Uebung 11

Multivariate Statistik SoSe 2019 Antje Jahn (FBMN, h_da) Neudert, Baudisch, Kopfmann

Aufgabe 1 a)

```
clust <- read.csv("Ex11.csv")</pre>
library('VIM')
clust <- format(clust, scientific = FALSE)</pre>
clust[c(1:40)] <- lapply(clust[c(1:40)], as.numeric)</pre>
Skalieren der Daten
scaled_data = t(as.matrix(scale(clust)))
#Let us apply kmeans for k=3 clusters
kmm = kmeans(scaled_data,5,nstart = 60,iter.max = 15) #we keep number of iter.max=15 to ensure the algo
#> K-means clustering with 5 clusters of sizes 4, 20, 5, 4, 7
#> Cluster means:
                        2
                                 3
#> 1 -0.78319049 -0.490905861 -1.0648990 0.51260323 -0.54926363 0.05930680
#> 2 -0.37161784 -0.130358987 -0.1191583 -0.27118251 0.09177602 -0.28814260
#> 4  0.89936710 -0.886482523 -0.4615916 -0.83505160  0.50537771 -0.26890651
#>
            7
                      8
                               9
                                        10
                                                  11
                                                           12
#> 1 -0.39487671 -0.1335777 -0.2372000 0.2735966 0.6870592 0.2779988
#> 2 -0.12113998 -0.3758642 -0.3708198 1.6266369 1.7205980 1.6640746
#> 4 -0.06507313 -0.3327903 0.8609246 -0.3699414 0.3863596 0.6372845
#> 5  0.38967844 -0.7004420  0.5342694 -0.2155363 -0.2602016 -0.1120106
#>
           13
                    14
                             15
                                       16
                                                 17
#> 1 -0.4819270 -0.2432016 -0.5271636 0.3573333 0.22185577 0.98873225
#> 2 1.5375534 1.3451297 1.3942105 1.2634387 1.43957792 1.36123116
#> 3  0.9113076  -0.1156746  -0.3424716  0.9084775  0.73365870  -0.21850362
#> 4 0.8098699 -0.3860585 0.0205460 0.1730230 -0.06545958 0.34741768
#> 5 -0.1185366 -0.3738859 0.2937372 -1.1420786 -0.37968330 -0.02035012
#>
           19
                    20
                              21
                                        22
                                                  23
#> 2 1.4899759 -0.1229951 -0.2710697 -0.09074504 -0.09921251 -0.21186056
#> 3  0.4475429 -0.2588835 -0.1567175  0.03364029  0.68532996  0.07316028
#> 4 -0.5243921    0.6494378 -0.1156610    0.16968059    0.60072607 -0.81896302
#> 5  0.5141695 -0.4658189  0.2163942 -0.53545219  0.45162831 -0.39463007
            25
                      26
                               27
                                         28
#> 1 -0.52013622 -0.44397290 -0.4517606 -0.36028324 -0.57687231 0.5015907
```

#> 2 -0.06460533 -0.13208107 -0.3669125 0.02543079 -0.21630879 -0.3471511

```
#> 4  0.27940209  0.01358927  0.1174558  0.35364984  0.54884580  0.3468985
#> 5 -0.17254591 0.40080397 0.4707122 0.06491765 -0.09214554 0.2607259
        31 32 33 34 35
#> 1 0.25472249 -0.7221197 0.004067165 0.87426310 0.3446951 0.3958152
#> 2 -0.26477050 -0.3687968 -0.105633410 0.07017628 -0.3253538 -0.2707660
#> 3  0.04559362  1.0624812  1.139961063  -0.43105209  0.1067249  -0.5576055
#> 4  0.01646702  0.3669387 -0.551271931  0.35127099  0.5371995 -1.2224206
#> 5 0.49711679 -0.3005947 0.175787416 -0.81855961 0.5509812 0.8543058
         37
                 38
                        39
                                  40
                                            41
#> 1 0.2704832 0.07022468 -0.06312819 -0.83725421 0.0247484214 -0.7335332
#> 2 -0.4575193  0.10645029 -0.14171386 -0.21895146 -0.5596232477 -0.2133864
#> 3  0.4245240 -0.38187188  0.56026033 -0.07384852  0.1709814400  0.1093972
#> 4  0.0169071  0.63986631  0.88099370 -0.22389973 -0.1950955800 -0.4292593
#> 5 0.2140117 0.08689231 -0.30190670 0.46809414 -0.0005607525 -0.4985573
               44 45 46 47
         43
#> 1 0.60943720 0.87873084 -0.3116950 0.278828806 -0.09055204 0.79385306
#> 3 -0.08829451 -0.16063630 -0.1821624 -0.132270893 -0.01619105 -0.43353607
#> 4  0.61073608  -0.06383615  0.5150996  -0.604720107  -0.65857955  -0.60662434
#> 5 -0.31058999 -0.30264605 -0.1089855 -0.002363227 0.26386913 0.03379864
          49
                 50
                        51
                                  52
                                           53
#> 1 0.67799384 -0.2726834 0.4434038 0.281835704 -0.58060013 0.76978840
#> 2 0.16897893 -0.1973227 -0.1096104 -0.390645446 0.06101166 0.10154772
#> 3 -0.22809365 -0.3805828 -1.0178979 -0.200541916 -0.74920512 0.54258470
#> 5  0.08616386 -0.3052436 -0.2715040  0.008048417 -0.18964785 -0.07267809
#>
         55
                 56 57 58
                                          59
#> 1 0.7143900 -0.06877729 0.03029892 0.5050880 1.33557834 -0.73307169
#> 2 -0.2237806 -0.19949061 -0.28284603 -0.3253625 -0.02415848 -0.07723587
#> 3  0.1691613 -0.38815574 -0.61552503  0.1245877 -0.59907441 -0.82420937
#> 4 0.7742004 -0.11880494 -0.16762984 -0.2887009 -0.08102975 -0.22021091
#> 5  0.1857365  0.56783154  1.02010508  -0.5684191  0.10255646  -0.29005727
                62 63
                                64 65
        61
#> 1 -0.7439120 -0.52931438 -1.0429400 0.5393907 0.007869601 -0.2978932
#> 4 -0.4506184 -0.44153805 0.2769826 0.5161701 0.558551012 -0.4066479
67
                 68
                          69
                                   70
                                           71
#> 2 0.06912834 -0.05795774 -0.20241258 -0.17327019 -0.39225824 -0.27524147
#> 3 -0.66518627 -0.76179051 -0.83642418 -0.36087681 0.40541631 -0.61064502
#> 5 0.64287100 0.16087391 -0.18516472 0.34123087 -0.32798440 0.08448288
                          75
                                  76
          73
                 74
                                           77
