Lab Report # 2: Simulating Simple Mechanisms

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Abstract

The simulations of several types of reactions were performed using 100 dice. Three areas A, B, and C represent species. The number of dice inside of an area represented the concentration of the species. The trial of dice rolled is representative of the time. Parallel:

$$A \longrightarrow B \tag{1}$$

 $A \longrightarrow C$ (2)

Reversible:

$$A \longleftrightarrow B$$
 (3)

Consecutive:

$$A \longrightarrow B$$
 (4)

$$B \longrightarrow C$$
 (5)

reactions were analyzed. These chemical reactions proceed with purely probabilistic behavior-or rather, the laws of thermodynamics which explain the behavior of very large numbers.

1 Data

Here, several tables and plots will appear that hold the data of rolled dice. Unfortunately, it will appear somewhat raw.

1.1 Parallel Reactions

First, is the data of dice rolled for parallel reactions. This was produced from the following instructions:

- 1) All dice begin in A
- 2) For t=1, roll all dice in A. All that land on 1 go to B and those landing on 2 or 3 move to C. The rest stay in A
- 3) Repeat until all dice are in B or C

The recorded data is listed in table 1.1.

This data was plotted along with the theoretical results for concentration as a function of time. More discussion on this is placed in the calculations section of this paper, but the plots generated are shown in figure 1.

Parallel				
Time	A	В	С	
0	100	0	0	
1	56	12	32	
2	32	20	48	
3	19	23	58	
4	12	26	62	
5	6	29	65	
6	1	31	68	
7	1	31	68	
8	0	31	69	

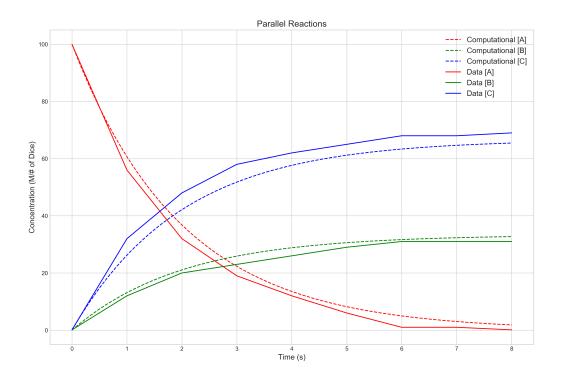


Figure 1: Concentration of species from parallel reactions as a function of time. Experimental and computed analytical results are plotted.

1.2 Reversible

The reversible reaction is modeled by the dice through these steps:

- 1) All dice begin in A
- 2) For t=1, roll all dice in A. Values 1 and 2 go to area B.
- 3) Roll all dice in A. Move values 1 and 2 to B. Roll all dice in B (excluding those just moved.) If a 6 is rolled, move it back to A.
- 4) Repeat step 3 until values are stable in A and B.

The corresponding values are recorded in table 1.2.

Reversible				
Time	A	В		
0	100	0		
1	67	33		
2	58	42		
3	48	52		
4	39	61		
5	40	60		
6	37	63		
7	38	62		
8	39	61		
9	38	62		

Similarly to parallel reactions I have plotted the data in figure 2.

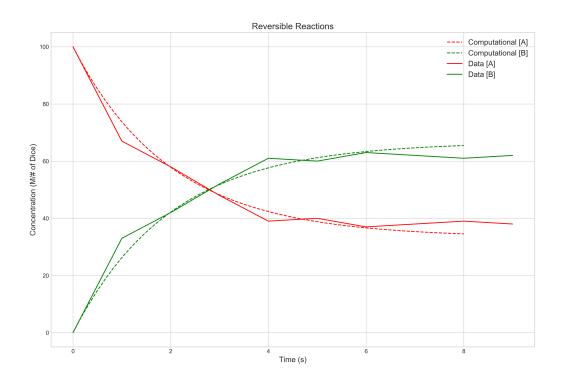


Figure 2: Concentration of species from reversible reactions as a function of time. Experimental and computed analytical results are plotted.

1.3 Consecutive Reactions

Consecutive reactions were simulated in the following manner using dice:

- 1) All dice begin in A
- 2) Roll all dice in A. Values between 1 and 5 move to area B. Sixes stay in A.
- 3) Roll all dice in B. If a 1 is rolled, it moves to C. Values between 2 and 6 stay in B. Now move all in A and move values 1-5 to B
- 4) Repeat until all dice are in C

A similar procedure is used, but with a "faster" second reaction. The data for consecutive reactions part 1 and 2 are recorded in table 1.3.

