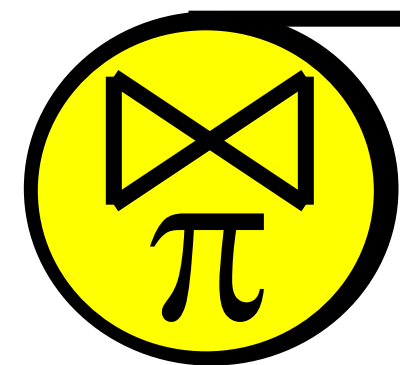




# Information Storage and Management I

Dr. Alejandro Arbelaez



Relational Algebra

# Find names of sailors who've reserved a red boat

$$\pi_{sname}((\sigma_{color='red'} Boats) \bowtie Reserves \bowtie Sailors)$$

Sid	Sname	Rating	Age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

Sid	Bid	Day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

Bid	Bname	Color
101	Interlake	Blue
102	Interlake	Red
103	Clipper	Green
104	Marine	Red

An Instance B1 of Boats

An Instance R2 of Reserves

# Find names of sailors who've reserved boat #103

Solution 1:

$$\pi_{sname}((\sigma_{bid=103} Reserves) \bowtie Sailors)$$

Solution 3:

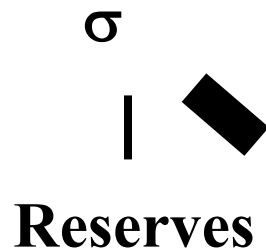
$$\pi_{sname}(\sigma_{bid=103}(Reserves \bowtie Sailors))$$

Which one to choose?  
and why?



Find names of sailors who've reserved boat #103

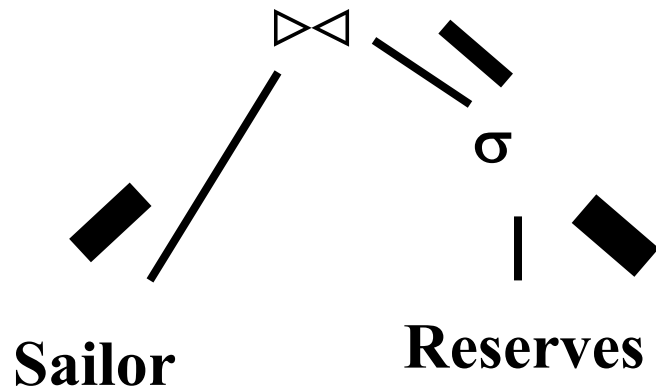
$\pi_{sname}((\sigma_{bid=103} \text{Reserves}) \bowtie \text{Sailors})$



Query  
Tree Plan

Find names of sailors who've reserved boat #103

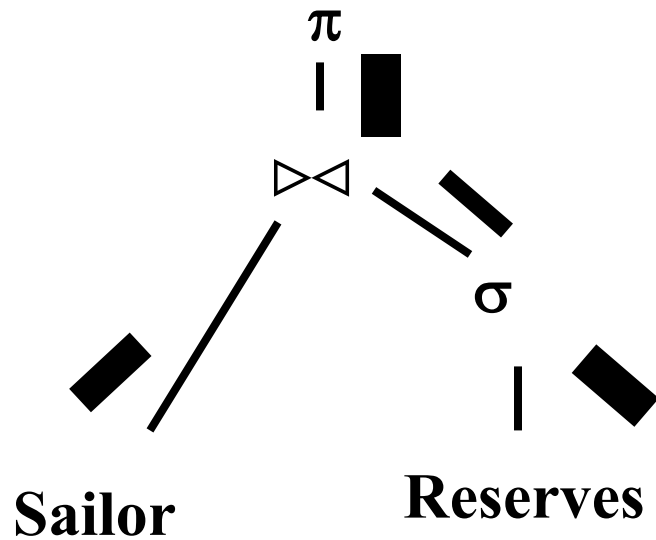
$\pi_{sname}((\sigma_{bid=103} Reserves) \bowtie Sailors)$



Query  
Tree Plan

Find names of sailors who've reserved boat #103

$\pi_{sname}((\sigma_{bid=103} Reserves) \bowtie Sailors)$

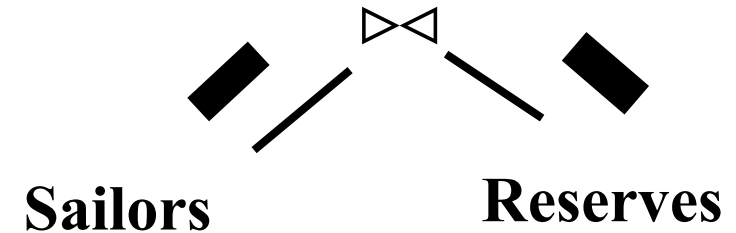


Query  
Tree Plan

Find names of sailors who've reserved boat #103

# Query Tree Plan

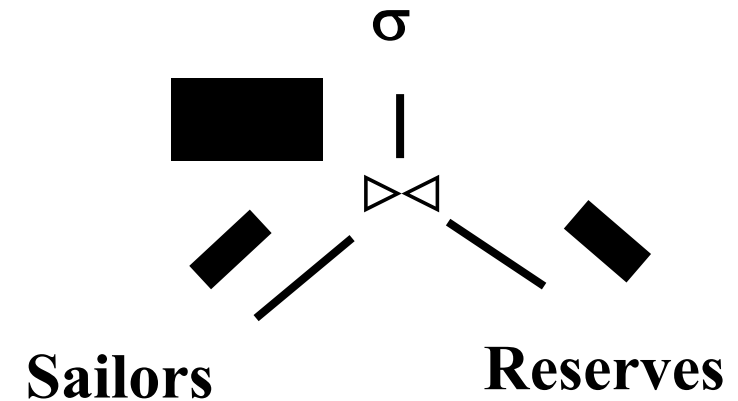
$\pi_{sname}(\sigma_{bid=103}(\text{Reserves} \bowtie \text{Sailors}))$



