*Intraspecific scaling of individual growth, consumption and metabolism with temperature and body mass across fishes*

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**KEY WORDS**:

**WORD COUNT**:

Abstract: ~270

Introduction: ~1400

Methods: ~ 1725

Results: ~884

Discussion: ~2100

Total: ~ 6100

**Abstract**

Warming of aquatic ecosystems is generally predicted to increase individual growth rates and reduce asymptotic body sizes of ectotherms. However, we lack a comprehensive understanding of how growth and the key processes affecting it (e.g., metabolism and consumption) depends on body mass and temperature. This limits our ability to inform mechanistic growth models, to link experimental data to observed patterns of growth and to advance mechanistic food web models. To estimate the effect of body size and temperature on growth, and to examine the link between growth, metabolism and consumption, we collated experimental data through a systematic literature review. We used only studies combining body mass and temperature treatments (in a factorial set-up), and fit hierarchical models to evaluate how growth, metabolism and maximum consumption rate scale jointly with mass and temperature within species, while accounting for variation between species. Mass-scaling exponents of maximum consumption are smaller than both the predicted ¾ and metabolism-exponents and are unimodal over the full temperature range. These features contribute to unimodal thermal responses of growth, which are characterized by declining peak temperatures for body growth with body mass. Accordingly, our analysis of growth data demonstrates that optimum growth temperatures decline with body size within species. Thus, small individuals within a species will likely be able to increase their growth rates with initial warming and larger individuals could be the first to experience negative effects of warming on growth. We argue that syntheses of existing experimental data on intra-specific scaling of key physiological rates, accounting for uncertainty at the species-level, can help overcome the mismatch between mechanistic growth and food webs models, general scaling theory, and observations.

**Introduction**

Individual body growth is a fundamental process powered by metabolism, and thus depends on body size and temperature (Brown *et al.* 2004). It affects individuals’ fitness and life history traits, such as maturation size, population growth rates (Savage *et al.* 2004) and ultimately energy transfer across trophic levels (Andersen *et al.* 2009; Barneche & Allen 2018). Therefore, understanding how it scales with body size and temperature is important for predicting the impacts of global warming on the structure and functioning of ecosystems.

Global warming is predicted to lead to declining body sizes of organisms (Daufresne *et al.* 2009; Gardner *et al.* 2011). The temperature size-rule predicts that warmer rearing temperatures lead to faster developmental times (and larger initial size-at-age or size-at-life-stage), but smaller adult body sizes (Atkinson 1994; Ohlberger 2013). This relationship is found in numerous experimental studies (Atkinson 1994), as well as latitudinal gradient studies of insects (Horne *et al.* 2015), and is stronger in aquatic than terrestrial environments (Forster *et al.* 2012; Horne *et al.* 2015). The underlying mechanisms are not well understood, but likely the TSR results from an interplay between ecology and physiology (Ohlberger 2013; Audzijonyte *et al.* 2018; Neubauer & Andersen 2019). Empirical evidence of climate change signals in time series of individual growth rate is accumulating. For instance, reconstructed growth histories of individual fish often show positive correlations between growth rates and temperature (Thresher *et al.* 2007; Neuheimer *et al.* 2011; Baudron *et al.* 2014; Huss *et al.* 2019). Increased growth rates with initial warming is not unexpected in natural environments, as growth rates increase with temperature until a peak is reached, and species in general occupy habitats below their peak growth temperature (Brett *et al.* 1969; Elliott & Hurley 1995; Jobling 1997; Neuheimer *et al.* 2011). Less clear is the negative effect of warming on the growth of large fish within populations, as would be predicted form the temperature size-rule. Some studies have found negative correlations between maximum or asymptotic body size and temperatures in commercially exploited fish species (Baudron *et al.* 2014; van Rijn *et al.* 2017). However, other studies, including large scale experiments, controlled experiments and latitudinal studies, have failed to find this relationship between maximum size and temperature (Barneche *et al.* 2019; Huss *et al.* 2019; van Denderen *et al.* 2019; van Dorst *et al.* 2019). Predictions about declines in asymptotic body mass, and declines in optimum temperature for growth, have also been made from theoretical growth models, namely the von Bertalanffy growth model (VBGM) (Morita *et al.* 2010; Pauly & Cheung 2018b). However, the physiological basis of these models has been questioned for multiple reasons, including unrealistically large effects of temperature on asymptotic size and mass scaling exponents not matching empirical observations (Lefevre *et al.* 2017; Marshall & White 2019a, b). As empirical findings vary and theoretical predictions are questioned, it remains unclear to which extent the growth of large fish within populations is limited by temperature.

