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Optimum growth temperature declines with body size within fish species

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## Abstract

According to the temperature-size rule, warming of aquatic ecosystems is generally predicted to increase individual growth rates but reduce asymptotic body sizes of ectotherms. However, we lack a comprehensive understanding of how growth and key processes affecting it, such as consumption and metabolism, depend on both temperature and body mass within species. This limits our ability to inform growth models, link experimental data to observed growth patterns, and advance mechanistic food web models. To examine the combined effects of body size and temperature on individual growth, as well as the link between maximum consumption, metabolism and body growth, we conducted a systematic review and compiled experimental data on fishes from 59 studies that combined body mass and temperature treatments. By fitting hierarchical models accounting for variation between species, we estimated how these three processes scale jointly with temperature and body mass within species. We found that whole-organism maximum consumption increases more slowly with body mass than metabolism, and is unimodal over the full temperature range, which leads to the prediction that optimum growth temperatures decline with body size. Using an independent dataset, we confirmed this negative relationship between optimum growth temperature and size within fish species. Small individuals may therefore exhibit increased growth with initial warming, whereas larger conspecifics could be the first to experience negative impacts of warming on growth. These findings help advance mechanistic models of individual growth and food web dynamics and improve our understanding of how climate warming affects the growth and size structure of aquatic ectotherms.

## **Significance statement**

Predicting organism responses to a warming climate requires understanding how physiological processes such as feeding, metabolism, and growth depend on body size and temperature. Common growth models predict declining optimum growth temperatures with body size if energetic costs (metabolism) increase faster than gains (feeding) with body size. However, the generality of these features has not been evaluated at the within-species level. By collating data on fish through a systematic literature review, we find support for both declining net energy gain and declining optimum growth temperatures with body size. This implies large individuals within populations may be the first to suffer poor growth due to warming, with consequences for fisheries yield and food web structure in warmer climates.

## Introduction

Individual body growth is a fundamental process powered by metabolism, and thus depends on body size and temperature (Brown *et al.* 2004). It affects individual fitness and life history traits, such as maturation size, population growth rates (Savage *et al.* 2004), and ultimately energy transfer across trophic levels (Andersen *et al.* 2009; Barneche & Allen 2018). Therefore, understanding how growth scales with body size and temperature is important for predicting the impacts of global warming on the structure and functioning of ecosystems.

Global warming is predicted to lead to declining body sizes of organisms (Daufresne *et al.* 2009; Gardner *et al.* 2011). The temperature size-rule ('TSR') states that warmer rearing temperatures lead to faster developmental times (and larger initial size-at-age or size-at-life-stage), but smaller adult body sizes in ectotherms (Atkinson 1994; Ohlberger 2013). This relationship is found in numerous experimental studies (Atkinson 1994), is reflected in latitudinal gradients (Horne *et al.* 2015), and is stronger in aquatic than terrestrial organisms (Forster *et al.* 2012; Horne *et al.* 2015). Support for the TSR exists in fishes, in particular in young fish, where reconstructed individual growth histories often reveal positive correlations between growth rates and temperature in natural systems (Thresher *et al.* 2007; Neuheimer *et al.* 2011; Baudron *et al.* 2014; Huss *et al.* 2019). However, whether the positive effect of warming on growth is indeed limited to small individuals within a species, as predicted by the temperature size-rule, is less clear. Negative correlations between maximum size, asymptotic size or size-at-age of old fish and temperature have been found in commercially exploited fish species (Baudron *et al.* 2014; van Rijn *et al.* 2017; Ikpewe *et al.* 2020). However, other studies, including large scale experiments, controlled experiments and latitudinal studies or observational data on unexploited species, have failed to find negative relationships between maximum size, growth of old fish or mean size and

temperature (Barneche *et al.* 2019; Huss *et al.* 2019; Van Dorst *et al.* 2019; Audzijonyte *et al.* 2020; Denderen *et al.* 2020) and differences between species may be related to life history traits and depend on local environmental conditions (Denderen *et al.* 2020; Wang *et al.* 2020).

While the support for TSR is mixed, and the underlying mechanisms are not well understood (Ohlberger 2013; Audzijonyte *et al.* 2019; Neubauer & Andersen 2019), theoretical growth models, such as Pütter growth models (Pütter 1920), including the von Bertalanffy growth model (VBGM) (von Bertalanffy 1957), commonly predict declines in asymptotic body mass with temperature and declines in optimum growth temperature with body mass, in line with the TSR (Morita *et al.* 2010; Pauly & Cheung 2018b; Pauly 2021). Yet, the physiological basis of these models has been questioned, as the commonly applied scaling parameters (mass exponents) tend to differ from empirical estimates (Lefevre *et al.* 2018; Marshall & White 2019). Hence, despite attempting to describe growth from first principles, Pütter growth models can also be viewed as phenomenological. In more mechanistic growth models, the difference between energy gain and expenditure is partitioned between somatic growth and gonads (Ursin 1967; Kitchell *et al.* 1977; Jobling 1997; Essington *et al.* 2001). Energy gain is normally the amount of energy extracted from consumed food and expenditure is defined as maintenance, activity and feeding metabolism. These components of the energetics of growth are found in dynamic energy budget models (Kitchell *et al.* 1977; Kooijman 1993), including physiologically structured population models (PSPMs) (de Roos & Persson 2001), and size-spectrum models (Hartvig *et al.* 2011; Maury & Poggiale 2013; Blanchard *et al.* 2017). Therefore, it is important to understand how consumption and metabolism rates scale with body mass and temperature in order to understand if and how growth of large fish within populations is limited by temperature, and to evaluate the physiological basis of growth models.