Find names of sailors who've reserved boat #103

## Query Tree Plan

$\pi_{sname}(\sigma_{bid=103}(Reserves \bowtie Sailors))$

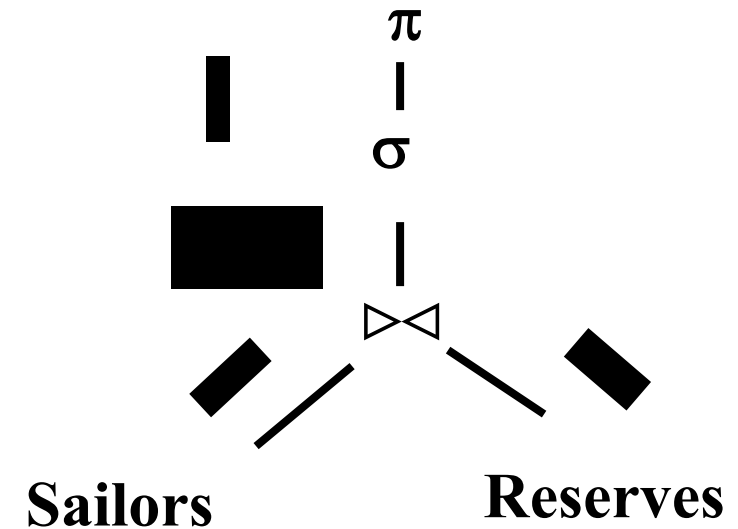




Find names of sailors who've reserved boat #103

## Query Tree Plan

$\pi_{sname}(\sigma_{bid=103}(Reserves \bowtie Sailors))$

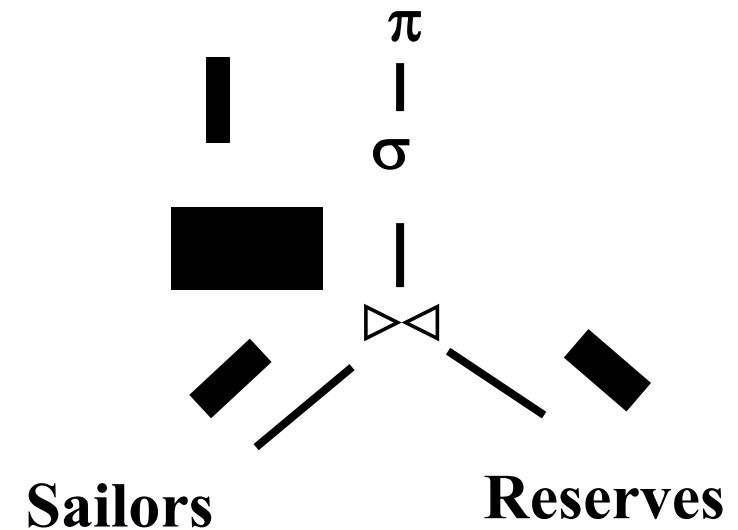
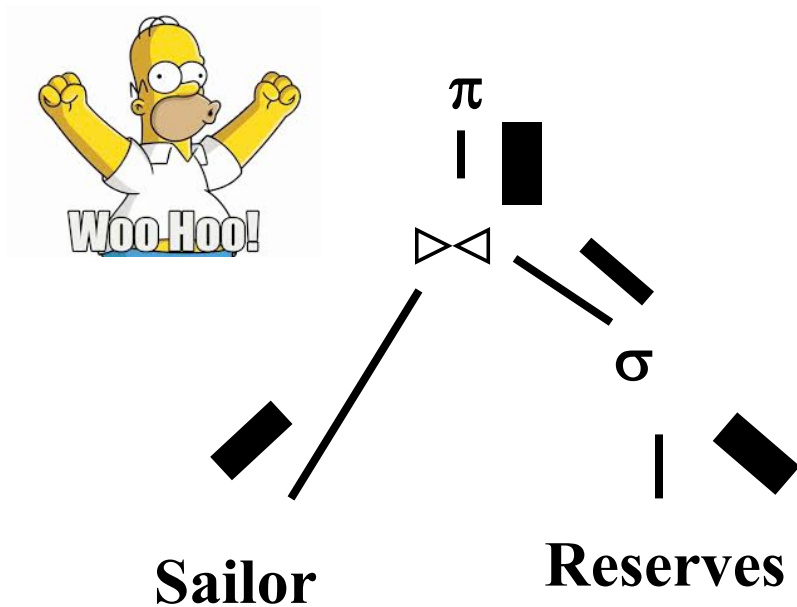


# Find names of sailors who've reserved boat #103

OBSERVATION: try to perform selections and projections early!

$$\pi_{sname}((\sigma_{bid=103} Reserves) \bowtie Sailors)$$

$$\pi_{sname}(\sigma_{bid=103}(Reserves \bowtie Sailors))$$



# Find names of sailors who've reserved a red boat

Information about boat color only available in Boats; so need an extra join:



Bid	Bname	Color
101	Interlake	Blue
102	Interlake	Red
103	Clipper	Green
104	Marine	Red

**An Instance B1 of Boats**

# Find names of sailors who've reserved a red boat

Information about boat color only available in Boats; so need an extra join:



Bid	Bname	Color
101	Interlake	Blue
102	Interlake	Red
103	Clipper	Green
104	Marine	Red

**An Instance B1 of Boats**

$$\sigma_{color='red'} Boats$$

# Find names of sailors who've reserved a red boat

Information about boat color only available in Boats; so need an extra join:

$$(\sigma_{color='red'} Boats) \bowtie Reserves$$

Sid	Bid	Day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

An Instance R2 of Reserves

Bid	Bname	Color
101	Interlake	Blue
102	Interlake	Red
103	Clipper	Green
104	Marine	Red

An Instance B1 of Boats

# Find names of sailors who've reserved a red boat

$$((\sigma_{color='red'} Boats) \bowtie Reserves \bowtie Sailors)$$

Sid	Sname	Rating	Age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

Sid	Bid	Day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

Bid	Bname	Color
101	Interlake	Blue
102	Interlake	Red
103	Clipper	Green
104	Marine	Red

An Instance B1 of Boats

An Instance R2 of Reserves

# Find names of sailors who've reserved a red boat

$$\pi_{sname}((\sigma_{color='red'} Boats) \bowtie Reserves \bowtie Sailors)$$

Sid	Sname	Rating	Age
22	Dustin	7	45.0
29	Brutus	1	33.0
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58	Rusty	10	35.0
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85	Art	3	25.5
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Sid	Bid	Day
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22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

Bid	Bname	Color
101	Interlake	Blue
102	Interlake	Red
103	Clipper	Green
104	Marine	Red

An Instance B1 of Boats

An Instance R2 of Reserves

# Find names of sailors who've reserved a red boat

Information about boat color only available in Boats; so need an extra join:

$$\pi_{sname}((\sigma_{color='red'} Boats) \bowtie Reserves \bowtie Sailors)$$

Alternative solution:

$$\pi_{sname}(\pi_{sid}((\pi_{bid} \sigma_{color='red'} Boats) \bowtie Res) \bowtie Sailors)$$