The specific somatic growth rate of an individual can be represented as the difference between energy acquisition and expenditure (von Bertalanffy 1938; Kitchell *et al.* 1977; Jobling 1997). In mature individuals, the remaining excess energy is partitioned between somatic growth and gonads. Usually, energy acquisition is the amount of energy extracted from consumed food and expenditure is defined as fasting, activity and feeding metabolism. Metabolic processes are in turn typically assumed to be related to resting metabolism, often measured as the oxygen consumption of unfed fish at rest (Jobling 1997). These components of the growth-energetics are found in simple mechanistic Pütter-type growth models, such as the VBGM, or the Ontogenetic Growth Model (OGM) (Pütter 1920; von Bertalanffy 1938; Ursin 1967; West *et al.* 2001), as well as more complex dynamic energy budget models (Kitchell *et al.* 1977; Kooijman 1993; Kearney 2019), including physiologically structured population models (PSPMs) (de Roos & Persson 2001) and size-spectrum models (Hartvig *et al.* 2011; Maury & Poggiale 2013; Blanchard *et al.* 2017). In order to understand growth dynamics in changing environments and to evaluate the physiological basis of growth models of varying complexity, it is therefore important to understand how metabolism and consumption rates in general scale with body size and temperature.

The effect of body mass and temperature should ideally be evaluated at the intraspecific rather than interspecific level, to better represent the individual-level processes, and because allometric and temperature relationships can differ within and between species (Glazier 2005; Rall *et al.* 2012; Jerde *et al.* 2019). However, despite this potential difference, the average scaling of individual growth, metabolism and consumption with body mass and temperature is often inferred from interspecific data even when applied to represent processes in individuals. In addition, the temperature- and mass dependence of metabolism and other related rates are also often assumed to follow the Arrhenius fractal supply model (AFS), as in the metabolic theory of ecology (Gillooly *et al.* 2001; Brown *et al.* 2004; Downs *et al.* 2008). The AFS assumes that metabolically-driven rates (, e.g. metabolism and consumption) scale as: , where is the activation energy [], is Boltzmann’s constant [] and is temperature []. Importantly, the model assumes a mass-scaling exponent of 3/4 when estimating temperature effects, as well as independent effects of mass and temperature (Downs *et al.* 2008). However, there are examples of deviations from this mass-scaling exponent (Clarke & Johnston 1999; Bokma 2004; Jerde *et al.* 2019), and cases when body mass and temperature can have interactive effects (Xie & Sun 1990; Glazier 2005; García García *et al.* 2011; Ohlberger *et al.* 2012; Lindmark *et al.* 2018) (but see Jerde *et al*. (2019)). The AFS tends to provide good statistical fits to interspecific data (Clarke 2004) and intraspecific data with a restricted temperature range (Brown *et al.* 2004; Clarke 2004; Rall *et al.* 2012) (but see (Englund *et al.* 2011)). However, within-species thermal response curves are generally unimodal (Dell *et al.* 2011; Englund *et al.* 2011; Rall *et al.* 2012; Uiterwaal & DeLong 2020). These simplifications could affect the estimates of temperature dependencies (Downs *et al.* 2008). Instead of mass- or temperature correcting rates according to the AFS (Brown *et al.* 2004), it could be more appropriate to fit multiple regression models where regression coefficients for mass and temperature are estimated jointly (Downs *et al.* 2008), as well as fit non-linear models that can capture the de-activation of biological rates at higher temperatures (Schoolfield *et al.* 1981; Dell *et al.* 2011; Englund *et al.* 2011).

Overall, average intraspecific scaling of rates with mass and temperature is less understood than interspecific scaling relationships. Contributing factors could be the logistical challenges of replicating experiments for ranges of body masses and temperature (Jerde *et al.* 2019) and a lack of comprehensive data sets (Dell *et al.* 2011). This appears to be especially true for consumption and growth rates (Englund *et al.* 2011; Barrios‐O’Neill *et al.* 2019). Scaling parameters are therefore often based on single experiments, which makes generalization across species difficult. However, as body size is a trait of an individual as well as a species, it is important to understand both general tendencies and variability of intraspecific body mass- and temperature scaling across species (Bolnick *et al.* 2011; Miller & Rudolf 2011; Persson & De Roos 2013; Brose *et al.* 2017). Therefore, overcoming the knowledge gap about intraspecific mass- and temperature scaling is important for advancing trait-based approaches to ecology.

In this study, we analyse how consumption, metabolism and body growth of fish scale intra-specifically with mass and temperature. To this end, we performed a systematic literature review by searching the Web of Science Core Collection. From this search, we compiled datasets on individual growth, maximum consumption and metabolic rates of fish from experiments in which the effect of fish body mass is replicated across multiple temperatures within species. We fit hierarchical Bayesian models to estimate general intraspecific scaling parameters while also accounting for variation between species. For consumption rates, we also fit quadratic models to a subset of the data to characterize the unimodal temperature dependence. We find that the temperature dependence of growth, consumption and metabolism at below peak temperatures is close to average intraspecific predictions (activation energies approximately 0.65 ), whereas the mass exponent of maximum consumption is smaller than the predicted 3/4. Over the full temperature range, consumption rates are unimodal, suggesting declines in optimum (peak) growth temperatures with body mass. Finally, using an independent data set, we demonstrate that optimum growth temperatures decline with body mass.

