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- Comment: The time series plot for GDP, household consumption, government expenditure and investment shows the strong correlation between those time series. Consumption, investment, and government expenditure make up for about 52, 22 and 24 percent of GDP, respectively.
- Comment: The stationary (cyclical) component of GDP, consumption, investment, and government expenditure is obtained using the HP filter with a smoothing parameter of 1600. The cyclical components for each variable are then plotted on the same graph. The plot shows how each variable deviates from its long-term trend over time. The cyclical component is much smoother than the original time series and captures the long-term trends in the data. From the curves, it appears that investments is the most volatile time series among the four.
- Comment: The results indicate that the cyclical components of output (Y), consumption (C), investment (I), and government spending (G) have standard deviations ranging from 0.2112 to 0.2438, and relative standard deviations ranging from 1.7054% to 2.1316%. The contemporaneous output correlations of cyclical components suggest that there are high positive correlations among Y, C, I, and G, with correlation coefficients ranging from 0.9786 to 1.0000. This indicates that the cyclical fluctuations in these variables tend to move together. The relative standard deviation of investment is the highest among the four variables, at 2.1316%. This suggests that investment is the most volatile of the four components. The relative standard deviation of consumption is slightly higher than that of output, at 1.7531% and 1.7054%, respectively. This suggests that consumption is also subject to some volatility, although less so than investment.
- Comment: The subsample analysis shows that cyclical components of output, consumption, investment, and government spending are highly correlated, with output and consumption being almost perfectly correlated. The relative standard deviation of the cyclical components for each variable is around 1.4%. Compared to the results of the full sample, the subsample analysis shows a slightly lower degree of cyclical volatility.
- Comment: For subsample 2, the standard deviations of cyclical components are much lower than both the full sample and subsample 1. The relative standard deviations are also much lower for subsample 2. The contemporaneous output correlations of cyclical components for subsample 2 show higher correlation between Y and G compared to subsample 1, but lower correlation between Y and I. Overall, subsample 2 shows much lower volatility and correlation compared to the full sample and subsample 1.

## Macroeconomics assignment 1

```
title = 'Advanced Macroeconomics 2 Assignment 1';
author = 'Tim Koenders and Max Heinze';
fprintf('%s\n%s\n\n', title, author);
```

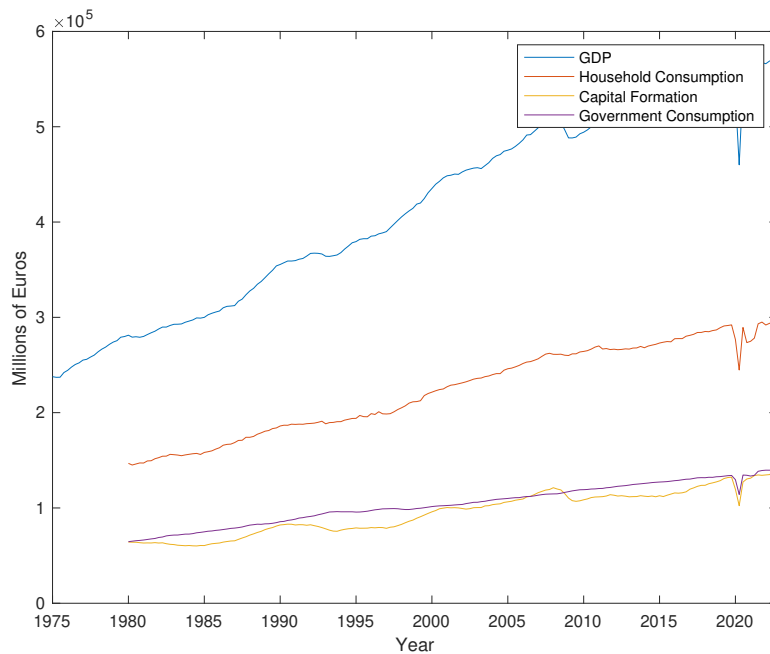
```
Advanced Macroeconomics 2 Assignment 1
Tim Koenders and Max Heinze
```