Find names of sailors who've reserved a red boat

$\pi_{sname}(\pi_{sid}((\pi_{bid} \sigma_{color='red'} Boats) \bowtie Res) \bowtie Sailors)$

Bid	Bname	Color
101	Interlake	Blue
102	Interlake	Red
103	Clipper	Green
104	Marine	Red

An Instance B1 of Boats

Find names of sailors who've reserved a red boat

$\pi_{sname}(\pi_{sid}((\pi_{bid} \sigma_{color='red'} Boats) \bowtie Res) \bowtie Sailors)$

Bid	Bname	Color
101	Interlake	Blue
102	Interlake	Red
103	Clipper	Green
104	Marine	Red

An Instance B1 of Boats

Sid	Bid	Day
22	101	10/10/98
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22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

An Instance R2 of Reserves

# Find names of sailors who've reserved a red boat

$\pi_{sname}(\pi_{sid}((\pi_{bid} \sigma_{color='red'} Boats) \bowtie Res) \bowtie Sailors)$

Bid	Bname	Color
101	Interlake	Blue
102	Interlake	Red
103	Clipper	Green
104	Marine	Red

An Instance B1 of Boats

Sid	Bid	Day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

An Instance B2 of Reserves

Sid	Sname	Rating	Age
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31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

# Find names of sailors who've reserved a red boat

Information about boat color only available in Boats; so need an extra join:

$$\pi_{sname}((\sigma_{color='red'} Boats) \bowtie Reserves \bowtie Sailors)$$

A more efficient solution:

$$\pi_{sname}(\pi_{sid}((\pi_{bid} \sigma_{color='red'} Boats) \bowtie Res) \bowtie Sailors)$$

*A query optimizer can find this given the first solution!*

# Find sailors who've reserved a red or a green boat

Can identify all red or green boats, then find sailors who've reserved one of these boats:

$$\rho (Tempboats, (\sigma_{color='red' \vee color='green'} Boats))$$

$$\pi_{sname}(Tempboats \bowtie Reserves \bowtie Sailors)$$

Can also define Tempboats using union! (How?)

What happens if  $\vee$  is replaced by  $\wedge$  in this query?





Find sailors who've reserved a red and a green boat

Previous approach won't work! Must identify sailors who've reserved red boats, sailors who've reserved green boats, then find the intersection (note that *sid* is a key for Sailors):

Find sailors who've reserved a red and a green boat

Previous approach won't work! Must identify sailors who've reserved red boats, sailors who've reserved green boats, then find the intersection (note that *sid* is a key for Sailors):

$$\rho \text{ (Tempred, } \pi_{sid}((\sigma_{color='red'} Boats) \bowtie Reserves))$$

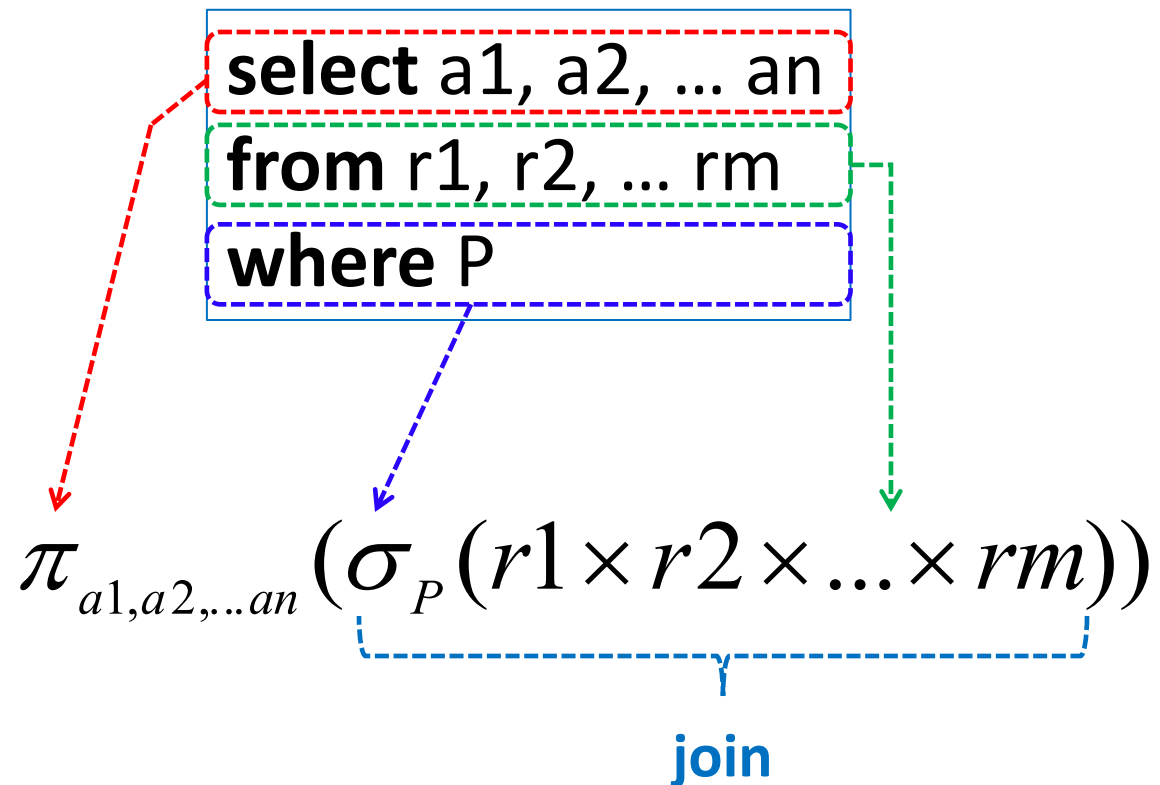
$$\rho \text{ (Tempgreen, } \pi_{sid}((\sigma_{color='green'} Boats) \bowtie Reserves))$$