#> 1 0.36263196 -0.02847437 -0.29489093 0.90374261 0.18491478 -0.8488177
#> 2 -0.43799840 -0.18168741 -0.37088891 -0.48893654 -0.76899089 -0.1778989
#> 4 0.77825893 1.04405293 0.06517628 0.57236468 -0.44827230 0.3683654
82 83
            80
                         81
```

```
#> 2 -0.3008811 -0.13918443  0.08066834 -0.2406257 -0.27338927 -0.07868906
#> 3 -0.7853967  0.15534807 -0.03604641  0.4211628  1.18372354 -0.83169212
#> 5 -0.1382745 -0.17985533 0.39347616 0.4478669 -0.09494545 0.40052385
                             87
           85
              86
#> 1 -0.16395288 -0.85655827 -1.099193232 0.28350738 0.38691686 -0.1134014
#> 2 -0.28508312 -0.02402128 -0.385837141 -0.03740294 -0.08604632 -0.4574942
#> 4  0.11594148  -0.45794949  0.290534409  0.81395907  -0.36037796  0.6964196
91
                   92
                       93
                                94
                                         95
#> 1 -0.44601228 -0.3565933 -0.2100048 0.15435173 -0.1903605 0.2258969
#> 2 -0.11113014 -0.2107736 -0.2856978 0.22069225 -0.3817440 -0.5200555
#> 3 -0.01632339 -0.1829915 -0.7954900 0.52777005 0.5607689 0.6251881
#> 4 -0.65795524  0.7831772 -0.5708544  0.56172795 -0.2821855 -0.2977616
#> 5  0.28202300 -0.4553339 -0.2474893 0.01959613  0.3073819 -0.6309792
          97
                   98
                       99
                                     100
                                               101
#> 1 0.06090514 0.1679564 0.33668665 0.1987313 -0.31713962 0.11908894
#> 2 -0.38868732 -0.1842695 -0.04823037 -0.2101826 -0.60903738 0.06862975
#> 3  0.24841885  0.1724229 -0.17583257  0.1275149  0.10328421 -0.40392214
#> 4 -0.06477453 -0.2851845 -0.44305405 -0.6438540 0.38261767 0.15830626
#> 5  0.78759061  0.3526806  -0.47058507  -0.2796540  0.01732605  0.10608407
#>
         103
                  104
                      105
                                      106
                                               107
#> 1 -0.3420998 0.57121002 0.56128863 0.32416558 0.46074442 0.1774898
#> 2 -0.4199700 0.03628597 -0.33782185 -0.09043603 -0.39731476 -0.3198139
#> 3 1.3448524 0.69942133 0.35148298 -0.45828920 -0.21850482 -0.6044132
#> 4 0.4590923 0.68110914 0.08844670 1.14608218 0.03920111 0.9598172
#> 5  0.1131651  0.04225576  0.06305415  -0.18512968  -0.14359554  0.1754803
                  110
                            111
                                      112
                                                113
#> 1 0.46605682 -0.0575877 0.07936352 -0.39001276 -0.44369862 0.5067358
#> 2 -0.18713798 -0.1828621 -0.41536508 -0.28570623 -0.15815029 -0.6940744
#> 3  0.09290962 -0.3503827 -0.21609216 -0.15212597 -0.17740626 -0.5049232
#> 4 0.07900613 0.2755472 0.02449221 -0.45533273 0.01489629 -1.1029775
#> 5 0.35435511 0.1548455 0.15313573 0.09361641 -0.04451963 -0.7793607
         115
                   116
                           117
                                118
                                          119
#> 1 -0.4311119  0.04180792  0.1682408 -0.02377467 -0.65666646  0.6590055
#> 2 -0.6548391 -0.28193948 -0.0248672 -0.16917252 -0.46087125 -0.1799984
#> 3  0.3539199  0.92622652  0.3167594  0.27955687  0.04582231 -0.7592796
#> 4  0.9265978  0.86698324 -1.3565611 -0.30484286 -0.57273684  0.2835622
#> 5  0.1103892 -0.68626534 -0.3635829  0.01494635 -0.56794132 -0.7830810
          121
                  122
                            123
                                  124 125
#> 2 -0.28478555 -0.12802134 -0.6209063 0.14749476 -0.2707339 -0.3693148
#> 3  0.33189204 -0.07728675  0.4949111 -0.45983800  0.3212993 -0.1555801
#> 5 -0.17365393  0.42011493  0.1678794  0.03719224  0.1166024  0.4035677
                             129
                   128
          127
                                       130
                                                131
#> 1 -1.07589491 -0.46488600 1.14166708 -0.24816891 0.92626262 -0.17280460
#> 2 -0.01486872 -0.04566675 -0.37258822 -0.59444011 0.01843100 -0.12154245
#> 5 -0.20045935 -0.35322913 0.22287757 -0.03528913 -0.10060242 0.25084324
                   134
                             135
                                      136
                                              137
          133
```

```
#> 1 1.64119959 0.6320004 0.10916596 -0.38459669 -0.79952701 -0.18998675
#> 4  0.05212207  0.8204540  0.98242612  0.31282913  -0.41041826  -0.48491513
#> 5 0.09238298 0.5598242 -0.08686416 0.01947662 0.02268627 -0.85705472
        139
               140
                      141
                              142
                                  143
#> 1 0.74610899 -0.09379896 -0.5642678 -0.47319445 -0.1859028 -0.6810929
#> 2 0.03507214 -0.59107106 0.1049791 -0.18441081 -0.1877522 -0.1874742
#> 3  0.61429970 -0.25260242 -0.6775036  0.84955351  0.6622943 -0.5576952
#> 4 0.42563242 0.27362557 0.3653238 -0.09656491 1.0341049 0.5994019
#> 5 -0.13592138 -0.38648221 -0.4361075 -0.87508398 0.2383186 -0.4179083
       145
               146
                      147
                              148
                                      149
#> 2 0.0273816 -0.20573727 -0.4051609 -0.52708075 -0.04983021 -0.1545578
#> 3 1.0043703 0.59038817 -0.6427747 -0.42992986 0.13715207 -0.4033692
#> 4 -0.6986928 -0.96579433 -0.7547006 -0.34956143 -0.68223123 0.6145225
#> 5  0.1925044 -0.22933210 -0.2175024  0.30322227  0.62191895  0.3030380
       151
           152
                     153
                             154
                                      155
#> 1 0.1634228 -0.1315224 -0.52381821 0.07497978 -1.45190328 0.4451738
#> 2 -0.1998927 -0.0248404 -0.33435454 -0.10711989 0.18935530 -0.3908296