Cons	secutiv	ve Pt	. 1	Cons	ecutiv	e Pt.	2
Time	A	В	С	Time	A	В	С
0	100	0	0	0	100	0	0
1	17	83	0	1	82	18	0
2	2	84	14	2	70	14	16
3	0	66	34	3	60	11	29
4	0	57	43	4	49	13	38
5	0	46	54	5	43	7	50
6	0	37	63	6	33	11	56
7	0	30	70	7	27	7	66
8	0	22	78	8	18	12	70
9	0	19	81	9	16	3	81
10	0	16	84	10	13	4	83
11	0	16	84	11	11	2	87
12	0	12	88	12	10	1	89
13	0	12	88	13	6	4	90
14	0	11	89	14	6	1	93
15	0	8	92	15	5	1	94
16	0	6	94	16	4	1	95
17	0	5	95	17	4	0	96
18	0	5	95	18	4	0	96
19	0	4	96	19	4	0	96
20	0	2	98	20	3	1	96
21	0	1	99	21	3	0	97
22	0	1	99	22	2	1	97
23	0	1	99	23	2	0	98
24	0	0	100	24	2	0	98

Pt. 2 Cont				
Time	A	В	С	
25	2	0	98	
26	2	0	98	
26 27 28 29	2	0	98	
28	2	0	98	
29	2	0	98	
30 31 32	2	0	98	
31	2	0	98	
32	2	0	98	
33	2	0	98	
33 34	2	0	98 98	
35	2	0	98	
36 37	2	0	98	
37	2	0	98	
38	2	0	98	
39	2	0	98	
40	2	0	98	
41	2	0	98	
42	2	0	98	
43	2	0	98	
44	2	0	98	
40 41 42 43 44 45 46	A 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	0	98	
46	2	0	98	
47	2	0	98	
47	2	0	98	
49	2	0	98	

Pt. 2 Cont				
Time	A	В	С	
50	2	0	98	
51	2	0	98	
52	1	1	98	
53	1	0	99	
54	1	0	99	
55	0	1	99	
56	0	0	100	
57	0	0	100	

Figure 3 contains the plots for the consecutive reactions part 1 and figure 4 shows them for part 2.

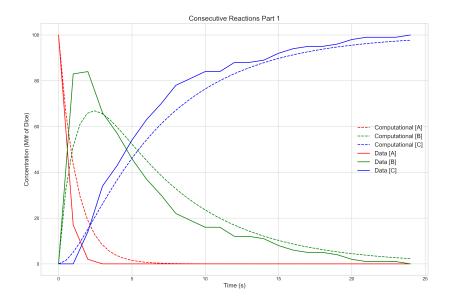


Figure 3: Concentration of species from consecutive reactions as a function of time. Experimental and computed analytical results are plotted.

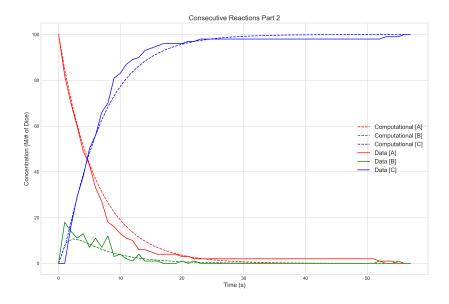


Figure 4: Concentration of species from consecutive reactions as a function of time. Experimental and computed analytical results are plotted.

2 Calculations

Quite simply, the tabulated data was determined through the probabilistic behavior of rolling dice. The data was then loaded into python and plotted along with computed analytical results of each type of reaction. The analytical results are obtained through the integration of the various rate laws that apply to each type of reaction. More information on how these analytical results were found in Atkins and Paula's text *PhysicalChemistry*: Thermodynamics, Structure, and Change chapter 20E.