$$\pi_{sname}((Tempred \cap Tempgreen) \bowtie Sailors)$$



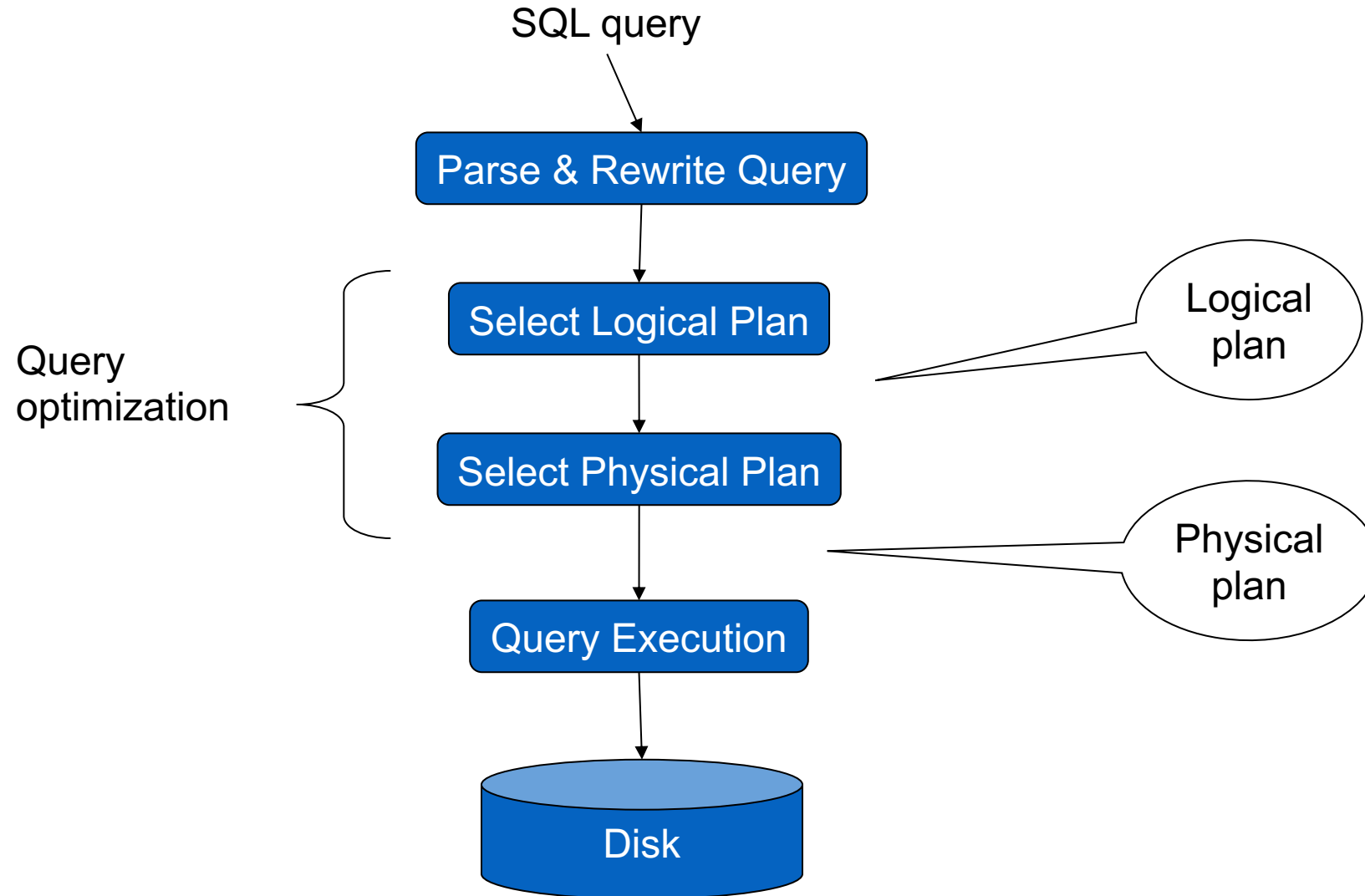
# Equivalence to Relational Algebra

- The basic form of an SQL query is as follows:





# Steps of the Query Processor



# Steps in Query Evaluation

- Step 0: Admission control
  - User connects to the db with username, password
  - User sends query in text format
- Step 1: Query parsing
  - Parses query into an internal format
  - Performs various checks using catalog
    - Correctness, authorization, integrity constraints
- Step 2: Query rewrite
  - View rewriting, flattening, etc.

# Rewritten Version of Our Query

- Original query:

```
SELECT sname  
FROM NearbySupp  
WHERE sno IN ( SELECT sno  
                FROM Supplies  
                WHERE pno = 2 )
```

- Rewritten query:

```
SELECT S.sname  
FROM Supplier S, Supplies U  
WHERE S.scity='Seattle' AND S.sstate='WA'  
AND S.sno = U.sno  
AND U.pno = 2;
```

# Continue with Query Evaluation

- Step 3: Query optimization
  - Find an efficient query plan for executing the query
- A query plan is
  - Logical query plan: an extended relational algebra tree
  - Physical query plan: with additional annotations at each node
    - Access method to use for each relation
    - Implementation to use for each relational operator

# Extended Algebra Operators

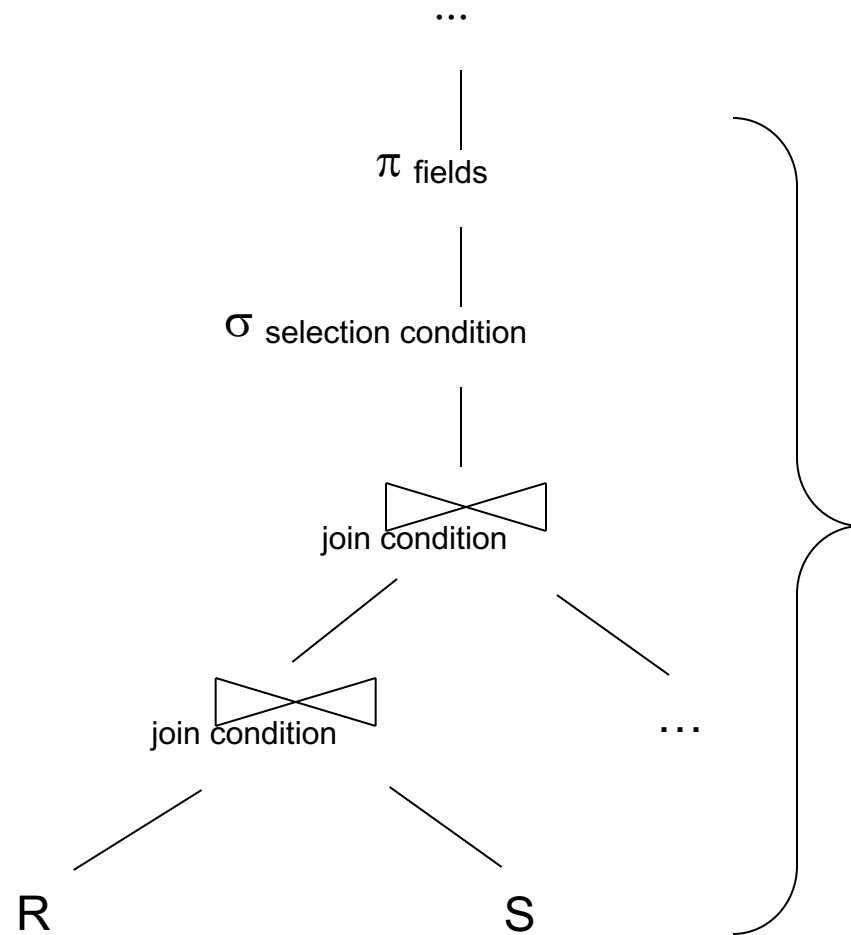
- Union  $\cup$ , intersection  $\cap$ , difference -
- Selection  $\sigma$
- Projection  $\pi$
- Join  $\bowtie$
- Duplicate elimination  $\rho$
- Grouping and aggregation  $g$
- Sorting  $\tau$
- Rename  $\rho$