#> 3  0.2088469  0.3367777 -0.14166261 -0.84113460 -0.76121773 -0.1619682
#> 4 -0.7780430 -1.5389609 -0.04884868 0.91687489 -0.76938465 -0.5787112
#> 5  0.6307117 -0.6832642  0.28338788 -0.41845877  0.07204854 -0.1129728
        157
               158
                       159
                               160
                                        161
#> 2 -0.149268758 -0.4070264 -0.04287047 -0.136501894 -0.19811885 -0.3636744
165
#>
         163
                164
                                166
                                        167
#> 1 -0.944913305  0.04471201 -0.01262969  0.50623115 -0.29404154
#> 5  0.626847387  0.78741362  0.38775943  0.60959543  -0.18749869
                        170
         168
                169
                               171
                                        172
#> 2 -0.332565488 -0.09039814 -0.33426566 -0.6903169 -0.476215285 -0.31287627
#> 4  0.035884965 -1.16392063  0.09822182 -0.1732114 -0.241641026 -0.41615442
#> 5  0.687567332  -0.01203657  0.58756100  0.4381306  -0.008153906  -0.09173515
               175
                      176
                              177
#> 1 0.28399307 -0.1241269 0.55564689 0.16528210 0.06335519 -0.42210989
#> 4 -0.21300637 -0.2414962 -0.24626536 0.23136465 0.66982775 0.02155075
180
               181
                     182
                               183
                                       184
#> 1  0.33945918 -0.05306831 -0.009699505 -0.05494839 -0.11863998 -0.6723188
#> 2 -0.34657703 -0.20360180 -0.055260829 0.04141384 -0.04641734 -0.3724033
#> 4  0.69454433  -0.12922965  -0.895039039  0.32433287  0.56067851  -0.1786226
#> 5  0.06411402  0.12255023  -0.214403781  0.14638787  0.44479542  -0.3944338
```

```
187 188 189 190 191
#> 186
#> 1 -0.1308761  0.1820566344 -1.43672269 -0.7931617 -0.009340915  0.50418100
#> 2 -0.1648925 -0.4662335164 -0.19450330 -0.2765365 -0.437107682 -0.02824591
#> 4 -0.2920132 -0.3917533732 0.46484282 -0.5721441 0.299278495 0.29250463
#> 5  0.1902300  -0.0702088630  -0.02747061  -0.5228911  -0.015303180  -0.23120340
#>
          192
                  193
                          194
                                    195
                                             196
#> 1 0.296240364 -0.1316477 -0.48136477 -0.186579852 -0.37784695
#> 3 0.164225772 1.2179206 0.47112904 0.474065677 -0.49551791
#> 4 -0.574731085 -0.2937810 -0.53659313 -0.388445854 0.15915305
#> 5 -0.004181992 -0.2507696 -0.60632940 0.293638957 0.01380123
                       199
                               200
#>
          197
                   198
#> 2 -0.2263358103 -0.05257738 -0.20729998 -0.05471169 -0.29813812
#> 3 -1.0837088929  0.05119780 -0.03766335  0.06962379 -0.31009826
#> 4 -0.2155062140 -0.07449045 -0.40002232 -0.27756480 -0.27322258
#> 5 -0.0002529404 -0.21557151 -0.49016444 -0.27383758 -0.04537234
         202
                  203
                          204
                                   205
                                            206
                                                    207
#> 1 0.28049117 0.06989101 1.11890002 -0.19947071 0.35767464 -0.79637225
#> 2 -0.47920679 -0.11496417 -0.15887606 -0.02950543 -0.29732272 -0.10165337
208
                209
                        210
                                 211
                                         212
#> 1 -0.2264914 -0.4595265 0.03204052 0.23877756 -0.77338759 -0.6087988
#> 2 -0.1573904 -0.3568093 -0.28051747 -0.08381073 -0.10372380 0.1112912
#> 3  0.2592052  0.2572658  -0.15248932  -0.04943063  -0.03265631  0.1476702
#> 4  0.7450872  -0.2799220  -0.13722361  -1.23632639  0.37896421  -0.2394464
215
                          216
                                   217
         214
#> 2 -0.09024021 -0.04638255 -0.25158235 -0.07630523 -0.2811819 -0.4373923
#> 4  0.77022228 -0.74398811 -0.07078981 -0.53404364 -0.8919359  0.6238815
#> 5  0.29892625  0.48862026  0.73856982  0.27964841  0.9062737  0.3840088
        220
                         222
                                 223
                221
                                         224
#> 2 -0.1759834 -0.3960632 -0.07066302 -0.6015252 -0.2032386 -0.2298713
#> 3 -0.3999141 -0.3913652 -0.11742526 -0.8717464 0.2649626 0.5435255
#> 5  0.1292045  0.1800003 -0.15950083  0.6502578 -0.3795136  0.3745273
#>
        226
                227
                         228
                                 229
                                          230
#> 1 0.3542746 -0.8212967 0.26843993 1.14341767 -0.13249192 0.44256694
#> 3 -0.0678005 -0.1850524 -0.62208340 0.29606390 -0.07805446 -0.48465490
#> 4  0.2648356  0.5033328  0.13233778  -0.84231642  1.16681543  -0.91107873
#> 5 -0.2324581  0.3152065  0.19061435 -0.77065317  0.66697194  0.39077531
#>
        232
                 233
                          234
                                 235
                                          236
                                                   237
#> 1 0.1858946 0.36959315 0.61467929 -0.24822058 -0.16427799 -0.7446304
#> 2 -0.3929308 -0.32400254 -0.12082307 -0.26343321 -0.11857208 -0.4379556
#> 3 0.3468832 0.05046548 0.39869891 0.96559455 0.03328685 0.5187517
#> 4 -0.5513142  0.04038679  0.56031153  0.06584341 -0.14973117 -0.7744570
```

```
#> 5 -0.3679888 -0.82314938 0.04865439 -0.35516239 -0.42146017 -0.4661391
            239 240 241 242 243
    238
#> 1 1.0378009 0.4161627 -0.53807222 -0.7436213 -0.4805238 0.02799714
#> 2 -0.1459399 -0.2161600 -0.20130498 -0.3089057 0.1601684 0.03920476
#> 3 -0.3118578 -0.4112022 -0.06929313 -0.2431546 -0.2437638 -0.61196425
#> 4  0.9410025 -0.5726428  0.15424684 -0.4781627 -0.5377578  0.44867130