For parallel reactions the concentration of each species can be expressed as functions of time and are shown below:

$$[A] = [A]_0 e^{-k_T t} \tag{6}$$

$$[B] = \frac{k_1}{k_T} [A]_0 (1 - e^{-k_T t}) \tag{7}$$

$$[C] = \frac{k_2}{k_T} [A]_0 (1 - e^{-k_T t}) \tag{8}$$

Where all k_n values along with $[A]_0$ are constants. The variable t is time and [N] represents the concentration of some species, N. These functions were evaluated for the same time period as the amount of "seconds" the dice simulations occurred and were plotting along with the data points recorded. The results are available in the figures in the data section. I will omit the equations used for the other reaction types as I feel they are redundant to the lab handout provided. However, I have provided the source code at the end of this report for the graphs I made. Note, all of the data that I pulled from excel for my python file is displayed in various tables around this report. In this script I have also included best fit data to attempt to determine the simulated k_n values. Fit lines were produced using the SciPy library and the best fit curves are included with the experimental data points for parallel, reversible, and consecutive respectively.

Values for $\frac{[B]}{[C]}$ and $\frac{k_1}{k_2}$ are shown in figure 9.

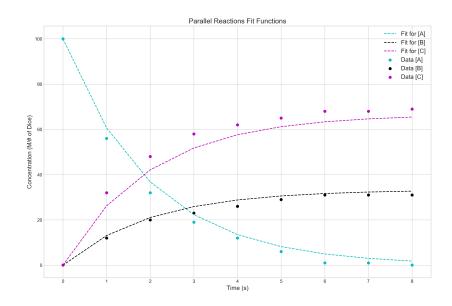


Figure 5: Best fit lines for parallel reaction simulation with dice.

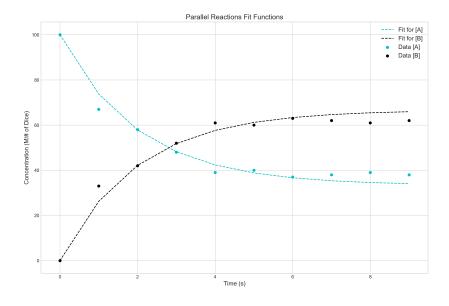


Figure 6: Best fit lines for reversible reaction simulation with dice.

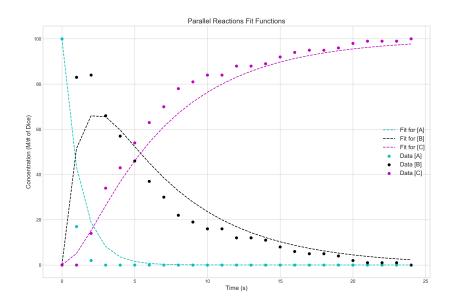


Figure 7: Best fit lines for consecutive reaction simulation with dice.

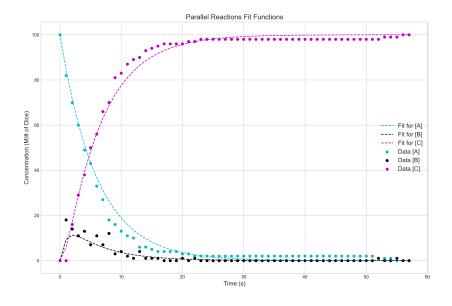


Figure 8: Best fit lines for consecutive reaction simulation with dice.

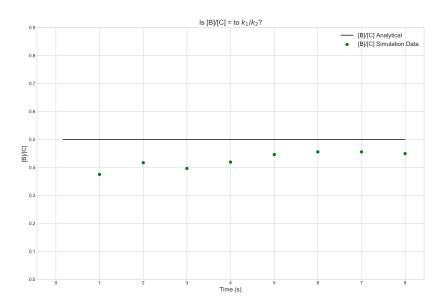


Figure 9: Concentration ratios and k constant ratios.

Branching ratios?

$$K_{eq} = \frac{[B]}{[A]} \bigg|_{eq} \tag{9}$$

Taking average of last three values for reversible reactions:

$$\frac{[B]}{[A]} = \frac{62 + 61 + 62}{38 + 39 + 38} = 1.609$$
(10)

Where k_1 and k_2 was found to be 2 using fit data and supposed values. This is off by approximately 20%.