### Question 1

```
% Read in macroeconomic data from an Excel file and prepare data
data=readtable("Data_Macro2_France.xlsx");
data.Year=datetime(data.TIME,'InputFormat','uuuu-qqq','Format','uuuu-qqq');
data_t timetable = table2timetable(data, 'RowTimes', 'Year');
Y = data.GDP;
C = data.HouseholdConsumption;
I = data.CapitalFormation;
G = data.GovernmentConsumption;
Year = data.Year;
C = rmmissing(C);
I = rmmissing(I);
G = rmmissing(G);
% Remove the first 20 years of GDP data to make time series balanced (since they contain missing values)
Y(1:20) = [];
Year(1:20) = [];

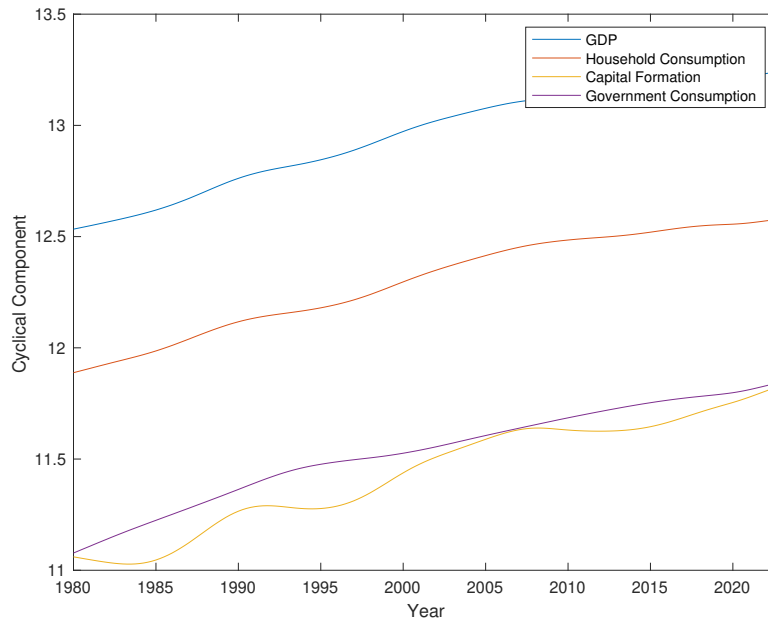
%Calculating sample means and plotting the time series
C_Y = C ./ Y;
I_Y = I ./ Y;
G_Y = G ./ Y;
fprintf('Sample means:\n');
fprintf('C/Y: %.4f\n', mean(C_Y));
fprintf('I/Y: %.4f\n', mean(I_Y));
fprintf('G/Y: %.4f\n', mean(G_Y));
figure;
plot(data.Year, data.GDP, data.Year, data.HouseholdConsumption, data.Year, data.CapitalFormation, data.Year, data.GovernmentConsumption);
xlabel('Year');
ylabel('Millions of Euros');
legend('GDP', 'Household Consumption', 'Capital Formation', 'Government Consumption');
```

Sample means:  
C/Y: 0.5203  
I/Y: 0.2201  
G/Y: 0.2418



**Comment:** The time series plot for GDP, household consumption, government expenditure and investment shows the strong correlation between those time series. Consumption, investment, and government expenditure make up for about 52, 22 and 24 percent of GDP, respectively.

```
%obtaining the stationary (cyclical) component using the HP filter and plot the cyclical component
lambda = 1600; % set the smoothing parameter
Y_cycle = hpfilter(log(Y), lambda);
C_cycle = hpfilter(log(C), lambda);
I_cycle = hpfilter(log(I), lambda);
G_cycle = hpfilter(log(G), lambda);
plot(Year, Y_cycle, Year, C_cycle, Year, I_cycle, Year, G_cycle);
xlabel('Year');
ylabel('Cyclical Component');
legend('GDP', 'Household Consumption', 'Capital Formation', 'Government Consumption');
```