#> 5  0.1210851 -0.1023701 -0.21490378  0.2777816 -0.4459685  0.44493831
                   245
                           246
                                    247
#> 1 0.27710936 0.07369758 -0.7705080 0.08363008 -0.222435057 0.17973221
#> 2 -0.44501823 -0.16336883 -0.2708567 0.10481967 -0.142031867 0.03639378
#> 3  0.31406700  0.30339352  -0.3374556  -0.46699953  -0.004375853  0.60983631
#> 5 0.01129367 0.46267055 -0.1806227 -0.02938150 0.405628381 0.27446116
         250
                   251
                            252
                                   253
                                            254
#> 1 0.24871080 -1.04194850 0.93602017 -0.2894260 0.1794442 0.04932595
#> 2 -0.54103175 -0.32408773 -0.04088518 -0.1988928 -0.1105994 -0.24760256
#> 3  0.18260785  0.07539887  0.07905145  0.8366328  -0.2736586  -0.91518007
#> 4 -0.03359202 -0.64842887 -0.13169675 0.3386403 -0.4237869 0.56336441
#> 5 -0.08257602 -0.14125264 -0.66089106 0.1155751 0.6222840 0.45797379
        #> 1 0.03477383 -0.87984830 0.40434173 1.5239140 -0.002196145 -0.36086655
#> 3  0.48251214 -0.03303544  0.01947692 -0.9591814 -0.416524299  0.30052738
#> 4  0.23565256  -0.30957957  1.06966037  -0.6025135  -0.053340209  -0.72057457
#> 5 -0.36156726 -0.21237582 0.16512121 -0.5308487 0.691027097 -0.03049815
        262
                          264
                 263
                                   265
                                         266
#> 1 0.2339480 1.1881637 -0.41690605 0.14355225 -0.38514991 -0.5458770
#> 2 -0.4279321 -0.0402355 0.04769223 0.06554644 -0.09646024 -0.3496827
#> 4  0.2218653  0.7575626  -0.19911222  0.51931534  0.64207356  -0.5213245
#> 5  0.6573086  0.3566815  -0.40558404  -0.49190639  -0.56148601  0.3646223
                         270 271
         268
                   269
                                        272
#> 1 -0.16788794 -0.677954245 -0.3253811 0.11916978 0.2604933 -0.6204638
#> 2  0.06494382  0.002909401 -0.2027082 -0.25075130 -0.2314319  0.3381160
#> 4 -0.70375883 1.462917829 -1.6003485 0.02161089 0.2886306 0.4289054
274
                   275
                           276
                                     277
                                             278
#> 2 -0.33674018 -0.05484301 -0.15554869 0.04224552 0.0387671 0.04702720
#> 3  0.07165287 -0.25318661 -0.26178472 -0.18181792  0.4381262 -0.76035065
280
                  281
                           282
                                   283
                                            284
                                                      285
#> 1 -0.97496722 -0.7847612 -0.01579165 -0.2225745 -0.13406296 -0.10324950
#> 2 -0.41011517 -0.2832606 -0.06664182 0.1157681 -0.15034506 0.04149202
#> 3 0.93335589 0.2640518 0.78949722 0.1487492 0.01427416 0.04584291
#> 4 -0.09567964 -0.1996855 -0.52039707 -1.1104042 -0.67565488 0.10080301
#> 5 0.13565148 0.1219156 -0.75257171 0.2351882 0.42904601 -0.48572758
          286
                  287
                           288
                                289
#> 2 -0.247258927 -0.3642095 -0.265870988 -0.01491961 -0.24217600 -0.1473592
#> 3  0.008539938 -0.4328292  0.165660403 -0.12430016 -0.17395338  0.1874795
```

```
#> 4 -0.430255896 -0.3775761 -0.531150996 0.79663857 0.84098630 -0.5545888
#> 5  0.560631080  0.3246904  -0.599223492  -0.16718959  -0.01614746  -0.1404405
                     293
           292
                               294
                                          295
#> 1 0.33252897 -0.2525349 -0.33154454 0.15130182 0.46741308 0.1813776
#> 2 -0.58905953 -0.2297312 -0.25714851 -0.23782320 -0.31711644 -0.3028338
#> 3 0.67759437 0.2709382 0.01195682 -0.25277207 -0.24387621 0.1272075
#> 4  0.19966888  0.5866494  0.12768882  -0.07959866  0.19670781  -0.8366950
#> 5 -0.03070189 -0.4693222 -0.03497585 0.16669478 0.04431829 0.3103002
                         300
          298
                    299
                                        301
                                                  302
#> 1 -0.4701671 -0.39564346  0.23185385 -0.3110922  0.7439579 -0.53397962
#> 2 -0.1451964 -0.18407702 -0.03907029 -0.1778240 -0.2214404 -0.03069261
#> 3 0.4147837 0.85795055 0.49734716 1.0817143 0.6284931 -0.56512063
#> 4  0.9694702  0.50386914  -0.69390026  0.2696656  -0.6501822  0.25098592
#> 5 -0.5974186 -0.09536663 -0.12482276 0.2436195 0.4252598 -0.10586664
                                                                  309
           304
                      305
                                306
                                            307
                                                      308
#> 1 -0.05304700 -0.341541176 -0.63943446 -0.85220806 -0.32272989 0.14425971
#> 2 -0.39330553 -0.128477272 -0.23837485 -0.25225570 -0.12461752 -0.32541250
#> 3 0.87582842 0.747959947 -0.09789844 -0.34975599 -0.19425254 1.03416519
#> 4 -0.28535071 -0.004958041 1.03055437 0.97386127 -0.63833202 0.24933279
*> 5  0.07880777  0.179944880  0.08958325  -0.05664419  0.03798823  -0.07228931
#>
           310
                      311
                               312
                                          313
                                                    314
                                                              315
#> 2 -0.18944727 -0.16876405 -0.1653466 -0.04097014 -0.2481535 -0.2592501
#> 3 -0.26784255 -0.42454943 0.9792883 -0.02372959 0.2412043 -0.3553563
#> 5  0.74374905 -0.03656166  0.8117475 -0.47955603 -0.3194781 -0.4691381
         316
               317
                          318 319
#> 1  0.2223656 -0.34211941 -0.828927030 -0.140623355  0.575562860
#> 2 -0.3146802 -0.18400773 -0.137916482 0.047753526 0.006345852
