Mostly Pointless Spatial Econometrics

(Gibbons & Overman, 2012)
Spatial Economics Seminar Presentation

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Spatial Econometric Models And Their Issues

The Experimentalist Paradigm And Spatial Econometrics

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$$y_i = \rho \mathbf{w}_i' \mathbf{y} + \mathbf{X} \boldsymbol{\beta} + \mathbf{w}_i' \mathbf{X} \boldsymbol{\gamma} + \mathbf{u}_i \boldsymbol{\gamma},$$
 (1) $\mathbf{u}_i = \lambda \mathbf{w}_i' \mathbf{u} + \mathbf{v}_i$

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(1)

$$y_{i} = \rho \mathbf{w}_{i}'(\rho \mathbf{W}\mathbf{y} + \mathbf{X}\boldsymbol{\beta} + \mathbf{W}\mathbf{X}\boldsymbol{\gamma} + \mathbf{u}) + \mathbf{w}_{i}'\boldsymbol{\beta} + \mathbf{w}_{i}'\mathbf{X}\boldsymbol{\gamma} + u_{i}$$

$$= \rho^{2}\mathbf{w}_{i}'\mathbf{W}\mathbf{y} + \rho \mathbf{w}_{i}'\mathbf{X}\boldsymbol{\beta} + \rho \mathbf{w}_{i}'\mathbf{X}\boldsymbol{\gamma} + \rho \mathbf{w}_{i}'\mathbf{u} + \mathbf{X}'\boldsymbol{\beta} + \mathbf{w}_{i}'\mathbf{X}\boldsymbol{\gamma} + u_{i}$$

$$= \rho^{2}\mathbf{w}_{i}'\mathbf{W}\mathbf{y} + \mathbf{X}'\boldsymbol{\beta} + \rho \mathbf{w}_{i}'(\mathbf{X}\boldsymbol{\beta} + \boldsymbol{\gamma}) + \rho \mathbf{w}_{i}'\mathbf{W}\mathbf{X}\boldsymbol{\gamma} + v_{i}$$

$$= \dots$$

$$= \rho^{n}(\mathbf{w})_{i}'\mathbf{W}^{n-1}\mathbf{y} + \mathbf{X}'\boldsymbol{\beta} + \mathbf{w}_{i}'\mathbf{X}(\rho\boldsymbol{\beta} + \boldsymbol{\gamma})$$

$$+ \rho \mathbf{w}_{i}'\mathbf{W}\mathbf{X}(\rho\boldsymbol{\beta} + \boldsymbol{\gamma}) + \rho^{2}\mathbf{w}_{i}'\mathbf{W}^{2}\mathbf{X}(\rho\boldsymbol{\beta} + \boldsymbol{\gamma}) + \dots + v_{i},$$

$$(2)$$

Under standard regularity conditions: $\lim_{n\to\infty} \rho^n(\mathbf{W}')^{n-1}\mathbf{W}^{n-1} = 0$

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However, all of these models have the same reduced form, namely:

$$y_i = \mathbf{x}_i' \beta + \mathbf{w}_i' \mathbf{X} \pi_1 + \mathbf{w}_i' \mathbf{W} \mathbf{X} \pi_2 + \mathbf{w}_i' \mathbf{W}^2 \mathbf{X} \pi_2 + \dots + v_i$$
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 (3)

Spatial Economics uses neighbors characteristics ($\mathbf{w}_{i}^{\prime}\mathbf{X}$, $\mathbf{w}_{i}^{\prime}\mathbf{W}\mathbf{X}$, ...) under the assumption that these are exogenous to instrument for $\mathbf{w}_{i}^{\prime}\mathbf{y}$

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$$\mathbf{y}_{i} = \rho_{1} \mathbf{E}[\mathbf{y}_{i}|a] + \mathbf{x}_{i}'\beta + \mathbf{E}[\mathbf{x}_{i}'|a]\gamma + \mathbf{v}_{i}, \tag{4}$$

Solving for the reduced form by taking the expectation of (4) and rearranging yields:

$$y_i = \mathbf{x}_i'\beta + \mathbf{E}[\mathbf{x}_i'|a]\frac{(\beta\rho_1 + \gamma)}{(1 - \rho_1)} + \frac{\rho_1}{1 - \rho_1}\mathbf{E}[\mathbf{v}_i|a] + \mathbf{v}_i$$
(5)

No chance that we can distinguish the endogenous (ρ_1) from the exogenous peer effects (γ)!

Spatial Durbin Model again:

$$y_i = \rho_1 \mathbf{w}_i' \mathbf{y} + \mathbf{x}_i' \beta + \mathbf{w}_i' \mathbf{X} \gamma + u_i$$
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Identification of parameters works because:

- ullet The structure of the spatial weights matrix $oldsymbol{W}$ is said to be known
- Exogeneity of X and w'_iWX, ...

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(7)

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Identification breaks down in most spatial econometric models because:

- the exact structure of **W** is not known! (exclusion restriction is not fulfilled)
- Weak Instruments because of high correlation between spatial lags w'_iX, w'_iWX, w'_iW²X,

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$$\mathbf{y}_{i} = \rho \mathbf{w}_{i}'\mathbf{y} + \mathbf{x}_{i}'\boldsymbol{\beta} + \mathbf{w}_{i}'\mathbf{X} \boldsymbol{\gamma} + u_{i}$$
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- These reflection issues transfer to differenced specifications and are not solved by randomization²

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Reduced Form SLX Models

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- How to proceed?

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"[Any] empirical research that aims to find out if x causes y needs to find a source of exogenous variation in x!"³

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Thank you!

Appendix: Spatial Econometric Models

Starting point:

$$y_i = \mathbf{x}_i'\beta + u_i \tag{9}$$

To incorporate spatial dependence we know the

SAR model:

$$y_i = \rho \mathbf{w}_i' \mathbf{y} + \mathbf{x_i} \boldsymbol{\beta} + \mathbf{u_i}$$
 (10)

SLX model:

$$\mathbf{y}_i = \mathbf{x}_i' \boldsymbol{\beta} + \mathbf{w}_i' \mathbf{X} \boldsymbol{\gamma} + u_i$$
 (11)

SE model:

$$y_i = \mathbf{x}_i' \boldsymbol{\beta} + u_i, \tag{12}$$

where
$$u_i = \rho \mathbf{w}_i' \mathbf{u} + \mathbf{v}_i$$
 (13)

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