**Comment:** The stationary (cyclical) component of GDP, consumption, investment, and government expenditure is obtained using the HP filter with a smoothing parameter of 1600. The cyclical components for each variable are then plotted on the same graph. The plot shows how each variable deviates from its long-term trend over time. The cyclical component is much smoother than the original time series and captures the long-term trends in the data. From the curves, it appears that investments is the most volatile time series among the four.

```
%creating summary table of business cycle stylized facts (full sample)
std_Y_cycle = std(Y_cycle);
std_C_cycle = std(C_cycle);
std_I_cycle = std(I_cycle);
std_G_cycle = std(G_cycle);
fprintf('Standard deviations of cyclical components:\n');
fprintf('Y_cycle: %.4f\n', std_Y_cycle);
fprintf('C_cycle: %.4f\n', std_C_cycle);
fprintf('I_cycle: %.4f\n', std_I_cycle);
fprintf('G_cycle: %.4f\n', std_G_cycle);
Y_rsd = std(Y_cycle) / mean(Y_cycle) * 100;
C_rsd = std(C_cycle) / mean(C_cycle) * 100;
I_rsd = std(I_cycle) / mean(I_cycle) * 100;
```

```

G_rsd = std(G_cycle) / mean(G_cycle) * 100;
fprintf('Relative Standard Deviations:\n');
fprintf('Y_cycle: %.4f%%\n', Y_rsd);
fprintf('C_cycle: %.4f%%\n', C_rsd);
fprintf('I_cycle: %.4f%%\n', I_rsd);
fprintf('G_cycle: %.4f%%\n', G_rsd);
corr_cyclical = corrcoef([Y_cycle, C_cycle, I_cycle, G_cycle]);
corr_matrix = corrcoef([Y_cycle, C_cycle, I_cycle, G_cycle]);
disp('Contemporaneous Output Correlations of Cyclical Components')
disp('-----')
disp('          Y          C          I          G')
disp(corr_matrix)
T = table(std_Y_cycle, std_C_cycle, std_I_cycle, std_G_cycle, Y_rsd, C_rsd, I_rsd, G_rsd, ...
    corr_matrix(1,1), corr_matrix(1,2), corr_matrix(1,3), corr_matrix(1,4), ...
    corr_matrix(2,1), corr_matrix(2,2), corr_matrix(2,3), corr_matrix(2,4), ...
    corr_matrix(3,1), corr_matrix(3,2), corr_matrix(3,3), corr_matrix(3,4), ...
    corr_matrix(4,1), corr_matrix(4,2), corr_matrix(4,3), corr_matrix(4,4), ...
    'VariableNames', {'Std_Y', 'Std_C', 'Std_I', 'Std_G', 'RSD_Y', 'RSD_C', 'RSD_I', ...
        'Corr_Y_Y', 'Corr_Y_C', 'Corr_Y_I', 'Corr_Y_G', ...
        'Corr_C_Y', 'Corr_C_C', 'Corr_C_I', 'Corr_C_G', ...
        'Corr_I_Y', 'Corr_I_C', 'Corr_I_I', 'Corr_I_G', ...
        'Corr_G_Y', 'Corr_G_C', 'Corr_G_I', 'Corr_G_G'});

```

```
disp(T)
```

Standard deviations of cyclical components:

Y\_cycle: 0.2208

C\_cycle: 0.2156

I\_cycle: 0.2438

G\_cycle: 0.2112

Relative Standard Deviations:

Y\_cycle: 1.7054%

C\_cycle: 1.7531%

I\_cycle: 2.1316%

G\_cycle: 1.8319%

Contemporaneous Output Correlations of Cyclical Components

```

-----
          Y          C          I          G
1.0000    0.9985    0.9921    0.9913
0.9985    1.0000    0.9924    0.9900
0.9921    0.9924    1.0000    0.9786
0.9913    0.9900    0.9786    1.0000

Std_Y      Std_C      Std_I      Std_G      RSD_Y      RSD_C      RSD_I      RSD_G      Corr
-----

