

Title Page

Optimum growth temperature declines with body size within fish species

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Abstract

According to the temperature-size rule, warming of aquatic ecosystems is generally predicted to increase individual growth rates but reduce asymptotic body sizes of ectotherms. However, we lack a comprehensive understanding of how growth and key processes affecting it, such as consumption and metabolism, depend on both temperature and body mass within species. This limits our ability to inform growth models, link experimental data to observed growth patterns, and advance mechanistic food web models. To examine the combined effects of body size and temperature on individual growth, as well as the link between maximum consumption, metabolism and body growth, we conducted a systematic review and compiled experimental data on fishes from 59 studies that combined body mass and temperature treatments. By fitting hierarchical models accounting for variation between species, we estimated how these three processes scale jointly with temperature and body mass within species. We found that whole-organism maximum consumption increases more slowly with body mass than metabolism, and is unimodal over the full temperature range, which leads to the prediction that optimum growth temperatures decline with body size. Using an independent dataset, we confirmed this negative relationship between optimum growth temperature and size within fish species. Small individuals may therefore exhibit increased growth with initial warming, whereas larger conspecifics could be the first to experience negative impacts of warming on growth. These findings help advance mechanistic models of individual growth and food web dynamics and improve our understanding of how climate warming affects the growth and size structure of aquatic ectotherms.

Introduction

Individual body growth is a fundamental process powered by metabolism, and thus depends on body size and temperature¹. It affects individual fitness and life history traits, such as maturation size, population growth rates², and ultimately energy transfer across trophic levels^{3,4}. Therefore, understanding how growth scales with body size and temperature is important for predicting the impacts of global warming on the structure and functioning of ecosystems.

Global warming is predicted to lead to declining body sizes of organisms^{5,6}. The temperature size-rule ('TSR') states that warmer rearing temperatures lead to faster developmental times (and larger initial size-at-age or size-at-life-stage), but smaller adult body sizes in ectotherms^{7,8}. This relationship is found in numerous experimental studies⁷, is reflected in latitudinal gradients⁹, and is stronger in aquatic than terrestrial organisms^{9,10}. Support for the TSR exists in fishes, in particular in young fish, where reconstructed individual growth histories often reveal positive correlations between growth rates and temperature in natural systems^{11–14}. However, whether the positive effect of warming on growth is indeed limited to small individuals within a species, as predicted by the temperature size-rule, is less clear. Negative correlations between maximum size, asymptotic size or size-at-age of old fish and temperature have been found in commercially exploited fish species^{13,15,16}. However, other studies, including large scale experiments, controlled experiments and latitudinal studies or observational data on unexploited species, have failed to find negative relationships between maximum size, growth of old fish or mean size and temperature^{14,17–20} and differences between species may be related to life history traits and depend on local environmental conditions^{20,21}.

While the support for TSR is mixed, and the underlying mechanisms are not well understood^{8,22,23}, theoretical growth models, such as Pütter growth models²⁴, including the von Bertalanffy

growth model (VBGM) ²⁵, commonly predict declines in asymptotic body mass with temperature and declines in optimum growth temperature with body mass, in line with the TSR ^{26–28}. Yet, the physiological basis of these models has been questioned, as the commonly applied scaling parameters (mass exponents) tend to differ from empirical estimates ^{29,30}. Hence, despite attempting to describe growth from first principles, Pütter growth models can also be viewed as phenomenological. In more mechanistic growth models, the difference between energy gain and expenditure is partitioned between somatic growth and gonads ^{31–34}. Energy gain is normally the amount of energy extracted from consumed food and expenditure is defined as maintenance, activity and feeding metabolism. These components of the energetics of growth are found in dynamic energy budget models ^{32,35}, including physiologically structured population models (PSPMs) ³⁶, and size-spectrum models ^{37–39}. Therefore, it is important to understand how consumption and metabolism rates scale with body mass and temperature in order to understand if and how growth of large fish within populations is limited by temperature, and to evaluate the physiological basis of growth models.

Moreover, the effect of body mass and temperature on growth dynamics should be evaluated over ontogeny at the intraspecific level (within species), which better represents the underlying process than interspecific data (among species) ³⁰. For instance, we do not expect an interspecific relationship between optimum growth temperature and body mass, but within species it may have a large effect on growth dynamics. Despite this, intraspecific body mass and temperature scaling is often inferred from interspecific data, and we know surprisingly little about average relationship between consumption and metabolic exponents within species ³⁰. Importantly, how physiological rates depend on mass and temperature within species can differ from the same relationships across species ^{40–42}. Across species, rates are often assumed and found to scale as power functions of mass

with exponents of $3/4$ for whole organism rates ($-1/4$ for mass-specific rates), exponentially with temperature, and with independent mass and temperature effects (e.g., in the Arrhenius fractal supply model (AFS) applied in the metabolic theory of ecology, MTE^{1,43,44}). In contrast, within species deviations from a general $3/4$ mass exponent are common^{42,45,46}, rates are typically unimodal^{41,47–49} and the effects of mass and temperature can be interactive^{40,50–53} (but see Jerde *et al.*⁴²). Alternative approaches that overcome these obstacles include fitting multiple regression models where coefficients for mass and temperature are estimated jointly⁴⁴, as well as fitting non-linear or polynomial models that can capture the de-activation of biological rates at higher temperatures^{47,48,54}. This requires intraspecific data with variation in both mass and temperature.

In this study, we analyze how maximum consumption, metabolism and growth rate of fish scale intraspecifically with mass and temperature. We performed a systematic literature review by searching the Web of Science Core Collection to compile datasets on individual-level maximum consumption, metabolism and growth rates of fish from experiments in which the effect of fish body mass is replicated across multiple temperatures within species (total $n=3672$, with data from 13, 20 and 34 species for each rate, respectively). We then fit hierarchical Bayesian models to estimate general intraspecific scaling parameters while accounting for variation between species. The estimated mass dependence and temperature sensitivity of mass-specific consumption and metabolism are used to quantify average changes in net energy gain (and hence, growth, assumed proportional to net energy gain) over temperature and body mass. Lastly, we compare our predicted changes in optimum growth temperature over body mass with an independent experimental dataset on optimum growth temperatures across individuals of different sizes within species.

Results

We identified that within species of fish, mass-specific metabolic rates increase faster with body mass than maximum consumption rates, and neither of these rates conform to the commonly predicted $-1/4$ scaling with body mass (Fig. 1). We also quantified the unimodal relationship of consumption rate over the full temperature range (Fig. 2). Combined, these scaling relationships lead to the prediction, based on Pütter-type growth models, that optimum growth temperature declines with body size (Fig. 3)²⁶. The prediction of declining optimum growth temperatures with size was confirmed by our analysis of independent experimental growth rate data. We find that within species the optimum growth temperature declines with body size by 0.31°C per unit increase in the natural log of relative body mass (Fig. 4). Below we present the underlying results in more detail.

We found that the average intraspecific mass exponent for mass-specific consumption rate is smaller (-0.38 [-0.46 , -0.30]) than that for metabolic rate (-0.21 [-0.26 , -0.16]), based on the non-overlapping Bayesian 95% credible intervals (Fig. 1). It is also probable that the mass-specific scaling exponents differ from $-1/4$ (that is predicted by the MTE), because $> 99\%$ of the posterior distribution of the mass exponent of maximum consumption is below $-1/4$, and 95% of the posterior distribution of the mass exponent of metabolic rate is above $-1/4$. Activation energies of maximum consumption rate and metabolism are both similar (0.69 [0.54 , 0.85] and 0.62 [0.57 , 0.67] respectively; Fig. 1) and largely fall within the prediction from the MTE (0.6 - 0.7 eV)¹. The global intraspecific intercept for routine and resting metabolic rate is estimated to be -1.93 [-2.11 , -1.74], and for standard metabolic rate it is -2.49 [-2.81 , -2.17] (Supplementary Fig. S7). Models where all coefficients varied by species were favored in terms of WAIC (M5 and M1, for consumption and metabolism, respectively) (Supplementary Table S4). We found statistical support for a species-varying mass and temperature interaction for metabolic rate. 98% of the

posterior distribution of the global interaction coefficient μ_{β_3} is above 0 (Supplementary Fig. S5). The estimated coefficient is 0.018 [0.0008, 0.0367] on the Arrhenius temperature scale, which corresponds to a decline in the mass scaling exponent of metabolic rate by $0.0026\text{ }^{\circ}\text{C}^{-1}$. The selected model for maximum consumption rate did not include an interaction term (M5).