Moreover, the effect of body mass and temperature on growth dynamics should be evaluated over ontogeny at the intraspecific level (within species), which better represents the underlying process than interspecific data (among species) (Marshall & White 2019). For instance, we do not expect an interspecific relationship between optimum growth temperature and body mass, but within species it may have a large effect on growth dynamics. Despite this, intraspecific body mass and temperature scaling is often inferred from interspecific data, and we know surprisingly little about average relationship between consumption and metabolic exponents within species (Marshall & White 2019). Importantly, how physiological rates depend on mass and temperature within species can differ from the same relationships across species (Glazier 2005; Rall *et al.* 2012; Jerde *et al.* 2019). Across species, rates are often assumed and found to scale as power functions of mass with exponents of  $3/4$  for whole organism rates ( $-1/4$  for mass-specific rates), exponentially with temperature, and with independent mass and temperature effects (e.g., in the Arrhenius fractal supply model (AFS) applied in the metabolic theory of ecology, MTE (Gillooly *et al.* 2001; Brown *et al.* 2004; Downs *et al.* 2008)). In contrast, within species deviations from a general  $3/4$  mass exponent are common (Clarke & Johnston 1999; Bokma 2004; Jerde *et al.* 2019), rates are typically unimodal (Dell *et al.* 2011; Englund *et al.* 2011; Rall *et al.* 2012; Uiterwaal & DeLong 2020) and the effects of mass and temperature can be interactive (Xie & Sun 1990; Glazier 2005; García García *et al.* 2011; Ohlberger *et al.* 2012; Lindmark *et al.* 2018) (but see Jerde *et al.* (2019)). Alternative approaches that overcome these obstacles include fitting multiple regression models where coefficients for mass and temperature are estimated jointly (Downs *et al.* 2008), as well as fitting non-linear or polynomial models that can capture the de-activation of biological rates at higher temperatures (Schoolfield *et al.* 1981; Dell *et al.* 2011; Englund *et al.* 2011). This requires intraspecific data with variation in both mass and temperature.

In this study, we analyze how maximum consumption, metabolism and growth rate of fish scale intraspecifically with mass and temperature. We performed a systematic literature review by searching the Web of Science Core Collection to compile datasets on individual-level maximum consumption, metabolism and growth rates of fish from experiments in which the effect of fish body mass is replicated across multiple temperatures within species (total  $n=3672$ , with data from 13, 20 and 34 species for each rate, respectively). We then fit hierarchical Bayesian models to estimate general intraspecific scaling parameters while accounting for variation between species. The estimated mass dependence and temperature sensitivity of mass-specific consumption and metabolism are used to quantify average changes in net energy gain (and hence, growth, assumed proportional to net energy gain) over temperature and body mass. Lastly, we compare our predicted changes in optimum growth temperature over body mass with an independent experimental dataset on optimum growth temperatures across individuals of different sizes within species.

## Results

We identified that within species of fish, mass-specific metabolic rates increase faster with body mass than maximum consumption rates, and neither of these rates conform to the commonly predicted  $-1/4$  scaling with body mass (Fig. 1). We also quantified the unimodal relationship of consumption rate over the full temperature range (Fig. 2). Combined, these scaling relationships lead to the prediction, based on Pütter-type growth models, that optimum growth temperature declines with body size (Fig. 3) (Morita *et al.* 2010). The prediction of declining optimum growth temperatures with size was confirmed by our analysis of independent experimental growth rate data. We find that within species the optimum growth temperature declines with body size by

0.31°C per unit increase in the natural log of relative body mass (Fig. 4). Below we present the underlying results in more detail.

We found that the average intraspecific mass exponent for mass-specific consumption rate is smaller (-0.38 [-0.46, -0.30]) than that for metabolic rate (-0.21 [-0.26, -0.16]), based on the non-overlapping Bayesian 95% credible intervals (Fig. 1). It is also probable that the mass-specific scaling exponents differ from -1/4 (that is predicted by the MTE), because > 99% of the posterior distribution of the mass exponent of maximum consumption is below -1/4, and 95% of the posterior distribution of the mass exponent of metabolic rate is above -1/4. Activation energies of maximum consumption rate and metabolism are both similar (0.69 [0.54, 0.85] and 0.62 [0.57, 0.67] respectively; Fig. 1) and largely fall within the prediction from the MTE (0.6-0.7 eV) (Brown *et al.* 2004)). The global intraspecific intercept for routine and resting metabolic rate is estimated to be -1.93 [-2.11, -1.74], and for standard metabolic rate it is -2.49 [-2.81, -2.17] (*SI Appendix*, Fig. S7). Models where all coefficients varied by species were favored in terms of WAIC (M5 and M1, for consumption and metabolism, respectively) (*SI Appendix*, Table S4). We found statistical support for a species-varying mass and temperature interaction for metabolic rate. 98% of the posterior distribution of the global interaction coefficient  $\mu_{\beta_3}$  is above 0 (*SI Appendix*, Fig. S5). The estimated coefficient is 0.018 [0.0008, 0.0367] on the Arrhenius temperature scale, which corresponds to a decline in the mass scaling exponent of metabolic rate by 0.0026 °C<sup>-1</sup>. The selected model for maximum consumption rate did not include an interaction term (M5).

We estimated the parameters of the Sharpe-Schoolfield equation (Eq. 4) for temperature-dependence of consumption including data beyond peak temperature as: activation energy,  $E_j = 0.58$  [0.45, 0.74], rate at reference temperature,  $C_{0j} = 0.70$  [0.52, 0.89], temperature at which the rate is reduced to half (of the rate in the absence of deactivation) due to high temperatures,  $T_h =$



4.03 [2.82, 4.98], and the rate of the decline past the peak,  $E_h = 2.64$  [2.17, 3.22]. This shows that the relationship between consumption rate and temperature is unimodal and asymmetric, where the decline in consumption rate at high temperatures is steeper than the increase at low temperatures (Fig. 2).

The above results provide empirical support for the two criteria outlined in Morita et al., (2010) that result in declining optimum temperatures with size, i.e. (i) smaller whole organism mass exponent for consumption than metabolism (Fig. 1) and (ii) that growth reaches an optimum over temperature. In our case, the second criterion is met because consumption reaches a peak over temperature (Fig. 2). We illustrate the consequence of these findings in Fig. 3, which shows that the optimum temperature for net energy gain is reached at a lower temperature for a smaller fish because of the difference in exponents and because net gain is unimodally related to temperature. Assuming growth is proportional to net energy gain, this predicts that optimum growth temperature declines with body size.