```

0.22085    0.21558    0.24376    0.21121    1.7054    1.7531    2.1316    1.8319

**Comment:** The results indicate that the cyclical components of output (Y), consumption (C), investment (I), and government spending (G) have standard deviations ranging from 0.2112 to 0.2438, and relative standard deviations ranging from 1.7054% to 2.1316%. The contemporaneous output correlations of cyclical components suggest that there are high positive correlations among Y, C, I, and G, with correlation coefficients ranging from 0.9786 to 1.0000. This indicates that the cyclical fluctuations in these variables tend to move together. The relative standard deviation of investment is the highest among the four variables, at 2.1316%. This suggests that investment is the most volatile of the four components. The relative standard deviation of consumption is slightly higher than that of output, at 1.7531% and 1.7054%, respectively. This suggests that consumption is also subject to some volatility, although less so than investment.

```
% Splitting the data into two parts based on the date range
Y_cycle1 = Y_cycle(1:112,:);
C_cycle1 = C_cycle(1:112,:);
I_cycle1 = I_cycle(1:112,:);
G_cycle1 = G_cycle(1:112,:);
Y_cycle2 = Y_cycle(113:end,:);
C_cycle2 = C_cycle(113:end,:);
I_cycle2 = I_cycle(113:end,:);
G_cycle2 = G_cycle(113:end,:);

% Summary table for the "until 2007Q4" sample (hereafter called "subsample 1"
std_Y_cycle1 = std(Y_cycle1);
std_C_cycle1 = std(C_cycle1);
std_I_cycle1 = std(I_cycle1);
std_G_cycle1 = std(G_cycle1);
fprintf('Standard deviations of cyclical components for subsample 1:\n');
fprintf('Y_cycle: %.4f\n', std_Y_cycle1);
fprintf('C_cycle: %.4f\n', std_C_cycle1);
fprintf('I_cycle: %.4f\n', std_I_cycle1);
fprintf('G_cycle: %.4f\n', std_G_cycle1);
```

```

Y_rsd1 = std(Y_cycle1) / mean(Y_cycle1) * 100;
C_rsd1 = std(C_cycle1) / mean(C_cycle1) * 100;
I_rsd1 = std(I_cycle1) / mean(I_cycle1) * 100;
G_rsd1 = std(G_cycle1) / mean(G_cycle1) * 100;
fprintf('Relative Standard Deviations for subsample 1:\n');
fprintf('Y_cycle: %.4f%%\n', Y_rsd1);
fprintf('C_cycle: %.4f%%\n', C_rsd1);
fprintf('I_cycle: %.4f%%\n', I_rsd1);
fprintf('G_cycle: %.4f%%\n', G_rsd1);
corr_matrix1 = corrcoef([Y_cycle1, C_cycle1, I_cycle1, G_cycle1]);
disp('Contemporaneous Output Correlations of Cyclical Components for subsample 1')
disp('-----')
disp('          Y          C          I          G')
disp(corr_matrix1)
T1 = table(std_Y_cycle1, std_C_cycle1, std_I_cycle1, std_G_cycle1, Y_rsd1, C_rsd1, I_rsd1, G_rsd1, ...
    corr_matrix1(1,1), corr_matrix1(1,2), corr_matrix1(1,3), corr_matrix1(1,4), ...
    corr_matrix1(2,1), corr_matrix1(2,2), corr_matrix1(2,3), corr_matrix1(2,4), ...
    corr_matrix1(3,1), corr_matrix1(3,2), corr_matrix1(3,3), corr_matrix1(3,4), ...
    corr_matrix1(4,1), corr_matrix1(4,2), corr_matrix1(4,3), corr_matrix1(4,4), ...
    'VariableNames', {'Std_Y', 'Std_C', 'Std_I', 'Std_G', 'RSD_Y', 'RSD_C', 'RSD_I', 'RSD_G', ...
        'Corr_Y_Y', 'Corr_Y_C', 'Corr_Y_I', 'Corr_Y_G', ...
        'Corr_C_Y', 'Corr_C_C', 'Corr_C_I', 'Corr_C_G', ...
        'Corr_I_Y', 'Corr_I_C', 'Corr_I_I', 'Corr_I_G', ...
        'Corr_G_Y', 'Corr_G_C', 'Corr_G_I', 'Corr_G_G'});

disp(T1)

```

Standard deviations of cyclical components for subsample 1:

Y\_cycle: 0.1801

C\_cycle: 0.1684

I\_cycle: 0.1944

G\_cycle: 0.1632

Relative Standard Deviations for subsample 1:

Y\_cycle: 1.4035%

C\_cycle: 1.3830%

I\_cycle: 1.7198%

G\_cycle: 1.4305%

Contemporaneous Output Correlations of Cyclical Components for subsample 1

```

-----
          Y          C          I          G
1.0000    0.9983    0.9877    0.9831
0.9983    1.0000    0.9905    0.9787
0.9877    0.9905    1.0000    0.9542
0.9831    0.9787    0.9542    1.0000

Std_Y      Std_C      Std_I      Std_G      RSD_Y      RSD_C      RSD_I      RSD_G      Corr_

```

-----	-----	-----	-----	-----	-----	-----	-----	-----
0.18006	0.16839	0.19437	0.16324	1.4035	1.383	1.7198	1.4305	1