**Methods**

**Data acquisition**

We searched the literature for experimental studies measuring the temperature- and mass dependence of individual growth rate, maximum consumption rate (feeding rate at unlimited food supply, *ad libitum*) and resting, routine and standard oxygen consumption rate as a proxy for metabolic rate (Nelson 2016). We used three different searches on the Web of Science Core Collection. For growth rate, we used the following topic terms: (growth) AND (mass OR weight OR size) AND (temperature\*) AND (optimum), as well as: (growth) AND (mass OR weight OR size) AND (temperature\*) AND (optim\*). For maximum consumption we used: (consumption OR feeding$rate OR food$intake OR bio$energ\* OR ingestion OR “food-intake”) AND (mass or weight or size) AND (temperature\*), as well as: (feeding-rate OR bio-energ\*) AND (mass OR weight OR size) AND (temperature\*). For metabolic rate we used: (metabolism OR "oxygen-consumption" OR "oxygen consumption") AND (mass OR weight OR size) AND (temperature\*). We also applied additional filters on subject: ‘marine freshwater biology’, ‘fisheries’, ‘ecology’, ‘zoology’, ‘biology’, ‘physiology’. For growth rates, we in addition included ‘limnology’ and for maximum consumption we included ‘limnology’ and ‘evolutionary biology’. The broader searches for growth and consumption reflects the lower data availability compared to metabolism. For more detailed information about the search protocol, we refer to Appendix S1.

We selected studies with a factorial body mass-temperature setup in order to estimate how these rates depend on both body size and temperature within species (size or temperature treatments 2). This reduces the number of data sets available in the literature (as most experimental studies use either a size or temperature treatment, not both). However, this criterion allows us to fit multiple regression models and estimate the effects of mass and temperature jointly, and to evaluate the probability of interactive mass- and temperature effects within species. We excluded larval studies as they represent a small fraction of the ontogeny of most fish. Studies were included if (i) a unique experimental temperature was recorded for each trial (1), (ii) fish were provided food at *ad libitum* for consumption and growth data, fish were unfed for measurements of resting, standard or routine metabolic rate, (iii) fish exhibited normal behaviour. We used only one study per species to ensure that all data within a given species are comparable as measurements of these rates can vary between studies due to e.g. measurement bias, differences in experimental protocols or because different sub-populations were used (Armstrong & Hawkins 2008; Jerde *et al.* 2019). In cases where we found more than one study for a species, we selected the study we found most suitable, based on how well it fit with our pre-defined criteria (for details, see Appendix S1). A more detailed description of the search protocol, criteria to select data, data acquisition procedure, quality control, collation of additional information and standardizing rates to common units can be found in Appendix S1.

We compiled four datasets: growth rate, maximum consumption rate, metabolic rate and the optimum growth rate temperature for each combination of body mass group and species. We compiled in total 227 (45 optimum temperatures), 2695 and 746 data points from published articles for each rate, from 13, 34 and 20 species, respectively, representing a diverse range of taxonomic groups, habitats and lifestyles (Appendix S1). We asked all the corresponding authors of each article to share data, else data were extracted from tables or figures using Web Plot Digitizer (Rohatgi 2012).

**Model fitting**

*Mass- and temperature dependence of growth, consumption and metabolism below peak temperatures*

Peak temperatures (referred to as optimum in the case of growth), here mean a subset of the data sets including only data points below the temperature at which the rate was maximized, by size group. For data below peak temperatures, we assumed that individual growth, maximum consumption rate and metabolism scale as a generalized version of the Arrhenius fractal supply model (Gillooly *et al.* 2001; Brown *et al.* 2004). Mass- and temperature dependence was not assumed a priori but estimated simultaneously. This is more appropriate than correcting for either variable if these parameters (mass exponent or activation energy) are unknown or vary across species and taxa (Downs *et al.* 2008; Isaac & Carbone 2010), and allows estimation of size-temperature interactions. We thus assumed the natural log of rate (growth, maximum consumption or metabolism) scales with mass and temperature as:

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| --- | --- | --- |
|  |  | (1) |

where is the intercept, is the mass scaling exponent on a linear scale when () and is the interaction coefficient. Oa linear, this

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We fit hierarchical models with different combinations of group (species)-varying coefficients. This is in contrast to the Arrhenius fractal supply model, which assumes only the intercept varies between taxa. The species-varying coefficients are thus estimated with shrinkage. This reduces the influence of outliers which could occur in species with small samples sizes, as here due to the relatively strict data selection criteria (Gelman & Hill 2007; Harrison *et al.* 2018). The full model with uncorrelated species-varying coefficients can be written as:

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| --- | --- | --- |
|  |  | (3) |
|  |  | (4) |
|  |  | (5) |

where is the th observation for species of the natural log of the rate (growth, consumption or metabolism), and indexes the regression coefficient (. In Eq. 4, is the natural log of body mass

*Mass- and temperature dependence of consumption including beyond peak temperatures*

Consumption rates are unimodal over a large enough thermal range. To characterize the intraspecific mass and temperature dependence of these rates, we fit second and third degree polynomial regressions to a subset of these data containing only species with data points extending beyond the temperature at which the rate is maximized (peak temperature). The models were fit with a random intercept ( to account for variation across species. The models of are:

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| --- | --- | --- |
|  |  | (6) |
|  |  | (7) |
|  |  | (8) |

where in Eq. 6 refers to mass-specific consumption rates divided by the mean value for species (), in Eq. 7 is mean-centred body mass () and is the mid-point of the temperature in the environment of species subtracted from the experimental temperature (). This rescaling is done to control the differences between species with respect to the experimental temperatures relative to their peak temperature. Due to the relatively small consumption data set we did not fit an interaction term that alters the optimum temperature by mass, although this has been identified in data rich experimental studies of single species (García García *et al.* 2011).

