# TDDE01: Machine Learning, LAB2

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#### 1 Assignment 2

The dataset for the first assignment contains information from a private enterprise about their customers. The goal is to predict how well a customer will manage their loans based on a number of predictive features such as marital status, job, age etc. We first split the data into subsets of 50/25/25 of train/validation/test.

#### 1.1 Fitting tree models

Next we fit two models using either the gini or the deviance measures of impurity. The misclassification rates are reported and the model with the lowest rate is selected.

```
cm = table(prediction, data$good_bad)
  return (cm)
}

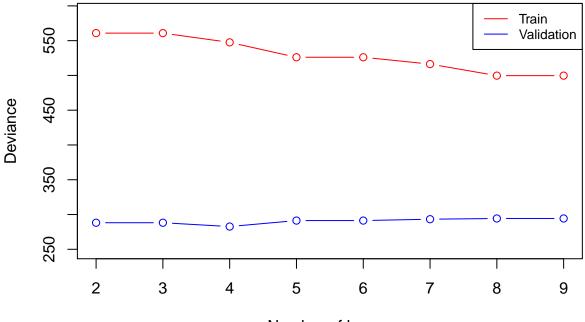
cat("\nmisclass rate using 'deviance' for train data: ",
    get_misclass_rate(model.deviance, train),
    "\nmisclass rate using 'deviance' for test data: ",
    get_misclass_rate(model.deviance, test),
    "\nmisclass rate using 'gini' for train data: ",
    get_misclass_rate(model.gini, train),
    "\nmisclass rate using 'gini' for test data: ",
    get_misclass_rate(model.gini, test))
```

```
##
## misclass rate using 'deviance' for train data: 0.212
## misclass rate using 'deviance' for test data: 0.284
## misclass rate using 'gini' for train data: 0.23
## misclass rate using 'gini' for test data: 0.34
```

Since deviance had the lower misclassification rates, this model is chosen for the subsequent steps.

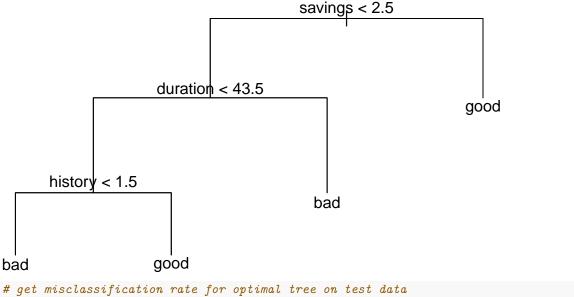
Next we use the training and validation sets to choose the optimal tree depth. This is done by measuring the deviance for when pruning the tree to have a set number of terminal nodes (leaves) in the range 2-9.

```
train_score = numeric(9)
validation_score = numeric(9)
# try number of terminal nodes in range 2-9 to find
# optimal depth, i.e tree with lowest deviance
for (i in 2:9)
 pruned_tree = prune.tree(model.deviance, best = i)
 prediction = predict(pruned_tree, newdata = validation, type = "tree")
 train score[i] = deviance(pruned tree)
  validation_score[i] = deviance(prediction)
plot(2:9, train_score[2:9],
     type="b", col="red", ylim=c(250, 590),
     xlab="Number of leaves", ylab="Deviance")
points(2:9, validation_score[2:9],
       type="b", col="blue")
legend("topright", legend=c("Train", "Validation"),
       col=c("red", "blue"), lty=1, cex=0.8)
```



#### Number of leaves

```
\# since i = 2...9, optimal i is equal to index + 1
optimal.leaves = which.min(validation_score[2:9]) + 1
# prune tree to optimal number of leaves
optimal.tree = prune.tree(model.deviance, best = optimal.leaves)
# get variables selected of optimal tree
summary(optimal.tree)
##
## Classification tree:
## snip.tree(tree = model.deviance, nodes = c(5L, 3L, 9L))
## Variables actually used in tree construction:
## [1] "savings" "duration" "history"
## Number of terminal nodes: 4
## Residual mean deviance: 1.117 = 547.5 / 490
## Misclassification error rate: 0.251 = 124 / 494
# Variables actually used in tree construction:
# "savings" "duration" "history"
# print the optimal tree
# depth = 3 (if root depth = 0)
plot(optimal.tree)
text(optimal.tree)
```



```
# get misclassification rate for optimal tree on test data
optimal.misclass = get_misclass_rate(optimal.tree, test)
cat("\nmisclass rate of optimal tree:", optimal.misclass)
```

```
##
## misclass rate of optimal tree: 0.26
```

The optimal tree has 4 leaves, with a depth of 3. The variables selected by the tree was Savings, Duration, and History, with the tree splitting for different values of these variables to do make predictions.