Here are the analytical results for the concentration functions of A, B, and C.

$$[A] = [A]_0 e^{-k_1 t} (11)$$

$$[B] = \frac{k_1}{k_2 - k_1} [A]_0 (e^{-k_1 t} - e^{-k_2 t})$$
(12)

$$[C] = [A]_0 \left[1 - \frac{k_1}{k_2 - k_1} (e^{-k_1 t} - e^{-k_2 t}) - e^{-k_1 t}\right]$$
(13)

When $k_1 > k_2$ we cannot make any assumptions, but when $k_1 >> k_2$ it is fair to say the coefficient: $\frac{k_1}{k_2-k_1} \approx -1$ because a relatively small number subtracted from a relatively large number simply leaves the relatively large number. This brings about:

$$[B] \approx -[A]_0(e^{-k_1t} - e^{-k_2t}) = [A]_0(e^{-k_2t} - e^{-k_1t})$$
(14)

As well as,

$$[C] \approx [A]_0[1 - (-1)(e^{-k_1t} - e^{-k_2t}) - e^{-k_1t}] = [A]_0[1 - e^{-k_2t}]$$
(15)

Now we will show:

$$[C] \approx [A]_0 - [A] - [B]$$
 (16)

Substituting equations 11 and 14 into 16:

$$[C] \approx [A]_0 - [A]_0 (e^{-k2t} - e^{-k_1 t}) - [A]_0 e^{-k_1 t}$$
(17)

Factoring $[A]_0$,

$$[C] \approx [A]_0 (1 - (e^{-k_2 t} - e^{-k_1 t}) - e^{-k_1 t}) = [A]_0 (1 - e^{-k_2 t})$$
(18)

It can be seen equation 15 and 18 are equivalent.

References

[1] Atkins, P. W., & Paula, J. D. (2014). Physical chemistry: thermodynamics, structure, and change. New York: W.H. Freeman.