#> 3  0.9004006  0.08630752  0.179946820  0.003227859  0.461031810
#> 4 0.3953488 -0.35727268 0.004913409 -0.250990301 0.451564525
#> 5 -0.2921420  0.29676398  0.792132156  0.537049977 -0.049833702
                       322
                                            324
            321
                                  323
#> 1 0.119711621 -0.709501690 0.04548457 0.4026670 -0.587450186
#> 2 0.001958132 0.003370876 -0.14369827 -0.1064390 -0.001195293
#> 3 -0.243563301  0.150717712 -0.39439455  0.3696635  0.001534561
#> 4 0.388025406 0.712971215 -0.36992640 -0.1643650 -1.049509746
326
                     327
                                328
                                           329
                                                      330
#> 1 0.09924276 -0.04531448 -0.26472306 0.25104815 -0.41389479 -0.1769660
#> 2 0.04353154 -0.01745769 -0.19870906 -0.27051534 0.05846314 -0.4936190
#> 3 -0.77302678 -0.06660898 -0.14582233 -0.04018509 -0.67820224 -1.0310421
#> 5  0.03956489  0.33032072  0.48178558  -0.36112209  -0.73250688  0.3778858
                     333
                                334
                                          335
          332
                                                     336
#> 1 -0.2920346 -0.88586877 0.41449245 -0.09969756 1.42235326 -0.04107408
#> 2 -0.1503602 -0.07860417 -0.06975969 -0.10062988 -0.40539145 -0.27236425
#> 3  0.9889065 -0.20864125  0.46759835 -0.47206400  0.33018811 -0.88639979
#> 4 -0.7412410 -0.05084770 -0.13206321 0.64350893 0.22149348 -0.05291229
#> 5 -0.4502054  0.03656155 -0.08379353  0.08488375  0.09403319  0.34923113
#>
           338
                    339
                           340
                                         341
                                                    342
                                                               343
#> 1 0.80773454 -0.5996987 0.25268863 0.1476692 -1.03644678 0.16091365
#> 2 -0.11237753 -0.2911199 -0.27427107 0.2414119 -0.01759022 0.09583896
```

```
#> 4 0.65440712 -0.7133311 1.30596992 0.4845319 0.54265747 0.11150413
#> 5 0.13224253 0.5792889 -0.07551028 0.1436556 0.45534317 0.17447723
         344
               345
                     346
                             347
                                     348
#> 1 -0.37176652 -0.4228240 -0.23409827 -0.1710362 0.46529874 0.09994455
#> 2 -0.09698348 -0.1572625 -0.06172079 -0.2623966 -0.09999711 -0.19624252
#> 3  0.85622337 -0.2552288 -0.68163560  0.1388101  0.70765168 -0.21759576
350
                 351
                         352
                                 353
                                          354
#> 1 0.1855504 -0.54945308 0.03860849 0.1298864 -0.2008702 -0.02056044
#> 2 -0.3284257 -0.05405561 -0.31294779 -0.4502637 -0.1579265 -0.29107030
#> 3 0.2085815 0.47041559 0.02132755 0.6019723 0.5316094 -0.07523944
#> 5 -0.9179963  0.10792505  0.33043762 -0.2721016 -0.2120456  0.25024670
         356
                 357 358
                                 359
                                        360
#> 1 0.99517526 -0.56057616 -0.06962256 0.3515926 0.16077494 -0.32466019
#> 2 -0.16708591 -0.13013313 -0.33794069 -0.3091052 -0.45904091 -0.20875168
#> 3 -0.09905788 -0.16890124 -0.09646622 -0.4654250 -0.46147520 -0.09541277
#> 4 0.71975639 -0.55651632 0.17987517 0.1125971 -1.00365607 0.48928733
362
                 363
                         364
                                  365
                                           366
#> 1 -0.05922967 -0.4646089 -0.1785681 0.46027876 -0.65281112 0.36082525
#> 2 -0.07006777 -0.1393705 -0.1542747 -0.25620489 0.01542249 -0.38631902
#> 3  0.54083391  0.5594272 -0.3330348 -0.01739434  0.53144556  0.51108613
#> 4  0.32441793  1.3130142 -0.0940888 -0.60988379  0.31034869  0.07031398
#> 5 -0.49038101 -0.5842797 0.2991317 0.17397919 0.40380038 -0.14546477
#>
                          370
                                  371
                                           372
         368
                  369
                                                    373
#> 1 0.18317938 -0.13160696 0.69274209 0.1806447 0.5773552 -0.75429855
#> 2 -0.36712460 -0.24027709 -0.49149346 -0.2708552 -0.6737554 -0.33842763
#> 4  0.38629462 -0.09080183 -0.51035873  0.5410262  0.1502805  0.07979357
#> 5 -0.03728689 -0.10251314 -0.45012348 -0.1784819 -0.3514918 0.11029479
        374
             375 376 377
                                      378
#> 2 -0.5355013 -0.31583914 -0.5327149 -0.221536710 -0.3636887 -0.1813889
#> 4  0.7405085    1.08340643    -0.9715184    -0.224578184    -0.1178642    0.3378584
#> 5  0.3318547 -0.01264365 -0.5582406 -0.008133706  0.1677135  0.4032372
         380
                 381
                         382
                                 383
                                          384
#> 1 0.42771746 -0.5072783 0.6025567 0.59242461 -0.8203269 0.3141775
#> 2 -0.25646959 -0.3060971 -0.4081535 -0.37485496 -0.2736635 -0.1785327
#> 3 -0.52265621 -0.8057297 -0.8151382 -0.38244210 0.3307753 -0.7194329
#> 4 -0.08106084 -0.1823275 -0.3878171 0.46517849 0.1076852 -0.1290640
386
                 387
                         388
                                 389
                                          390
#> 2 -0.5832506 -0.33211130 -0.2824488 -0.2438087 -0.36787504 -0.3123191
#> 3 0.3501657 -0.75921776 0.4640110 -0.3585379 -0.06654572 0.4165018
#> 4 0.4352784 1.31733958 0.1803132 0.1350609 1.44203681 0.1940563
393 394 395 396
#> 1 0.9753885 0.211874225 1.20023173 -0.2424197 0.26477857 0.54819208
```

```
#> 3  0.6662049  0.546848689 -0.09583335  0.2746839  0.11573568  0.04180138
