```
// Ukkonen's algorithm O(n)
const int A = 27; // Alphabet size
struct SuffixTree {
   struct Node { // [1, r) !!!
        int 1, r, link, par;
        int nxt[A];
       Node(): 1(-1), r(-1), link(-1), par(-1) { fill(nxt, nxt + A, -1); }
       Node(int _1, int _r, int _link, int _par):
       1(_1), r(_r), link(_link), par(_par) { fill(nxt, nxt + A, -1); }
        int &next(int c) { return nxt[c]; }
        int get_len() const { return r - 1; }
   };
   struct State { int v, len; };
   vec< Node > t;
   State cur_state;
   vec< int > s;
   SuffixTree(): cur_state({0, 0}) { t.push_back(Node()); }
   // v \rightarrow v + s[l, r) !!!
   State go(State st, int 1, int r) {
        while(1 < r)  {
            if(st.len == t[st.v].get_len()) {
                State nx = State(\{ t[st.v].next(s[1]), 0 \});
                if(nx.v == -1) return nx;
                st = nx;
                continue;
            }
            if(s[ t[st.v].l + st.len ] != s[l]) return State({-1, -1});
            if(r - 1 < t[st.v].get_len() - st.len)
                return State({st.v, st.len + r - 1});
            1 += t[st.v].get_len() - st.len;
            st.len = t[st.v].get_len();
        }
       return st;
   }
   int get_vertex(State st) {
        if(t[st.v].get_len() == st.len) return st.v;
        if(st.len == 0) return t[st.v].par;
       Node &v = t[st.v];
       Node &pv = t[v.par];
       Node add(v.1, v.1 + st.len, -1, v.par);
        // nxt
       pv.next(s[v.1]) = (int)t.size();
       add.next(s[v.l + st.len]) = st.v;
        // par
       v.par = (int)t.size();
        // [l, r)
       v.l += st.len;
       t.push_back(add); // !!!
       return (int)t.size() - 1;
   }
   int get_link(int v) {
        if(t[v].link != -1) return t[v].link;
        if(t[v].par == -1) return 0;
        int to = get_link(t[v].par);
        to = get_vertex(
            go(State({to, t[to].get_len()}), t[v].l + (t[v].par == 0), t[v].r)
       );
       return t[v].link = to;
   }
   void add_symbol(int c) {
```

```
const int LOG = 21;
struct SuffixArray {
    vector< int > p, c[LOG];
    SuffixArray() = default;
    SuffixArray(string s) {
        s.push_back(0);
        int n = (int)s.size();
        vector<int> pn, cn, cnt;
        p.resize(n);
        for(int i = 0;i < LOG;i++) c[i].resize(n);</pre>
        pn.resize(n), cn.resize(n), cnt.assign(300, 0);
        for (int i = 0; i < n; i++) cnt[s[i]]++;
        for (int i = 1; i < (int) cnt.size(); i++) cnt[i] += cnt[i - 1];
        for (int i = n - 1; i \ge 0; i - - p[--cnt[s[i]]] = i;
        for (int i = 1; i < n; i++) {
            c[0][p[i]] = c[0][p[i - 1]];
            if(s[p[i]] != s[p[i - 1]]) c[0][p[i]]++;}
        for (int lg = 0, k = 1; k < n; k <<= 1, lg++) {
            for (int i = 0; i < n; i++)
                if((pn[i] = p[i] - k) < 0) pn[i] += n;
            cnt.assign(n, 0);
            for (int i = 0; i < n; i++) cnt[c[lg][pn[i]]]++;
            for (int i = 1; i < (int) cnt.size(); i++) cnt[i] += cnt[i - 1];
            for (int i = n - 1; i >= 0; i--) p[--cnt[c[lg][pn[i]]]] = pn[i];
            for (int 11, r1, 12, r2, i = 1; i < n; i++) {
                cn[p[i]] = cn[p[i - 1]];
                11 = p[i - 1], r1 = (11 + k) \% n;
                12 = p[i], r2 = (12 + k) \% n;
                if(c[lg][l1] != c[lg][l2] || c[lg][r1] != c[lg][r2]) cn[p[i]]++;}
            c[lg + 1] = cn;
        }p.erase(p.begin(), p.begin() + 1);}
    int get_lcp(int i, int j) {
        int res = 0; for (int lg = LOG - 1; lg >= 0; lg--) {
            if (i + (1 << lg) > (int) p.size() || j + (1 << lg) > (int) p.size()) continue;
            if (c[lg][i] == c[lg][j])
                i += (1 << lg), j += (1 << lg), res += (1 << lg);}return res;}};
```

```
vector<int> base, suf, len;
    vector<vector<int>> g;
    int last, sz;
    suf_auto(): base(26, -1), g(1, base), suf(1, -1), len(1, 0), last(0), sz(1){}
    void add_string(const string &s) {
        for (char c : s) {
            c -= 'a';
            int cur = last;
            last = sz++;
            g.push_back(base);
            suf.emplace_back();
            len.push_back(len[cur] + 1);
            while (cur != -1 \&\& g[cur][c] == -1)
                g[cur][c] = last, cur = suf[cur];
            if (cur == -1) {
                suf[last] = 0;
                continue;
            int nx = g[cur][c];
            if (len[nx] == len[cur] + 1) {
                suf[last] = nx;
                continue;
            }
            int cl = sz++;
            g.push_back(g[nx]);
            suf.push_back(suf[nx]);
            len.push_back(len[cur] + 1);
            suf[last] = suf[nx] = cl;
            while (cur != -1 \&\& g[cur][c] == nx)
                g[cur][c] = cl, cur = suf[cur];
        }
    }
};
```

```
vector<int> get_lcp(const string& s, const vector<int>& suf){
   int n = (int)suf.size();
   vector<int> back(n);
   for(int i = 0; i < n; i++) back[suf[i]] = i;
   vector<int> lcp(n - 1);
   for(int i = 0, k = 0; i < n; i++){
      int x = back[i]; k = max(0, k - 1);
      if(x == n - 1){k = 0; continue;}
      while(s[suf[x] + k] == s[suf[x + 1] + k]) k++;
      lcp[x] = k;
   }
   return lcp;
}</pre>
```

```
struct Edge {
   int fr, to, id;
   int get(int v) { return v == fr ? to : fr;}};
```

```
void dfs(const vector<vector<Edge>> &g, vector<int> &fup, vector<int> &tin,
    vector<int> &used, int &timer, int v, int par = -1) {
    tin[v] = fup[v] = timer++; used[v] = 1;
    for (Edge e : g[v]) {
        int to = e.get(v);
        if (to == par) continue;
        if (used[to]) {fup[v] = min(fup[v], tin[to]);
        } else { dfs(g, fup, tin, used, timer, to, v);
            fup[v] = min(fup[v], fup[to]);}}
void paintEdges(const vector<vector<Edge>> &g, vector<int> &fup,
    vector<int> &tin, vector<int> &used,
    vector<int> &colors, int v, int curColor, int &maxColor, int par = -1) {
    used[v] = 1;
    for (Edge e : g[v]) {
        int to = e.get(v);
        if (to == par) continue;
        if (!used[to]) {
            if (tin[v] <= fup[to]) { int tmpColor = maxColor++;</pre>
                colors[e.id] = tmpColor;
                paintEdges(g, fup, tin, used, colors, to, tmpColor, maxColor, v);
            } else { colors[e.id] = curColor;
                paintEdges(g, fup, tin, used, colors, to, curColor, maxColor, v);}
        } else if (tin[to] < tin[v]) { colors[e.id] = curColor;}}}</pre>
vector<vector<Edge>> get2components(const vector<vector<Edge>> &g,
    int m, const vector<Edge> &es) {
    int n = (int)g.size(); vector<int> fup(n), tin(n), used(n);
    vector<int> colors(m);
    int timer; used.assign(n, 0); timer = 0;
    for (int v = 0; v < n; v++) { if (used[v]) continue;
        dfs(g, fup, tin, used, timer, v);}
                         timer = 0; for (int v = 0; v < n; v++) {
    used.assign(n, 0);
        if (used[v]) continue;
        paintEdges(g, fup, tin, used, colors, v, timer, timer, -1); }
    vector<vector<Edge>> res(timer);
    for (int i = 0; i < m; i++) { res[colors[i]].push_back(es[i]); }</pre>
    return res;}
```

```
vector<int> get_z(const string& s) {