# Query Block

- Most optimizers operate on individual query blocks
- A query block is an SQL query with no nesting
  - Exactly one
    - SELECT clause
    - FROM clause
  - At most one
    - WHERE clause
    - GROUP BY clause
    - HAVING clause

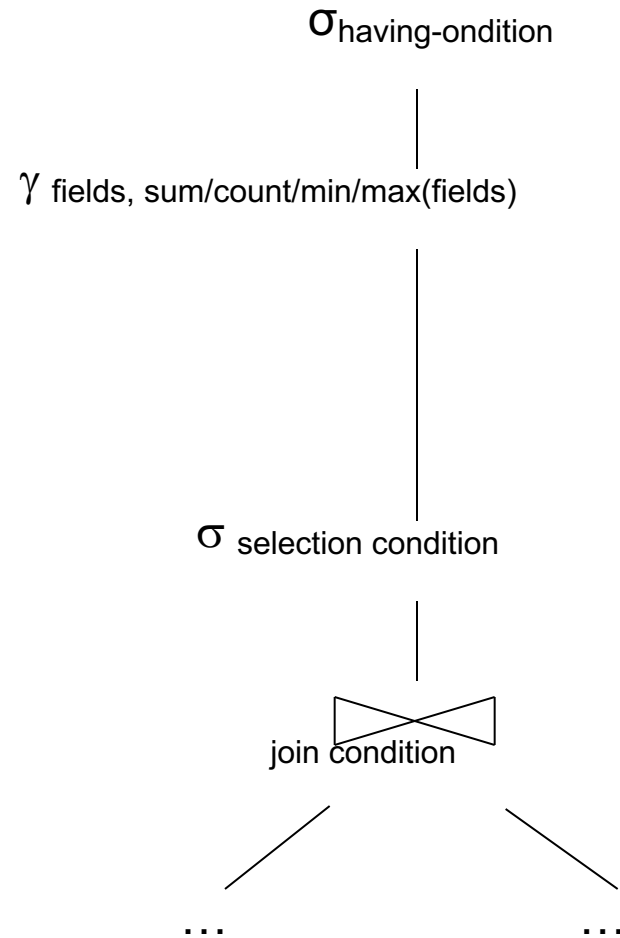


# Typical Plan for Block



SELECT-PROJECT-JOIN  
Query

# Typical Plan For Block



# Physical Query Plan

Supplier(sno,sname,scity,sstate)  
Part(pno,pname,psize,pcolor)  
Supply(sno,pno,price)

(On the fly)

$\pi_{\text{sname}}$

(On the fly)

$\sigma_{\text{sscity}='Seattle' \wedge \text{sstate}='WA' \wedge \text{pno}=2}$

(Nested loop)

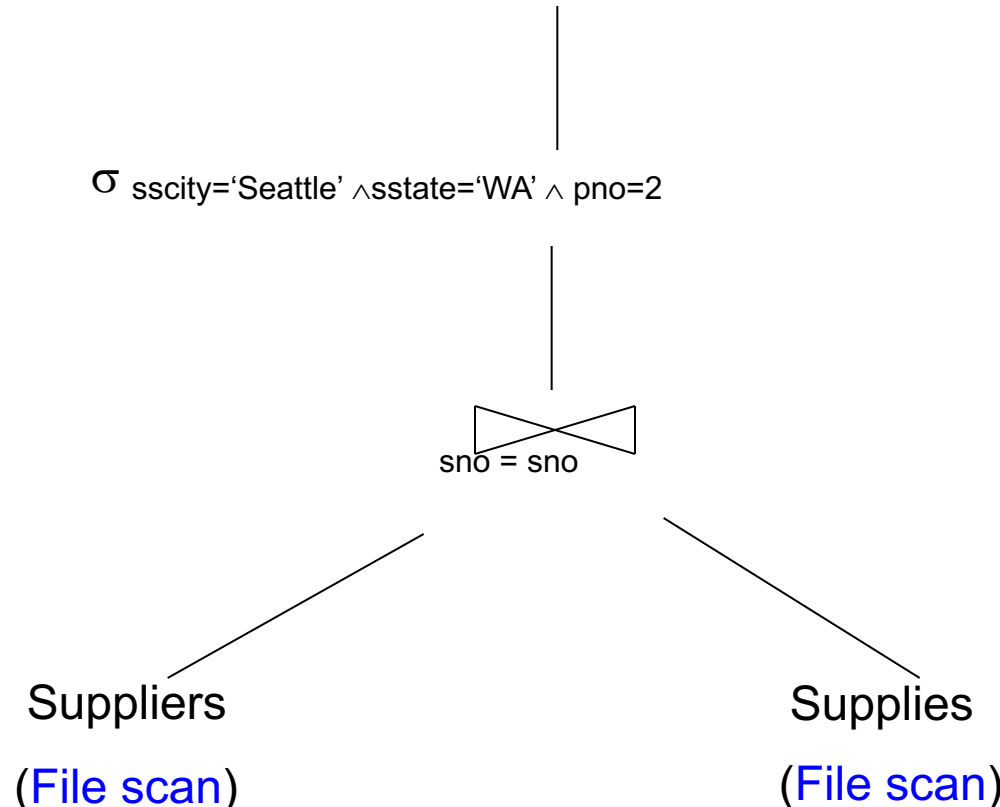
sno = sno

Suppliers

(File scan)

Supplies

(File scan)