We estimated the parameters of the Sharpe-Schoolfield equation (equation (4)) for temperature-dependence of consumption including data beyond peak temperature as: activation energy, $E_j = 0.58$ [0.45, 0.74], rate at reference temperature, $C_{0_j} = 0.70$ [0.52, 0.89], temperature at which the rate is reduced to half (of the rate in the absence of deactivation) due to high temperatures, $T_h = 4.03$ [2.82, 4.98], and the rate of the decline past the peak, $E_h = 2.64$ [2.17, 3.22]. This shows that the relationship between consumption rate and temperature is unimodal and asymmetric, where the decline in consumption rate at high temperatures is steeper than the increase at low temperatures (Fig. 2).

The above results provide empirical support for the two criteria outlined in Morita et al.,²⁶ that result in declining optimum temperatures with size, i.e. (i) smaller whole organism mass exponent for consumption than metabolism (Fig. 1) and (ii) that growth reaches an optimum over temperature. In our case, the second criterion is met because consumption reaches a peak over temperature (Fig. 2). We illustrate the consequence of these findings in Fig. 3, which shows that the optimum temperature for net energy gain is reached at a lower temperature for a larger fish because of the difference in exponents and because net gain is unimodally related to temperature. Assuming growth is proportional to net energy gain, this predicts that optimum growth temperature declines with body size.

Using independent data from growth trials across a range of body sizes and temperatures, we also find strong statistical support for a decline in optimum growth temperature with body mass

within species, because 92% of the posterior density of the global slope estimate (μ_{β_1}) is below 0. The models with and without species-varying slopes were indistinguishable in terms of WAIC (Supplementary Table S5), and we present the results for the species-varying intercept and slope model, due to slightly better model diagnostics (Supplementary Fig. S24-27). The global relationship is given by the model: $T_{opt} = -0.074 - 0.31 \times m$, where m is the natural log of the rescaled body mass, calculated as the species-specific ratio of mass to maturation mass.

Discussion

In this study, we systematically analyzed the intraspecific scaling of consumption, metabolism and growth with body mass and temperature. We found strong evidence for declining optimum growth temperatures as individuals grow in size based on two independent approaches. First, we find differences in the intraspecific mass-scaling of consumption and metabolism, and a unimodal temperature dependence of consumption, which lead to predicted declines in optimum temperature for net energy gain (and hence growth) with size. Second, we confirm this prediction using intraspecific growth rate data of fish. Our analysis thus demonstrates the importance of understanding intraspecific scaling relationships when predicting responses of fish populations to climate warming.

That warming increases growth and development rates but reduces maximum or adult size is⁵⁵ well known from experimental studies, also referred to as the temperature-size rule (TSR). Yet, the mechanisms underlying the TSR remain poorly understood. Pütter-type growth models, including the von Bertalanffy growth equation (VBGE), predict that the asymptotic size declines with warming if the ratio of the coefficients for energy gains and losses (H/K in equation (7))²⁷ declines with temperature. However, the assumptions underlying the VBGE were recently

questioned because of the lack of empirical basis for the scaling exponents and the effects of those on the predicted effects of temperature on asymptotic size^{29,30}. Specifically, the allometric exponent of energy gains (a) is assumed to be smaller than that of energetic costs (b) (equation (7)). This is based on the assumption that anabolism scales with the same power as surfaces to volumes ($a = 2/3$) and catabolism, or maintenance metabolism, is proportional to body mass ($b = 1$)^{25,55}. In contrast, maintenance costs are commonly thought to instead be proportional to standard metabolic rate, which in turn often is proportional to intake rates at the interspecific level^{1,30}. This leads to $a \approx b$, resulting in unrealistic growth trajectories and temperature dependences of growth dynamics in Pütter models^{29,30}. However, similar to how the existence of large fishes in tropical waters does not invalidate the hypothesis that old individuals of large-bodied fish may reach smaller sizes with warming, interspecific scaling parameters cannot reject or support these model predictions on growth within species. We show that the average intraspecific whole-organism mass scaling exponent of metabolism is larger than that of maximum consumption, i.e., the inequality $a < b$ holds at the intraspecific level. This implies that on average within species of fish, energetic costs increase faster with body mass than gains (all else equal). Importantly, when accounting for this difference in the exponents, and the unimodal thermal response of consumption, the thermal response of net energy gain is characterized by the optimum temperature being a function of body size²⁶. Therefore, empirically derived intraspecific parameterizations of simple growth models result in predictions in line with the TSR, in this case via declines in optimum growth temperatures over ontogeny rather than declines in asymptotic sizes.

Declines in optimum growth temperatures over ontogeny as a mechanism for TSR-like growth dynamics do not rely on the assumption that the ratio of the coefficients for energy gains and losses declines with temperature. In fact, we find that when using data from sub-peak temperatures only,

the average intraspecific predictions about the activation energy of metabolism and consumption do not differ substantially, which implies there is no clear loss or gain of energetic efficiency with warming within species. This is in contrast to other studies, e.g. Lemoine & Burkepile⁵⁶ and Rall *et al.*⁵⁷. However, it is in line with the finding that growth rates increase with temperature e.g.⁵⁸, which is difficult to reconcile from a bioenergetics perspective if warming always reduced net energy gain. Our analysis instead suggests that the mismatch between gains and losses occurs when accounting for unimodal consumption rates over temperature. The match, or mismatch, between the temperature dependence of feeding vs. metabolic rates is a central question in ecology that extends from experiments to meta-analyses to food web models^{56,57,59–61}. Our study highlights the importance of accounting for non-linear thermal responses for two main reasons. First, the thermal response of net energy gain reaches a peak at temperatures below the peak for consumption. Secondly, as initial warming commonly leads to increased growth rates, the effect of warming on growth rates should depend on temperature rather than growth being assumed to be monotonically related to temperature.

Life-stage dependent optimum growth temperatures have previously been suggested as a component of the TSR⁸. Although previous studies have found declines in optimum growth temperatures with body size in some species of fishes and other aquatic ectotherms^{62–66}, others have not^{67,68}. Using systematically collated growth data from experiments with variation in both size and temperature treatments (13 species), we find that for an average fish, the optimum growth temperature declines as it grows in size. This finding emerges despite the small range of body sizes used in the experiments (only 10% of observations are larger than 50% of maturation size) (Supplementary Fig. S2). Individuals of such small relative size likely invest little energy in reproduction, which suggests that physiological constraints contribute to reduced growth

performance of large compared to small fish, in addition to increasing investment into reproduction⁶⁹.

Translating results from experimental data to natural systems is challenging because maximal feeding rates, unlimited food supply, lack of predation, and constant temperatures do not reflect natural conditions, yet affect growth rates^{67,70,71}. In addition, total metabolic costs in the wild also include additional costs for foraging and predator avoidance. It is, however, typically found and assumed that standard metabolic rate and natural feeding levels are proportional to routine metabolic rate and maximum consumption rate, respectively, and thus exhibit the same mass-scaling relationships^{32,72}. Intraspecific growth rates may not appear to be unimodally related to temperature when measured over a temperature gradient across populations within a species²⁰, because each population can be adapted to local climate conditions and thus display different temperature optima. However, each population likely has a thermal optimum for growth, which differs between individuals of different size. Hence, each population might have a unimodal relationship with temperature as it warms. This highlights the importance of understanding the time scale of environmental change in relation to that of immediate physiological responses, acclimation, adaptation and community reorganization for the specific prediction about climate change impacts.