Using independent data from growth trials across a range of body sizes and temperatures, we also find strong statistical support for a decline in optimum growth temperature with body mass within species, because 92% of the posterior density of the global slope estimate ( $\mu_{\beta_1}$ ) is below 0. The models with and without species-varying slopes were indistinguishable in terms of WAIC (*SI Appendix*, Table S5), and we present the results for the species-varying intercept and slope model, due to slightly better model diagnostics (*SI Appendix*, Fig. S24-27). The global relationship is given by the model:  $T_{opt} = -0.074 - 0.31 \times m$ , where  $m$  is the natural log of the rescaled body mass, calculated as the species-specific ratio of mass to maturation mass.

## Discussion

In this study, we systematically analyzed the intraspecific scaling of consumption, metabolism and growth with body mass and temperature. We found strong evidence for declining optimum growth temperatures as individuals grow in size based on two independent approaches. First, we find differences in the intraspecific mass-scaling of consumption and metabolism, and a unimodal temperature dependence of consumption, which lead to predicted declines in optimum temperature for net energy gain (and hence growth) with size. Second, we confirm this prediction using intraspecific growth rate data of fish. Our analysis thus demonstrates the importance of understanding intraspecific scaling relationships when predicting responses of fish populations to climate warming.

That warming increases growth and development rates but reduces maximum or adult size is well known from experimental studies, also referred to as the temperature-size rule (TSR). Yet, the mechanisms underlying the TSR remain poorly understood. Pütter-type growth models, including the von Bertalanffy growth equation (VBGE), predict that the asymptotic size declines with warming if the ratio of the coefficients for energy gains and losses ( $H/K$  in Eq. 7) (Pauly & Cheung 2018b) declines with temperature. However, the assumptions underlying the VBGE were recently questioned because of the lack of empirical basis for the scaling exponents and the effects of those on the predicted effects of temperature on asymptotic size (Lefevre *et al.* 2018; Marshall & White 2019). Specifically, the allometric exponent of energy gains ( $a$ ) is assumed to be smaller than that of energetic costs ( $b$ ) (Eq. 7). This is based on the assumption that anabolism scales with the same power as surfaces to volumes ( $a = 2/3$ ) and catabolism, or maintenance metabolism, is proportional to body mass ( $b = 1$ ) (von Bertalanffy 1957; Pauly & Cheung 2018a). In contrast, maintenance costs are commonly thought to instead be proportional to standard metabolic rate, which in turn often is proportional to intake rates at the interspecific level (Brown *et al.* 2004;

Marshall & White 2019). This leads to  $a \approx b$ , resulting in unrealistic growth trajectories and temperature dependences of growth dynamics in Pütter models (Lefevre *et al.* 2018; Marshall & White 2019). However, similar to how the existence of large fishes in tropical waters does not invalidate the hypothesis that old individuals of large-bodied fish may reach smaller sizes with warming, interspecific scaling parameters cannot reject or support these model predictions on growth within species. We show that the average intraspecific whole-organism mass scaling exponent of metabolism is larger than that of maximum consumption, i.e., the inequality  $a < b$  holds at the intraspecific level. This implies that on average within species of fish, energetic costs increase faster with body mass than gains (all else equal). Importantly, when accounting for this difference in the exponents, and the unimodal thermal response of consumption, the thermal response of net energy gain is characterized by the optimum temperature being a function of body size (Morita *et al.* 2010). Therefore, empirically derived intraspecific parameterizations of simple growth models result in predictions in line with the TSR, in this case via declines in optimum growth temperatures over ontogeny rather than declines in asymptotic sizes.

Declines in optimum growth temperatures over ontogeny as a mechanism for TSR-like growth dynamics do not rely on the assumption that the ratio of the coefficients for energy gains and losses declines with temperature. In fact, we find that when using data from sub-peak temperatures only, the average intraspecific predictions about the activation energy of metabolism and consumption do not differ substantially, which implies there is no clear loss or gain of energetic efficiency with warming within species. This is in contrast to other studies, e.g. Lemoine & Burkepile (2012) and Rall *et al.* (2010). However, it is in line with the finding that growth rates increase with temperature (e.g. Angilletta & Dunham 2003), which is difficult to reconcile from a bioenergetics perspective if warming always reduced net energy gain. Our analysis instead suggests that the mismatch

between gains and losses occurs when accounting for unimodal consumption rates over temperature. The match, or mismatch, between the temperature dependence of feeding vs. metabolic rates is a central question in ecology that extends from experiments to meta-analyses to food web models (Vasseur & McCann 2005; Rall *et al.* 2010; Lemoine & Burkepile 2012; Fussmann *et al.* 2014; Lindmark *et al.* 2019). Our study highlights the importance of accounting for non-linear thermal responses for two main reasons. First, the thermal response of net energy gain reaches a peak at temperatures below the peak for consumption. Secondly, as initial warming commonly leads to increased growth rates, the effect of warming on growth rates should depend on temperature rather than growth being assumed to be monotonically related to temperature.

Life-stage dependent optimum growth temperatures have previously been suggested as a component of the TSR (Ohlberger 2013). Although previous studies have found declines in optimum growth temperatures with body size in some species of fishes and other aquatic ectotherms (Wyban *et al.* 1995; Panov & McQueen 1998; Steinarsson & Imsland 2003; Björnsson *et al.* 2007; Handeland *et al.* 2008), others have not (Brett *et al.* 1969; Elliott & Hurley 1995). Using systematically collated growth data from experiments with variation in both size and temperature treatments (13 species), we find that for an average fish, the optimum growth temperature declines as it grows in size. This finding emerges despite the small range of body sizes used in the experiments (only 10% of observations are larger than 50% of maturation size) (*SI Appendix*, Fig. S2). Individuals of such small relative size likely invest little energy in reproduction, which suggests that physiological constraints contribute to reduced growth performance of large compared to small fish, in addition to increasing investment into reproduction (Barneche *et al.* 2018).

