wil [27], Alb [2], Gen [10], Min [20], Wan [25] and Ito [15].

Several things about the data set were discovered. It was learned that there were contaminates coming from the fragmentation of the ^{12}C in the plastic scintillator. The beta decaying products could be a cause of why the beta spectrum for the PVT detector looks so odd. It was also discovered that the rate dependent gain effect in the CsI(Na) implant detector is significant. Before doing this measurement, it was assumed that the low rates would make that effect negligible. It was learned that after the coincidence, the amount of background left in the spectrum is negligible, and that we have no contaminates in the beam.

Chapter 7

GEANT4 Monte Carlo

After the half-life measurement was completed, the next step was to use the shape of the spectrum to deduce Fierz term. In order to get a measurement of the Fierz term, the spectrum shape needed to be carefully described. In addition to all the theoretical corrections, the effect of bremsstrahlung and the efficiency of the detectors needed to be accounted for. The way this was done was with a GEANT4 simulation [1]. The most updated copy of the code can be found at <https://github.com/maximilian29631/Geant4for20F/tree/RealDeadLayer>.

7.1 GEANT4 Monte Carlo

The corrected beta decay spectrum was fed as input to a Monte Carlo. The program used to model the detectors was GEANT4. In order to use the program, a model of the detector set-up and the initial energies of the primary particles need to be introduced.

7.1.1 Detector Geometry

A source of the detector geometry were the technical drawings of detectors. A drawing of the CsI(Na) implant detector is shown in figure 7.1

The geometry of the detector set-up was programmed into the simulation. The implant detector was modeled as a square prism of CsI. The rectangular prism was 9.76 cm deep with

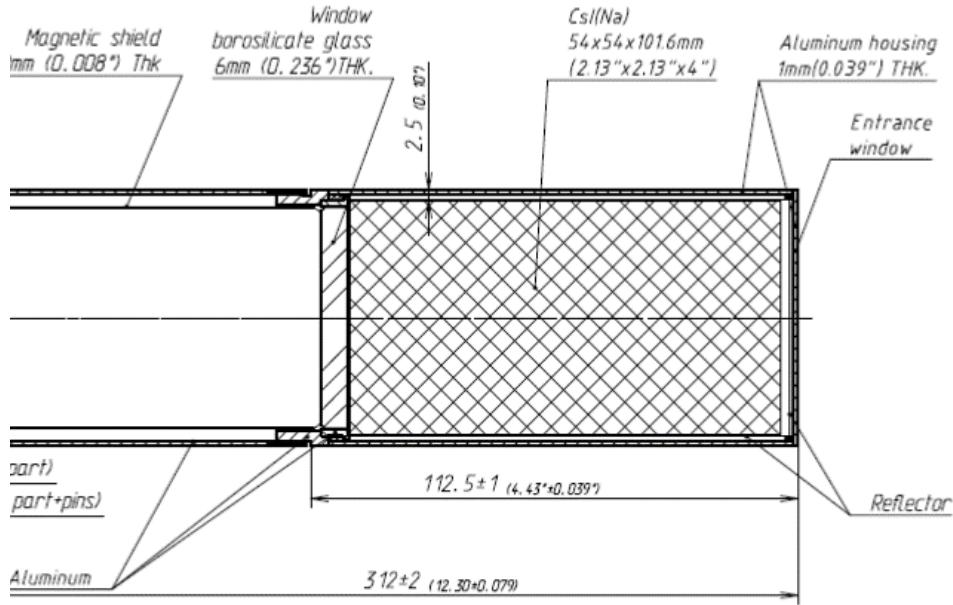


Figure 7.1: A technical drawing of the CsI(Na) implant detector

a 5 cm square base. The front edge implant detector was put at the center of the simulation.

The aluminum sheath and MgO layer was not simulated for the implant detector.

The four large gamma detectors also square prisms. The active volume was 79.5 by 79.5 by 76.2 mm. It was also made of CsI. There was a 2 mm dead layer of vacuum around the detector. Above this dead layer, a 1.5 mm layer of MgO was added. On top of this, the can of aluminum, 1 mm thick, was added into the simulation.