*Mass-dependence of optimum growth temperature*

To evaluate how the optimum temperature () in degrees Celsius for individual growth depends on body mass, we fit the following hierarchical model to account for variation between species in both the intercept and slope:

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| --- | --- | --- |
|  |  | (9) |
|  |  | (10) |
|  |  | (11) |

Here is mean-centred optimum growth temperature within species (), to control for species having different thermal optima. is the natural log of the ratio between mass and body mass at maturation within species: , as we were interested in examining relationships within species while accounting for variation in relative body masses between experiments, and because we assume there is no interspecific relationship between optimum growth temperature and body mass. The mass corresponds to either geometric mean body mass in the time interval where growth was measured in the experiments or simply size class depending on how it was defined in the original study. Subscript in Eq. 11 refers to regression parameters (0 for intercept and 1 for slope). We also fit the model with only a random intercept (

*Parameter estimation*

We fit the models in a Bayesian framework, using R version 3.5.0 (R Core Team 2018) and JAGS (Plummer 2003) through the R-package ‘*rjags*’ (Plummer 2019). We used a mix of flat, weakly informative and non-informative priors to facilitate convergence (Table 1). Weakly informative priors were given mean values around average prediction from the MTE (Brown *et al.* 2004), with large variances to make them less informative. We used 3 Markov chains with 15000 iterations each saving every 5th sample, following a burn-in of 15000 iterations and 5000 iterations for adaptation. Model convergence was assessed by visually inspecting trace plots and potential scale reduction factors () (Gelman *et al.* 2003) (Appendix S1). compares chain variance with the pooled variance, and values <1.1 suggest all three chains converged to a common distribution. We relied heavily on the R packages within the *tidyverse’* (Wickham 2017) for data processing, as well as ‘*ggmcmc*’ (Fernández-i-Marín 2016), ‘*mcmcviz*’ (Youngflesh 2018) and ‘*bayesplot*’ (Gabry *et al.* 2019) for visualization.

*Model comparison*

We compared the parsimony of models with different hierarchical structures, and with or without mass-temperature interactions, using the Watanabe-Akaike information criterion (WAIC) (Watanabe 2013; Vehtari *et al.* 2017), which is based on the posterior predictive distribution. We report WAIC for each model descried above (Table 2), and examine models with WAIC values < 2, where WAIC is each models difference to the lowest WAIC across models, in line with common convention (Olmos *et al.* 2019).

**Table 1** Description of model parameters and their prior distributions. refers to a normal distribution (mean and standard deviation) and to a uniform distribution (interval).

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| --- | --- | --- | --- |
| Model | Parameter | Description | Prior distribution |
| Log-linear regressions  for growth, consumption and metabolism (Eqns. 3-5) |  | Hyperparameter (intercept) |  |
|  | Hyperparameter (mass coefficient) |  |
|  | Hyperparameter (temperature coefficient) |  |
|  | Hyperparameter (interaction) |  |
|  | Hyperparameter (intercept variance) |  |
|  | Hyperparameter (mass coefficient variance) |  |
|  | Hyperparameter (temperature coefficient variance) |  |
|  | Hyperparameter (interaction variance) |  |
|  | Variance |  |
| Polynomial models  for consumption (Eqns. 6-8) |  | Intercept |  |
|  | Mass coefficient |  |
|  | Temperature coefficient |  |
|  | Quadratic temperature coefficient |  |
|  | Cubic temperature coefficient |  |
|  | Variance |  |
| Linear  models  (Eqns. 9-11) |  | Hyperparameter (intercept) |  |
|  | Hyperparameter (mass coefficient) |  |
|  | Hyperparameter (intercept variance) |  |
|  | Hyperparameter (mass coefficient variance) |  |
|  | Variance |  |

**Results**

*Below peak temperatures*

At below peak temperatures, the intraspecific mass- and temperature dependence of specific growth at below optimum temperatures can be described by the equation: (Fig. 1). The parameters are posterior medians of the global parameters, thus representing an average, unmeasured fish. The estimated interaction coefficient is both small and uncertain, and only leads to marginal better fits to data compared to the model without the interactions (WAIC of the model without interaction, M5, is 2.4; Table 2). We estimate it to 0.0046 [-0.064, 0.075], where Bayesian 95% credible intervals are indicated in square brackets. The mass-scaling exponent of growth is estimated to be -0.36 [-0.5, -0.23] and the activation energy (-) of growth is estimated to be -0.74 [-0.95, -0.53].