#### 1.2 Fitting a Naive Bayes classifier

##

Next we use the training data to perform classification using a Naive Bayes classifier, measuring its misclassification rates and confusion matrices on the test and training data.

```
# fit a naive bayes model to train data
model.bayes = naiveBayes(formula = good_bad ~ .,
                         data = train)
# misclass-rate is higher for train than test..
cat("\nmisclass rate for naive bayes model on train data:",
    get_misclass_rate(model.bayes, train),
    "\nmisclass rate for naive bayes model on test data:",
   get_misclass_rate(model.bayes, test))
##
## misclass rate for naive bayes model on train data: 0.3
## misclass rate for naive bayes model on test data: 0.32
cat("\n\nCM for naiveBayes (train):")
##
##
## CM for naiveBayes (train):
print(get_confusion_matrix(model.bayes, train))
```

```
## prediction bad good
##
               95
         bad
                    98
         good 52 255
##
cat("\nCM for naiveBayes (test):")
##
## CM for naiveBayes (test):
print(get_confusion_matrix(model.bayes, test))
## prediction bad good
##
         bad
               47
                    49
##
         good 31
                  123
```

From the results we can see that the Naive Bayes classifier has a higher misclassification rate than our optimal tree model.

For the final task we use a modified loss matrix for our naive bayes classifier where the penalty for misclassifying a future loan management as good when the true classification was actually bad is 10 times higher than the inverse misclassification. To calculate the new misclassification rate and confusion matrix using this loss matrix, we get the raw probabilities for each class from our classifier, and apply the new classification policy to our probabilities.

```
# qet raw probabilities for both classes from naiveBayes classifier
raw.train = predict(model.bayes, newdata = train, type = "raw")
raw.test = predict(model.bayes, newdata = test, type = "raw")
# predicting 'good' must be 10x more probable than bad
# to make the prediction 'good' with new loss-matrix
preds.train = (raw.train[, 2] / raw.train[, 1]) > 10
preds.test = (raw.test[, 2] / raw.test[, 1]) > 10
# convert booleans to good/bad labels
preds.train[which(preds.train == TRUE)] = "good"
preds.train[which(preds.train == FALSE)] = "bad"
preds.test[which(preds.test == TRUE)] = "good"
preds.test[which(preds.test == FALSE)] = "bad"
# CM for train and test
cm.train = table(preds.train, train$good_bad)
cm.test = table(preds.test, test$good_bad)
cat("\nCM for naiveBayes + new loss matrix (train):")
##
## CM for naiveBayes + new loss matrix (train):
print(cm.train)
##
## preds.train bad good
##
          bad 137
                    263
##
          good 10
                     90
cat("\nCM for naiveBayes + new loss matrix (test):")
```

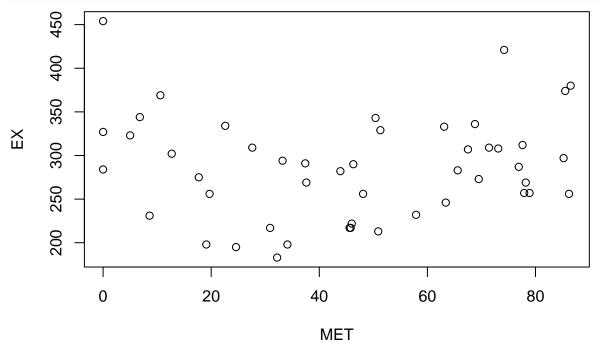
```
##
## CM for naiveBayes + new loss matrix (test):
print(cm.test)
## preds.test bad good
##
         bad
               70 131
##
         good
              8 41
\# misclass-rate for train and test
misclass.train = (cm.train[1,2] + cm.train[2,1]) / sum(cm.train)
misclass.test = (cm.test[1,2] + cm.test[2,1]) / sum(cm.test)
cat("\nmisclass rate naiveBayes + new loss matrix (train data):",
    misclass.train,
    "\nmisclass rate naiveBayes + new loss matrix (test data):",
    misclass.test)
##
## misclass rate naiveBayes + new loss matrix (train data): 0.546
```

As we can see our misclassification rates have increased from the previous model, but our rates have lowered for classifying a customers future loan management as good when the true classification is bad, which was the point of the modified loss matrix.