In natural systems, climate warming may also result in stronger food limitation^{71,73}. Hence, as optimum growth temperatures decline not only with size but also food availability^{67,74}, and realized consumption rates are a fraction of the maximum consumption rate (20-70%) (Kitchell *et al.* 1977; Neuenfeldt *et al.* 2019), species may be negatively impacted by warming even when controlled experiments show they can maintain growth capacity at these temperatures. Supporting

this point is the observation that warming already has negative or lack of positive effects on body growth in populations living at the edge of their physiological tolerance in terms of growth ^{12,14}.

Whether the largest fish of a population will be the first to experience negative effects of warming, as suggested by our finding that optimum growth temperature declines with body size, depends on the environmental temperatures they typically experience compared to smaller conspecifics. They may for instance inhabit colder temperatures compared to small fish due to ontogenetic habitat shifts ^{75,76}; see also Heincke's law ^{77,78}. That said, there is already empirical evidence of the largest individuals in natural populations being the first to suffer from negative impacts of warming from heatwaves ⁷⁹, or not being able to benefit from warming ^{14,18}. Hence, assuming that warming affects all individuals of a population equally is a simplification that can bias predictions of the biological impacts of climate change.

The interspecific scaling of fundamental ecological processes with body mass and temperature has been used to predict the effects of warming on body size, size structure, and population and community dynamics ^{26,59,80,81}. We argue that a contributing factor to the discrepancy between mechanistic growth models, general scaling theory, and empirical data has been the lack of data synthesis at the intraspecific level. The approach presented here can help overcome limitations of small data sets by borrowing information across species in a single modelling framework, while accounting for the intraspecific scaling of rates. Accounting for the faster increase in whole-organism metabolism than consumption with body size, the unimodal thermal response of consumption, and resulting size-dependence of optimum growth temperatures is essential for understanding what causes observed growth responses to global warming. Acknowledging these mechanisms is also important for improving predictions on the consequences of warming effects

on fish growth for food web functioning, fisheries yields and global food production in warmer climates.

Materials and methods

Data acquisition

We searched the literature for experimental studies evaluating the temperature response of individual maximum consumption rate (feeding rate at unlimited food supply, *ad libitum*), resting, routine and standard oxygen consumption rate as a proxy for metabolic rate⁸² and growth rates across individuals of different sizes within species. We used three different searches on the Web of Science Core Collection (see Supplement for details). In order to estimate how these rates depend on body size and temperature within species, we selected studies that experimentally varied both body size and temperature (at least two temperature treatments and at least two body masses). The average number of unique temperature treatments (temperature rounded to nearest °C) by species is 7.2 for growth and 4.3 for consumption and metabolism data). The criteria for both mass and temperature variation in the experiments reduces the number of potential data sets, as most experimental studies use either size or temperature treatments, not both. However, this criterion allows us to fit multiple regression models and estimate the effects of mass and temperature jointly, and to evaluate the probability of interactive mass- and temperature effects within species. Following common practice we excluded larval studies, which represents a life stage exhibiting different constraints and scaling relationships⁴⁰.

Studies were included if (i) a unique experimental temperature was recorded for each trial ($\pm 1^\circ\text{C}$), (ii) fish were provided food at *ad libitum* (consumption and growth data) or if they were unfed (resting, standard or routine metabolic rate), and (iii) fish exhibited normal behavior during

the experiments. We used only one study per species and rate to ensure that all data within a given species are comparable as measurements of these rates can vary between studies due to e.g. measurement bias, differences in experimental protocols, or because different populations were studied^{42,83}. In cases where we found more than one study for a given rate and species, we selected the most suitable study based on our pre-defined criteria (for details, see Supplement). We ensured that the experiments were conducted at ecologically relevant temperatures (Supplementary Figs. S1, S3). A more detailed description of the search protocol, data selection, acquisition, quality control, collation of additional information and standardizing of rates to common units can be found in Supplement.

We compiled four datasets: maximum consumption rate, metabolic rate, growth rate and the optimum growth temperature for each combination of body mass group and species. We compiled a total of 746 measurements of maximum consumption rate (of which 666 are below peak), 2699 measurements of metabolic rate and 227 measurements of growth rate (45 optimum temperatures) from published articles for each rate, from 20, 34 and 13 species, respectively, from different taxonomic groups, habitats and lifestyles (Table S1-S2). We requested original data from all corresponding authors of each article. In cases where we did not hear from the corresponding author, we extracted data from tables or figures using Web Plot Digitizer⁸⁴.

Model fitting

Model description

To each dataset, we fit hierarchical models with different combinations of species-varying coefficients, meaning they are estimated with shrinkage. This reduces the influence of outliers which could occur in species with small samples sizes^{85,86}. The general form of the model is:

$$y_{ij} \sim N(\mu_{ij}, \sigma) \quad (1)$$

$$\mu_{ij} = \beta_{0j} + \sum_{p=1}^n (\beta_p \times x_{ip}) \quad (2)$$

$$\beta_{0j} \sim N(\mu_{\beta_0}, \sigma_{\beta_0}) \quad (3)$$

where y_{ij} is the i th observation for species j for rate y , β_{0j} is a species-varying intercept, x_{ip} is a predictor and β_p is its coefficient, with $p = 1, \dots, n$, where n is the number of predictors considered in the model (mass, temperature, and their interaction). Predictors are mean centered to improve interpretability⁸⁷. Species-level intercepts follow a normal distribution with hyperparameters μ_{β_0} (global intercept) and σ_{β_0} (between-species standard deviation). For most models we also allow the coefficient β_p to vary between species, such that β_p becomes β_{pj} and x_{ip} becomes x_{ijp} , where $\beta_{pj} \sim N(\mu_{\beta_p}, \sigma_{\beta_p})$. For each dataset, we evaluate multiple combinations of species-varying coefficients (from varying intercept to n varying coefficients). We used a mix of flat, weakly informative, and non-informative priors. For the temperature and mass coefficients we used the predictions from the MTE as the means of the normal prior distributions¹, but with large standard deviations (see Supplementary Table S3). Below we describe how the model in Eqns. 1-3 is applied to each data set.

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Mass- and temperature dependence of consumption, metabolism and growth below peak temperatures

Peak temperatures (optimum in the case of growth) refer to the temperature at which the rate was maximized, by size group. For data below peak temperatures, we assumed that mass-specific maximum consumption rate, metabolism and growth scale allometrically (as a power function of the form $I = i_0 M^{b_0}$) with mass, and exponentially with temperature. Hence, after log-log (natural log) transformation of mass and the rate, and temperature in Arrhenius temperature ($1/kT$ in unit

eV⁻¹, where k is Boltzmann's constant [8.62×10^{-5} eV K⁻¹]), the relationship between the rate and its predictors becomes linear. This is similar to the MTE, except that we estimate all coefficients instead of correcting rates, and allow not only the intercepts but also slopes to vary across species.

When applied to Eqns. 1-3, y_{ij} is the i th observation for species j of the natural log of the rate (consumption, metabolism or growth), and the predictors are m_{ij} (natural log of body mass), $t_{A,ij}$ (Arrhenius temperature, $1/kT$ in unit eV⁻¹), both of which were mean-centered, and their interaction. Body mass is in g, consumption rate in g g⁻¹ day⁻¹, metabolic rate in mg O₂ g⁻¹ h⁻¹ and specific growth rate in unit % day⁻¹. We use resting or routine metabolism (mean oxygen uptake of a resting unfed fish only showing some spontaneous activity) and standard metabolism (resting unfed and no activity, usually inferred from extrapolation or from low quantiles of routine metabolism, e.g. lowest 10% of measurements) to represent metabolic rate^{88,89}. Routine and resting metabolism constitute 58% of the data used and standard metabolism constitutes 42%. We accounted for potential differences between these types of metabolic rate measurements by adding two dummy coded variables, $type_r$ and $type_s$, the former taking the value 0 for standard and 1 for a routine or resting metabolic rate measurement, and vice versa for the latter variable. Thus, for metabolism, we replace the overall intercept β_{0j} in Eqns. 2-3 with β_{0rj} and β_{0sj} . β_{0sj} is forced to 0 for a species that has a routine or resting metabolic rate and vice versa. We assume these coefficients vary by species following normal distributions with global means $\mu_{\beta_{0r}}$ and $\mu_{\beta_{0s}}$, and standard deviations $\sigma_{\beta_{0r}}$ and $\sigma_{\beta_{0s}}$, i.e. $\beta_{0rj} \sim N(\mu_{\beta_{0r}}, \sigma_{\beta_{0r}})$ and $\beta_{0sj} \sim N(\mu_{\beta_{0s}}, \sigma_{\beta_{0s}})$.