Python script for plotting.

```
1 # -*- coding: utf-8 -*-
2 ", ", ",
<sup>3</sup> Created on Tue Sep 17 09:41:40 2019
5 @author: maxhu
  " " "
6
                            -----Modules
8 import matplotlib.pyplot as plt
9 import numpy as np
10 import pandas as pd
11 from scipy.optimize import curve_fit
plt.style.use('seaborn-whitegrid')
                             =Constants
15 #==Parallel==
16 A_0 = 100
_{17} k_{-}1p = 1/6
k_{2}p = 2/6
19 k_T = .5
20 #Reversible #
k_1 = 2/6
k_2 = 1/6
23 #——Consecutive=pt.1==#
k_1c1 = 5/6
k_2c1 = 1/6
26 #——Consecutive=pt.2==#
k_1c2 = 1/6
  k_2c2 = 5/6
29
                            ====Functions=
30
32 #==Parallel===#
33
  def AP(t):
34
      return A_0 * np.exp(-k_T * t)
  def BP(t):
36
      return (k_1p / k_T) * A_0 * (1 - np.exp(-k_T * t))
37
  def CP(t):
38
      return (k_2p / k_T) * A_0 * (1 - np.exp(-k_T * t))
39
40
  #===Reversible===#
41
42
  def AR(t):
43
      num = A_{-0} * (k_{-2}r + k_{-1}r * np.exp((-k_{-1}r - k_{-2}r) * t))
44
      den = k_1r + k_2r
      return num / den
46
  def BR(t):
47
      num = k_1 r * A_0 * (1 - np.exp((-k_1 r - k_2 r) * t))
48
      den = k_1r + k_2r
49
      return num / den
50
51
52 #——Consecutive=pt.1==#
```

```
def AC1(t):
                 return A_0 * np.exp(-k_1c1 * t)
 55
       def BC1(t):
 56
                 num = k_1c1 * A_0 * (np.exp(-k_1c1 * t) - np.exp(-k_2c1 * t))
 57
                 den = k_2c1 - k_1c1
 58
                 return num / den
 59
       def CC1(t):
 60
                 return A_0 * (1 - (k_1c1 / (k_2c1 - k_1c1))
 61
                                                     * (np.exp(-k_1c1 * t) - np.exp(-k_2c1 * t))
 63
                                                      -\operatorname{np.exp}(-k_1c1 * t)
           65
       def AC2(t):
 67
                 return A_0 * np.exp(-k_1c2 * t)
       def BC2(t):
                 return (k_1c2 / k_2c2) * A_0 * (np.exp(-k_1c2 * t) - np.exp(-k_2c2 * t))
 70
       def CC2(t):
 71
                 return A_0 - A_0 * np.exp(-k_1c2 * t) - (k_1c2 / k_2c2) * A_0 * (np.exp(-k_1c2 / k_2c2)) * A_0 * 
 72
                                      -k_1c2 * t) - np.exp(-k_2c2 * t)
 73
 74
 75 #===Fitting==#
       def AP_FIT(x, c):
 76
                 return 100 * np.exp(-c*x)
 77
 78
       def BP\_FIT(x, a, c):
 79
                 return a *100 * (1 - np.exp(-c*x))
 80
 81
       def CP_FIT(x, a, c):
 82
                 return a *100 * (1 - np.exp(-c*x))
 83
                                                              ---#
 84
       def AR\_FIT(x, a, b):
                 return (100 / (a + b)) * (b + a * np.exp((-a - b) * x))
 86
 87
       def BR\_FIT(x, a, b, c):
 88
                 return (a * 100 * (1 - np.exp((-a - b) * x))) / (a + b)
 89
 90
       def AC_FIT(x, a):
 91
                 return 100 * np.exp(-a*x)
 92
 93
       def BC_FIT(x, b):
 94
                 return (0.83333333 / (b - 0.83333333)) * 100 * (
 95
                                      np.exp(-0.833333333 * x) - np.exp(-b * x))
 96
 97
       def CC_FIT(x, b):
                 return 100 * (1 - (0.83333333 / (b - 0.83333333)) * (
 99
                                      np.exp(-0.833333333 * x) - np.exp(-b * x)) -
100
                           np.exp(-0.833333333 * x))
101
       def AC_FIT2(x, a):
103
                 return 100 * np.exp(-a*x)
104
105
def BC_FIT2(x, b):
```

```
return (.16666667 / (b - .16666667)) * 100 * (
                np.exp(-.16666667 * x) - np.exp(-b * x))
108
109
   def CC_FIT2(x, b):
       return 100 * (1 - (.16666667 / (b - .16666667)) * (
                np.exp(-.16666667 * x) - np.exp(-b * x)) -
112
           np. exp(-.16666667 * x))
113
114
                                         =Data=
   Par_data = pd.read_excel (r'C:\Users\maxhu\Documents\PChem\Lab 2\Lab2.xlsx',