We find that the intraspecific scaling of mass-specific maximum consumption rate for an average fish can be described by the equation as (Fig. 2). For mass-specific metabolic rate, the relationship is: . In the model for consumption rate, all coefficients vary by species (M5) whereas for metabolism, all coefficients except the interaction vary by species (M2) (Table 2). Maximum consumption scales with a smaller mass exponent (-0.38 [-0.45, -0.30) compared to metabolic rate (-0.20 [-0.25, -0.15]), based on the non-overlapping Bayesian 95% credible intervals (Fig. 3). This difference implies that maximum consumption rates do not increase as fast with body size as does metabolic rate. We also find it probable that the mass-specific scaling exponents differ from the predicted -0.25 from the metabolic theory of ecology. 99.7% of the posterior distribution of the mass exponent of maximum consumption is below -0.25, and only 3.8% of the posterior distribution for the mass exponent of metabolism is below -0.25 (Fig. 3), meaning there is a high probability that the value is larger than -0.25. Activation energies of maximum consumption rate and metabolism are both similar (0.69 [0.54, 0.84] and 0.61 [0.56, 0.67] respectively; Fig. 3) and largely fall within the prediction from the MTE (0.6-0.7 eV) (Brown *et al.* 2004)).

For maximum consumption, the model with a global interaction term, , (M2) has a WAIC of 1.3 compared to the best model (M5) without an interaction term, meaning that WAIC offers little support for one of these models over the other (Table 2). For illustration of model predictions (Fig. 2B), we therefore chose model M5 (without interaction) because it is simpler and the estimate of in M2 is small (posterior median of -0.01 on Arrhenius temperature scale).We find strong statistical support for a negative global interaction between the effect of body mass and temperature on metabolic rate (99.7% of the posterior distribution of is above 0 Fig. S9). However, the effect size is very small. We estimate it to be 0.014 [0.0039, 0.024] on an Arrhenius temperature scale, which corresponds to a decline in the mass scaling exponent of metabolic rate by 0.002 . For metabolism, the model with a species-varying interaction term (M1) has a WAIC of 0.6, suggesting it is comparable to the model with a single global interaction term (M2). We chose the latter to illustrate predictions (Fig. 2A) because of its simpler model structure.

*Including peak temperatures*

Over a larger temperature range, biological rates are unimodal. We identified such tendencies in 11 species in the consumption data set, and fit hierarchical polynomial models with a random intercept (). The model that included also cubic temperature term had slightly lower WAIC than the model with a quadratic term (718.3 vs 719.6, respectively). The equation for rescaled mass-specific consumption rate over the full temperature range in the data can therefore be written as: (Fig. SX).

The implication of a peak in consumption rate over temperature is that even if maximum consumption rates increase at the same rate as metabolism with temperature initially (at below peak temperature), consumption rates eventually decline relative to metabolism with further warming. The effect of temperature on the mismatch between metabolic costs and feeding gains depends on the current temperature relative to peak temperature. The net energy gain, i.e. the difference between exponentially increasing metabolic rates (proportional to energetic costs) and consumption (proportional to energetic gains) also becomes unimodal over the full temperature range. The thermal response curve of net energy gain in addition shows declines in the optimum temperature with increasing body masses, as shown when predicting consumption, metabolism and net energy gain from our fitted models for two different body sizes (Fig. 4). This is an implication of the unimodal net energy curve over temperature and that the mass-scaling exponent of consumption is smaller than that of metabolism, as shown by Morita *et al.* (2010).

The prediction of declining optimal growth temperatures with size within species is further corroborated in our analysis of experimental growth rates. Specifically, we find that within species, the optimum growth temperature (rescaled within species) declines with body size by 0.31 per unit increase in the natural log of body mass (rescaled to size-at-maturation within species) (Fig. 5). The decline in optimum temperature with mass is clear, as 92% of the posterior density of the global slope estimate () is below 0. The models with and without species-varying slopes were indistinguishable in terms of WAIC (177.3 vs 178.3, respectively), and we present the results for the random intercept and slope model. The general relationship is given by the model: , where is the natural log the rescaled body mass.

**Table 2**. Model comparison for the log-linear regressions of how consumption, metabolism and growth depend on mass and temperature (below optimum temperatures). M1 is the full model and is described in text (Eqns. 3-5). The column m\*t indicates whether the model for the rate includes an interactive effect of mass and temperature. The WAIC columns shows WAIC and absolute WAIC in brackets, rounded to the nearest decimal, where WAIC is the difference between each models’ WAIC and the lowest WAIC across models. Bold indicates models with WAIC < 2.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Model | m\*t | Species-varying parameter(s) | WAIC  metabolism | WAIC consumption | WAIC growth |
| M1 | Yes |  | **0.6 (271.9)** | 3.9 (564.5) | **0 (47.2)** |
| M2 |  | **0 (271.3)** | **1.3 (561.9)** | 7.4 (55.6) |
| M3a |  | 306 (577.3) | 147.5 (708.1) | 24 (71.2) |
| M3b |  | 388.6 (659.9) | 69.7 (630.3) | 33 (80.1) |
| M4 |  | 652.3 (923.6) | 190.6 (751.2) | 43.7 (90.8) |
| M5 | No |  | 6.3 (277.6) | **0 (560.6)** | 5.5 (52.7) |
| M6a |  | 347.8 (619.1) | 166.1 (726.7) | 21.7 (68.9) |
| M6b |  | 390.5 (661.8) | 73.7 (634.3) | 34.8 (82) |
| M7 |  | 684.6 (955.9) | 212.9 (773.5) | 44.8 (92) |