   int n = (int) s.size(); vector<int> z(n);
   for (int l = 0, r = -1, i = 1; i < n; i++) {
      z[i] = i <= r ? min(r - i, z[i - 1]) : 0;
      while (i + z[i] < n && s[z[i]] == s[i + z[i]]) z[i]++;
      if (i + z[i] > r) l = i, r = i + z[i];} return z;}
```

```
vector<int> get_pi(const string& s) {
   int n = (int) s.size(); vector<int> p(n);
   for (int j, i = 1; i < n; i++) {
      for (j = p[i - 1]; j > 0 && s[i] != s[j]; j = p[j - 1]);
      p[i] = (j += (s[i] == s[j]));} return p;}
```

```
pair<vector<int>, vector<int>> manacker(const string& s) { // -> {d0, d1}. RUN test!
    int n = (int) s.size();
    vector<int> d0(n), d1(n);
    for (int l = 0, r = -1, i = 0; i < n; i++) { // d1
        d1[i] = i <= r ? min(r - i, d1[l + r - i]) : 0;
        while (i >= d1[i] && i + d1[i] < n && s[i - d1[i]] == s[i + d1[i]]) d1[i]++;
        d1[i]--; if (i + d1[i] > r) l = i - d1[i], r = i + d1[i];}
    for (int l = 0, r = -1, i = 0; i < n; i++) {
        d0[i] = i < r ? min(r - i, d0[l + r - i - 1]) : 0;
        while (i >= d0[i] && i + d0[i] + 1 < n && s[i - d0[i]] == s[i + d0[i] + 1]) d0[i]++;
        if (d0[i] > 0 && i + d0[i] > r) l = i - d0[i] + 1, r = i + d0[i];}
    return {d0, d1};}
```

```
const int A = 26; // alph size
struct Aho {
   struct Node {
        int nxt[A], go[A], par, pch, link, good;
       Node(): par(-1), pch(-1), link(-1), good(-1) {
            fill(nxt, nxt + A, -1); fill(go, go + A, -1);}};
   vector<Node> a; Aho() { a.emplace_back(); }
   int add_string(const string& s) {
        int v = 0; for (char cc : s) {
            int c = cc - '0'; if (a[v].nxt[c] == -1) {
                a[v].nxt[c] = (int) a.size();
                a.emplace_back();
                a.back().par = v, a.back().pch = c;}
            v = a[v].nxt[c]; } a[v].good = 1; return v; }
   int go(int v, int c) {
        if (a[v].go[c] == -1) {
            if (a[v].nxt[c] != -1) a[v].go[c] = a[v].nxt[c];
            else a[v].go[c] = v ? go(get_link(v), c) : 0;
        } return a[v].go[c];}
    int get_link(int v) {
        if (a[v].link == -1) {
            if (!v || !a[v].par) a[v].link = 0;
            else a[v].link = go(get_link(a[v].par), a[v].pch);
        } return a[v].link;}
   int is_good(int v) {
        if (v <= 0) return false;
        if (a[v].good != -1) return a[v].good;
       return a[v].good = is_good(get_link(v));}};
```

```
vector<int> Hungarian(const vector< vector<int> >& a){ // ALARM: INT everywhere
  int n = (int)a.size();
  vector<int> row(n), col(n), pair(n, -1), back(n, -1), prev(n, -1);
  auto get = [&](int i, int j){ return a[i][j] + row[i] + col[j];};
  for(int v = 0; v < n; v++){
    vector<int> min_v(n, v), A_plus(n), B_plus(n);
    A_plus[v] = 1; int jb;
    while(true){
```

```
int pos_i = -1, pos_j = -1;
            for(int j = 0; j < n; j++){
                if(!B_plus[j] && (pos_i == -1 ||
                    get(min_v[j], j) < get(pos_i, pos_j))) {</pre>
                    pos_i = min_v[j], pos_j = j;
                }
            }
            int weight = get(pos_i, pos_j);
            for(int i = 0; i < n; i++) if(!A_plus[i]) row[i] += weight;</pre>
            for(int j = 0; j < n; j++) if(!B_plus[j]) col[j] -= weight;
            B_plus[pos_j] = 1, prev[pos_j] = pos_i;
            int x = back[pos_j];
            if(x == -1) \{ jb = pos_j; break; \}
            A_plus[x] = 1;
            for(int j = 0; j < n; j++)
                if(get(x, j) < get(min_v[j], j))
                    \min_{v[j]} = x;
        while(jb != -1){
            back[jb] = prev[jb];
            swap(pair[prev[jb]], jb);
        }
    }
    return pair;
}
```

```
struct HopcroftKarp {
    int n, m;
    vec< vec< int > > g;
    vec< int > pl, pr, dist;
    HopcroftKarp(): n(0), m(0) \{ \}
    HopcroftKarp(int _n, int _m): n(_n), m(_m) { g.resize(n); }
    void add_edge(int u, int v) { g[u].push_back(v); }
    bool bfs() {
        dist.assign(n + 1, inf);
        queue < int > q;
        for(int u = 0; u < n; u++) {
            if(pl[u] < m) continue;</pre>
            dist[u] = 0;
            q.push(u);
        while(!q.empty()) {
            int u = q.front();
            q.pop();
            if(dist[u] >= dist[n]) continue;
            for(int v : g[u]) {
                if(dist[ pr[v] ] > dist[u] + 1) {
                    dist[pr[v]] = dist[u] + 1;
                    q.push(pr[v]);
                }
            }
```

```
return dist[n] < inf;</pre>
    }
    bool dfs(int v) {
        if(v == n) return 1;
        for(int to : g[v]) {
             if(dist[ pr[to] ] != dist[v] + 1) continue;
            if(!dfs(pr[to])) continue;
            pl[v] = to;
            pr[to] = v;
            return 1;
        }
        return 0;
    }
    int find_max_matching() {
        pl.resize(n, m);
        pr.resize(m, n);
        int result = 0;
        while(bfs()) {
            for(int u = 0; u < n; u++) {
                 if(pl[u] < m) continue;</pre>
                 result += dfs(u);
            }
        }
        return result;
    }
};
```

```
struct Line {
    ll k, b;
    int type;
    ld x;
    Line(): k(0), b(0), type(0), x(0) { }
    Line(ll _k, ll _b, ld _x = 1e18, int _type = 0):
        k(_k), b(_b), x(_x), type(_type) { }
    bool operator<(const Line& other) const {</pre>
        if(type + other.type > 0) { return x < other.x;</pre>
        }else { return k < other.k; }</pre>
    ld intersect(const Line& other) const {
        return ld(b - other.b) / ld(other.k - k);
    }
    11 get_func(11 x0) const {
        return k * x0 + b;
    }
};
struct CHT {
    set< Line > qs;
    set< Line > :: iterator fnd, help;
    bool hasr(const set< Line > :: iterator& it) {
        return it != qs.end() && next(it) != qs.end(); }
```

```
bool hasl(const set< Line > :: iterator& it) {
        return it != qs.begin(); }
    bool check(const set< Line > :: iterator& it) {
        if(!hasr(it)) return true;
        if(!hasl(it)) return true;
        return it->intersect(*prev(it)) < it->intersect(*next(it)); }
    void update_intersect(const set< Line > :: iterator& it) {
        if(it == qs.end()) return;
        if(!hasr(it)) return;
        Line tmp = *it;
        tmp.x = tmp.intersect(*next(it));
        qs.insert(qs.erase(it), tmp);
    }
    void add_line(Line L) {
        if(qs.empty()) { qs.insert(L); return; }
            fnd = qs.lower_bound(L);
            if(fnd != qs.end() \&\& fnd->k == L.k) {
                if(fnd->b >= L.b) return;
                else qs.erase(fnd);
            }
        }
        fnd = qs.insert(L).first;
        if(!check(fnd)) { qs.erase(fnd); return; }
        while(hasr(fnd) && !check(help = next(fnd))) { qs.erase(help); }
        while(hasl(fnd) && !check(help = prev(fnd))) { qs.erase(help); }
        if(hasl(fnd)) { update_intersect(prev(fnd)); }
        update_intersect(fnd);
    }
    11 \text{ get_max}(1d x0)  {
        if(qs.empty()) return -inf64;
        fnd = qs.lower_bound(Line(0, 0, x0, 1));
        if(fnd == qs.end()) fnd--;
        ll res = -inf64; int i = 0;
        while(i < 2 && fnd != qs.end()) {
            res = max(res, fnd->get_func(x0));