Mass- and temperature dependence of consumption including beyond peak temperatures

Over a large temperature range, many biological rates are unimodal. We identified such tendencies in 10 out of 20 species in the consumption data set. To characterize the decline in consumption

rate beyond peak temperature, we fit a mixed-effects version of the Sharpe Schoolfield equation⁵⁴ as parameterized in⁹⁰, to equations 1-2 with y_{ij} as rescaled consumption rates (C). Specifically, we model μ_{ij} in equation (1) with the Sharpe-Schoolfield equation:

$$\mu_{ij} = \frac{C_{0j}(T_C) e^{\frac{E_j}{kT_C} - \frac{1}{kT}}}{1 + e^{\frac{E_h}{kT_h} - \frac{1}{kT}}} \quad (4)$$

$$E_j \sim N(\mu_E, \sigma_E) \quad (5)$$

$$C_{0j} \sim N(\mu_{C_0}, \sigma_{C_0}) \quad (6)$$

where $C_{0j}(T_C)$ is the rate at a reference temperature T_C in Kelvin [K] (here set to 263.15), E_j [eV] is the activation energy, E_h [eV] characterizes the decline in the rate past the peak temperature and T_h [K] is the temperature at which the rate is reduced to half (of the rate in the absence of deactivation) due to high temperatures. We assume E_j and C_{0j} vary across species according to a normal distribution with means μ_E and μ_{C_0} , and standard deviations σ_E and σ_{C_0} , equation (5-6). Prior to rescaling maximum consumption (in unit g day^{-1}) by dividing $C_{i,j}$ with the mean within species \bar{C}_j , we mass-normalize it by dividing it with m^a where m is mass in g and a is the whole-organism mass-exponent calculated from the estimated mass-specific exponent with the log-linear model fitted to data below peak temperature. Temperature, T , is centered by subtracting the temperature at peak consumption estimated separately for each species using a linear model with a quadratic temperature term. The rescaling is done to control for differences between species with respect to the experimental temperatures relative to the temperature that maximizes their consumption rate such that data can be pooled.

Mass-dependence of optimum growth temperature

To evaluate how the optimum temperature ($t_{opt,ij}$, in degrees Celsius) for individual growth depends on body mass, we fit Eqns. 1-3 with y_{ij} as the mean-centered optimum growth temperature within species ($t_{opt,ij} = T_{opt,ij} - \bar{T}_{opt,j}$), to account for species being adapted to different thermal regimes. m_{ij} , the predictor variable for this model, is the natural log of the ratio between mass and mass at maturation within species: $m_{ij} = \ln(M_{ij}/M_{mat,j}) - \overline{\ln(M_{ij}/M_{mat,j})}$. This rescaling is done because we are interested in examining relationships within species over “ontogenetic size”, and because we do not expect an interspecific relationship between optimum growth temperature and body mass because species are adapted to different thermal regimes. We consider both the intercept and the effect of mass to potentially vary between species.

Parameter estimation

We fit the models in a Bayesian framework, using R version 4.0.2⁹¹ and JAGS⁹² through the R-package ‘rjags’⁹³. We used 3 Markov chains with 5000 iterations for adaptation, followed by 15000 iterations burn-in and 15000 iterations sampling where every 5th iteration saved. Model convergence was assessed by visually inspecting trace plots and potential scale reduction factors (\hat{R}) (Supplement). \hat{R} compares chain variance with the pooled variance, and values <1.1 suggest all three chains converged to a common distribution⁹⁴. We relied heavily on the R packages within ‘tidyverse’⁹⁵ for data processing, as well as ‘ggmcmc’⁹⁶, ‘mcmcviz’⁹⁷ and ‘bayesplot’⁹⁸ for visualization.

Model comparison

We compared the parsimony of models with different hierarchical structures, and with or without mass-temperature interactions, using the Watanabe-Akaike information criterion (WAIC)^{99,100},

which is based on the posterior predictive distribution. We report WAIC for each model described above (Table S4-S5), and examine models with ΔWAIC values < 2 , where ΔWAIC is each models difference to the lowest WAIC across models, in line with other studies¹⁰¹.

Net energy gain

The effect of temperature and mass dependence of maximum consumption and metabolism (proportional to biomass gain and losses, respectively)^{31,32,34} on growth is illustrated by visualizing the net energy gain. The model for the net energy gain (growth) can be viewed as a Pütter-type model, which is the result of two antagonistic allometric processes, biomass gains and biomass losses:

$$\frac{dM}{dt} = H(T)M^a - K(T)M^b \quad (7)$$

where M is body mass and T is temperature, H and K the allometric constants and a and b the exponents of the processes underlying gains and losses, respectively. We convert metabolism from oxygen consumption [$\text{mg O}_2 \text{ h}^{-1} \text{ day}^{-1}$] to g day^{-1} by assuming $1 \text{ kcal} = 295 \text{ mg O}_2$ (based on an oxycaloric coefficient of 14.2 J/mg O_2)¹⁰², $1 \text{ kcal} = 4184 \text{ J}$ and an energy content of 5600 J/g ¹⁰³, and convert consumption to g day^{-1} from $\text{g g}^{-1} \text{ day}^{-1}$. Consumption and metabolic rate are calculated for two sizes (5 and 1000 g, which roughly correspond to the 25th percentile of both datasets and the maximum mass in the consumption data, respectively), using the global allometric relationships found in the log-log models fit to sub-peak temperatures. These allometric functions are further scaled with the temperature correction factors r_c for consumption and r_m for metabolism. r_c is based on the Sharpe-Schoolfield model and r_m is given by the temperature dependence of metabolic rate from the log-linear model. Because r_c and r_m are fitted to data on different scales, we divide these functions by their maximum. Lastly, we rescale the product

between the allometric functions and r_c and r_m such that the rate at 19°C (mean temperature in both data sets) equals the temperature-independent rate.

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Author contributions

ML conceived the study; ML, JO, AG designed research; ML performed research with input from JO and AG; ML, JO, AG wrote the paper and contributed to revisions of the manuscript.

Data accessibility statement

All data and R code (lists of studies in literature search, data preparation, analyses and figures) can be downloaded from a GitHub repository (<https://github.com/maxlindmark/scaling>) and will be archived on Zenodo upon publication.

References

1. Brown, J. H., Gillooly, J. F., Allen, A. P., Savage, V. M. & West, G. B. Toward a metabolic theory of ecology. *Ecology* **85**, 1771–1789 (2004).