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**Fig. 1**. *Effects of temperature and body mass on body growth below optimum temperature. Panel A) shows the natural log of specific growth rate as a function of body mass on a logarithmic x-axis (for readability, note the model is fitted with ln(mass) as a predictor), such that the slope corresponds to the mass-scaling exponent. The line in panel A is the global prediction from model M1, while the temperature is held at its mean (corresponding to 14, but note the model is fitted using Arrhenius temperature). Shaded areas correspond to 80% and 95% credible intervals. Point colours indicate species (n=13, legend not shown). The posterior distributions of (B) the average mass-scaling exponent, , (C) the temperature coefficient, and (D) the mass-temperature interaction, , are shown in the bottom row. Dashed white line shows the posterior median and red vertical line in (D) indicates zero.*

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***Fig. 2****. Natural log of mass-specific maximum consumption rate (B) and metabolic rate (A) against body mass on a logarithmic x-axis. Lines are global predictions at the average temperatures in each data set (both 19, but note the model is fitted using mean-centred Arrhenius temperature). Shaded areas correspond to 80% and 95% credible intervals. Species are grouped by colour (legend not shown, n=20 for consumption and n=34 for metabolism, respectively).*

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***Fig. 3****. Global and species-level effects of mass- and temperature on maximum consumption and metabolic rate. Vertical lines show the posterior medians of the global activation energies and mass exponents of maximum consumption and metabolism ( and in Eqs. 6-8 for the mass and temperature coefficients, respectively). The shaded vertical bars correspond to the posterior median standard deviations. Points and triangles show each species’ prediction (for maximum consumption rate and metabolic rate, respectively), and the horizontal bars show their 80% and 95% credible interval.*

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***Fig. 4.*** *Illustration of predicted maximum consumption rate (green) and metabolism (orange), and the difference between them (purple) for two body sizes (10g = solid, 100g = dashed). As they are measured in different units, fitted on different scales and with different independent variables, the predictions were rescaled to the maximum with reach rate in order to plot these curves on the same graph. The orange curve (representing the net energy gain) is calculated on these rescaled rates. The maximum consumption curve is the prediction from the polynomial model with a quadratic and cubic term, and metabolism is from (M2, see ‘Results’). Vertical arrows indicate the temperature where the difference in net energy acquisition is maximized for the two body sizes, which occurs at different temperatures despite that consumption peaks at the same temperature for both body sizes.*

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**Fig. 5**. *Optimum temperature for growth declines with body mass. The y-axis shows how the optimum temperature within species (rescaled by subtracting the mean temperature for the species) as a function of mean-centred natural log of rescaled body mass (ratio of mass to maturation mass within species). Probability bands represent 80% and 95% credible intervals and the solid line shows the global prediction ( and ). Colors indicate species (n=13) and the point size corresponds to the non-scaled mass in unit .*

**Discussion**

Individual growth, consumption and metabolism represent fundamental processes in ecology, and their scaling with body mass and temperature is used to predict the effects of warming on individual growth, body size, and population and community dynamics in mechanistic models (Vasseur & McCann 2005; Rall *et al.* 2010; Cheung *et al.* 2013). How biological rates scale with temperature and/or mass is commonly inferred from either meta-analysis of single-species studies (Glazier 2005) or interspecific relationships (Brown *et al.* 2004). However, the former can result in large variation in intraspecific scaling parameters due to variation between species, and the latter relies on the assumption that rates scale identically within as between species, which is often not the case (Glazier 2005; Rall *et al.* 2012; Jerde *et al.* 2019). As growth, consumption and metabolism represent individual-level processes, it is important to understand how these rates depend on temperature and mass within species, ideally over ontogeny. At below peak temperatures, we find it probable that activation energies of metabolism, consumption and growth are close to predictions from the metabolic theory of ecology (MTE), i.e. with an activation energy of ~0.65 . This means that a “metabolic mismatch” does not occur in this temperature range. However, over a larger temperature range, the intraspecific thermal responses for maximum consumption rate are unimodal (Englund *et al.* 2011; Rall *et al.* 2012; Jutfelt *et al.* 2020) (Fig. 4). A mismatch between consumption and metabolism can therefore occur at higher temperatures, and this likely contributes to unimodal thermal response of growth (Jobling 1997). An important aspect of in addition accounting for the body mass dependence of consumption and metabolism is that it leads to a decline in optimum growth temperature with body size. This prediction from the simple model of net energy gain as a difference between allometric functions describing energetic costs and gains is also verified using independent experimental growth data.