117
                           sheet_name='Parallel')
118
   Rev_data = pd.read_excel (r'C:\Users\maxhu\Documents\PChem\Lab 2\Lab2.xlsx',
119
                           sheet_name='Reversible')
   Cons1_data = pd.read_excel (r'C:\Users\maxhu\Documents\PChem\Lab 2\Lab2.xlsx',
                           sheet_name='Consecutive pt. 1')
   Cons2_data = pd.read_excel (r'C:\Users\maxhu\Documents\PChem\Lab 2\Lab2.xlsx',
123
                           sheet_name='Consecutive pt. 2')
124
      ——Making some lists with my data——#
126
   A_p = pd.DataFrame(Par_data, columns= ['A'])
128
   B_p = pd.DataFrame(Par_data, columns= ['B'])
   C_p = pd. DataFrame(Par_data, columns= ['C'])
130
  A_p = A_p.values.tolist()
132
B_p = B_p.values.tolist()
  C_p = C_p. values. tolist ()
134
  A_p = [val for sublist in A_p for val in sublist]
136
  B_p = [val for sublist in B_p for val in sublist]
   C_p = [val \text{ for sublist in } C_p \text{ for val in sublist}]
139
140
  A_r = pd.DataFrame(Rev_data, columns= ['A'])
142
   B_r = pd. DataFrame(Rev_data, columns= ['B'])
144
   A_r = A_r \cdot values \cdot tolist()
   B_r = B_r \cdot values \cdot tolist()
146
147
   A_r = [val \text{ for sublist in } A_r \text{ for val in sublist}]
   B_r = [val \text{ for sublist in } B_r \text{ for val in sublist}]
149
   A_c1 = pd. DataFrame(Cons1_data, columns= ['A'])
   B_c1 = pd.DataFrame(Cons1_data, columns= ['B'])
   C_c1 = pd. DataFrame (Cons1_data, columns= ['C'])
155
A_c1 = A_c1 \cdot values \cdot tolist()
   B_c1 = B_c1.values.tolist()
  C_{-c1} = C_{-c1}. values. tolist()
```

```
A_c1 = [val \text{ for sublist in } A_c1 \text{ for val in sublist}]
B_c1 = [val \text{ for sublist in } B_c1 \text{ for val in sublist}]
   C_{-c1} = [val \text{ for sublist in } C_{-c1} \text{ for val in sublist}]
163
164
165 #
166
   A_c2 = pd. DataFrame(Cons2_data, columns= ['A'])
167
  B_c2 = pd.DataFrame(Cons2_data, columns= ['B'])
   C<sub>c2</sub> = pd. DataFrame (Cons2_data, columns= ['C'])
  A_c2 = A_c2. values. tolist()
171
  B_c2 = B_c2. values. tolist()
   C_c2 = C_c2.values.tolist()
   A_c2 = [val for sublist in A_c2 for val in sublist]
  B_c2 = [val for sublist in B_c2 for val in sublist]
   C_{-c2} = [val \text{ for sublist in } C_{-c2} \text{ for val in sublist}]
178
179
                                ==Plotting=
180
181
     ------Parallel----#
182
   t_{values} = np.linspace(0, 8)
   t_{data} = np. linspace(0, 8, 9)
184
185
   fig = plt. figure (1, figsize = (15, 10))
186
   my_fig = fig.add_subplot(111)
   my_fig.set_title('Parallel Reactions', fontsize = '15')
   #Computational Values
   plt.plot(t_values, AP(t_values), color = 'r', label = 'Computational [A]',
190
             linestyle = '--'
   plt.plot(t_values, BP(t_values), color = 'g', label = 'Computational [B]',
             linestyle = '--'
193
   plt.plot(t_values, CP(t_values), color = 'b', label = 'Computational [C]',
194
             linestyle = '--'
195
196 #Actual Data
   plt.plot(t_data, A_p, color = 'r', label = 'Data [A]')
   plt.plot(t_data, B_p, color = 'g', label = 'Data [B]')
   plt.plot(t_data, C_p, color = 'b', label = 'Data [C]')
199
   my_fig.set_xlabel('Time (s)', fontsize = '13')
201
   my_fig.set_ylabel('Concentration (M/# of Dice)', fontsize = '13')
202
203
   plt.legend(loc='best', fontsize = '13')
   plt.savefig('PCHEML2PARALLEL', dpi=300)
205
   #===Reversible===#
207
208
   t_values = np.linspace(0, 8)
209
   t_data = np.linspace(0, 9, 10)
211
fig = plt.figure (2, figsize = (15, 10))
my_fig = fig.add_subplot(111)
my_fig.set_title('Reversible Reactions', fontsize = '15')
```

```
215 #Computational Values
   plt.plot(t_values, AR(t_values), color = 'r', label = 'Computational [A]',
            linestyle = '--'
217
   plt.plot(t_values, BR(t_values), color = 'g', label = 'Computational [B]',