- 458 2. Savage, V. M., Gillooly, J. F., Brown, J. H., West, G. B. & Charnov, E. L. Effects of body
459 size and temperature on population growth. *The American Naturalist* **163**, 429–441 (2004).
- 460 3. Andersen, K. H., Beyer, J. E. & Lundberg, P. Trophic and individual efficiencies of size-
461 structured communities. *Proceedings of the Royal Society B: Biological Sciences* **276**, 109–
462 114 (2009).
- 463 4. Barneche, D. R. & Allen, A. P. The energetics of fish growth and how it constrains food-
464 web trophic structure. *Ecology Letters* **21**, 836–844 (2018).
- 465 5. Daufresne, M., Lengfellner, K. & Sommer, U. Global warming benefits the small in aquatic
466 ecosystems. *Proceedings of the National Academy of Sciences, USA* **106**, 12788–12793
467 (2009).
- 468 6. Gardner, J. L., Peters, A., Kearney, M. R., Joseph, L. & Heinsohn, R. Declining body size:
469 a third universal response to warming? *Trends in Ecology & Evolution* **26**, 285–291 (2011).
- 470 7. Atkinson, D. Temperature and organism size—A biological law for ectotherms? in
471 *Advances in Ecological Research* vol. 25 1–58 (Elsevier, 1994).
- 472 8. Ohlberger, J. Climate warming and ectotherm body size – from individual physiology to
473 community ecology. *Functional Ecology* **27**, 991–1001 (2013).
- 474 9. Horne, C. R., Hirst, Andrew. G. & Atkinson, D. Temperature-size responses match
475 latitudinal-size clines in arthropods, revealing critical differences between aquatic and
476 terrestrial species. *Ecology Letters* **18**, 327–335 (2015).
- 477 10. Forster, J., Hirst, A. G. & Atkinson, D. Warming-induced reductions in body size are
478 greater in aquatic than terrestrial species. *PNAS* **109**, 19310–19314 (2012).
- 479 11. Thresher, R. E., Koslow, J. A., Morison, A. K. & Smith, D. C. Depth-mediated reversal of
480 the effects of climate change on long-term growth rates of exploited marine fish.
481 *Proceedings of the National Academy of Sciences, USA* **104**, 7461–7465 (2007).
- 482 12. Neuheimer, A. B., Thresher, R. E., Lyle, J. M. & Semmens, J. M. Tolerance limit for fish
483 growth exceeded by warming waters. *Nature Climate Change* **1**, 110–113 (2011).
- 484 13. Baudron, A. R., Needle, C. L., Rijnsdorp, A. D. & Marshall, C. T. Warming temperatures
485 and smaller body sizes: synchronous changes in growth of North Sea fishes. *Global Change*
486 *Biology* **20**, 1023–1031 (2014).
- 487 14. Huss, M., Lindmark, M., Jacobson, P., Van Dorst, R. M. & Gårdmark, A. Experimental
488 evidence of gradual size-dependent shifts in body size and growth of fish in response to
489 warming. *Glob Change Biol* **25**, 2285–2295 (2019).
- 490 15. Ikpewe, I. E., Baudron, A. R., Ponchon, A. & Fernandes, P. G. Bigger juveniles and smaller
491 adults: Changes in fish size correlate with warming seas. *Journal of Applied Ecology* **Early**
492 **View**, (2020).
- 493 16. van Rijn, I., Buba, Y., DeLong, J., Kiflawi, M. & Belmaker, J. Large but uneven reduction
494 in fish size across species in relation to changing sea temperatures. *Global Change Biology*
495 **23**, 3667–3674 (2017).
- 496 17. Barneche, D. R., Jahn, M. & Seebacher, F. Warming increases the cost of growth in a
497 model vertebrate. *Functional Ecology* **33**, 1256–1266 (2019).
- 498 18. Van Dorst, R. M. *et al.* Warmer and browner waters decrease fish biomass production.
499 *Global Change Biology* **25**, 1395–1408 (2019).
- 500 19. Audzijonyte, A. *et al.* Fish body sizes change with temperature but not all species shrink
501 with warming. *Nat Ecol Evol* **4**, 809–814 (2020).

20. Denderen, D. van, Gislason, H., Heuvel, J. van den & Andersen, K. H. Global analysis of fish growth rates shows weaker responses to temperature than metabolic predictions. *Global Ecology and Biogeography* **29**, 2203–2213 (2020).
21. Wang, H.-Y., Shen, S.-F., Chen, Y.-S., Kiang, Y.-K. & Heino, M. Life histories determine divergent population trends for fishes under climate warming. *Nature Communications* **11**, 4088 (2020).
22. Audzijonyte, A. *et al.* Is oxygen limitation in warming waters a valid mechanism to explain decreased body sizes in aquatic ectotherms? *Global Ecology and Biogeography* **28**, 64–77 (2019).
23. Neubauer, P. & Andersen, K. H. Thermal performance of fish is explained by an interplay between physiology, behaviour and ecology. *Conserv Physiol* **7**, (2019).
24. Pütter, A. Studien über physiologische Ähnlichkeit VI. Wachstumsähnlichkeiten. *Pflügers Arch.* **180**, 298–340 (1920).
25. von Bertalanffy, L. Laws in metabolism and growth. *The quarterly review of biology* **32**, 217–231 (1957).
26. Morita, K., Fukuwaka, M., Tanimata, N. & Yamamura, O. Size-dependent thermal preferences in a pelagic fish. *Oikos* **119**, 1265–1272 (2010).
27. Pauly, D. & Cheung, W. W. L. Sound physiological knowledge and principles in modeling shrinking of fishes under climate change. *Global Change Biology* **24**, e15–e26 (2018).
28. Pauly, D. The gill-oxygen limitation theory (GOLT) and its critics. *Science Advances* **7**, eabc6050 (2021).
29. Lefevre, S., McKenzie, D. J. & Nilsson, G. E. In modelling effects of global warming, invalid assumptions lead to unrealistic projections. *Global Change Biology* **24**, 553–556 (2018).
30. Marshall, D. J. & White, C. R. Have we outgrown the existing models of growth? *Trends in Ecology & Evolution* **34**, 102–111 (2019).
31. Ursin, E. A Mathematical Model of Some Aspects of Fish Growth, Respiration, and Mortality. *Journal of the Fisheries Research Board of Canada* **24**, 2355–2453 (1967).
32. Kitchell, J. F., Stewart, D. J. & Weininger, D. Applications of a bioenergetics model to yellow perch (*Perca flavescens*) and walleye (*Stizostedion vitreum vitreum*). *Journal of the Fisheries Board of Canada* **34**, 1922–1935 (1977).
33. Jobling, M. Temperature and growth: modulation of growth rate via temperature change. in *Global Warming: Implications for Freshwater and Marine Fish* (eds. Wood, C. M. & McDonald, D. G.) vol. 61 225–254 (Cambridge University Press, 1997).
34. Essington, T. E., Kitchell, J. F. & Walters, C. J. The von Bertalanffy growth function, bioenergetics, and the consumption rates of fish. *Canadian Journal of Fisheries and Aquatic Sciences* **58**, 2129–2138 (2001).
35. Kooijman, S. A. L. M. *Dynamic energy budgets in biological systems*. (Cambridge University Press, 1993).
36. de Roos, A. M. & Persson, L. Physiologically structured models – from versatile technique to ecological theory. *Oikos* **94**, 51–71 (2001).
37. Hartvig, M., Andersen, K. H. & Beyer, J. E. Food web framework for size-structured populations. *Journal of Theoretical Biology* **272**, 113–122 (2011).
38. Maury, O. & Poggiale, J.-C. From individuals to populations to communities: A dynamic energy budget model of marine ecosystem size-spectrum including life history diversity. *Journal of Theoretical Biology* **324**, 52–71 (2013).