## misclass rate naiveBayes + new loss matrix (test data): 0.556

#### 2 Assignment 3

The next assignment examines how the per capita state and local public expenditures (EX) depend on the percentage of population living in standard metropolitan areas (MET). We order our data with respect to MET, and plot EX vs. MET.

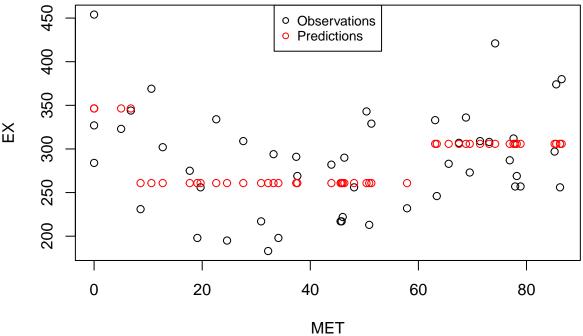


#### 2.1 Fitting a regression tree

There doesn't seem to be any clear pattern in the relationship between the EX and MET variables, so using linear or polynomial regression won't work. We try using a regression tree model using EX as our target and MET as our predictor variable. Cross-validation is used, and the minimum number of observation in any leaf is set to 8.

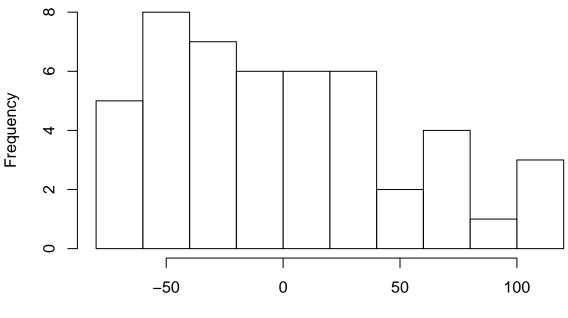
```
summary(model.optimal)
##
## Regression tree:
## snip.tree(tree = model, nodes = c(7L, 6L))
## Number of terminal nodes: 3
## Residual mean deviance: 2698 = 121400 / 45
## Distribution of residuals:
                              Mean 3rd Qu.
##
      Min. 1st Qu. Median
                                              Max.
   -77.88 -43.88
                     -4.88
                              0.00
                                     30.13
                                           115.20
#plot original and fitted data
fitted_data = predict(model.optimal, newdata = data.ordered)
plot(data.ordered$MET, data.ordered$EX, col="black",
     xlab="MET", ylab="EX")
points(data.ordered$MET, fitted_data, col="red")
legend("top", legend=c("Observations", "Predictions"),
       col=c("black", "red"), pch=1, cex=0.8)
     450
            0

    Observations
```



```
# histogram of residuals
hist(resid(model.optimal), xlab="Residuals of optimal model")
```

### Histogram of resid(model.optimal)



Residuals of optimal model

As we can

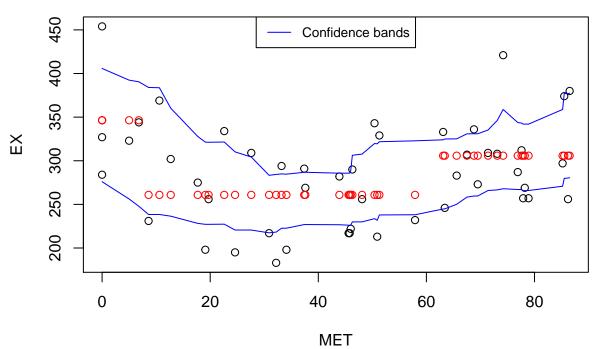
see the predicted values only have three discting values for the feature EX. This is because the optimal model selected only has three leaf nodes, and makes it difficult to fit the model to the scattered observations. Looking at the histogram we can also see that the distribution of the residuals is not a Gaussian distribution, and the most frequent value for the residuals is around -50, which would also suggest that the model is not a good fit for the data.