That optimum growth temperatures decline with body size has been reported in some studies, including but not limited to fish (Panov & McQueen 1998; Steinarsson & Imsland 2003; Björnsson *et al.* 2007; Handeland *et al.* 2008). However, this was not found for e.g. brown trout (*Salmo trutta*) (Elliott & Hurley 1995) nor in sockeye salmon (*Onchorhynchus nerka*) (Brett *et al.* 1969). We find that for an average fish, the optimum growth temperature declines as it grows in size, despite that the small range of body sizes used in the experiments (10% of observations are larger than 50% of maturation size). Individuals of such small relative size likely invest little energy in reproduction. This suggests that reduced growth performance of large fish with warming cannot only be explained by earlier maturation and changes in energy allocation from somatic growth to gonads, but may also represent physiological constraints.

Translating results from experimental data to natural systems is challenging because unlimited food supply, lack of predation, and constant temperatures do not reflect natural conditions but largely affect growth rates (Brett *et al.* 1969; Lorenzen 1996; Huey & Kingsolver 2019). Species in fluctuating environments tend to live in temperatures that are cooler than those maximizing growth (Fig. SX) (Bernhardt *et al.* 2018). Some warming can therefore be beneficial for growth, although, it is important to consider that climate warming may also introduce higher food limitation, which would further lower the optimum temperature for growth (Huey & Kingsolver 2019). MoreoverWhether or not the negative effects of warming will be first experienced by the largest fish depends on if they live closer to their thermal optimum for growth. They may for instance inhabit colder temperatures compared to small fish due to ontogenetic habitat shifts (Werner & Hall 1988), see also Heincke’s law (Heincke 1913; Audzijonyte & Pecl 2018). That said, there is already empirical evidence of the largest individuals being the first to suffer from negative impacts of warming from heatwaves (Pörtner & Knust 2007), or not being able to benefit from warming (Huss *et al.* 2019). Hence, assuming that species occupy thermal habitats where warming can lead to increased growth rate, for all individuals in a population, is a simplification that may not always be warranted in a climate change context.

Interestingly, a decline in optimum growth temperature with mass is also predicted by general Pütter-type growth models (Pütter 1920), where growth is the result of two antagonistic processes, anabolism and catabolism representing build up and break down of body materials: , where is body mass and is temperature. In these models, optimum growth temperatures decline with size under two conditions: (1) (also a necessity for growth being asymptotic) and (2) that growth is unimodal over temperature (Morita *et al.* 2010). While this is one of the most commonly applied growth models, the first condition has been debated recently. In the von Bertalanffy growth model (VBGM) – a special case of the Pütter model – it is assumed that catabolism is proportional to body mass (). This stems from the argument that spontaneous denaturation occurs in every cell (von Bertalanffy 1957; Pauly & Cheung 2018a), but likely also for mathematical convenience and lack of empirical data (Ursin 1967). The model can also be restated in terms of energy, as a balance between energy gains and costs. From a physiological perspective, it is common to assume maintenance costs are proportional to standard metabolic rate (Ursin 1967; Jobling 1997; Lefevre *et al.* 2017), which has a mass exponent typically around 0.8 (Clarke & Johnston 1999; Jerde *et al.* 2019) and not 1. In this case, classic Pütter models of growth, such as the VBGM or the similar ontogenetic growth model (West *et al.* 2001), either fail to represent the physiological processes they aim to capture, or fail to exhibit asymptotic growth (Marshall & White 2019b). This dichotomy can be resolved by considering the overlooked energetic investment into reproduction and its hyperallometric mass scaling (exponent larger than 1) (Marshall & White 2019b), or by describing more complex energy pathways in dynamic energy budget models (Kearney 2019). The recent debate about scaling coefficients in growth models calls for an investigation of the intraspecific scaling of metabolic rate in relation to assimilation or consumption. Our finding that the mass scaling exponent of metabolism is larger than that for maximum consumption implies that “costs” for maintenance increase faster with body mass than energy gains. Bioenergetics models may need to account for this difference in the mass scaling of metabolism and consumption, which is in contrast to predictions from metabolic theory.

In addition to resolving the scaling of net energy gain with body mass, it is important to understand how the balance between energy gains and costs is affected by temperature. The match, or mismatch, between the temperature dependence of feeding vs. metabolic rates is a central question in experiments, meta-analyses and food web models (Vasseur & McCann 2005; Rall *et al.* 2010; Lemoine & Burkepile 2012; Fussmann *et al.* 2014; Lindmark *et al.* 2019). We find that when using strictly sub optimum temperatures, the general (average intraspecific) predictions about the activation energy of metabolism and consumption vary, but the 95% credible intervals largely overlap, meaning there is no clear loss or gain of energetic efficiency with warming within species. This is in contrast to other studies, e.g. (Lemoine & Burkepile 2012; Rall *et al.* 2012). However, it is in line with the finding that growth rates increase with temperature, which would be difficult to explain from a bioenergetics perspective if warming always reduced net energy gains.