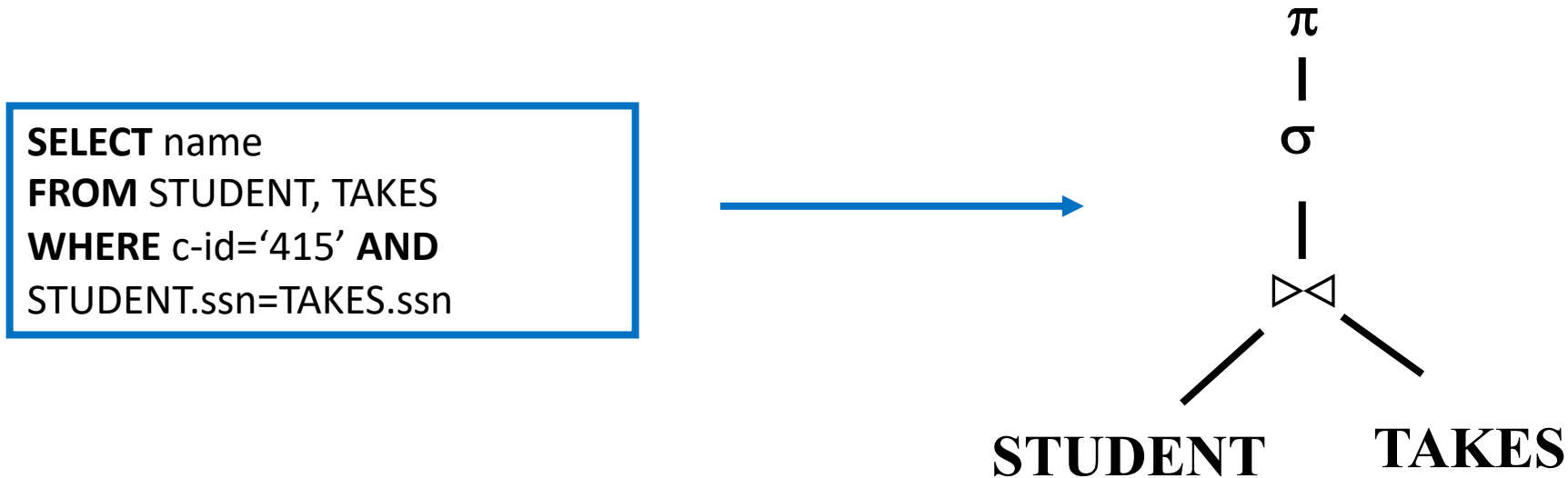


# Final Step in Query Processing

- Step 4: Query execution
  - How to synchronize operators?
  - How to pass data between operators?
- What techniques are possible?
  - One thread per query
  - Iterator interface
  - Pipelined execution
  - Intermediate result materialization