Translating results from experimental data to natural systems is challenging because maximal feeding rates, unlimited food supply, lack of predation, and constant temperatures do not reflect natural conditions, yet affect growth rates (Brett *et al.* 1969; Lorenzen 1996; Huey & Kingsolver 2019). In addition, total metabolic costs in the wild also include additional costs for foraging and predator avoidance. It is, however, typically found and assumed that standard metabolic rate and natural feeding levels are proportional to routine metabolic rate and maximum consumption rate, respectively, and thus exhibit the same mass-scaling relationships (Kitchell *et al.* 1977; Neuenfeldt *et al.* 2020). Intraspecific growth rates may not appear to be unimodally related to temperature when measured over a temperature gradient across populations within a species (Denderen *et al.* 2020), because each population can be adapted to local climate conditions and thus display different temperature optima. However, each population likely has a thermal optimum for growth, which differs between individuals of different size. Hence, each population might have a unimodal relationship with temperature as it warms. This highlights the importance of understanding the time scale of environmental change in relation to that of immediate physiological responses, acclimation, adaptation and community reorganization for the specific prediction about climate change impacts.

In natural systems, climate warming may also result in stronger food limitation (Ohlberger *et al.* 2011; Huey & Kingsolver 2019). Hence, as optimum growth temperatures decline not only with size but also food availability (Brett *et al.* 1969; Brett 1971), and realized consumption rates are a fraction of the maximum consumption rate (20-70%) (Kitchell *et al.* 1977; Neuenfeldt *et al.* 2019), species may be negatively impacted by warming even when controlled experiments show they can maintain growth capacity at these temperatures. Supporting this point is the observation that warming already has negative or lack of positive effects on body growth in populations living

at the edge of their physiological tolerance in terms of growth (Neuheimer *et al.* 2011; Huss *et al.* 2019).

Whether the largest fish of a population will be the first to experience negative effects of warming, as suggested by our finding that optimum growth temperature declines with body size, depends on the environmental temperatures they typically experience compared to smaller conspecifics. They may for instance inhabit colder temperatures compared to small fish due to ontogenetic habitat shifts (Werner & Hall 1988; Lloret-Lloret *et al.* 2020); see also Heincke's law (Heincke 1913; Audzijonyte & Pecl 2018). That said, there is already empirical evidence of the largest individuals in natural populations being the first to suffer from negative impacts of warming from heatwaves (Pörtner & Knust 2007), or not being able to benefit from warming (Huss *et al.* 2019; Van Dorst *et al.* 2019). Hence, assuming that warming affects all individuals of a population equally is a simplification that can bias predictions of the biological impacts of climate change.

The interspecific scaling of fundamental ecological processes with body mass and temperature has been used to predict the effects of warming on body size, size structure, and population and community dynamics (Vasseur & McCann 2005; Morita *et al.* 2010; Cheung *et al.* 2013; Gilbert *et al.* 2014). We argue that a contributing factor to the discrepancy between mechanistic growth models, general scaling theory, and empirical data has been the lack of data synthesis at the intraspecific level. The approach presented here can help overcome limitations of small data sets by borrowing information across species in a single modelling framework, while accounting for the intraspecific scaling of rates. Accounting for the faster increase in whole-organism metabolism than consumption with body size, the unimodal thermal response of consumption, and resulting size-dependence of optimum growth temperatures is essential for understanding what causes observed growth responses to global warming. Acknowledging these mechanisms is also

important for improving predictions on the consequences of warming effects on fish growth for food web functioning, fisheries yields and global food production in warmer climates.

## **Materials and methods**

### **Data acquisition**

We searched the literature for experimental studies evaluating the temperature response of individual maximum consumption rate (feeding rate at unlimited food supply, *ad libitum*), resting, routine and standard oxygen consumption rate as a proxy for metabolic rate (Nelson 2016) and growth rates across individuals of different sizes within species. We used three different searches on the Web of Science Core Collection (see *SI Appendix*, for details). In order to estimate how these rates depend on body size and temperature within species, we selected studies that experimentally varied both body size and temperature (at least two temperature treatments and at least two body masses). The average number of unique temperature treatments (temperature rounded to nearest °C) by species is 7.2 for growth and 4.3 for consumption and metabolism data). The criteria for both mass and temperature variation in the experiments reduces the number of potential data sets, as most experimental studies use either size or temperature treatments, not both. However, this criterion allows us to fit multiple regression models and estimate the effects of mass and temperature jointly, and to evaluate the probability of interactive mass- and temperature effects within species. Following common practice we excluded larval studies, which represents a life stage exhibiting different constraints and scaling relationships (Glazier 2005).

Studies were included if (i) a unique experimental temperature was recorded for each trial ( $\pm 1^\circ\text{C}$ ), (ii) fish were provided food at *ad libitum* (consumption and growth data) or if they were unfed (resting, standard or routine metabolic rate), and (iii) fish exhibited normal behavior during

the experiments. We used only one study per species and rate to ensure that all data within a given species are comparable as measurements of these rates can vary between studies due to e.g. measurement bias, differences in experimental protocols, or because different populations were studied (Armstrong & Hawkins 2008; Jerde *et al.* 2019). In cases where we found more than one study for a given rate and species, we selected the most suitable study based on our pre-defined criteria (for details, see *SI Appendix*). We ensured that the experiments were conducted at ecologically relevant temperatures (*SI Appendix*, Figs. S1, S3). A more detailed description of the search protocol, data selection, acquisition, quality control, collation of additional information and standardizing of rates to common units can be found in *SI Appendix*.

We compiled four datasets: maximum consumption rate, metabolic rate, growth rate and the optimum growth temperature for each combination of body mass group and species. We compiled a total of 746 measurements of maximum consumption rate (of which 666 are below peak), 2699 measurements of metabolic rate and 227 measurements of growth rate (45 optimum temperatures) from published articles for each rate, from 20, 34 and 13 species, respectively, from different taxonomic groups, habitats and lifestyles (Table S1-S2). We requested original data from all corresponding authors of each article. In cases where we did not hear from the corresponding author, we extracted data from tables or figures using Web Plot Digitizer (Rohatgi 2012).