The four large gamma detectors were arranged into a square around the implant detector. Each square base of the gamma detectors was centered one inch upstream from the face of the implant detector. This modeled how the implant detector was recessed in the experiment.

A visualization of the CsI crystals in GEANT4 is shown in figure 7.2

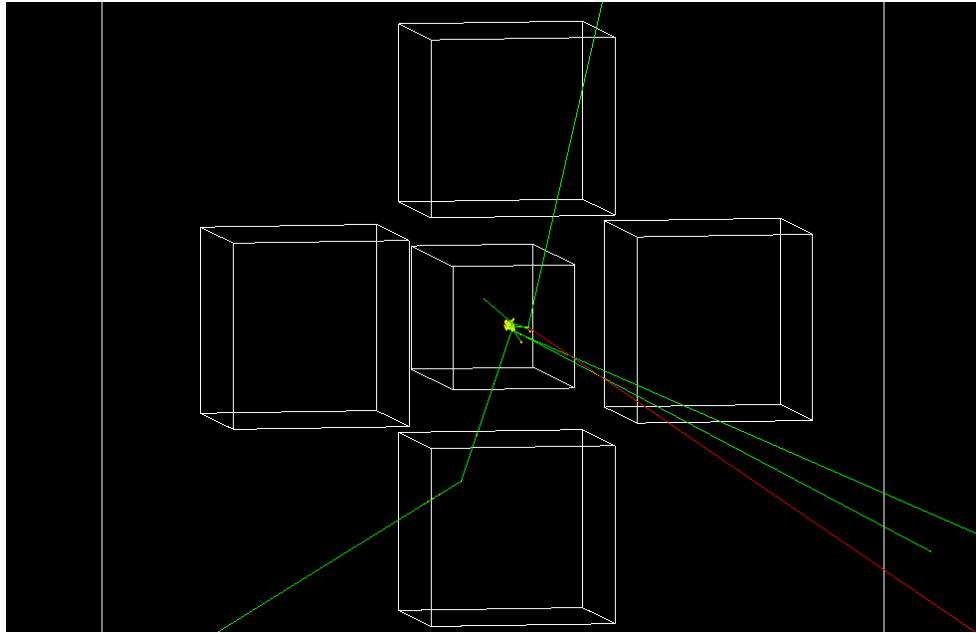


Figure 7.2: The detector geometry inside GEANT4

7.1.2 Source Definition

The next step was to define a region inside the implant detector. This region was where the gamma and beta particles originated from. The depth of the region was calculated using LISE++, a ion optics code. The vertical and horizontal size of the region was calculated by using the PPAC measurement and an ion optics simulation. This size was 0.4 mm deep, 3.5 mm wide, and 3.6 mm tall. The source was implanted 1.156 cm into the detector.

7.1.3 Primary Particle Definitions

There were three primary particles generated. Two were photons and one was an electron. All three particles had an isotropic angular distribution, and would propagate in different directions.

The first particle was an electron. This selected the point in the source region. In order to generate the correct energy for this electron, the following process was used. First, all

the corrections described in chapter 3 were multiplied with equation 3.5. This resulting function was evaluated at 1024 evenly space points from 0 keV to the end point energy. This list of 1024 points was fed into GEANT4 as a histogram, as GEANT4 can only take a histogram of up to 1024 bins. Linear interpolation was used to make this histogram back into a smooth function. This is not exactly a histogram of the beta energy spectrum. The original function was fit to the generated beta energies, and no distortions were generated using this procedure.

The next photon was the 1.6336 MeV photon from the ^{20}F decay. This initial photon is monochromatic and isotropic.