- 548 39. Blanchard, J. L., Heneghan, R. F., Everett, J. D., Trebilco, R. & Richardson, A. J. From
549 bacteria to Whales: Using functional size spectra to model marine ecosystems. *Trends in*
550 *Ecology & Evolution* **32**, 174–186 (2017).
- 551 40. Glazier, D. S. Beyond the ‘3/4-power law’: variation in the intra- and interspecific scaling
552 of metabolic rate in animals. *Biological Reviews of the Cambridge Philosophical Society*
553 **80**, 611–662 (2005).
- 554 41. Rall, B. C. *et al.* Universal temperature and body-mass scaling of feeding rates.
555 *Philosophical Transactions of the Royal Society of London, Series B: Biological Sciences*
556 **367**, 2923–2934 (2012).
- 557 42. Jerde, C. L. *et al.* Strong Evidence for an Intraspecific Metabolic Scaling Coefficient Near
558 0.89 in Fish. *Front. Physiol.* **10**, 1166 (2019).
- 559 43. Gillooly, J. F., Brown, J. H., West, G. B., Savage, V. M. & Charnov, E. L. Effects of size
560 and temperature on metabolic rate. *Science* 2248–2251. (2001).
- 561 44. Downs, C. J., Hayes, J. P. & Tracy, C. R. Scaling metabolic rate with body mass and
562 inverse body temperature: A test of the Arrhenius fractal supply model. *Functional Ecology*
563 **22**, 239–244 (2008).
- 564 45. Clarke, A. & Johnston, N. M. Scaling of metabolic rate with body mass and temperature in
565 teleost fish. *Journal of Animal Ecology* **68**, 893–905 (1999).
- 566 46. Bokma, F. Evidence against universal metabolic allometry. *Functional Ecology* **18**, 184–
567 187 (2004).
- 568 47. Dell, A. I., Pawar, S. & Savage, V. M. Systematic variation in the temperature dependence
569 of physiological and ecological traits. *Proceedings of the National Academy of Sciences*
570 **108**, 10591–10596 (2011).
- 571 48. Englund, G., Öhlund, G., Hein, C. L. & Diehl, S. Temperature dependence of the functional
572 response. *Ecology Letters* **14**, 914–921 (2011).
- 573 49. Uiterwaal, S. F. & DeLong, J. P. Functional responses are maximized at intermediate
574 temperatures. *Ecology* **101**, e02975 (2020).
- 575 50. Xie, Xiaojun. & Sun, Ruyung. The Bioenergetics of the Southern Catfish (*Silurus*
576 *meridionalis* Chen). I. Resting Metabolic Rate as a Function of Body Weight and
577 Temperature. *Physiological Zoology* **63**, 1181–1195 (1990).
- 578 51. García García, B., Cerezo Valverde, J., Aguado-Giménez, F., García García, J. &
579 Hernández, M. D. Effect of the interaction between body weight and temperature on growth
580 and maximum daily food intake in sharpsnout sea bream (*Diplodus puntazzo*). *Aquaculture*
581 *International* **19**, 131–141 (2011).
- 582 52. Ohlberger, J., Mehner, Thomas., Staaks, Georg. & Hölker, Franz. Intraspecific temperature
583 dependence of the scaling of metabolic rate with body mass in fishes and its ecological
584 implications. *Oikos* **121**, 245–251 (2012).
- 585 53. Lindmark, M., Huss, M., Ohlberger, J. & Gårdmark, A. Temperature-dependent body size
586 effects determine population responses to climate warming. *Ecology Letters* **21**, 181–189
587 (2018).
- 588 54. Schoolfield, R. M., Sharpe, P. J. H. & Magnuson, C. E. Non-linear regression of biological
589 temperature-dependent rate models based on absolute reaction-rate theory. *Journal of*
590 *Theoretical Biology* **88**, 719–731 (1981).
- 591 55. Pauly, D. & Cheung, W. W. L. On confusing cause and effect in the oxygen limitation of
592 fish. *Global Change Biology* **24**, e743–e744 (2018).

56. Lemoine, N. P. & Burkepile, D. E. Temperature-induced mismatches between consumption and metabolism reduce consumer fitness. *Ecology* **93**, 2483–2489 (2012).
57. Rall, B. C., Vucic-Pestic, O., Ehnes, R. B., Emmerson, M. & Brose, U. Temperature, predator–prey interaction strength and population stability. *Global Change Biology* **16**, 2145–2157 (2010).
58. Angilletta, M. J. & Dunham, A. E. The temperature-size rule in ectotherms: simple evolutionary explanations may not be general. *The American Naturalist* **162**, 332–342 (2003).
59. Vasseur, D. A. & McCann, K. S. A mechanistic approach for modelling temperature-dependent consumer-resource dynamics. *The American Naturalist* **166**, 184–198 (2005).
60. Fussmann, K. E., Schwarzmüller, F., Brose, U., Jousset, A. & Rall, B. C. Ecological stability in response to warming. *Nature Climate Change* **4**, 206–210 (2014).
61. Lindmark, M., Ohlberger, J., Huss, M. & Gårdmark, A. Size-based ecological interactions drive food web responses to climate warming. *Ecology Letters* **22**, 778–786 (2019).
62. Wyban, J., Walsh, W. A. & Godin, D. M. Temperature effects on growth, feeding rate and feed conversion of the Pacific white shrimp (*Penaeus vannamei*). *Aquaculture* **138**, 267–279 (1995).
63. Panov, V. E. & McQueen, D. J. Effects of temperature on individual growth rate and body size of a freshwater amphipod. **76**, 1107–1116 (1998).
64. Steinarsson, A. & Imsland, A. K. Size dependent variation in optimum growth temperature of red abalone (*Haliotis rufescens*). *Aquaculture* **224**, 353–362 (2003).
65. Björnsson, B., Steinarsson, A. & Arnason, T. Growth model for Atlantic cod (*Gadus morhua*): Effects of temperature and body weight on growth rate. *Aquaculture* **271**, 216–226 (2007).
66. Handeland, S. O., Imsland, A. K. & Stefansson, S. O. The effect of temperature and fish size on growth, feed intake, food conversion efficiency and stomach evacuation rate of Atlantic salmon post-smolts. *Aquaculture* **283**, 36–42 (2008).
67. Brett, J. R., Shelbourn, J. E. & Shoop, C. T. Growth rate and body composition of fingerling sockeye salmon, *Oncorhynchus nerka*, in relation to temperature and ration size. *J. Fish. Res. Bd. Can.* **26**, 2363–2394 (1969).
68. Elliott, J. M. & Hurley, M. A. The functional relationship between body size and growth rate in fish. *Functional Ecology* **9**, 625 (1995).
69. Barneche, D. R., Robertson, D. R., White, C. R. & Marshall, D. J. Fish reproductive-energy output increases disproportionately with body size. *Science* **360**, 642–645 (2018).
70. Lorenzen, K. The relationship between body weight and natural mortality in juvenile and adult fish: a comparison of natural ecosystems and aquaculture. *Journal of Fish Biology* **49**, 627–642 (1996).
71. Huey, R. B. & Kingsolver, J. G. Climate warming, resource availability, and the metabolic meltdown of ectotherms. *The American Naturalist* **194**, E140–E150 (2019).
72. Neuenfeldt, S. *et al.* Feeding and growth of Atlantic cod (*Gadus morhua* L.) in the eastern Baltic Sea under environmental change. *ICES Journal of Marine Science* **77**, 624–632 (2020).
73. Ohlberger, J., Edeline, E., Vollestad, L. A., Stenseth, N. C. & Claessen, D. Temperature-driven regime shifts in the dynamics of size-structured populations. *The American Naturalist* **177**, 211–223 (2011).