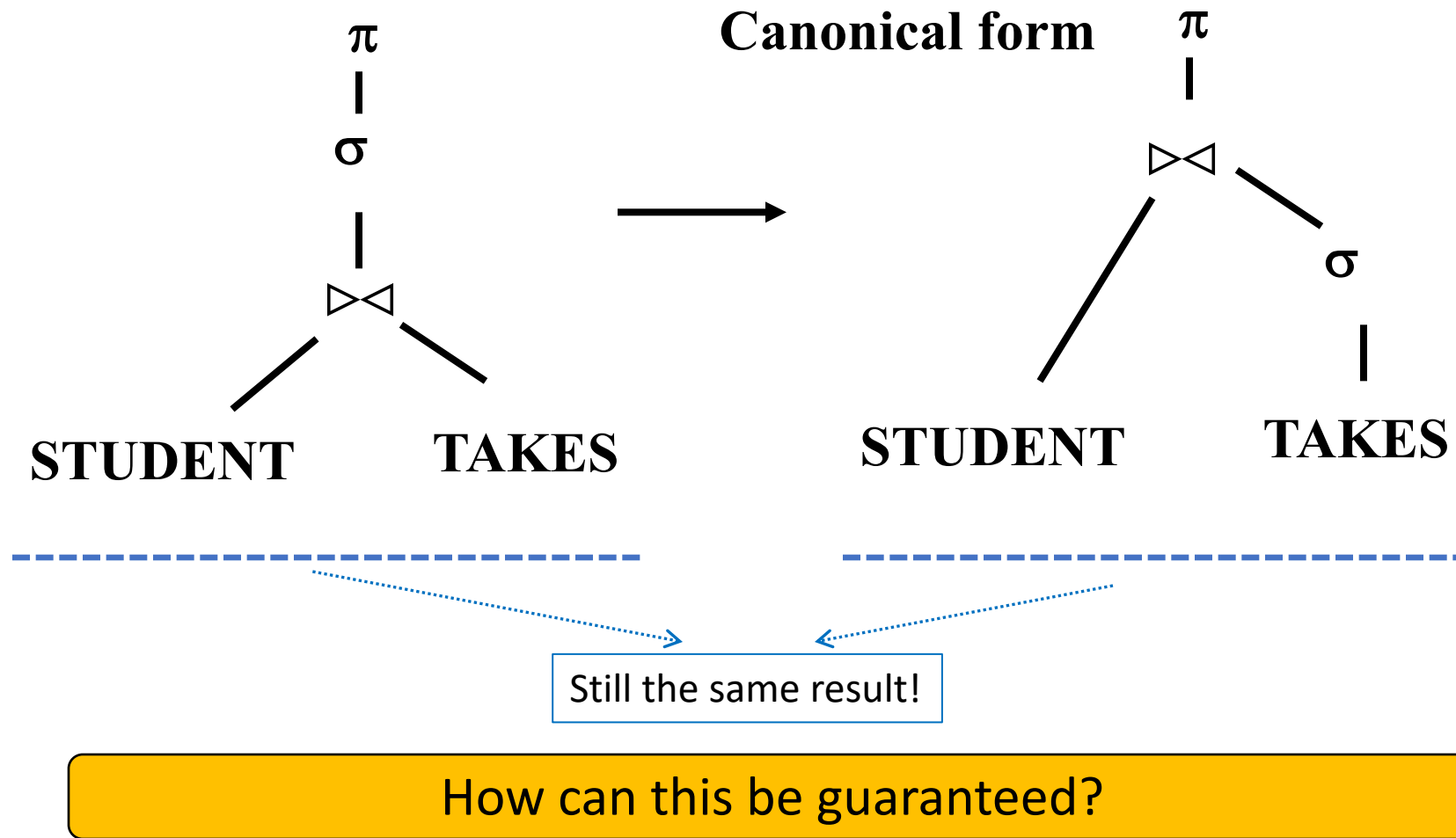


# Translating SQL Queries Into Relational Algebra Trees

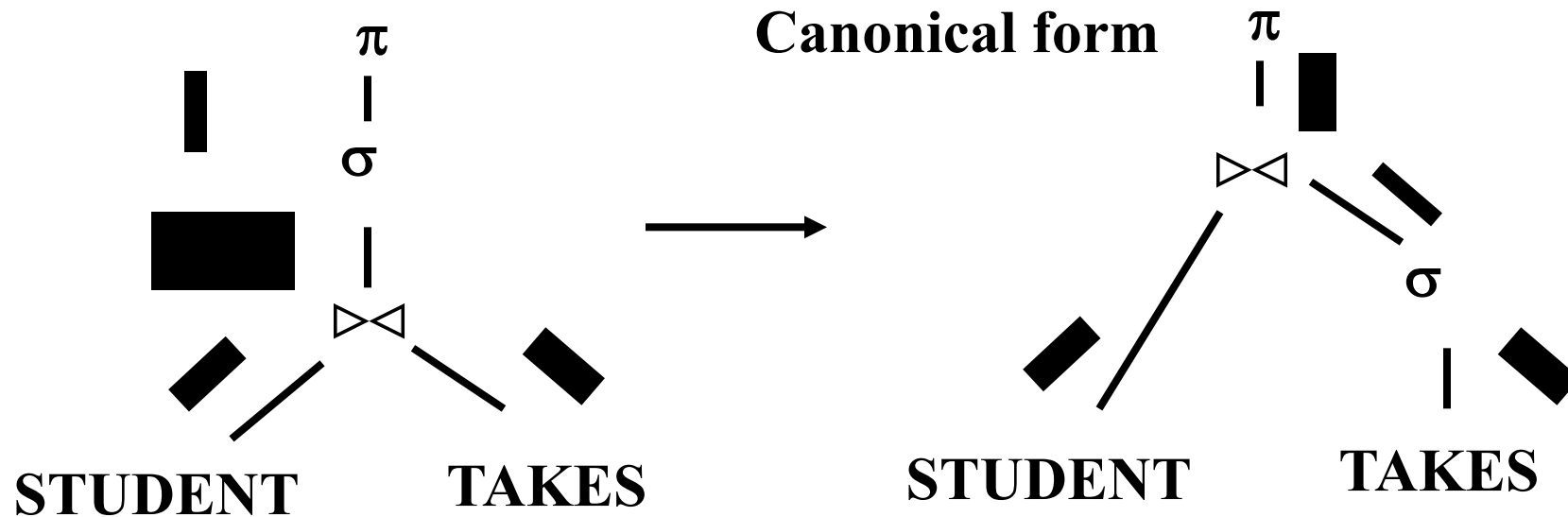


- An SQL block can be thought of as an algebra expression containing:
  - A cross-product of all relations in the FROM clause
  - Selections in the WHERE clause
  - Projections in the SELECT clause
- Remaining operators can be carried out on the result of such SQL block

# Translating SQL Queries Into Relational Algebra Trees



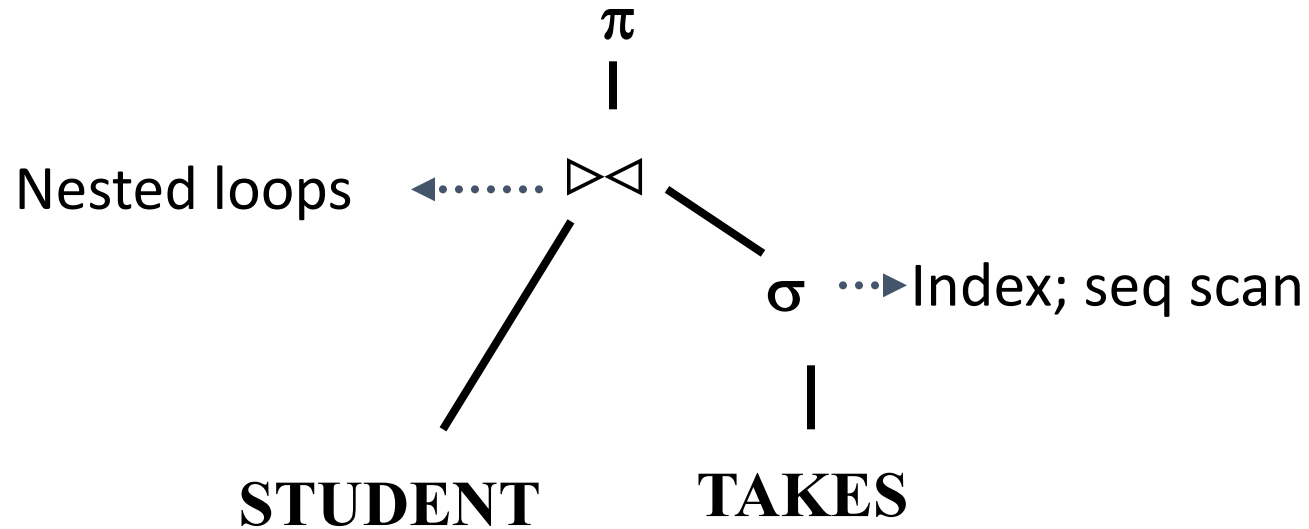
# Translating SQL Queries Into Relational Algebra Trees



OBSERVATION: try to perform selections and projections early!



# Translating SQL Queries Into Relational Algebra Trees



How to evaluate a query plan (as opposed to evaluating an operator)?

# Query Evaluation Plans

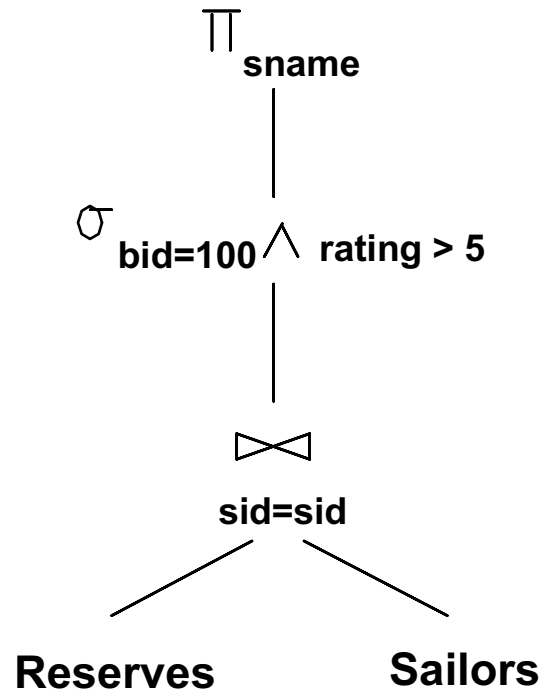
- A query evaluation plan (or simply a plan) consists of an extended relational algebra tree (or simply a tree)
- A plan tree consists of annotations at each node indicating:
  - The access methods to use for each relation
  - The implementation method to use for each operator
- Consider the following SQL query Q:

```
SELECT S.sname  
FROM Reserves R, Sailors S  
WHERE R.sid=S.sid AND  
       R.bid=100 AND S.rating>5
```

What is the  
corresponding  
RA of **Q**?