            fnd++;
            i++;
        }
        while(i-- > 0) fnd--;
        while(i < 2) {
            res = max(res, fnd->get_func(x0));
            if(hasl(fnd)) {
                fnd--; i++;
            }else {
                break;
        }
        return res;
    }
};
```

```
const int mod = 998244353;
const int root = 31;
const int LOG = 23;
const int N = 1e5 + 5;
vec < int > G[LOG + 1];
vec< int > rev[LOG + 1];
inline void _add(int &x, int y);
inline int _sum(int a, int b);
inline int _sub(int a, int b);
inline int _mul(int a, int b);
inline int _binpow(int x, int p);
inline int _rev(int x);
void precalc() {
    for(int start = root, lvl = LOG; lvl >= 0; lvl--, start = _mul(start, start)) {
        int tot = 1 << lvl;</pre>
        G[lvl].resize(tot);
        for(int cur = 1, i = 0;i < tot;i++, cur = _mul(cur, start)) {
            G[lvl][i] = cur;
        }
    for(int lvl = 1;lvl <= LOG;lvl++) {</pre>
        int tot = 1 << lvl;</pre>
        rev[lvl].resize(tot);
        for(int i = 1;i < tot;i++) {</pre>
            rev[lvl][i] = ((i & 1) << (lvl - 1)) | (rev[lvl][i >> 1] >> 1);
        }
    }
void fft(vec< int > &a, int sz, bool invert) {
    int n = 1 \ll sz;
    for(int j, i = 0; i < n; i++) {
        if((j = rev[sz][i]) < i) {
            swap(a[i], a[j]);
        }
    }
    for(int f1, f2, lvl = 0, len = 1;len < n;len <<= 1, lvl++) {
        for(int i = 0; i < n; i += (len << 1)) {
            for(int j = 0; j < len; j++) {
                 f1 = a[i + j];
                f2 = _{mul}(a[i + j + len], G[lvl + 1][j]);
                 a[i + j] = _sum(f1, f2);
                 a[i + j + len] = _sub(f1, f2);
            }
        }
    }
    if(invert) {
        reverse(a.begin() + 1, a.end());
        int rn = _rev(n);
        for(int i = 0; i < n; i++) {
            a[i] = _{mul}(a[i], rn);
```

```
}
    }
}
vec< int > multiply(const vec< int > &a, const vec< int > &b) {
    vec< int > fa(ALL(a));
    vec< int > fb(ALL(b));
    int n = (int)a.size();
    int m = (int)b.size();
    int maxnm = max(n, m), sz = 0;
    while((1 << sz) < maxnm) sz++; sz++;
    fa.resize(1 << sz);</pre>
    fb.resize(1 << sz);</pre>
    fft(fa, sz, false);
    fft(fb, sz, false);
    int SZ = 1 << sz;</pre>
    for(int i = 0;i < SZ;i++) { fa[i] = _mul(fa[i], fb[i]); }
    fft(fa, sz, true);
    while((int)fa.size() > 1 && !fa.back()) fa.pop_back();
    return fa;
}
```

```
struct Complex {
    ld rl = 0, im = 0;
   Complex() = default;
    Complex(ld x, ld y = 0): rl(x), im(y) { }
    Complex & operator = (const Complex &o) {
        if(this != &o) {
            rl = o.rl;
            im = o.im;
        }
        return *this;
    }
    Complex operator + (const Complex &o) const { return {rl + o.rl, im + o.im}; }
    Complex operator - (const Complex &o) const { return {rl - o.rl, im - o.im}; }
    Complex operator * (const Complex &o) const {
        return {rl * o.rl - im * o.im, rl * o.im + im * o.rl}; }
   Complex & operator *= (const Complex &o) {
        (*this) = (*this) * o;
        return *this;
    Complex operator / (const Complex &o) const {
        ld md = o.rl * o.rl + o.im * o.im;
        return {(rl * o.rl + im * o.im) / md, (im * o.rl - rl * o.im) / md};
    Complex & operator /= (int k) {
        rl /= k;
        im /= k;
        return *this;
    }
    ld real() const { return rl; }
    ld imag() const { return im; }
```

```
};
typedef Complex base;
const int LOG = 20;
const int N = 1 << LOG;</pre>
int rev[N];
vec< base > PW[LOG + 1];
void precalc() {
    for(int i = 1; i < N; i++) {
        rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (LOG - 1)); }
    for(int lvl = 0;lvl <= LOG;lvl++) {
        int sz = 1 << lvl;</pre>
        1d alpha = 2 * pi / sz;
        base root(cos(alpha), sin(alpha));
        base cur = 1;
        PW[lvl].resize(sz);
        for(int j = 0; j < sz; j++) {
            PW[lvl][j] = cur;
            cur *= root;
        }
    }
void fft(base *a, bool invert = 0) {
    for(int j, i = 0; i < N; i++) {
        if((j = rev[i]) > i) swap(a[i], a[j]);
    }
    base u, v;
    for(int lvl = 0; lvl < LOG; lvl++) {
        int len = 1 << lvl;</pre>
        for(int i = 0; i < N; i += (len << 1)) {
            for(int j = 0; j < len; j++) {
                u = a[i + j];
                v = a[i + j + len] *
                     (invert?PW[lvl+1][j?(len << 1)-j:0]:PW[lvl+1][j]);
                 a[i + j] = u + v;
                a[i + j + len] = u - v;
            }
        }
    }
    if(invert) {
        for(int i = 0;i < N;i++) {
            a[i] /= N;
        }
    }
}
```

```
int fact[N];
int rfact[N];

void precalc2() {
   fact[0] = 1;
   for (int i = 1; i < N; i++) {</pre>
```

```
fact[i] = _mul(fact[i - 1], i);
    }
    rfact[N - 1] = rev(fact[N - 1]);
    for (int i = N - 2; i \ge 0; i - -) {
        rfact[i] = _mul(rfact[i + 1], i + 1);
    }
}
int getMulOnSegment(int 1, int r) {
    assert(1 \le r);
    if (1 == 0 \&\& r == 0) return 1;
    if (r <= 0) {
        int res = getMulOnSegment(-r, -1);
        int cnt = r - 1 + 1;
        if (cnt % 2) {
            res = (-res \% mod + mod) \% mod;
        }
        return res;
    }
    if (1 < 0) {
        int resl = getMulOnSegment(0, -1);
        if (1 % 2) {
            resl = (-resl % mod + mod) % mod;
        }
        int resr = getMulOnSegment(0, r);
        return _mul(resl, resr);
    }
    assert(1 >= 0);
    int res = fact[r];
    if (1 > 0) {
        res = _mul(res, rfact[l - 1]);
    }
    return res;
}
vector<int> extrapolate(vector<int> y, int m) {
    vector<int> yy = y;
    int n = (int)y.size() - 1;
    for (int i = 0; i \le n; i++) {
        yy[i] = _mul(y[i], _rev(getMulOnSegment(i - n, i - 0)));
    }
    vector<int> ff(n + m + 1);
    for (int i = 1; i \le n + m; i++) {
        ff[i] = _mul(fact[i - 1], rfact[i]);
    vector<int> ss = multiply(yy, ff);
    for (int i = 1; i <= m; i++) {
        int cc = getMulOnSegment(i, n + i);
        int Si = ss[n + i];
        y.push_back(_mul(cc, Si));
    }
```

```
return y;
}
```

```
struct pal_tree {
    int sz;
    vector<unordered_map<int,int>> g;
    vector<int> len, suf, cn, base;
    vector<int> fin;
    int cur, v;
    pal_tree(): g(2), sz(2), len(\{-1, 0\}), cn(\{0, 0\}), suf(\{0, 0\}), cur(0), v(1)\{\}
    void add_string (const string &s) {
        for (int i = 0; i < s.length(); i++) {
            char c = s[i] - 'a';
            while (i - len[v] - 1 < 0 \mid | s[i - len[v] - 1] - 'a' != c)
                v = suf[v];
            if (!g[v].count(c)) {
                g.emplace_back();
                int t = len[v];
                len.push_back(t + 2);
                int u = v;
                do {
                     u = suf[u];
                } while (u && s[i - len[u] - 1] - 'a' != c);
                suf.push_back(!g[u].count(c) ? 1 : g[u][c]);
                t = cn[suf.back()];
                cn.push_back(t + 1);
                g[v][c] = sz++;
                cur++;
            }
            v = g[v][c];
            fin.push_back(cn[v]);
        }
        return;
    }
};
```