#> 4 0.4152580 0.307405500 -0.16403233 -0.5701874 0.28619579 0.02508277
#> 5  0.2434140  0.004148762  -0.70276684  -0.2411100  0.48518124  -0.35853858
                                     401
         398
                   399
                       400
                                              402
#> 1 0.1158466 0.428822792 -0.5596434 0.45262523 0.37316434 0.67681765
#> 4 0.1966767 0.008641107 -1.4355137 1.25571204 -0.81793726 0.02975207
405
          404
                        406
                                 407 408
#> 1 -0.20151842 -0.04247271 -0.6268045 0.58015434 0.48245525 -0.3657118
#> 2 -0.28613375 -0.15010200 -0.1686094 0.01137207 -0.18227131 -0.4122705
#> 3  0.12531745 -0.01729958  0.1823735  0.30715326 -0.19935850  0.2199596
#> 4 0.39913923 0.56652129 -0.6807854 -0.12641051 -0.36917155 0.4147116
#> 5  0.06276683  -0.15912653  0.6988902  0.45839435  0.02322228  0.6587007
          410
                              412
                                       413
                    411
                                                 414
#> 1 0.10636764 0.058301912 0.68555670 0.25945030 1.27439211 -1.02362228
#> 2 -0.08372707 -0.002538823 -0.03598376 -0.34680987 -0.44714677 -0.37552233
#> 3  0.28727605  -0.336954505  -0.03204302  -0.28544004  -0.26001039  0.05558587
#> 5 -0.33203267 -0.081155314 -0.53259576 -0.19635993 -0.88359528 -0.76569823
                                                420
          416
                  417
                            418
                                     419
#> 1 0.37962244 0.5386123 0.17522030 -0.52949880 0.07827378 0.24159622
#> 2 -0.26240783 -0.1413251 -0.09062592 -0.17284778 -0.07375267 -0.33212074
#> 3  0.01887641  0.6974577  0.39184947  0.02668802  -0.37098528  0.08640535
#> 4  0.49062355 -0.6012888  0.36118465 -0.56302389 -0.05714889 -0.57852355
#> 5  0.23613427  0.2215923  -0.37465818  -0.06244950  0.21983158  -0.07841564
           422
                              424
                     423
                                       425
                                                 426
#> 1 -0.005229472 -0.299820048 -0.28578761 -0.70873747 0.7297806 -0.2823974
#> 2 -0.267680985 -0.021916430 -0.09298312 -0.44861305 -0.2467827 -0.1111693
#> 3 -0.571267242 -0.618948819 -0.23981438 -0.01944948 0.8300803 0.9083199
#> 4  0.339245721 -0.003307715  0.23092327 -1.19076642  0.7771500  0.6176845
#> 5  0.400784990 -0.496072711 -0.22958629  0.50882800  0.0975385 -0.1026508
          428
                   429
                       430
                                 431
                                             432
#> 1 0.15537317 -0.13018269 -0.14579196 -0.1052613 0.1909620 0.8565839189
#> 2 0.08872618 -0.38322810 -0.10487494 -0.2593596 -0.4259408 -0.0002521077
#> 4 -0.29428196  0.12400194 -0.51022166  0.5566151 -0.2495756  0.3938010806
#> 5 0.17236478 0.07163089 -0.31952992 -0.2635459 -0.1002015 -0.0269607080
                   435
                             436
                                               438
                                  437
          434
#> 1 0.52445277 -0.17676614 0.51675535 -0.7231504 -0.53369534 -0.0571556
#> 3  0.72798237  0.13853584 -1.10335551  0.3929360 -0.05996675  0.1839056
#> 4 -0.54534597 -0.01484509 -0.09921647 -0.3790672 0.11831357 -0.1159084
#> 5 -0.56509154 -0.13578323 -0.04458835 0.1110423 -0.21844676 -0.2638713
                                      443
          440
                    441
                             442
                                                444
#> 1 -0.93596861 -0.30199466 -0.50382351 0.1495253 0.05660391 -0.422254154
#> 2 0.10009186 0.10490384 -0.02943465 -0.3664160 -0.04114866 -0.001734693
#> 4  0.34223744  0.40526484  -0.35166654  0.1945876  -0.57454557  0.379287713
#> 5 -0.03417180  0.01054663  0.52817125  0.4169894 -0.09146260  0.368957209
                   447
                            448
                                      449
                                              450
```

```
#> 1 -0.26468162 -0.2165981 -0.40413175 -0.11926934 0.5173956 -0.1529362
#> 3 -0.03122875 -0.1907304 -0.36082873 0.08663955 0.4767729 -0.4188516
#> 4  0.64056899  0.2196603  0.08204993  -1.15780231  -0.8501747  -0.3396465
#> 5 -0.60384303 -0.9210548 0.10222505 0.56023090 0.1677438 0.3070068
         452
                 453
                          454
                                  455
                                           456
#> 1 0.4177025 0.21341059 -0.11039574 -0.4617551 -0.6022680 0.20616634
#> 2 -0.3151017 -0.01194468 -0.59435062 -0.3623187 0.1153119 -0.04620186
#> 3 1.7221393 -0.13846549 -0.20383845 0.2098309 0.3276072 -0.18915101
#> 4 -0.9293458  0.14671245  0.08551173  0.4902468 -0.1997303  0.74289406
#> 5  0.5658953 -0.38513227  0.08391665 -0.2250990 -0.7188385 -0.18959252
                 459
                          460
                                   461
                                            462
#> 1 0.7859190 0.15082357 0.01462283 0.1785230 1.40877475 0.07717735
#> 3 -0.1136719 -0.54827652 -0.14919429 0.2351770 0.03798641 0.18567141
#> 4  0.2438137  0.07313056  0.30328623  -0.4203141  -0.20831467  0.79250083
#> 5 1.2839891 -0.02198250 0.27783397 0.1508458 0.03703431 -0.63159147
               465
                      466
        464
                               467
                                       468
#> 4  0.4232838  1.4609113  0.16601997  0.06694808  1.0167968  -0.08207232
#> 5  0.1080584 -0.1881601 -0.55394826 -0.77359324  0.6462494  0.10849269
         470
                 471
                         472
                                  473
                                           474