218
            linestyle = '--'
219
220 #Actual Data
   plt.plot(t_data, A_r, color = 'r', label = 'Data [A]')
   plt.plot(t_data, B_r, color = 'g', label = 'Data [B]')
223
   my_fig.set_xlabel('Time (s)', fontsize = '13')
   my_fig.set_ylabel('Concentration (M/# of Dice)', fontsize = '13')
225
  plt.legend(loc='best', fontsize = '13')
227
   plt.savefig('PCHEML2REVERSIBLE', dpi=300)
229
      —Consecutive 1——#
230
231
   t_{values} = np.linspace(0, 24)
232
   t_data = np.linspace(0, 24, 25)
233
fig = plt.figure (3, figsize = (15, 10))
   my_fig = fig.add_subplot(111)
  my_fig.set_title('Consecutive Reactions Part 1', fontsize = '15')
238 #Computational Values
   plt.plot(t_values, AC1(t_values), color = 'r', label = 'Computational [A]',
            linestyle = '--'
240
   plt.plot(t_values, BC1(t_values), color = 'g', label = 'Computational [B]',
            linestyle = '--'
242
   plt.plot(t_values, CC1(t_values), color = 'b', label = 'Computational [C]',
            linestyle = '--'
244
245 #Actual Data
  plt.plot(t_data, A_c1, color = 'r', label = 'Data [A]')
   plt.plot(t_data, B_c1, color = 'g', label = 'Data [B]')
   plt.plot(t_data, C_c1, color = 'b', label = 'Data [C]')
  my_fig.set_xlabel('Time (s)', fontsize = '13')
250
   my_fig.set_ylabel('Concentration (M/# of Dice)', fontsize = '13')
251
252
   plt.legend(loc='best', fontsize = '13')
   plt.savefig('PCHEML2CONSECUTIVE1', dpi=300)
254
255
  #____Consecutive 2____#
256
257
   t_{\text{values}} = \text{np.linspace}(0, 57)
   t_{data} = np. linspace (0, 57, 58)
259
  fig = plt. figure (4, figsize = (15, 10))
  my_fig = fig.add_subplot(111)
  my_fig.set_title('Consecutive Reactions Part 2', fontsize = '15')
264 #Computational Values
  plt.plot(t_values, AC2(t_values), color = 'r', label = 'Computational [A]',
            linestyle = '--'
  plt.plot(t_values, BC2(t_values), color = 'g', label = 'Computational [B]',
267
           linestyle = '--'
```

```
plt.plot(t_values, CC2(t_values), color = 'b', label = 'Computational [C]',
            linestyle = '--'
270
271 #Actual Data
plt.plot(t_{data}, A_{c2}, color = 'r', label = 'Data [A]')
plt.plot(t_{data}, B_{c2}, color = 'g', label = 'Data [B]')
  plt.plot(t_data, C_c2, color = 'b', label = 'Data [C]')
275
  my_fig.set_xlabel('Time (s)', fontsize = '13')
  my_fig.set_ylabel('Concentration (M/# of Dice)', fontsize = '13')
   plt.legend(loc='best', fontsize = '13')
279
   plt.savefig('PCHEML2CONSECUTIVE2', dpi=300)
281
282
283
                               =Plotting=
285
        —Parallel—
286
  t_{values} = np. linspace(0, 8)
t_{\text{data}} = \text{np.linspace}(0, 8, 9)
289 #Fits
  popt, pcov = curve_fit (AP_FIT, t_data, AP(t_data))
290
291
  fig = plt. figure (5, figsize = (15, 10))
  my_fig = fig.add_subplot(111)
  my_fig.set_title('Parallel Reactions Fit Functions', fontsize = '15')
295 #Computational Values
   plt.plot(t_data, AP_FIT(t_data, *popt), color = 'c', label = 'Fit for [A]',
296
            linestyle = '---')
   print (popt)
298
  popt, pcov = curve_fit(BP_FIT, t_data, BP(t_data))
300
   plt.plot(t_data, BP_FIT(t_data, *popt), color = 'k', label = 'Fit for [B]',
301
            linestyle = '--'
302
   print (popt)
303
304
  popt, pcov = curve_fit (CP_FIT, t_data, CP(t_data))
305
306
  plt.plot(t_data, CP_FIT(t_data, *popt), color = 'm', label = 'Fit for [C]',
307
            linestyle = '--'
308
   print(popt)
309
310
311 #Actual Data
  plt.scatter(t_data, A_p, color = 'c', label = 'Data [A]')
   plt.scatter(t_data, B_p, color = 'k', label = 'Data [B]')
313
   plt.scatter(t_data, C_p, color = 'm', label = 'Data [C]')
315
   my_fig.set_xlabel('Time (s)', fontsize = '13')
   my_fig.set_ylabel('Concentration (M/# of Dice)', fontsize = '13')
317