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
using namespace std;
typedef
    tree<
        pair< int, int >,
        null_type,
        less< pair< int, int > >,
        rb_tree_tag,
        tree_order_statistics_node_update
    > stat_set;
// ...
ordered_set X;
X.insert(1);
```

```
X.insert(2);
    X.insert(4);
    X.insert(8):
    X.insert(16);
    cout<<*X.find_by_order(1)<<endl; // 2</pre>
    cout<<*X.find_by_order(2)<<endl; // 4</pre>
    cout<<*X.find_by_order(4)<<endl; // 16</pre>
    cout<<(end(X)==X.find_by_order(6))<<endl; // true</pre>
    cout<<X.order_of_key(-5)<<endl; // 0</pre>
    cout<<X.order_of_key(1)<<endl;</pre>
    cout<<X.order_of_key(3)<<endl;</pre>
                                        // 2
    cout<<X.order_of_key(4)<<endl;</pre>
                                      // 2
    cout<<X.order_of_key(400)<<endl; // 5</pre>
// ...
// pbds
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
using namespace __gnu_pbds;
gp_hash_table<int, int> table; // the usage is the same as the unordered_map
```

```
struct Dinic {
    struct Edge { int fr, to, cp, id, fl; };
    int n, S, T;
    vec< Edge > es;
   vec< vec< int > > g;
    vec< int > dist, res, ptr;
    Dinic(int _n, int _S, int _T):
        n(_n), S(_S), T(_T) { g.resize(n); }
    void add_edge(int fr, int to, int cp, int id) {
        g[fr].push_back((int)es.size());
        es.push_back({fr, to, cp, id, 0});
        g[to].push_back((int)es.size());
        es.push_back({to, fr, 0, -1, 0});
    }
    bool bfs(int K) {
        dist.assign(n, inf);
        dist[S] = 0;
        queue < int > q;
        q.push(S);
        while(!q.empty()) {
            int v = q.front();
            q.pop();
            for(int ps : g[v]) {
                Edge &e = es[ps];
                if(e.fl + K > e.cp) continue;
                if(dist[e.to] > dist[e.fr] + 1) {
                    dist[e.to] = dist[e.fr] + 1;
                    q.push(e.to);
                }
            }
        }
```