**Comment:** The subsample analysis shows that cyclical components of output, consumption, investment, and government spending are highly correlated, with output and consumption being almost perfectly correlated. The relative standard deviation of the cyclical components for each variable is around 1.4%. Compared to the results of the full sample, the subsample analysis shows a slightly lower degree of cyclical volatility.

```
% Summary table for the "from 2008Q1" sample (hereafter called "subsample 2")
std_Y_cycle2 = std(Y_cycle2);
std_C_cycle2 = std(C_cycle2);
std_I_cycle2 = std(I_cycle2);
std_G_cycle2 = std(G_cycle2);
fprintf('Standard deviations of cyclical components for subsample 2:\n');
fprintf('Y_cycle: %.4f\n', std_Y_cycle2);
fprintf('C_cycle: %.4f\n', std_C_cycle2);
fprintf('I_cycle: %.4f\n', std_I_cycle2);
fprintf('G_cycle: %.4f\n', std_G_cycle2);
Y_rsd1 = std(Y_cycle2) / mean(Y_cycle2) * 100;
C_rsd1 = std(C_cycle2) / mean(C_cycle2) * 100;
I_rsd1 = std(I_cycle2) / mean(I_cycle2) * 100;
G_rsd1 = std(G_cycle2) / mean(G_cycle2) * 100;
fprintf('Relative Standard Deviations for subsample 2:\n');
fprintf('Y_cycle: %.4f%%\n', Y_rsd1);
fprintf('C_cycle: %.4f%%\n', C_rsd1);
fprintf('I_cycle: %.4f%%\n', I_rsd1);
fprintf('G_cycle: %.4f%%\n', G_rsd1);
corr_matrix1 = corrcoef([Y_cycle2, C_cycle2, I_cycle2, G_cycle2]);
disp('Contemporaneous Output Correlations of Cyclical Components for subsample 2')
disp('-----')
disp('          Y          C          I          G')
disp(corr_matrix1)
T2 = table(std_Y_cycle2, std_C_cycle2, std_I_cycle2, std_G_cycle2, Y_rsd1, C_rsd1, I_rsd1, G_rsd1, ...
    corr_matrix1(1,1), corr_matrix1(1,2), corr_matrix1(1,3), corr_matrix1(1,4), ...
    corr_matrix1(2,1), corr_matrix1(2,2), corr_matrix1(2,3), corr_matrix1(2,4), ...
    corr_matrix1(3,1), corr_matrix1(3,2), corr_matrix1(3,3), corr_matrix1(3,4), ...
    corr_matrix1(4,1), corr_matrix1(4,2), corr_matrix1(4,3), corr_matrix1(4,4), ...
    'VariableNames', {'Std_Y', 'Std_C', 'Std_I', 'Std_G', 'RSD_Y', 'RSD_C', 'RSD_I', 'RSD_G'})
```



```

'Corr_Y_Y', 'Corr_Y_C', 'Corr_Y_I', 'Corr_Y_G', ...
'Corr_C_Y', 'Corr_C_C', 'Corr_C_I', 'Corr_C_G', ...
'Corr_I_Y', 'Corr_I_C', 'Corr_I_I', 'Corr_I_G', ...
'Corr_G_Y', 'Corr_G_C', 'Corr_G_I', 'Corr_G_G'});

disp(T2)

```

Standard deviations of cyclical components for subsample 2:

Y\_cycle: 0.0391

C\_cycle: 0.0327

I\_cycle: 0.0640

G\_cycle: 0.0517

Relative Standard Deviations for subsample 2:

Y\_cycle: 0.2969%

C\_cycle: 0.2611%

I\_cycle: 0.5475%

G\_cycle: 0.4401%

Contemporaneous Output Correlations of Cyclical Components for subsample 2

-----							
Y	C	I	G				
1.0000	0.9982	0.9178	0.9900				
0.9982	1.0000	0.9046	0.9924				
0.9178	0.9046	1.0000	0.8785				
0.9900	0.9924	0.8785	1.0000				
Std_Y	Std_C	Std_I	Std_G	RSD_Y	RSD_C	RSD_I	RSD_G
-----	-----	-----	-----	-----	-----	-----	-----
0.039122	0.032702	0.063977	0.05172	0.29695	0.26113	0.54754	0.44013

**Comment:** For subsample 2, the standard deviations of cyclical components are much lower than both the full sample and subsample 1. The relative standard deviations are also much lower for subsample 2. The contemporaneous output correlations of cyclical components for subsample 2 show higher correlation between Y and G compared to subsample 1, but lower correlation between Y and I. Overall, subsample 2 shows much lower volatility and correlation compared to the full sample and subsample 1.

```
save('my_workspace.mat')
```