  plt.legend(loc='best', fontsize = '13')
   plt.savefig('PCHEML2PARALLELFITS', dpi=300)
320
321
322 #Reversible
```

```
t_{values} = np.linspace(0, 8)
   t_{data} = np.linspace(0, 9, 10)
325
  popt, pcov = curve_fit (AR_FIT, t_data, AR(t_data))
327
328
  fig = plt. figure (6, figsize = (15, 10))
329
  my_fig = fig.add_subplot(111)
  my_fig.set_title('Parallel Reactions Fit Functions', fontsize = '15')
  #Computational Values
   plt.plot(t_data, AR_FIT(t_data, *popt), color = 'c', label = 'Fit for [A]',
333
            linestyle = '--'
   print (popt)
335
  popt, pcov = curve_fit(BR_FIT, t_data, BR(t_data))
337
  plt.plot(t_data, BR_FIT(t_data, *popt), color = 'k', label = 'Fit for [B]',
            linestyle = '--'
339
   print (popt)
340
341
342 #Actual Data
   plt.scatter(t_data, A_r, color = 'c', label = 'Data [A]')
   plt.scatter(t_data, B_r, color = 'k', label = 'Data [B]')
344
345
  my_fig.set_xlabel('Time (s)', fontsize = '13')
   my_fig.set_ylabel('Concentration (M/# of Dice)', fontsize = '13')
348
   plt.legend(loc='best', fontsize = '13')
   plt.savefig('PCHEML2REVERSIBLEFITS', dpi=300)
351
  # Consecutive 1 #
352
   t_{values} = np. linspace (0, 24)
   t_{data} = np. linspace(0, 24, 25)
355
356
  popt, pcov = curve_fit (AC_FIT, t_data, AC1(t_data), maxfev=4000)
357
358
  fig = plt. figure (7, figsize = (15, 10))
359
  my_fig = fig.add_subplot(111)
  my_fig.set_title('Parallel Reactions Fit Functions', fontsize = '15')
  #Computational Values
   plt.plot(t_data, AC_FIT(t_data, *popt), color = 'c', label = 'Fit for [A]',
363
            linestyle = '--'
364
  print (popt)
365
  popt, pcov = curve_fit(BC_FIT, t_data, BC1(t_data), maxfev=4000)
367
  plt.plot(t_data, BC_FIT(t_data, *popt), color = 'k', label = 'Fit for [B]',
            linestyle = '--'
369
   print (popt)
371
  popt, pcov = curve_fit (CC_FIT, t_data, CC1(t_data), maxfev=2000)
372
373
   plt.plot(t_data, CC_FIT(t_data, *popt), color = 'm', label = 'Fit for [C]',
374
            linestyle = '--'
375
376 print (popt)
```

```
379 #Actual Data
  plt.scatter(t_data, A_c1, color = 'c', label = 'Data [A]')
  plt.scatter(t_data, B_c1, color = 'k', label = 'Data [B]')
   plt.scatter(t_data, C_c1, color = 'm', label = 'Data [C]')
383
   my_fig.set_xlabel('Time (s)', fontsize = '13')
   my_fig.set_ylabel('Concentration (M/# of Dice)', fontsize = '13')
   plt.legend(loc='best', fontsize = '13')
387
   plt.savefig('PCHEML2CONSECUTIVE1FITS', dpi=300)
389
  #——Consecutive 2——#
391
   t_{values} = np.linspace(0, 57)
   t_{data} = np.linspace(0, 57, 58)
393
394
  popt, pcov = curve_fit(AC_FIT2, t_data, AC2(t_data), maxfev=4000)
395
396
  fig = plt. figure (8, figsize = (15, 10))
397
   my_fig = fig.add_subplot(111)
398
  my_fig.set_title('Parallel Reactions Fit Functions', fontsize = '15')
  #Computational Values
   plt.plot(t_data, AC_FIT2(t_data, *popt), color = 'c', label = 'Fit for [A]',
            linestyle = '--'
402
   print (popt)
  popt, pcov = curve_fit (BC_FIT2, t_data, BC2(t_data), maxfev=4000)
404
   plt.plot(t_data, BC_FIT2(t_data, *popt), color = 'k', label = 'Fit for [B]',
406
            linestyle = '--'
   print (popt)
408
409
  popt, pcov = curve_fit (CC_FIT2, t_data, CC2(t_data), maxfev=2000)
410
411
   plt.plot(t_data, CC_FIT2(t_data, *popt), color = 'm', label = 'Fit for [C]',
412
            linestyle = '--'
413
   print(popt)
414
415
416
417 #Actual Data
plt.scatter(t_data, A_c2, color = 'c', label = 'Data [A]')
  plt.scatter(t_data, B_c2, color = 'k', label = 'Data [B]')
   plt.scatter(t_data, C_c2, color = 'm', label = 'Data [C]')
421
  my_fig.set_xlabel('Time (s)', fontsize = '13')
  my_fig.set_ylabel('Concentration (M/# of Dice)', fontsize = '13')
423
  plt.legend(loc='best', fontsize = '13')
plt.savefig('PCHEML2CONSECUTIVE2FITS', dpi=300)
```