```
return dist[T] < inf;</pre>
}
int dfs(int v, int _push = INT_MAX) {
    if(v == T || !_push) return _push;
    for(int &iter = ptr[v];iter < (int)g[v].size();iter++) {</pre>
        int ps = g[v][ ptr[v] ];
        Edge &e = es[ps];
        if(dist[e.to] != dist[e.fr] + 1) continue;
        int tmp = dfs(e.to, min(_push, e.cp - e.fl));
        if(tmp) {
            e.fl += tmp;
            es[ps ^1].fl = tmp;
            return tmp;
        }
    }
    return 0;
}
ll find_max_flow() {
    ptr.resize(n);
    11 max_flow = 0, add_flow;
    for(int K = 1 \ll 30; K > 0; K >>= 1) {
        while(bfs(K)) {
            ptr.assign(n, 0);
            while((add_flow = dfs(S))) {
                max_flow += add_flow;
            }
        }
    }
    return max_flow;
}
void assign_result() {
    res.resize(es.size());
    for(Edge e : es) if(e.id != -1) res[e.id] = e.fl; }
int get_flow(int id) { return res[id]; }
bool go(int v, vec< int > &F, vec< int > &path) {
    if(v == T) return 1;
    for(int ps : g[v]) {
        if(F[ps] <= 0) continue;</pre>
        if(go(es[ps].to, F, path)) {
            path.push_back(ps);
            return 1;
        }
    }
    return 0;
vec< pair< int, vec< int > > > decomposition() {
    find_max_flow();
    vec< int > F((int)es.size()), path, add;
    vec< pair< int, vec< int > > > dcmp;
    for(int i = 0;i < (int)es.size();i++) F[i] = es[i].fl;
    while(go(S, F, path)) {
```