The last photon was to account for the inner bremsstrahlung. The radiative correction used to generate the electron energy was the formula that assumes all real photon energy is absorbed (equation 3.13). After the electron energy is generated, the formula describing the energy spectrum of the inner bremsstrahlung photons is generated. This spectrum is written out in equation 3.14. Further discussion of this formula is found in the theory chapter. A cutoff of 50 keV is imposed to the formula, as it has a singularity at zero photon energy. In addition, with this geometry, all photon energies below 100 keV are absorbed. Then, the formula is numerical integrated from 50 keV to the electron energy over 1000 steps using the trapezoidal rule. This is the total probability that an electron emits a KUB photon. This number is compared to a random number from 0 to 1. If the random number is below the integral, the inner bremsstrahlung energy spectrum is sampled. The algorithm used for this sampling is the van Neumann method [23]. The sampled energy is given to the third primary particle. If the random number is more than the integral, the third primary particle is given an energy of 0 keV. The energy of the electron is reduced accordingly.

The two photons had their initial points moved to match that of the electrons. All three

particles were then free to propagate through the detectors.

7.2 Particle Propagation

GEANT4 propagates the particles in steps. During or after each step, different physics processes are carried out. The physics process may create secondary particles. If these secondary particles cannot make it the length of the range cut, they will not be created. These cuts can be set differently for different particles. For this experiment, the range cut corresponds to about 15 keV in aluminum. These steps happen until the primary particle runs out of energy.

7.3 MC Output

The particles were tracked and the energy deposited in each detector summed up. The energies deposited into the implant detector was summed up into two categories. The energy deposited from the initial gamma ray was one category. The other was the energy deposited from the initial electron. After the energies of the particles reached a certain threshold, the simulation of one decay was finished. All the energies deposited into each of the detectors was summed up and saved as an event in a ROOT tree. Then, the process was repeated. A new location inside the region was generated and another decay generated.

In order to get to get the necessary statistics, $2 * 10^9$ events had to be generated. This initially took 7 days to run. In order to decrease the time it took to run, the range cuts on the gamma rays were changed. The range cuts were changed from $5 \mu\text{m}$ to 5 mm for all gamma rays. The range cuts for other particles stayed at $5 \mu\text{m}$.

7.4 Simulation Development

The GEANT4 simulation is based on the example TestEm5. The first changes were to add the proper detector geometry, as shown above. The next changes were to add a second primary particle, which was the gamma ray from the decay curve. The energies absorbed in all of the detectors was also added.

Initially, all energy absorbed by the implant was recorded, regardless of its origin. This was found not to be the correct way to fit the data. To counteract that, the class G4VUserTrackInformation was implemented. This gave each track the information about the primary particle. To split the energies from different detectors, the initial energy and charge of each primary particle was checked. Since the gamma rays are mono-chromatic, the energy of the primary particle was compared to 1.6336 MeV. If the primary particle had charge or it was a photon without an initial energy of 1.6336 MeV, it was put in the category of energy from the initial electron. This took care of most cases, unless a sampled inner bremsstrahlung photon had exactly that energy, which was rare enough to be negligible.

The radiative correction used was changed. Initially, it was assumed that all the real photons generated by the radiative correction would be absorbed. It was also assumed that the higher energy inner bremsstrahlung would not come in large enough numbers to have an appreciable effect. This would make the radiative correction in equation 3.13 adequate. However, after explicitly generating the inner bremsstrahlung photons, this was found not to be true. Therefore, the entire simulation had to be rerun with the inner bremsstrahlung photons generated explicitly.

Chapter 8

Fitting Beta Spectrum

The output of the GEANT4 was used to fit the data spectra. First, however, it had to be processed.

8.1 Simulation Results Processing

After the GEANT4 simulation was done, the output file had to be processed further. Much like the experimental data, the simulated data had to be filtered. This was done using the TTrees from the output files of the GEANT4 simulation. The energy absorbed in the implant detector was filtered by the energy absorbed in the outer four gamma detectors in the simulation.