## **Model fitting**

### *Model description*

To each dataset, we fit hierarchical models with different combinations of species-varying coefficients, meaning they are estimated with shrinkage. This reduces the influence of outliers



which could occur in species with small samples sizes (Gelman & Hill 2007; Harrison *et al.* 2018).

The general form of the model is:

$$y_{ij} \sim N(\mu_{ij}, \sigma) \quad (1)$$

$$\mu_{ij} = \beta_{0j} + \sum_{p=1}^n (\beta_p \times x_{ip}) \quad (2)$$

$$\beta_{0j} \sim N(\mu_{\beta_0}, \sigma_{\beta_0}) \quad (3)$$

where  $y_{ij}$  is the  $i$ th observation for species  $j$  for rate  $y$ ,  $\beta_{0j}$  is a species-varying intercept,  $x_{ip}$  is a predictor and  $\beta_p$  is its coefficient, with  $p = 1, \dots, n$ , where  $n$  is the number of predictors considered in the model (mass, temperature, and their interaction). Predictors are mean centered to improve interpretability (Schielzeth 2010). Species-level intercepts follow a normal distribution with hyperparameters  $\mu_{\beta_0}$  (global intercept) and  $\sigma_{\beta_0}$  (between-species standard deviation). For most models we also allow the coefficient  $\beta_p$  to vary between species, such that  $\beta_p$  becomes  $\beta_{pj}$  and  $x_{ip}$  becomes  $x_{ijp}$ , where  $\beta_{pj} \sim N(\mu_{\beta_p}, \sigma_{\beta_p})$ . For each dataset, we evaluate multiple combinations of species-varying coefficients (from varying intercept to  $n$  varying coefficients). We used a mix of flat, weakly informative, and non-informative priors. For the temperature and mass coefficients we used the predictions from the MTE as the means of the normal prior distributions (Brown *et al.* 2004), but with large standard deviations (see *SI Appendix*, Table S3). Below we describe how the model in Eqns. 1-3 is applied to each data set.

### *Mass- and temperature dependence of consumption, metabolism and growth below peak temperatures*

Peak temperatures (optimum in the case of growth) refer to the temperature at which the rate was maximized, by size group. For data below peak temperatures, we assumed that mass-specific maximum consumption rate, metabolism and growth scale allometrically (as a power function of

the form  $I = i_0 M^{b_0}$ ) with mass, and exponentially with temperature. Hence, after log-log (natural log) transformation of mass and the rate, and temperature in Arrhenius temperature ( $1/kT$  in unit  $\text{eV}^{-1}$ , where  $k$  is Boltzmann's constant [ $8.62 \times 10^{-5} \text{ eV K}^{-1}$ ]), the relationship between the rate and its predictors becomes linear. This is similar to the MTE, except that we estimate all coefficients instead of correcting rates, and allow not only the intercepts but also slopes to vary across species.

When applied to Eqns. 1-3,  $y_{ij}$  is the  $i$ th observation for species  $j$  of the natural log of the rate (consumption, metabolism or growth), and the predictors are  $m_{ij}$  (natural log of body mass),  $t_{A,ij}$  (Arrhenius temperature,  $1/kT$  in unit  $\text{eV}^{-1}$ ), both of which were mean-centered, and their interaction. Body mass is in g, consumption rate in  $\text{g g}^{-1} \text{ day}^{-1}$ , metabolic rate in  $\text{mg O}_2 \text{ g}^{-1} \text{ h}^{-1}$  and specific growth rate in unit  $\% \text{ day}^{-1}$ . We use resting or routine metabolism (mean oxygen uptake of a resting unfed fish only showing some spontaneous activity) and standard metabolism (resting unfed and no activity, usually inferred from extrapolation or from low quantiles of routine metabolism, e.g. lowest 10% of measurements) to represent metabolic rate (Beamish 1964; Ohlberger *et al.* 2007). Routine and resting metabolism constitute 58% of the data used and standard metabolism constitutes 42%. We accounted for potential differences between these types of metabolic rate measurements by adding two dummy coded variables,  $type_r$  and  $type_s$ , the former taking the value 0 for standard and 1 for a routine or resting metabolic rate measurement, and vice versa for the latter variable. Thus, for metabolism, we replace the overall intercept  $\beta_{0j}$  in Eqns. 2-3 with  $\beta_{0rj}$  and  $\beta_{0sj}$ .  $\beta_{0sj}$  is forced to 0 for a species that has a routine or resting metabolic rate and vice versa. We assume these coefficients vary by species following normal distributions with global means  $\mu_{\beta_{0r}}$  and  $\mu_{\beta_{0s}}$ , and standard deviations  $\sigma_{\beta_{0r}}$  and  $\sigma_{\beta_{0s}}$ , i.e.  $\beta_{0rj} \sim N(\mu_{\beta_{0r}}, \sigma_{\beta_{0r}})$  and  $\beta_{0sj} \sim N(\mu_{\beta_{0s}}, \sigma_{\beta_{0s}})$ .

## Mass- and temperature dependence of consumption including beyond peak temperatures

Over a large temperature range, many biological rates are unimodal. We identified such tendencies in 10 out of 20 species in the consumption data set. To characterize the decline in consumption rate beyond peak temperature, we fit a mixed-effects version of the Sharpe Schoolfield equation (Schoolfield *et al.* 1981) as parameterized in (Padfield *et al.* 2020), to equations 1-2 with  $y_{ij}$  as rescaled consumption rates ( $C$ ). Specifically, we model  $\mu_{ij}$  in Eq. 1 with the Sharpe-Schoolfield equation:

$$\mu_{ij} = \frac{C_{0j}(T_C) e^{E_j \left( \frac{1}{kT_C} - \frac{1}{kT} \right)}}{1 + e^{E_h \left( \frac{1}{kT_h} - \frac{1}{kT} \right)}} \quad (4)$$