```
int mn = INT_MAX;
    for(int ps : path) mn = min(mn, F[ps]);
    for(int ps : path) F[ps] -= mn;
    for(int ps : path) add.push_back(es[ps].id);
    reverse(ALL(add));
    dcmp.push_back({mn, add});
    add.clear();
    path.clear();
}
return dcmp;
}
```

```
struct MCMF {
    struct Edge { int fr, to, cp, fl, cs, id; };
    int n, S, T;
    vec< Edge > es;
    vec< vec< int > > g;
    vec< 11 > dist, phi;
    vec< int > from;
    MCMF(int _n, int _S, int _T): n(_n), S(_S), T(_T)
    { g.resize(n); }
    void add_edge(int fr, int to, int cp, int cs, int id) {
        g[fr].push_back((int)es.size());
        es.push_back({fr, to, cp, 0, cs, id});
        g[to].push_back((int)es.size());
        es.push_back({to, fr, 0, 0, -cs, -1});
    void init_phi() {
        dist.assign(n, LLONG_MAX);
        dist[S] = 0;
        for(int any, iter = 0;iter < n - 1;iter++) { // Ford Bellman</pre>
            any = 0;
            for(Edge e : es) {
                if(e.fl == e.cp) continue;
                if(dist[e.to] - dist[e.fr] > e.cs) {
                    dist[e.to] = dist[e.fr] + e.cs;
                    any = 1;
                }
            }
            if(!any) break;
        phi = dist;
    bool Dijkstra() {
        dist.assign(n, LLONG_MAX);
        from.assign(n, -1);
        dist[S] = 0;
        priority_queue< pair< 11, int >, vec< pair< 11, int > >,
            greater< pair< 11, int > > > pq;
        pq.push({dist[S], S});
```

```
while(!pq.empty()) {
        int v;
        ll di;
        tie(di, v) = pq.top();
        pq.pop();
        if(di != dist[v]) continue;
        for(int ps : g[v]) {
            Edge &e = es[ps];
            if(e.fl == e.cp) continue;
            if(dist[e.to] - dist[e.fr] > e.cs + phi[e.fr] - phi[e.to]) {
                dist[e.to] = dist[e.fr] + e.cs + phi[e.fr] - phi[e.to];
                from[e.to] = ps;
                pq.push({dist[e.to], e.to});
            }
        }
    }
    for(int v = 0; v < n; v++) {
        phi[v] += dist[v];
    }
    return dist[T] < LLONG_MAX;</pre>
}
pll find_mcmf() {
    init_phi();
    11 \text{ flow} = 0, \text{ cost} = 0;
    while(Dijkstra()) {
        int mn = INT_MAX;
        for(int v = T; v != S; v = es[ from[v] ].fr) {
            mn = min(mn, es[from[v]].cp - es[from[v]].fl);
        }
        flow += mn;
        for(int v = T;v != S;v = es[ from[v] ].fr) {
            es[from[v]].fl += mn;
            es[ from[v] ^ 1 ].fl -= mn;
        }
    }
    for(Edge &e : es) {
        if(e.fl >= 0)
            cost += 111 * e.fl * e.cs;
    return make_pair(flow, cost);
}
bool go(int v, vec< int > &F, vec< int > &path, vec< int > &used) {
    if(used[v]) return 0;
    used[v] = 1;
    if(v == T) return 1;
    for(int ps : g[v]) {
        if(F[ps] <= 0) continue;</pre>
        if(go(es[ps].to, F, path, used)) {
            path.push_back(ps);
            return 1;
        }
```