The two different categories of energy absorbed in the implant detector were built into two histograms. One histogram had a condition that the energy absorbed by the initial gamma ray had to be zero. This histogram was the energy absorbed without any summing. The second histogram was the energy absorbed where there was a contribution from the gamma ray. This histogram was known as the energy absorbed with summing. These two histograms can be seen in figure 8.1

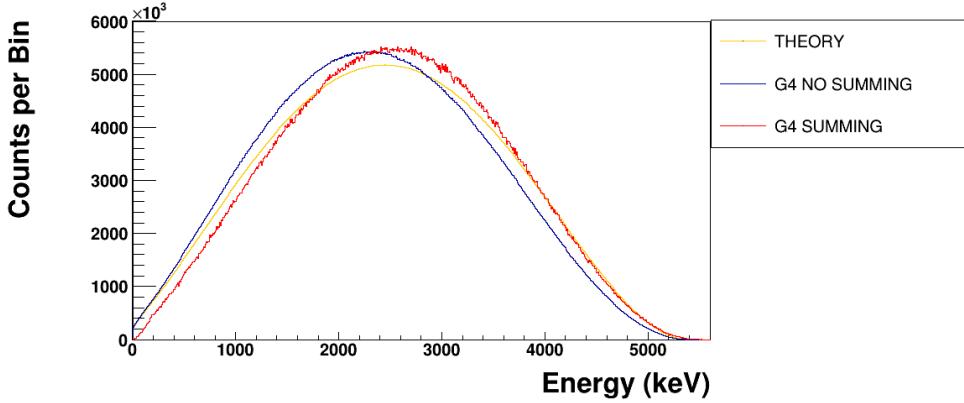


Figure 8.1: The shapes of the different histograms from the output of the GEANT4 simulation. The input beta spectrum is also plotted. The histograms are put to the same scale.

8.1.0.1 Detector Resolution

The next step was the apply the detector resolution to this histogram. This was done by applying a convolution function to the histograms built from the GEANT4 output files. The convolution function was

$$\sigma = A\sqrt{E} \quad (8.1)$$

where σ was the energy resolution, E the energy, and A a constant found through a calibration. This was done by looping through each of the histograms bin by bin and reading the number of counts in each bin. For each bin a Gaussian function was built. The centroid of the Gaussian was the center of each bin in keV. The σ of the Gaussian was calculated by using equation 8.1. This Gaussian function was sampled as many times as there were counts in the bin. These samples were filled into a new histogram. This was repeated bin by bin until all bins were distributed.

8.1.0.2 Determining Detector Resolution

In order to properly fit the energy spectrum, a calibration of the CsI(Na) detector had to be done. The calibration was used to find what the detector resolution was. Several different energy lines were used to find the calibration and the energy resolution function. The lines were the 1.173228 MeV and 1.332492 MeV gammas from a ^{60}Co source, the 0.661657 MeV gamma ray from a ^{137}Cs source, and the 0.511 MeV and 1.274527 MeV gamma rays from a ^{22}Na source. These gamma rays were fitting with a Gaussian and a background. The background varied from a linear background, a quadratic background, and an error function background. For the ^{60}Co , both peaks were fit at once. These different background gave slightly different results for the centroids and the widths of the Gaussian. The different widths and centroids were taken as a systematic error. From the centroids, the calibration for each detector was calculated and shown in equation 8.2.4

$$C = G * E + b \quad (8.2)$$

where C is the location of the peak in ADC channels, G the gain in channels/keV, and b the offset in channels. This calibration curve was only used for the resolution determination. The widths of the peaks were calibrated with the gain and plotted vs energy. Then, equation 8.1 was fit to the results in order to determine A . The value of A used for this procedure was 1.118.

8.1.0.3 Pile-up Modeling

After the convolution, the simulation data was sent through a simulation to model pile-up. The model used for the CsI(Na) signals was a linear rise and then an exponential decay.

The linear part went from 0 to 1 over 100 ns. The exponential piece started at 100 ns at 1 and decayed with a τ of 760 ns. This analytic equation was scaled up or down to whatever energy was sampled. It was then fed into a model of trapezoidal filter of PIXIE. The math was the same as described in the chapter on data acquisition.