#### 2.2 Estimating uncertainty

In order to measure the uncertainty in the predictions of our model, we compute the 95% confidence bands using bootstrapping. Since we don't know the underlying distribution of the observations, we use non-parametric bootstrapping, which resamples the data with replacement.

## Warning in prune.tree(model, best = best.size): best is bigger than tree
## size

## Confidence bands (non-parametric)



can see that the confidence band is bumpy along each prediction. This is because we have discrete predictions, so the confidence bands will also have discrete points. Since more than 5% of the observations are outside the confidence bands, the model doesn't seem to be a good fit.

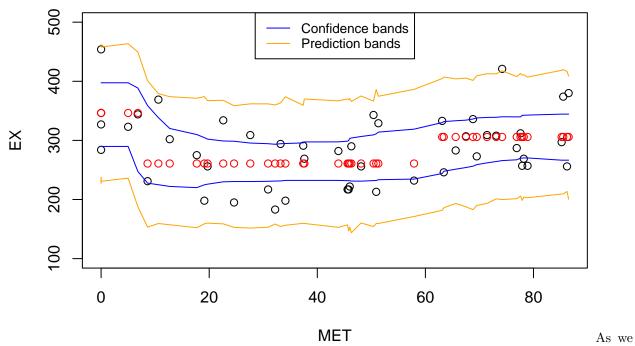
Next we assume that the observations fall under the distribution:

$$Y \sim N(\mu_i, \theta^2) \tag{1}$$

This allows us to use *parametric bootstrapping*, in which we draw new observations from the assumed underlying distribution instead of resampling from the same data. We also calculate and plot the prediction bands, which is the 95% confidence interval for the assumed distribution.

```
return (prediction)
rng=function(data, mle)
 new_data = data.frame(EX = data$EX, MET = data$MET)
 n = length(data$EX)
 new data$EX = rnorm(n, predict(mle, newdata = data), sd(resid(mle)))
 return(new data)
prediction=function(data)
 model = tree(formula = EX ~ MET,
               data = data,
               control = tree.control(nrow(data), minsize = 8))
  model.pruned = prune.tree(model, best = best.size)
  preds = predict(model.pruned, newdata = data.ordered)
  n = length(data.ordered$EX)
  preds_ = rnorm(n, preds, sd(resid(model.optimal)))
 return (preds_)
boot.param = boot(data = data.ordered,
                  statistic = parametric,
                  R = 1000,
                  mle = model.optimal,
                  ran.gen = rng,
                  sim = "parametric")
boot.param.preds = boot(data = data.ordered,
                        statistic = prediction,
                        R = 1000,
                        mle = model.optimal,
                        ran.gen = rng,
                        sim = "parametric")
boot.param.cb = envelope(boot.param, level = 0.95)
boot.param.pb = envelope(boot.param.preds, level = 0.95)
## Warning in envelope(boot.param.preds, level = 0.95): unable to achieve
## requested overall error rate
# plot cb:s and pb:s for parametric bootstrap
plot(data.ordered$MET, data.ordered$EX, col="black", ylim=c(100, 500),
     xlab="MET", ylab="EX", main="Confidence and prediction bands (parametric)")
points(data.ordered$MET, fitted data, col = "red")
lines(data.ordered$MET, boot.param.cb$point[1, ], col="blue")
lines(data.ordered$MET, boot.param.cb$point[2, ], col="blue")
lines(data.ordered$MET, boot.param.pb$point[1, ], col="orange")
lines(data.ordered$MET, boot.param.pb$point[2, ], col="orange")
legend("top", legend=c("Confidence bands", "Prediction bands"),
       col=c("blue", "orange"), lty=1, cex=0.8)
```

## **Confidence and prediction bands (parametric)**



can see the prediction bands does seem to cover more than 95% of the observations. But since the histogram of the residuals earlier showed that the distribution did not look like a Gaussian distribution, it is probably more suitable to use the non-parametric bootstrapping.

## 3 Assignment 4