#> 1 0.01732972 0.3802164 -0.1952438 0.7622597 0.37242666 0.10047930
#> 2 -0.13648942 -0.2245483 -0.1083608 -0.3168872 -0.10136342 -0.05327698
#> 4 -0.83521901 -0.7388429 -0.3123499 0.6140113 -0.03344613 -0.44025496
#> 5 -0.09304531 -0.1105153 0.2258077 -0.5536466 0.31297481 -0.07401753
          476
                                           480
#>
                   477
                           478
                                   479
#> 2 -0.195056381 -0.23994858 -0.1893485 -0.3722569 -0.3026113 0.2169076
#> 3  0.116796359 -0.35093062 -0.6046975  0.4693833  0.1617052  0.1002573
#> 4 0.007937774 0.06577704 0.4499839 -0.3831534 0.7362858 -0.6682704
485
         482
                 483
                          484
                                            486
#> 1 -0.1867254  0.7950097  0.497964799 -0.42134970  0.43190217 -0.19284489
#> 2 -0.1454142 -0.0906823 -0.279315574 -0.05678101 -0.15822770 0.03711207
#> 4 -0.5956793 -0.6038399 -0.691949499 -0.40101960 -0.16124575 -0.16881817
#> 5 0.3250473 0.3905028 -0.062877562 -0.30752794 0.23449597 0.72721726
                                  491
         488
                 489
                      490
#> 2 -0.12372008 -0.2484519 -0.08492515 -0.38761921 0.12294725 -0.7367763
#> 4  0.25545463 -0.2441930  0.21335266  0.05198864  0.50653619 -0.5474732
#> 5 -0.45308409 -0.6579099 -0.29027556 0.01062389 -0.42254698 0.1685931
                                  497
        494
                 495
                         496
                                          498
#> 1 0.2786129 0.49606524 -0.9147054 1.3165209 0.51789914 0.0611995566
#> 2 -0.1277114  0.05164898 -0.4289807 -0.1578162  0.07362897 -0.0003274374
#> 3 -0.4443128  0.39953227  0.3747079  0.7766565  0.05139764 -0.2238802672
#> 4 1.0162637 0.77860710 0.4758349 -0.4117801 0.52753678 0.1797240827
#> 5  0.1640952 -0.22190427 -0.1668797 -0.3230103 -0.03216461 -0.1172581580
```

```
#> 500 501 502 503 504 505
#> 1 0.07111883 -0.2863167 0.42106490 0.8632818 1.1182051 0.91472906
#> 2 1.40456267 1.7518977 1.69711663 1.2419118 1.6470960 1.54380721
#> 3  0.50805822 -0.3292576 -0.37979619 -0.2949293  0.2089479 -0.28039223
#> 4  0.53767158  0.2856222  0.23775230 -1.1155342 -0.3011684  0.43573242
#> 5 -0.13107196 -0.4123177 -0.01281975 -0.1756702 -0.4899308 0.01079503
         506
                 507
                          508
                                  509
                                           510
                                                   511
#> 1 -0.46086625 -0.2787639 0.19107343 0.4064875 -0.26476026 0.1121307
#> 2 1.28571572 1.8528533 1.80178763 1.2003172 1.81109212 1.4792762
#> 3 0.10232216 0.4927130 0.94771068 -0.3878430 -0.16861671 0.3641264
#> 4 -0.33184551 1.1532511 -0.05544254 0.3316130 0.95857358 0.1666057
513
#>
         512
                         514
                                  515
                                           516
#> 2 1.4622884 1.52935766 1.524880161 1.55596188 1.55896838 0.9514437
#> 3 -1.0169763 -0.16518368 0.288489227 -0.11286867 0.24290761 0.6594552
#> 5 0.2196741 -0.28413499 0.266655401 -0.84545888 0.29143948 0.1831472
        518
                519
                        520
                               521
                                       522
#> 1 0.2096767 -0.3137832 0.09324847 -0.5095456 0.1330409 -0.1350190
#> 2 1.2921855 1.5536766 1.61736671 1.5975176 1.5324968 1.4368595
#> 4 0.2848031 -0.1413627 0.13583283 -0.1348727 -0.7608462 -0.4278928
526 527 528
         524
              525
#> 1 0.09448719 0.05082684 0.4668918 -0.4742186 -0.1686239 -0.48356212
#> 2 1.14485742 1.60852329 1.4969632 1.1416396 1.5170490 1.47116568
#> 3  0.50829943  0.65447439  -0.7731548  -0.6449729  -0.1390035  0.77932595
#> 4 -0.56988509 -0.12121544 -0.4704581 0.1210400 -0.6036427 -0.04481908
#> 5 0.06135171 0.07820141 0.7246046 -0.4684908 -0.4095513 -0.03893401
                531
                        532
                                  533
#> 1 0.1659317 -0.1234020 -0.3492770 -0.09297852 -1.3191741 -0.1951218
#> 2 1.3995933 1.1143836 1.4742794 1.74672549 1.5174088 1.4683968
#> 3  0.2982503  -0.5356788  -0.1335862  0.14798222  0.3125371  -0.5675948
#> 5 0.1317764 -0.1230892 -0.1074967 0.77376517 -0.2633075 -0.0401968
                         538
                                 539
        536
                537
                                         540
                                                 541
#> 1 0.6817900 -0.02217292 -0.7939106 -0.3562951 0.4235008 0.6979044
#> 2 1.5041989 1.65671952 1.4586037 1.7832946 1.5866890 1.4969298
#> 3 0.3548434 -0.45659717 0.3943691 0.6389420 -0.2188437 -0.2965263
#> 4 0.2374804 0.07853836 0.3053681 0.6594037 -0.1056998 -0.4857282
#> 5 0.7382150 -0.21199029 0.3262759 -1.1621049 0.2133632 0.2912287
                        544
        542
                543
                            545
                                          546
#> 2 1.4424795 1.4690633 1.6410311 1.5515175 1.30506255 1.81634975
#> 4  0.5386767  0.2186951  -0.3137020  -0.6474111  -0.08936502  0.32328328
#> 5  0.3689191 -0.1123954  0.2154258 -0.4797276 -0.09722892 -0.23198147
         548
                  549
                        550
                                   551
                                         552
                                                    553
#> 2 1.68647279 1.625985598 1.94061734 1.22568109 1.31728614 1.6505580
#> 3  0.04577635  -0.058646923  0.18526140  0.35991320  0.04618584  -0.2154819
```

```
554 555 556 557 558 559
#> 1 0.8303239 0.20331216 0.3196292 0.84938983 0.63833256 -0.0009207093
#> 2 1.5802521 1.50256650 1.2358365 1.73024094 1.57494048 1.5913168344