This model was tuned on calibration data. A run was taken of ^{137}Cs at 25000 counts per second. A 2000 counts per second ^{137}Cs run was used as a background and subtracted off. Then, samples of the background-subtracted spectrum were taken up to the end of the 661 keV peak. Monte Carlo methods were used to model the time difference between two samples. If the two samples fell within the pile-up window, then the piled-up signal models were fed into the trapezoidal filter. The calculated pile-up energy was saved to a histogram. If the two samples did not fall within the pile-up window, then they were not fed into the filter model and just filled into the histogram. The parameters were adjusted until the generated pile-up matched the measured pile-up in the spectrum. The results of the tuning is seen in figure 8.2

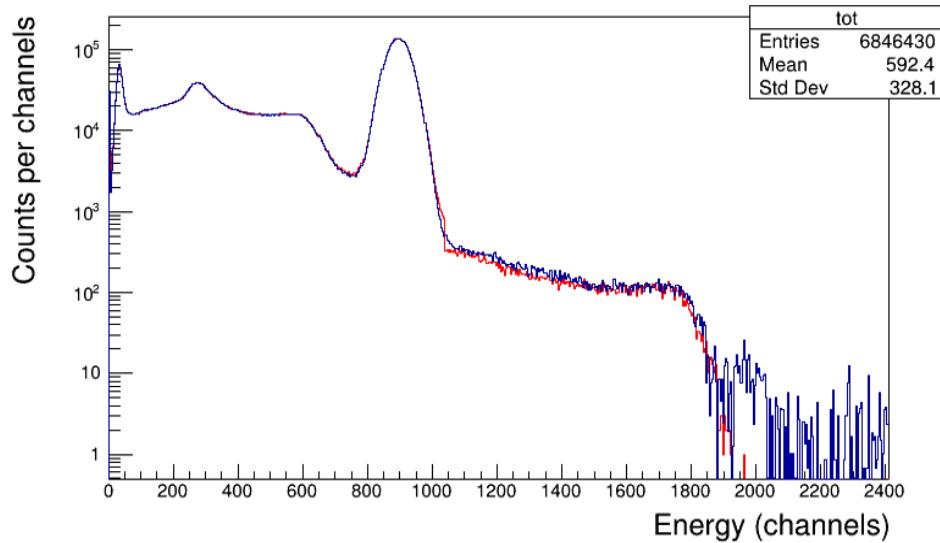


Figure 8.2: The tuning of the pile-up. The input spectrum is in blue. It was sampled up to 1000 channels. The generated spectrum is in red.

8.2 Fitting Procedure

The simulation described above were only part of what was needed. Other simulations included in the fit had the phase space times corrections times or divided an additional factor of the total energy of the electron.:wq: The simulations were all convoluted and filtered as described above.

8.2.1 Fit Method Characterization

To characterize the fitting method, two GEANT4 Monte Carlos were generated. One had had the nuclear shape factor with the nominal value of b_{wm} . The other had no shape factor, much like the fitting function. After applying the gamma filtering to both simulations, the simulation results without the shape factor were used to fit the simulation results with the shape factor. The gain in these fits was left as a free parameter, and the offset was fixed to a value of 0. The spectrum with the shape factor became the pseudo-data spectrum. To manually check the statistical uncertainty, the pseudo-data spectrum was fluctuated. Each bin had its content and error read. That bin error and content was used to build a Gaussian random number distribution. This random number distribution was sampled, and a new bin center created. After doing this to the entire spectrum, the new spectrum was fit. The resulting b_{wm} was recorded. Then, b_{wm} was set to 43.3, and the Fierz term fit. These fitted terms were saved to a histogram. This was done 1000 times to get a spread of values. From this, it was discovered that spline interpolation was the best way to fit the spectra.

The same method was used to see if the fitting method induced a lower beta cut effect or not. 1000 spectra were generated by scrambling one spectrum over and over. These spectra were fit from a lower beta cut up to the end point minus 100 keV. The lower beta cut was

varied from 200 keV up to 2 MeV. From this it was found that this fitting method induced an effect above 1200 keV. This effect was very large in the measurement of b_{gt} .