```
}
        return 0;
    }
    vec< pair< int, vec< int > > > decomposition(ll &_flow, ll &_cost) {
        tie(_flow, _cost) = find_mcmf();
        vec< int > F((int)es.size()), path, add, used(n);
        vec< pair< int, vec< int > > > dcmp;
        for(int i = 0;i < (int)es.size();i++) F[i] = es[i].fl;</pre>
        while(go(S, F, path, used)) {
            used.assign(n, 0);
            int mn = INT_MAX;
            for(int ps : path) mn = min(mn, F[ps]);
            for(int ps : path) F[ps] -= mn;
            for(int ps : path) add.push_back(es[ps].id);
            reverse(ALL(add));
            dcmp.push_back({mn, add});
            add.clear();
            path.clear();
        }
        return dcmp;
    }
};
```

```
namespace FACTORIZE {
    const 11 \text{ MAXX} = 1000;
    const int FERMA_ITER = 30;
    // const int POLLARD_PO_ITER = 10000;
    int POLLARD_PO_ITER;
    inline ll sqr(ll n) { return n * n; }
    ll check_small(ll n) {
        for(ll x = 1; sqr(x) \le n \&\& x \le MAXX; x++) {
            if(x > 1 \&\& n \% x == 0) {
                 return x;
            }else if(sqr(x + 1) > n) {
                 return -1;
            }
        }
        return -1;
    11 check_square(ll n) {
        11 bl = 0;
        11 br = 3e9+1;
        11 bm;
        while(br - bl > 1) {
            bm = (bl + br) / 2;
            if(sqr(bm) \le n) {
                 bl = bm;
            }else {
                 br = bm;
        }
```

```
if(sqr(bl) == n \&\& bl > 1) {
        return bl;
    }else {
        return -1;
    }
}
inline 11 _mul(11 a, 11 b, 11 m) {
    static __int128 xa = 1;
    static __int128 xb = 1;
    static _{-}int128 xm = 1;
    xa = a;
    xb = b;
    xm = m;
    return ll(xa * xb % xm);
}
/*
ll \_mul(ll x, ll y, ll mod) {
    ll q = ld(x) * ld(y) / ld(mod);
    ll r = x * y - q * mod;
    return (r % mod + mod) % mod;
}*/
inline 11 _binpow(11 x, 11 p, 11 m) {
    static ll res = 1;
    static 11 tmp = 1;
    res = 1;
    tmp = x;
    while(p > 0)  {
        if(p & 111) {
            res = _mul(res, tmp, m);
        tmp = _mul(tmp, tmp, m);
        p >>= 1;
    }
    return res;
}
mt19937_64 next_rand(179);
11 gcd(ll x, ll y) { return !x ? y : gcd(y % x, x); }
bool is_prime(ll n) {
    if(n <= 1) return false;</pre>
    if(n == 2) return true;
    ll a, g;
    for(int iter = 0;iter < FERMA_ITER;iter++) {</pre>
        a = next_rand() \% (n - 2);
        if(a < 0) a += n - 2;
        a += 2;
        assert(1 < a && a < n);
        g = gcd(a, n);
        if(g != 1) { return false; }
        if(_binpow(a, n - 1, n) != 1) { return false; }
    }
    return true;
```

```
}
    inline 11 _func(11 x, 11 n) {
        static ll result = 1;
        result = _{mul}(x, x, n);
        return result + 1 < n ? result + 1 : 0;
    }
    11 pollard_po(ll n) {
        POLLARD_PO_ITER = 5 + 3 * pow(n, 0.25);
        ll a, b, x, g;
        while(1) {
            a = next_rand() % n;
            if(a < 0) a += n;
            b = next_rand() % n;
            if(b < 0) b += n;
            for(int iter = 0;iter < POLLARD_PO_ITER;iter++) {</pre>
                x = a >= b ? a - b : b - a;
                g = gcd(x, n);
                if(1 < g \&\& g < n)  {
                    return g;
                }
                a = func(a, n);
                b = func(func(b, n), n);
            }
        }
    }
    ll get_div(ll n) {
        ll res;
        res = check_small(n);
        if(res != -1) { return res; }
        res = check_square(n);
        if(res != -1) { return res; }
        if(is_prime(n)) { return n; }
        return pollard_po(n);
    }
}
```

```
class EulerTourTrees {
    /*graph - forest 1 .. n get = is connected?
    no memory leaks 1 <= n, q <= 10^5 0.7 sec*/
private:
    struct Node {
        Node *1; Node *r; Node *p;
        int prior; int cnt; int rev;
    };
    void do_rev(Node *v) {if(v) v->rev ^= 1, swap(v->l, v->r);}
    int get_cnt(Node *v) const {return v ? v->cnt : 0;}
    void update(Node *v) {if(!v) return;
        v->cnt = 1 + get_cnt(v->l) + get_cnt(v->r);
        v->p = nullptr;if(v->l) v->l->p = v;if(v->r) v->r->p = v;}
    void push(Node *v) {
        if(!v) return; if(v->rev) {do_rev(v->l);do_rev(v->r);v->rev ^= 1;}}
}
```