While we find no clear evidence of mismatch between metabolic demands and maximum consumption induced by temperature at sub optimum temperatures, we do find clear mismatches at higher temperatures. These are due to consumption rates being unimodally related to temperature, whereas metabolic rates increase exponentially over much wider temperature range. A recent hypothesis suggests that the reason for unimodal consumption responses is to protect aerobic scope by not overshoot post-meal oxygen consumption, which would causally explain why also growth curves are unimodal (Jutfelt *et al.* 2020). While our data are limited in number of species and relative temperatures are simple approximations, we do find that the average optimum for consumption and growth occur at largely similar temperatures (measured in distance from environmental midpoint temperature). This suggests that consumption may be a driver of unimodal growth curves (as is often argued from a conceptual point of view (Jobling 1997). However, we cannot discriminate between other potential factors, such as temperature-dependent changes in assimilation efficiency or cost of growth (Barneche *et al.* 2019), and our samples sizes are small and uncertain. Nevertheless, unimodal thermal responses are likely important for understanding impacts of climate change (Neuheimer *et al.* 2011). Therefore, a priority should be to identify generalized approaches and parameters for characterizing the unimodal shape of consumption rate, which would require more data and experiments with factorial mass and temperature treatments.

We also find the general temperature scaling of metabolic and maximum consumption at temperatures below optimum are less uncertain than what has been reported previously (e.g. in (Downs *et al.* 2008; Englund *et al.* 2011). A likely contributing factor is our use of hierarchical models and partial pooling to estimate higher level (across species) scaling from species data. No pooling, by contrast is equivalent of fitting fixed species effect, which does not lead to shrinkage towards the mean which leads to larger variation in species predictions (Gelman & Hill 2007; Harrison *et al.* 2018).

In contrast to the MTE, we find that body mass can affect the temperature dependence of physiological rates, which previously has been reported only for single species studies (Beamish 1964; Xie & Sun 1990; Ohlberger *et al.* 2012; Lindmark *et al.* 2018; Fossen *et al.* 2019) and between species (Killen *et al.* 2010). This prediction is in line with the metabolic boundary-level hypothesis, which predicts a negative relationship between resting metabolic exponents and temperature (Glazier 2010). This was however not found in a recent study on the intraspecific mass scaling exponent of metabolic rate in fishes (Jerde *et al.* 2019), which could be due to different data collection protocols, where we specifically used studies with temperature replicates within species. The effect size of the interaction is, however, relatively small. We do not find strong evidence for average effects of temperature-size interactions in growth or consumption, although it has been reported for some species (García García *et al.* 2011). A possible explanation is that we strictly exclude temperatures beyond optimum for the log-linear model, and inclusion of these could lead to significant negative interactions if optimum occurs at lower temperature for large fish. The ecological implications of temperature-size interactions at sub optimum temperatures could therefore be small, although larger estimates have been reported in single species studies (Ohlberger *et al.* 2012). It could also be that the overall effect is masked by variation between species, as studies have found both positive and negative interaction between mass and temperature (Ohlberger *et al.* 2012; Messmer *et al.* 2016; Lindmark *et al.* 2018). Given the between species variation, one approach forward could be to control for taxonomic structure at multiple levels when assessing intraspecific mass- and temperature scaling of these rates.

Because we evaluated the joint effect of body mass and temperature on rates of body growth, metabolism and consumption, the number of studies included in our analysis constitutes a small fraction of the available experimental data, which mostly consists of experiments testing only a single temperature or body size (Appendix S1). It also resulted in that the size replicates within each temperature treatment, or vice versa, are relatively small. The relatively small amount of data is especially evident for the consumption experiments, which show larger variation both within and between species, compared to metabolism. This is likely due to the more manual estimations in feeding experiments (e.g. weighing added food and subtracting uneaten food) compared to oxygen depletion rates (metabolism) measured in respirometry, or growth trials. Therefore, the data collated here contains uncertainty from many sources, including differences in experimental protocols. Our selection criteria lead to using a small fraction of all available data being used, which limits the hierarchical model structures we can consider. However, as it is important to jointly estimate the effects of mass- and temperature when scaling coefficients differ from general predictions (Downs *et al.* 2008), we argue that our approach also has merit, because hierarchical models (e.g. in a Bayesian framework with literature-informed priors) can overcome difficulties with small data sets.

Understanding the scaling of rates such as growth, metabolism and consumption is fundamental for linking individual processes to population and food web dynamics. We argue that one contributing factor to the discrepancy between mechanistic models, general scaling theory, and data is the lack of data synthesis at the intraspecific level. Systematic data analysis of existing experimental data combined with models that account for uncertainty at the species-level constitutes an approach that can guide process-based predictions of climate change effects, from individuals to food webs.

**Acknowledgements**

We thank Dennis Tomalá, Vanessa Messmer, Björn Björnsson, Albert Imsland, Tomas Árnasson, Yiping Luo, Takeshi Tomiyama and Myron Peck for generously providing data, Magnus Huss and Ken Haste Andersen for providing useful comments on earlier versions of the manuscript and Matthew Low for an introduction to Bayesian inference. This study was supported by grants from the Swedish Research Council FORMAS (no. 217‐2013‐1315) and the Swedish Research Council (no. 2015‐03752) (both to AG).

**Author contributions**

ML conceived the study; ML, JO, AG designed research; ML performed research; ML analyzed data; ML, JO, AG wrote the paper and contributed to revisions of the manuscript.

**Data accessibility statement**

All data and R code (data manipulation, analyses and figures) can be downloaded from a GitHub repository (<https://github.com/maxlindmark/scaling>) and will be archived on Zenodo upon publication.

**References**

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