8.2.2 Experimental Data Processing

The data was processes from the TTrees described in the previous section. The energy spectrum of the implant detector was put in coincidence with the 4 gamma detectors. The energy cuts of the gamma detectors were the same as in the life-time measurement. There was a time difference condition as well. For this measurement, the time difference between a beta event and a gamma event had to be between -300 and 24 ns. Then, a 2-D histogram was built, with energy on one axis and time since last beam on the other. Since afterglow causes an effect that looks like a gain shift, different time cuts of equal statistics were taken from this 2-D histogram. These time cuts were then fit. The gain was left as a free parameter to counteract this afterglow effect.

8.2.3 Fit Function

The fit function used was as follows. First, the x axis of the data was read. This number was in ADC units, so equation 8.2.4 was used to turn this number into energy in keV. For the fitting, the gain G was left as a free parameter, but the offset b was set from the calibration.

$$H(E) = A * (f(E)_{nosum} * S(E, b_{wm}) + f(E)_{summing}) + B * p(E) \quad (8.3)$$

where A is the normalization, B the level of pile-up, E the energy, b_{wm} the weak magnetism, $S(E, b_{wm})$ the shape factor, $f(E)_{nosum}$ the output of the GEANT4 simulation without any energy summing between the ga: Gamma and beta, and $f(E)_{summing}$ the output

of the GEANT4 simulation with energy summing. The free parameters here are A , B , and b_{wm} .

8.2.4 Determining Offset for Shape Fit

Initially, the offset used was the offset from the calibration in equation . The offset used was 10.05 ADC units. This calibration was determined using photons instead of electrons. Electrons generate 2% less light than photons [?] This means that the offset found from this fit is suspect to apply to our electron shape measurement.

When applying an offset of 10.05 in a fit of the data, it was found that the output varied greatly as a function of where the fit was started. This is seen in figure ??.

While investigating this effect, several different potential causes were investigated. The first is if the facator A in equation 8.1 used in to convolute the detector simulation was not the same as the actual detector resolution. To test that, a Monte Carlo simulation was written. The space space in equation 3.5 was multiplied by the shape factor in equation 3.30. This function was sampled 10^9 times twice to build two histograms. Both histograms had a detector resolution applied as described in section 8.1.0.1 One histogram was sampled a further 10^6 times 10 times to build a sample data set. The other convoluted histogram was used to fit the generated data set. The first histogram's A was fixed, while the second histogram's A was adjusted. When the sample data's A matched the A that were used, no dependence of b_{wm} on the start of the fit. When the A of the data sample and the A , the first thing that happened was that the b_{wm} changed. If the A differ by a factor of 2 or more, a shift in b_{wm} appears. However, A was determined to 10% (FIX) Having a wrong A cannot explain the effect seen in ??

The largest effect comes from having the wrong offset in the calibration. A similar Monte

Carlo was written where no convolution was applied. Sample histograms were generated directly from an analytic function instead of a histogram. These histograms were generated with an offset of 10 ADC units. Then, the fit function had a different offset applied to it. For example, fitting the histogram generated with an offset of 10, and fit with an offset of 20 gives an effect as seen in ???. This is on the same order of magnitude as the effect we see in the data in figure ??.

This effect can be exploited to determine the offset using only electron data. The size of the slope induced is linear compared to the offset. By adjusting the offset and noting the slope of the b_{wm} vs the lower beta cut and plotting against the offset, the location of zero slope can be calculated. This was done, and the result is seen in figure ??

Doing this procedure gives an offset of -5.11 ADC units.

8.2.5 Fit details

The fit was done run by run. First a prefit for each section was done to calibrate the energy. Then, two endpoints in keV were used for the fit. The fitting function with a fixed offset was fit using a maximum likelihood method. The resulting b_{wm} was recorded. For the Fierz term fit, the b_{wm} of ^{20}F decay (43.4) was applied to the shape factor. Then, the Fierz term was applied to the no summing spectrum and fit.

The offset used for the fit was -5.11 channels. The end points for the calibration pre-fit were 540 channels to 7000 channels. The calibrated end points were 800 keV to 7500 keV.

8.2.6 Systematic effects

Chapter 9

Conclusion

9.1 Discussion of Results

9.2 Results Compared to Other Measurements

9.3 Further Refinements to Technique

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