```
void merge(Node *& v, Node *1, Node *r) {
        if(!1 || !r) {v = 1 ? 1 : r;return;}
        push(1);push(r);
        if(1->prior < r->prior) {merge(1->r, 1->r, r);v = 1;}else {
            merge(r->1, 1, r->1); v = r; update(v);
    void split_by_cnt(Node *v, Node *& 1, Node *& r, int x) {
        if(!v) {l = r = nullptr;return;}push(v);
        if(get_cnt(v->1) + 1 \le x) {
            split_by_cnt(v->r, v->r, r, x - get_cnt(v->l) - 1); l = v;
        }else {split_by_cnt(v->1, 1, v->1, x);r = v;}
        update(1);update(r);
    void push_path(Node *v) {
        if(!v) return;push_path(v->p);push(v);}
    int get_pos(Node *v) {
        push_path(v);int res = 0, ok = 1;
        while(v) {if(ok) res += get_cnt(v->1) + 1;
            ok = v->p \&\& v->p->r == v;v = v->p;
        return res;}
    Node *get_root(Node *v) const{while(v && v->p) v = v->p;return v;}
    Node *shift(Node *v) {
        if(!v) return v; int pos = get_pos(v);
        Node *nl = nullptr, *nr = nullptr; Node *root = get_root(v);
        split_by_cnt(root, nl, nr, pos - 1);do_rev(nl);do_rev(nr);
        merge(root, nl, nr);do_rev(root);return root;}
public:EulerTourTrees() = default;
    EulerTourTrees(int _n): n(_n) {ptr.resize(_n + 1);
        where_edge.resize(_n + 1);}
    bool get(int u, int v) const {if(u == v) return true;
        Node *ru = get_root(ptr[u].empty() ? nullptr : *ptr[u].begin());
        Node *rv = get_root(ptr[v].empty() ? nullptr : *ptr[v].begin());
        return ru && ru == rv;}
    void link(int u, int v) {
        Node *ru = shift(ptr[u].empty() ? nullptr : *ptr[u].begin());
        Node *rv = shift(ptr[v].empty() ? nullptr : *ptr[v].begin());
        Node *uv = new Node();Node *vu = new Node();
        ptr[u].insert(uv);ptr[v].insert(vu);
        where_edge[u][v] = uv;where_edge[v][u] = vu;
        merge(ru, ru, uv);merge(ru, ru, rv);merge(ru, ru, vu);}
    void cut(int u, int v) {
        Node *uv = where_edge[u][v]; Node *vu = where_edge[v][u];
        ptr[u].erase(uv);ptr[v].erase(vu);
        Node *root = shift(uv); Node *nl = nullptr, *nm = nullptr, *nr = nullptr;
        int pos1 = get_pos(uv);int pos2 = get_pos(vu);
        if(pos1 < pos2) {split_by_cnt(root, nl, nr, pos2);</pre>
            split_by_cnt(nl, nl, vu, pos2 - 1);split_by_cnt(nl, nl, nm, pos1);
            split_by_cnt(nl, nl, uv, pos1 - 1);merge(nl, nl, nr);}else {
            split_by_cnt(root, nl, nr, pos1);split_by_cnt(nl, nl, uv, pos1 - 1);
            split_by_cnt(nl, nl, nm, pos2);split_by_cnt(nl, nl, vu, pos2 - 1);
            merge(nl, nl, nm);}delete uv;delete vu;}
private:int n = 0;vec< set< Node* > > ptr;
```

```
vec< unordered_map< int, Node* > > where_edge; // ptr to node
};
```

```
struct Edge {
    int fr, to, w, id;
    bool operator < (const Edge& o) const { return w < o.w; }
};
// find oriented mst (tree)
// there are no edge --> root (root is 0)
// 0 .. n - 1, weights and vertices will be changed, but ids are ok
vector<Edge> work(const vector<vector<Edge>>& graph) {
    int n = (int) graph.size();
    vector<int> color(n), used(n, -1);
    for (int i = 0; i < n; i++)
        color[i] = i;
    vector<Edge> e(n);
    for (int i = 0; i < n; i++) {
        if (graph[i].empty()) {
            e[i] = \{-1, -1, -1, -1\};
        } else {
            e[i] = *min_element(graph[i].begin(), graph[i].end());
        }
    }
    vector<vector<int>> cycles;
    used[0] = -2;
    for (int s = 0; s < n; s++) {
        if (used[s] != -1)
            continue;
        int x = s;
        while (used[x] == -1) {
            used[x] = s;
            x = e[x].fr;
        }
        if (used[x] != s)
            continue;
        vector<int> cycle = {x};
        for (int y = e[x].fr; y != x; y = e[y].fr)
            cycle.push_back(y), color[y] = x;
        cycles.push_back(cycle);
    }
    if (cycles.empty())
        return e;
    vector<vector<Edge>> next_graph(n);
    for (int s = 0; s < n; s++) {
        for (const Edge& edge : graph[s]) {
            if (color[edge.fr] != color[s])
                next_graph[color[s]].push_back({
                    color[edge.fr], color[s], edge.w - e[s].w, edge.id
                });
        }
```

```
}
    vector<Edge> tree = work(next_graph);
    for (const auto& cycle : cycles) {
        int cl = color[cycle[0]];
        Edge next_out = tree[cl], out{};
        int from = -1;
        for (int v : cycle) {
            tree[v] = e[v];
            for (const Edge& edge : graph[v])
                if (edge.id == next_out.id)
                    from = v, out = edge;
        }
        tree[from] = out;
    }
    return tree;
}
```

Gomory-Hu tree (Gusfield's algorithm): label nodes from 0 to (|V|-1) and set $p_i = 0 \forall i > 0$. $\forall i > 0$: find min-cut (S,T) between i and p_i , where $i \in S, p_i \in T$; for each node j, s.t. $i < j, j \in S, p_j = p_i$ set $p_j = i$