# Pushing Selections

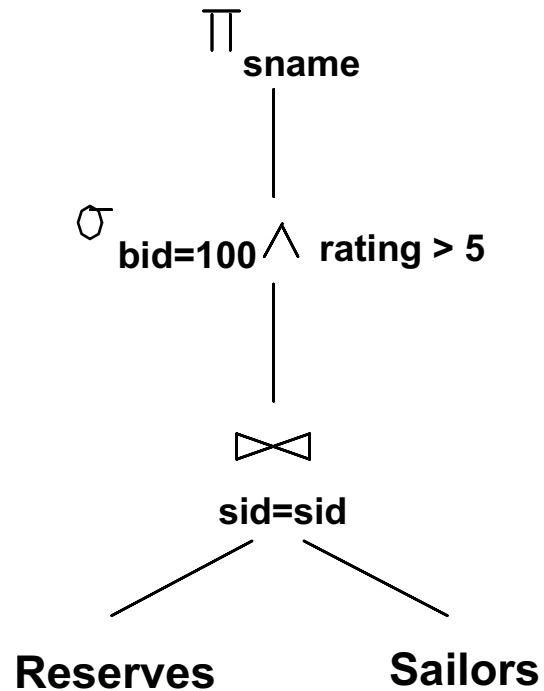
```
SELECT S.sname
FROM Reserves R, Sailors S
WHERE R.sid=S.sid AND
      R.bid=100 AND S.rating>5
```



# Pushing Selections

```
SELECT S.sname
FROM Reserves R, Sailors S
WHERE R.sid=S.sid AND
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```

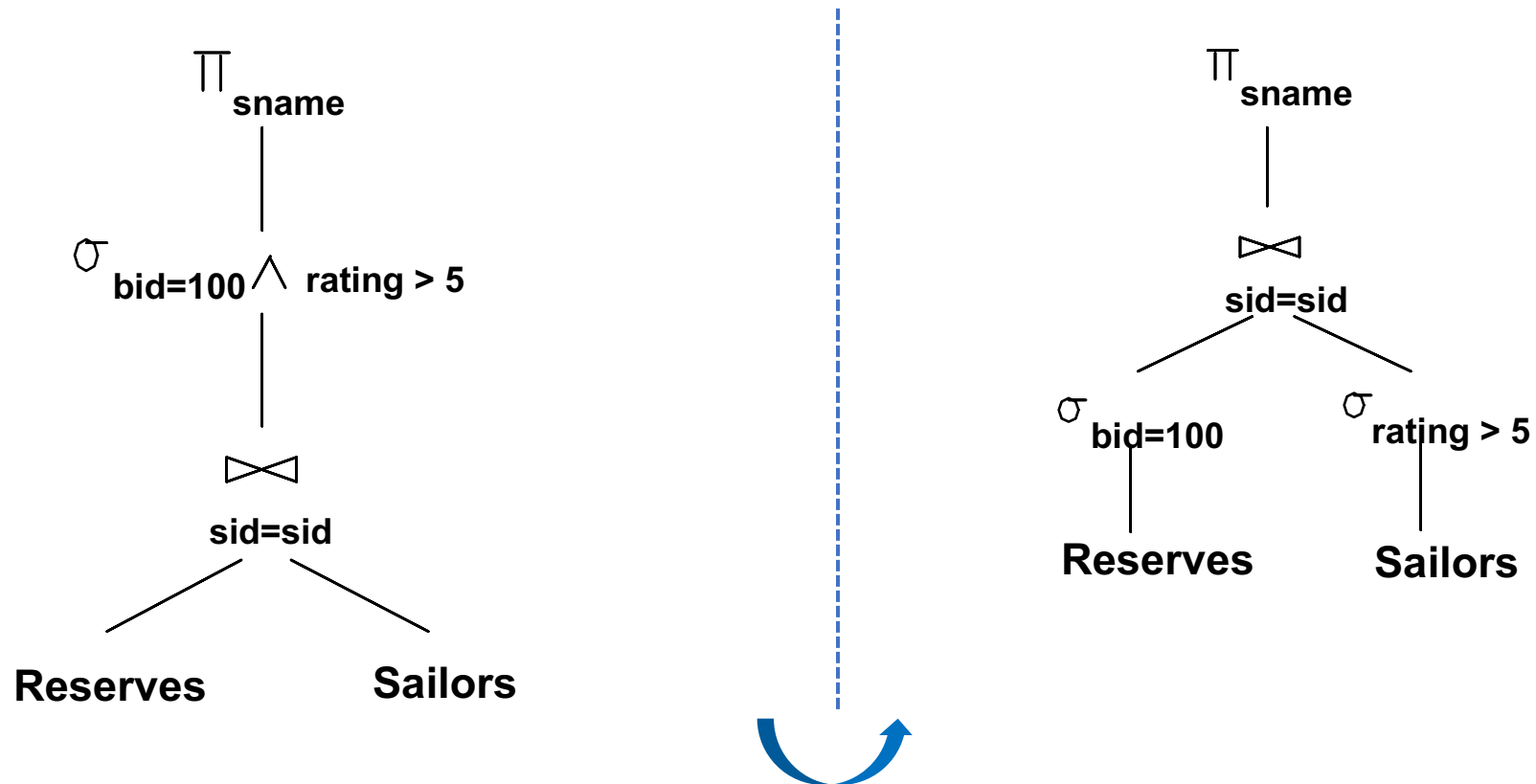
- How can we reduce the cost of a join?
  - By reducing the sizes of the input relations!



# Pushing Selections

```
SELECT S.sname
FROM Reserves R, Sailors S
WHERE R.sid=S.sid AND
      R.bid=100 AND S.rating>5
```

- How can we reduce the cost of a join?
  - By reducing the sizes of the input relations!



# Relational Algebra Equivalences

- A relational query optimizer uses **relational algebra equivalences** to identify many **equivalent expressions** for a given query
- Two relational algebra expressions over the same set of input relations are said to be equivalent if they produce the same result on all relations' instances
- Relational algebra equivalences allow us to:
  - **Push selections and projections ahead of joins**
  - **Combine selections and cross-products into joins**
  - **Choose different join orders**