$$E_j \sim N(\mu_E, \sigma_E) \quad (5)$$

$$C_{0j} \sim N(\mu_{C_0}, \sigma_{C_0}) \quad (6)$$

where  $C_{0j}(T_C)$  is the rate at a reference temperature  $T_C$  in Kelvin [K] (here set to 263.15),  $E_j$  [eV] is the activation energy,  $E_h$  [eV] characterizes the decline in the rate past the peak temperature and  $T_h$  [K] is the temperature at which the rate is reduced to half (of the rate in the absence of deactivation) due to high temperatures. We assume  $E_j$  and  $C_{0j}$  vary across species according to a normal distribution with means  $\mu_E$  and  $\mu_{C_0}$ , and standard deviations  $\sigma_E$  and  $\sigma_{C_0}$  (Eq. 5-6). Prior to rescaling maximum consumption (in unit  $\text{g day}^{-1}$ ) by dividing  $C_{i,j}$  with the mean within species  $\bar{C}_j$ , we mass-normalize it by dividing it with  $m^a$  where  $m$  is mass in g and  $a$  is the whole-organism mass-exponent calculated from the estimated mass-specific exponent with the log-linear model fitted to data below peak temperature. Temperature,  $T$ , is centered by subtracting the temperature at peak consumption estimated separately for each species using a linear model with a quadratic temperature term. The rescaling is done to control for differences between species with respect to

the experimental temperatures relative to the temperature that maximizes their consumption rate such that data can be pooled.

#### *Mass-dependence of optimum growth temperature*

To evaluate how the optimum temperature ( $t_{opt,ij}$ , in degrees Celsius) for individual growth depends on body mass, we fit Eqns. 1-3 with  $y_{ij}$  as the mean-centered optimum growth temperature within species ( $t_{opt,ij} = T_{opt,ij} - \bar{T}_{opt,j}$ ), to account for species being adapted to different thermal regimes.  $m_{ij}$ , the predictor variable for this model, is the natural log of the ratio between mass and mass at maturation within species:  $m_{ij} = \ln(M_{ij}/M_{mat,j}) - \overline{\ln(M_{ij}/M_{mat,j})}$ . This rescaling is done because we are interested in examining relationships within species over “ontogenetic size”, and because we do not expect an interspecific relationship between optimum growth temperature and body mass because species are adapted to different thermal regimes. We consider both the intercept and the effect of mass to potentially vary between species.

#### *Parameter estimation*

We fit the models in a Bayesian framework, using R version 4.0.2 (R Core Team 2020) and JAGS (Plummer 2003) through the R-package ‘rjags’ (Plummer 2019). We used 3 Markov chains with 5000 iterations for adaptation, followed by 15000 iterations burn-in and 15000 iterations sampling where every 5<sup>th</sup> iteration saved. Model convergence was assessed by visually inspecting trace plots and potential scale reduction factors ( $\hat{R}$ ) (SI Appendix).  $\hat{R}$  compares chain variance with the pooled variance, and values <1.1 suggest all three chains converged to a common distribution (Gelman *et al.* 2003). We relied heavily on the R packages within ‘tidyverse’ (Wickham *et al.* 2019) for data

processing, as well as ‘*ggmcmc*’ (Fernández-i-Marín 2016), ‘*mcmcviz*’ (Youngflesh 2018) and ‘*bayesplot*’ (Gabry *et al.* 2019) for visualization.

#### *Model comparison*

We compared the parsimony of models with different hierarchical structures, and with or without mass-temperature interactions, using the Watanabe-Akaike information criterion (WAIC) (Watanabe 2013; Vehtari *et al.* 2017), which is based on the posterior predictive distribution. We report WAIC for each model described above (Table S4-S5), and examine models with  $\Delta$ WAIC values  $< 2$ , where  $\Delta$ WAIC is each model's difference to the lowest WAIC across models, in line with other studies (Olmos *et al.* 2019).

#### *Net energy gain*

The effect of temperature and mass dependence of maximum consumption and metabolism (proportional to biomass gain and losses, respectively) (Ursin 1967; Kitchell *et al.* 1977; Essington *et al.* 2001) on growth is illustrated by visualizing the net energy gain. The model for the net energy gain (growth) can be viewed as a Pütter-type model, which is the result of two antagonistic allometric processes, biomass gains and biomass losses:

$$\frac{dM}{dt} = H(T)M^a - K(T)M^b \quad (7)$$

where  $M$  is body mass and  $T$  is temperature,  $H$  and  $K$  the allometric constants and  $a$  and  $b$  the exponents of the processes underlying gains and losses, respectively. We convert metabolism from oxygen consumption [ $\text{mg O}_2 \text{ h}^{-1} \text{ day}^{-1}$ ] to  $\text{g day}^{-1}$  by assuming  $1 \text{ kcal} = 295 \text{ mg O}_2$  (based on an oxycaloric coefficient of  $14.2 \text{ J/mg O}_2$ ) (Hepher 1988),  $1 \text{ kcal} = 4184 \text{ J}$  and an energy content of  $5600 \text{ J/g}$  (Rijnsdorp & Ibelings 1989), and convert consumption to  $\text{g day}^{-1}$  from  $\text{g g}^{-1} \text{ day}^{-1}$ .

Consumption and metabolic rate are calculated for two sizes (5 and 1000 g, which roughly correspond to the 25<sup>th</sup> percentile of both datasets and the maximum mass in the consumption data, respectively), using the global allometric relationships found in the log-log models fit to sub-peak temperatures. These allometric functions are further scaled with the temperature correction factors  $r_c$  for consumption and  $r_m$  for metabolism.  $r_c$  is based on the Sharpe-Schoolfield model and  $r_m$  is given by the temperature dependence of metabolic rate from the log-linear model. Because  $r_c$  and  $r_m$  are fitted to data on different scales, we divide these functions by their maximum. Lastly, we rescale the product between the allometric functions and  $r_c$  and  $r_m$  such that the rate at 19°C (mean temperature in both data sets) equals the temperature-independent rate.

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## Author contributions

ML conceived the study; ML, JO, AG designed research; ML performed research with input from JO and AG; ML, JO, AG wrote the paper and contributed to revisions of the manuscript.