- 638 74. Brett, J. R. Energetic responses of salmon to temperature. A study of some thermal relations
639 in the physiology and freshwater ecology of sockeye salmon (*Oncorhynchus nerka*). *Integr*
640 *Comp Biol* **11**, 99–113 (1971).
- 641 75. Werner, E. E. & Hall, D. J. Ontogenetic habitat shifts in bluegill: The foraging rate-
642 predation risk trade-off. *Ecology* **69**, 1352–1366 (1988).
- 643 76. Lloret-Lloret, E. *et al.* The seasonal distribution of a highly commercial fish is related to
644 ontogenetic changes in its feeding strategy. *Front. Mar. Sci.* **7**, (2020).
- 645 77. Heincke, F. Rapp. Proc. Verb. Réunion. ICES 16, 1–70. (1913).
- 646 78. Audzijonyte, A. & Pecl, G. T. Deep impact of fisheries. *Nature Ecology & Evolution* **2**,
647 1348–1349 (2018).
- 648 79. Pörtner, H. O. & Knust, R. Climate change affects marine fishes through the oxygen
649 limitation of thermal tolerance. *Science* **315**, 95–97 (2007).
- 650 80. Cheung, W. W. L. *et al.* Shrinking of fishes exacerbates impacts of global ocean changes on
651 marine ecosystems. *Nature Climate Change* **3**, 254–258 (2013).
- 652 81. Gilbert, B. *et al.* A bioenergetic framework for the temperature dependence of trophic
653 interactions. *Ecology Letters* **17**, 902–914 (2014).
- 654 82. Nelson, J. A. Oxygen consumption rate v. rate of energy utilization of fishes: a comparison
655 and brief history of the two measurements. *Journal of Fish Biology* **88**, 10–25 (2016).
- 656 83. Armstrong, J. D. & Hawkins, L. A. Standard metabolic rate of pike, *Esox lucius*: variation
657 among studies and implications for energy flow modelling. *Hydrobiologia* **601**, 83–90
658 (2008).
- 659 84. Rohatgi, A. *WebPlotDigitalizer: HTML5 based online tool to extract numerical data from*
660 *plot images. Version 4.1. [WWW document] URL <https://automeris.io/WebPlotDigitizer>*
661 *(accessed on January 2019)*. (2012).
- 662 85. Gelman, A. & Hill, J. *Data Analysis Using Regression and Multilevel/Hierarchical Models*.
663 (Cambridge University Press, 2007).
- 664 86. Harrison, X. A. *et al.* A brief introduction to mixed effects modelling and multi-model
665 inference in ecology. *PeerJ* **6**, e4794 (2018).
- 666 87. Schielzeth, H. Simple means to improve the interpretability of regression coefficients:
667 Interpretation of regression coefficients. *Methods in Ecology and Evolution* **1**, 103–113
668 (2010).
- 669 88. Beamish, F. W. H. Respiration of fishes with special emphasis on standard oxygen
670 consumption II. Influence of weight and temperature on respiration of several species'.
671 *Canadian Journal of Zoology/Revue Canadienne de Zoologie* **42**, 177–188 (1964).
- 672 89. Ohlberger, J., Staaks, G. & Hölker, F. Effects of temperature, swimming speed and body
673 mass on standard and active metabolic rate in vendace (*Coregonus albula*). *Journal of*
674 *Comparative Physiology, B* **177**, 905–916 (2007).
- 675 90. Padfield, D., Castledine, M. & Buckling, A. Temperature-dependent changes to host-
676 parasite interactions alter the thermal performance of a bacterial host. *The ISME Journal*
677 **14**, 389–398 (2020).
- 678 91. R Core Team. *R: A Language and Environment for Statistical Computing. R Foundation for*
679 *Statistical Computing*. (2020).
- 680 92. Plummer, M. JAGS: A program for analysis of Bayesian graphical models using Gibbs
681 sampling. *Working Papers* **8** (2003).
- 682 93. Plummer, M. *rjags*. (2019).

94. Gelman, A., Carlin, J., Stern, H. & Rubin, D. *Bayesian Data Analysis. 2nd edition.* (Chapman and Hall/CRC, 2003).
95. Wickham, H. *et al.* Welcome to the tidyverse. *Journal of Open Source Software* 1686 (2019) doi:<https://doi.org/10.21105/joss.01686>.
96. Fernández-i-Marín, X. ggmcmc: Analysis of MCMC Samples and Bayesian Inference. *Journal of Statistical Software* **70**, 1–20 (2016).
97. Youngflesh, C. MCMCvis: Tools to Visualize, Manipulate, and Summarize MCMC Output. *Journal of Open Source Software* **3**, 640 (2018).
98. Gabry, J., Simpson, D., Vehtari, A., Betancourt, M. & Gelman, A. Visualization in Bayesian workflow. *J. R. Stat. Soc. A* **182**, 389–402 (2019).
99. Watanabe, S. A Widely Applicable Bayesian Information Criterion. *Journal of Machine Learning Research* **14**, 867–897 (2013).
100. Vehtari, A., Gelman, A. & Gabry, J. Practical Bayesian model evaluation using leave-one-out cross-validation and WAIC. *Stat Comput* **27**, 1413–1432 (2017).
101. Olmos, M. *et al.* Spatial synchrony in the response of a long range migratory species (*Salmo salar*) to climate change in the North Atlantic Ocean. *Global Change Biology* **26**, 1319–1337 (2019).
102. Hepher, B. *Nutrition of Pond Fishes.* (Cambridge University Press, 1988).
103. Rijnsdorp, A. D. & Ibelings, B. Sexual dimorphism in the energetics of reproduction and growth of North Sea plaice, *Pleuronectes platessa* L. *Journal of Fish Biology* **35**, 401–415 (1989).

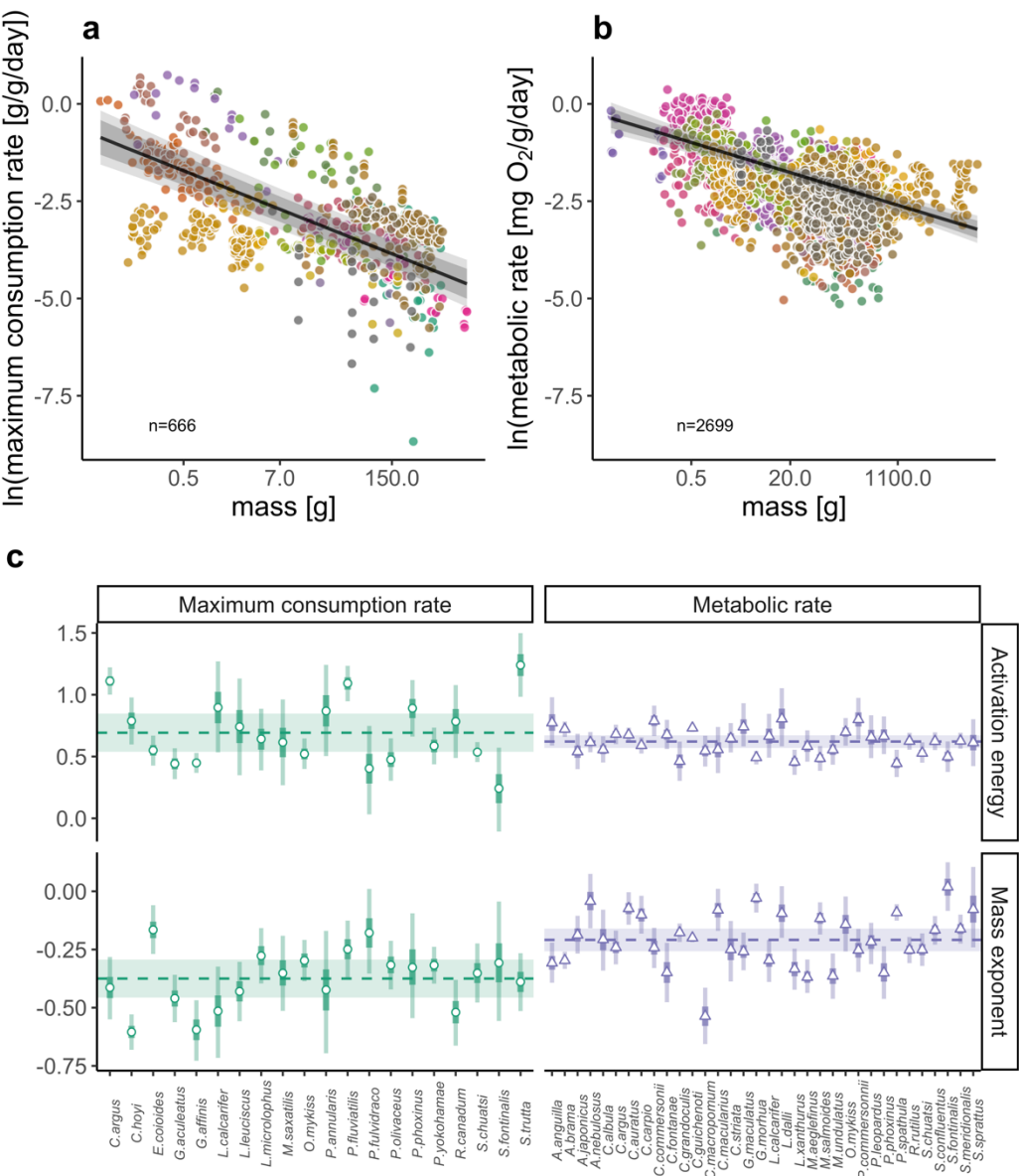


Figure 1. Natural log of mass-specific maximum consumption rate (A) and metabolic rate (B) against body mass on a logarithmic x-axis. Lines are global predictions at the average temperature in each data set (both 19°C, but note the model is fitted using mean-centred Arrhenius temperature). Shaded areas correspond to 80% and 95% credible intervals. Species are grouped by color (legend not shown, n=20 for consumption and n=34 for metabolism, respectively). C)