## Data accessibility statement

All data and R code (lists of studies in literature search, data preparation, analyses and figures) can be downloaded from a GitHub repository (<https://github.com/maxlindmark/scaling>) and will be archived on Zenodo upon publication.

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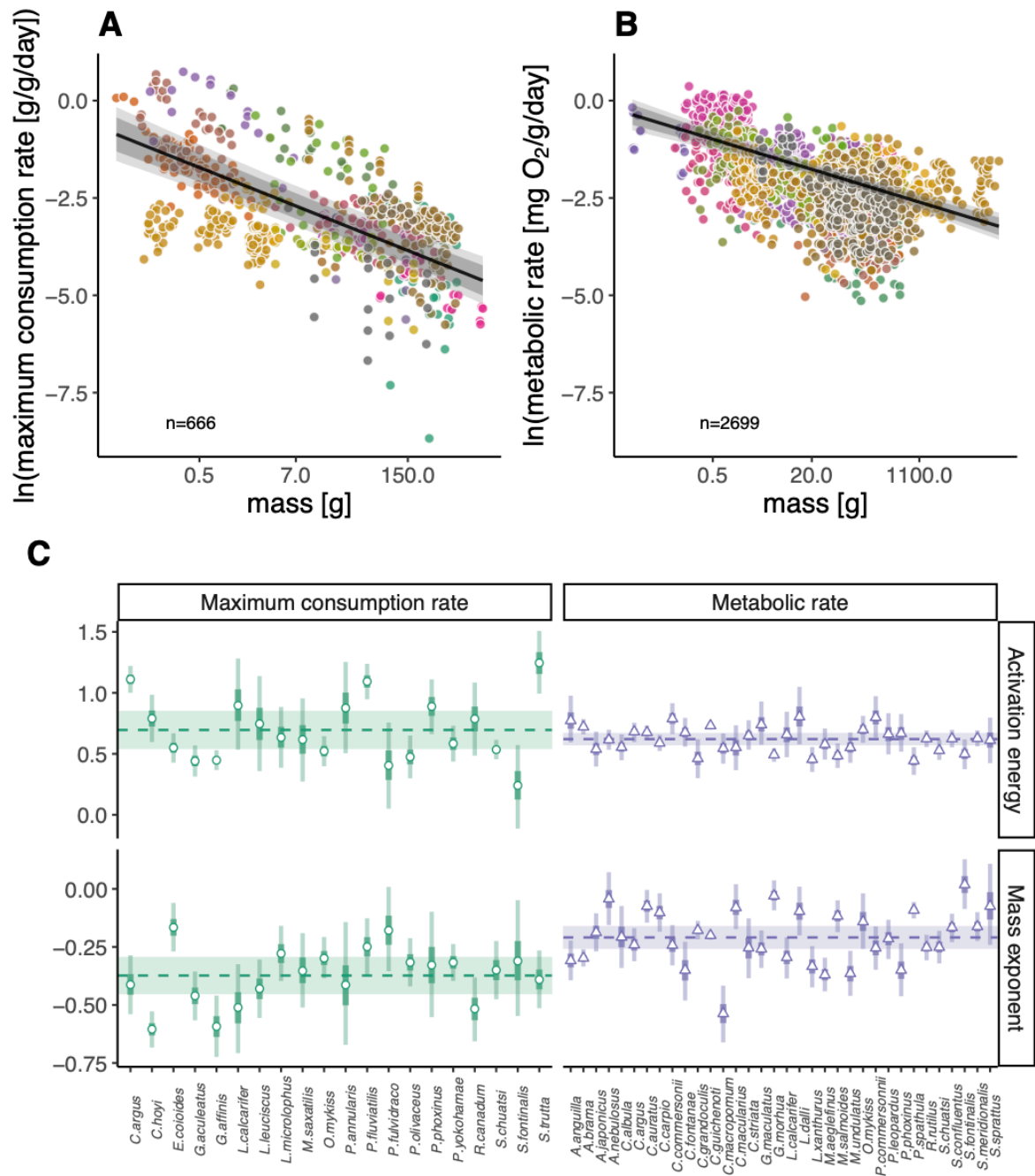


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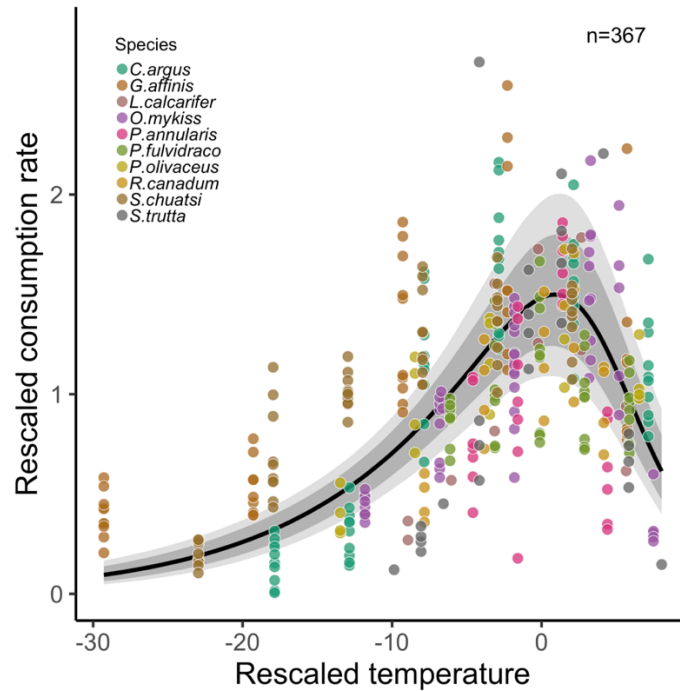
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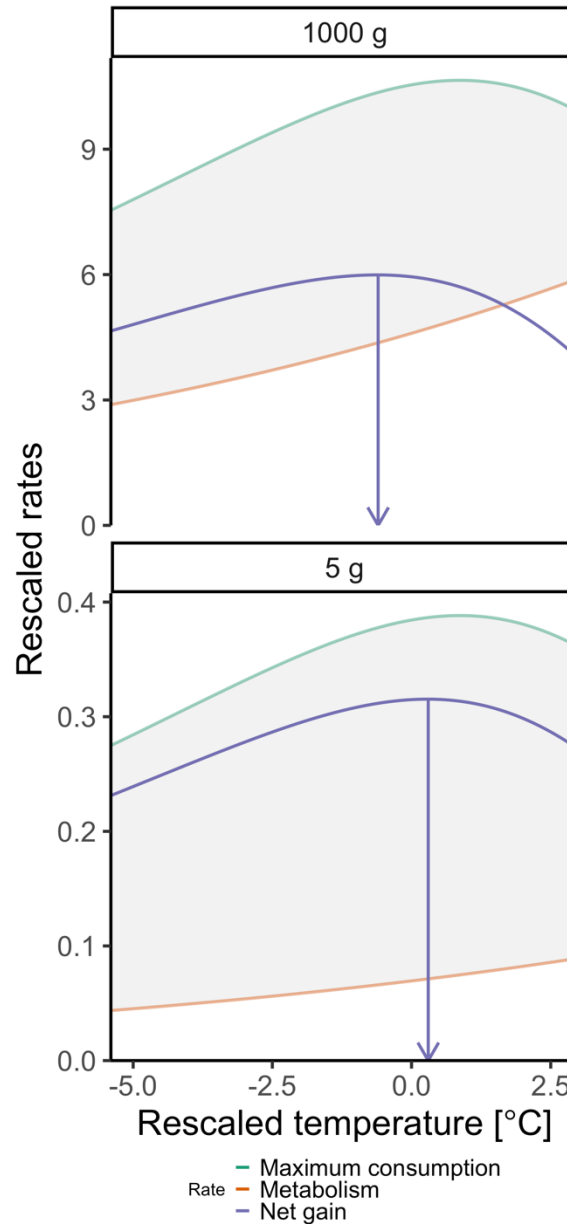


763  
764 **Figure 1.** Natural log of mass-specific maximum consumption rate (A) and metabolic rate (B)  
765 against body mass on a logarithmic x-axis. Lines are global predictions at the average temperature  
766 in each data set (both 19°C, but note the model is fitted using mean-centred Arrhenius  
767 temperature). Shaded areas correspond to 80% and 95% credible intervals. Species are grouped

768 by color (legend not shown,  $n=20$  for consumption and  $n=34$  for metabolism, respectively). C)  
769 Global and species-level effects of mass- and temperature on specific maximum consumption rate  
770 and metabolic rate. Horizontal lines show the posterior medians of the global activation energies  
771 and mass exponents of maximum consumption and metabolism ( $\mu_{\beta_1}$  and  $\mu_{\beta_2}$  in Eqs. 6-8 for the  
772 mass and temperature coefficients, respectively). The shaded horizontal rectangles correspond to  
773 the posterior median  $\pm 2$  standard deviations. Points and triangles show the posterior medians for  
774 each species-level coefficient (for maximum consumption rate and metabolic rate, respectively),  
775 and the vertical bars show their 80% and 95% credible interval.

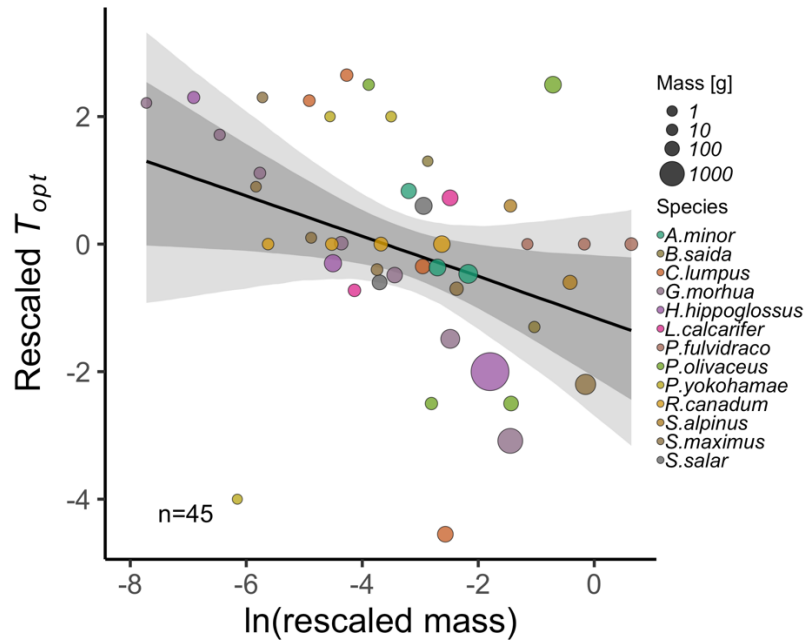


**Figure 2.** Mass-specific maximum consumption rate increases until a maximum is reached, after which it declines steeper than the initial rate of increase. Maximum consumption rates are relative to the average maximum consumption rates within species and temperature is the difference between the experimental temperature and the temperature where maximum consumption peaks (also by species). Lines show posterior median of predictions from the Sharpe-Schoolfield model (using the average intercept across species and the common coefficients), grey bands show 95% and 80% credible intervals. Colors indicate species.



**Figure 3.** Illustration of predicted whole-organism maximum consumption rate (green), metabolic rate (purple) and the difference between them (orange) for two body sizes (top=1000g, bottom=5g) (see 'Materials and Methods'). Vertical arrows indicate the temperature where the difference in net energy gain (energy available for growth) is maximized for the two body sizes, which occurs at different temperatures despite that consumption peaks at the same temperature for both body sizes.





**Figure 4.** Experimental data demonstrating optimum growth temperature declines with body mass. The plot shows the optimum temperature within species (rescaled by subtracting the mean optimum temperature from each observation, by species) as a function of the natural log of rescaled body mass (ratio of mass to maturation mass within species). Probability bands represent 80% and 95% credible intervals, and the solid line shows the global prediction ( $\mu_{\beta_0}$  and  $\mu_{\beta_1}$ ). Colors indicate species and the area of the circle corresponds to body mass in unit g.