713 *Global and species-level effects of mass- and temperature on specific maximum consumption rate*
714 *and metabolic rate. Horizontal lines show the posterior medians of the global activation energies*
715 *and mass exponents of maximum consumption and metabolism (μ_{β_1} and μ_{β_2} in Eqs. 6-8 for the*
716 *mass and temperature coefficients, respectively). The shaded horizontal rectangles correspond to*
717 *the posterior median ± 2 standard deviations. Points and triangles show the posterior medians for*
718 *each species-level coefficient (for maximum consumption rate and metabolic rate, respectively),*
719 *and the vertical bars show their 80% and 95% credible interval.*

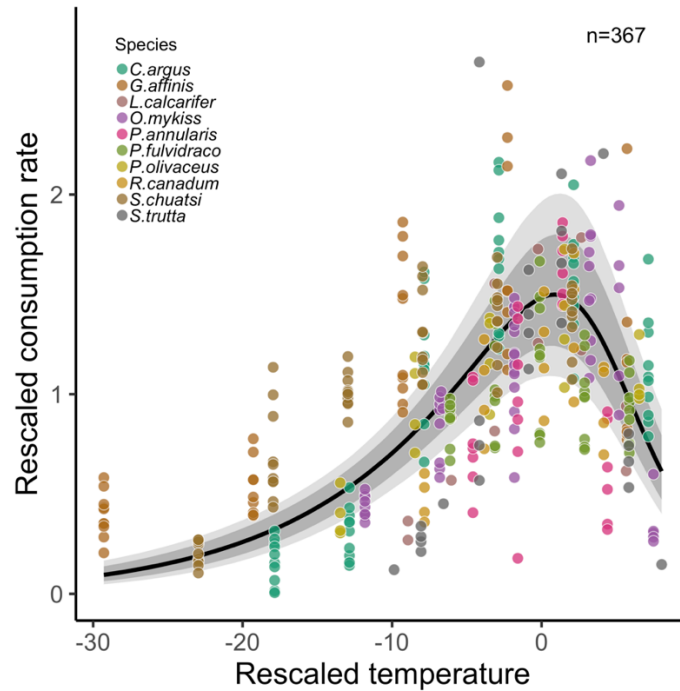


Figure 2. Mass-specific maximum consumption rate increases until a maximum is reached, after which it declines steeper than the initial rate of increase. Maximum consumption rates are relative to the average maximum consumption rates within species and temperature is the difference between the experimental temperature and the temperature where maximum consumption peaks (also by species). Lines show posterior median of predictions from the Sharpe-Schoolfield model (using the average intercept across species and the common coefficients), grey bands show 95% and 80% credible intervals. Colors indicate species.

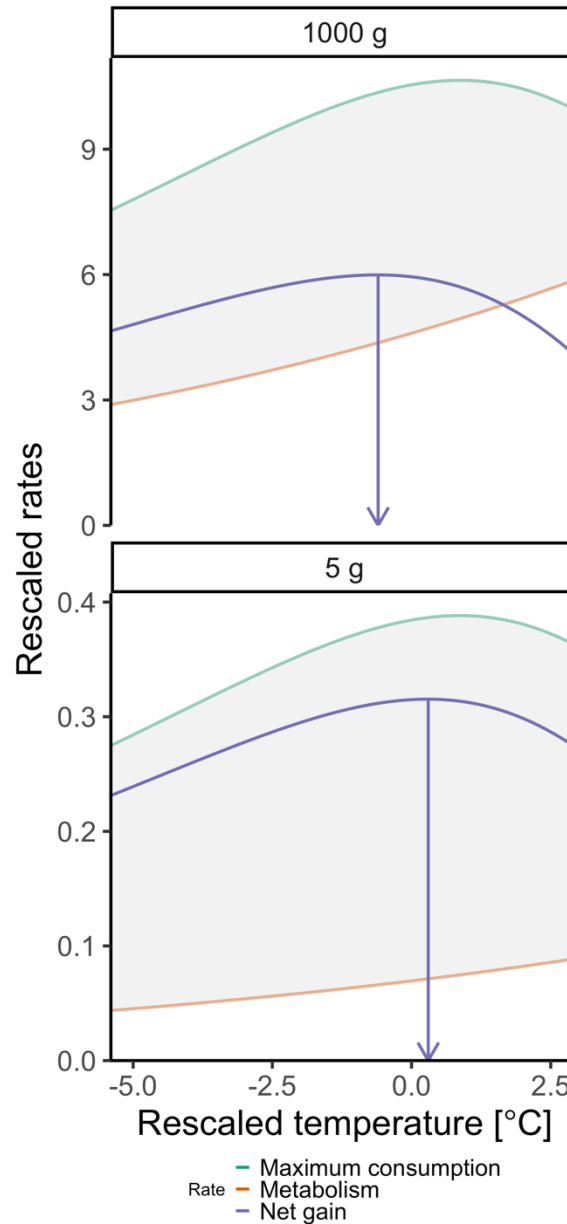


Figure 3. Illustration of predicted whole-organism maximum consumption rate (green), metabolic rate (purple) and the difference between them (orange) for two body sizes (top=1000g, bottom=5g) (see 'Materials and Methods'). Vertical arrows indicate the temperature where the difference in net energy gain (energy available for growth) is maximized for the two body sizes, which occurs at different temperatures despite that consumption peaks at the same temperature for both body sizes.

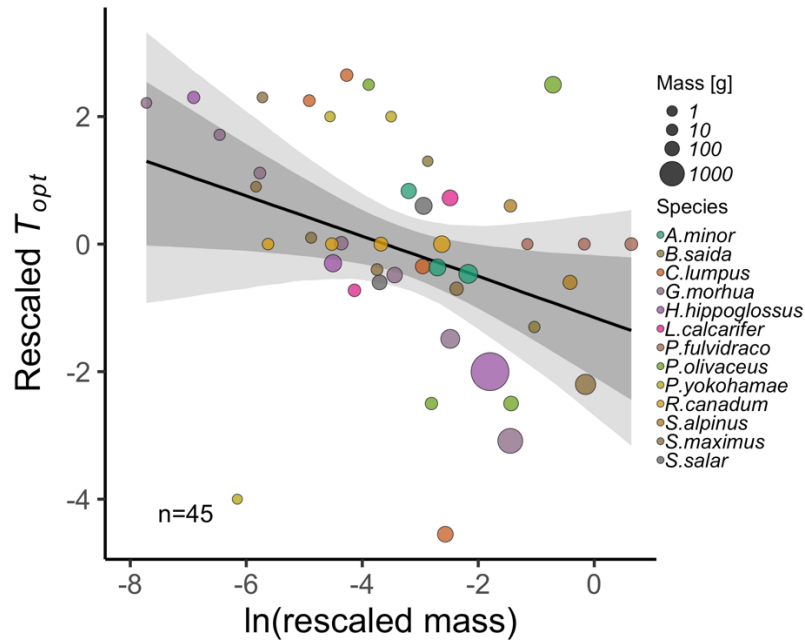


Figure 4. Experimental data demonstrating optimum growth temperature declines with body mass. The plot shows the optimum temperature within species (rescaled by subtracting the mean optimum temperature from each observation, by species) as a function of the natural log of rescaled body mass (ratio of mass to maturation mass within species). Probability bands represent 80% and 95% credible intervals, and the solid line shows the global prediction (μ_{β_0} and μ_{β_1}). Colors indicate species and the area of the circle corresponds to body mass in unit g.