#> 3  0.1670767  0.54490475  -0.3703036  0.79749240  -0.33918335  0.7450449095
#> 4  0.2759966  0.04847735  0.1973862  -0.05995545  0.52546930  0.2861137641
#> 5 -0.5805537 -0.04499848 0.2153615 0.07843756 0.09476516 -0.0628314403
                 561
         560
                          562
                                   563
#> 1 0.18022183 -0.04452153 0.4964256 -0.09497711 0.03097238 -0.0183718
#> 2 1.75745771 1.52481737 1.4058075 1.51072908 1.78406743 1.7867569
#> 3  0.39947040 -1.24573934  0.3979741 -0.58729087 -0.16144320  0.8107932
#> 4 -0.07170321 -0.46674601 -0.5388460 -1.06654042 0.36803196 -0.5478114
#> 5 -0.55392716 -0.03431250 -0.2889257 0.72450272 -0.44612721 0.4144785
         566
                 567
                         568
                                   569
                                           570
                                                   571
#> 1 -0.3600169  0.8083770 -0.2799513 -0.26258186  0.5448299 0.0507760
#> 2 1.4454094 1.7113705 1.4419683 1.58246904 1.5467432 1.6619796
#> 5  0.3030332  -0.9838342  -0.1101984  0.08128005  -0.7858459  0.1692143
                 573 574 575 576
#> 1 -0.1663153 -0.484090275 -0.10646694 0.59321849 0.06093792 0.1044598
#> 2 1.2223396 1.345872234 1.49711124 1.54213003 1.20447941 1.7034082
#> 3 -0.8497688 -0.200504565 -0.03718371 -0.74293407 -0.07597246 0.8100905
#> 4  0.6429577  0.002940139  -0.65017387  0.67070053  -0.07170875  1.2406209
#> 5  0.5556865 -0.580619140  0.33939091  0.07813195 -0.33094523  0.6852672
                                          582
         578
                 579
                         580
                                 581
#> 1 -0.5070787 1.1913064 0.6586431 -1.0510220 0.2864017 -1.0808397
#> 2 1.4527622 1.3075129 1.3765522 1.7017904 1.4281791 1.7395391
#> 4  0.1961984 -0.1042774 -0.3848520  0.2275191 -0.2716495 -0.1444318
#> 5  0.4382467  0.3306781  0.5691289  0.1319321  0.2976336  0.0330684
                        586
         584
               585
                                  587
                                           588
#> 1 0.10513547 0.2705651 0.31053594 0.01821627 -0.148451395 0.1732367338
#> 2 1.37440276 1.7323401 1.63504939 1.40340087 1.899091288 1.5767420761
#> 3 0.62880323 0.2278982 -0.11823495 -0.17536502 0.610056335 -0.4243226305
#> 4 0.51113469 0.2802533 0.08149583 0.11307289 -0.008840132 -0.1368134487
#> 5 0.07317537 0.2282277 0.20629529 -0.24992189 0.067317355 0.0006092487
         590
                 591
                          592
                                  593
                                             594
#> 2 1.50443415 1.3857247 1.7467402 1.45882776 1.484530419 1.52339500
#> 4 -0.03480752 -0.3177120 -0.1642498 0.79607574 -0.189697599 0.06607883
#> 5  0.72956090 -0.8136234  0.4206747  0.28806675  0.003284867  0.35568665
                  597
                        598
          596
                                599
                                            600
#> 1 0.878773768 -0.8329163 -1.3524148 -0.7376680 -0.27420850 0.04900825
#> 2 1.577738678 1.2996369 1.4844597 1.5823443 -0.24354123 -0.19986019
#> 5 0.194942810 0.3920132 -0.2598890 -0.3122502 0.07419277 0.07650939
                 603 604
                                  605
#> 1 0.7914306 0.12635620 -0.0238759 0.76572675 0.3058640 0.18609242
#> 3  0.1434316 -0.35251423 -0.1713286  0.55865919  0.1158955  0.66297696
```

```
#> 4  0.1521167  0.33983632  0.5773382  -0.22081187  0.8131217  0.22523327
608
                 609
                         610
                                 611
                                          612
#> 1 0.65799923 -0.18778931 -0.07365719 -0.49848413 -0.2099471 -0.53922053
#> 2 -0.11779342 -0.27969178 -0.55803218 -0.10676764 -0.5715339 -0.07543696
#> 3  0.51943101  0.14881502 -0.03962198  0.27194061 -0.3615011  0.57050562
#> 5  0.20238330  -0.04263232  0.43463799  0.05237434  0.4755862  0.10636272
                                 617
        614
            615 616
                                     618
#> 1 0.5953518 0.1971690 -0.91917202 0.02976190 -0.1004828 -0.41463397
#> 2 0.3928630 -0.2455006 -0.05202011 -0.18741144 0.0429536 0.19820379
#> 3 -0.3958236 -0.1865562 0.39545845 -0.07337524 0.2890863 -0.11581924
#> 5 -0.4199137 -0.1794641 -0.46912280 0.63269743 0.2259444 -0.18524073
        620
                 621
                         622
                                  623
                                          624
#> 2 -0.1502433 -0.54992814 -0.3304632 -0.23346947 -0.2151197 -0.358948940
#> 3  0.5500808 -0.11091303  0.2015030  0.32486341 -0.6422944 -0.605025309
#> 4 -0.2881611 -0.01887711 -0.2971456 1.76652483 -0.5961369 -0.007263279
628
                                      630
#>
         626
                 627
                                  629
#> 1 0.25386036 -0.4494797 -0.58803042 -0.03009723 -0.32441588 0.1278640
#> 3  0.22148295  0.6780076  -0.45030891  0.62794699  -0.08296229  -0.6120962
#> 5 -0.50771512 -0.3190814  0.15887161 -0.01745410 -0.35732788  0.4689602
         632 633 634 635 636
#> 1 0.04749958 0.67512192 0.4743874 -0.13130291 0.50155283 -0.56929412
#> 3 -0.05933556 -0.13910332 -0.6688913 0.70180295 -0.35845477 0.35436980
#> 4 -0.11919773 -0.06501447 0.5634770 0.22238834 0.49120268 -0.51119761
#> 5  0.95562330 -0.88058418  0.4197082 -0.03071179  0.01498011 -0.03732817
        638
                639
                              641
                         640
                                        642
                                                 643
#> 1 -0.8723628 -0.2781045 0.11191824 -0.8162324 0.4787585 -0.8401758
#> 3 0.4182009 -0.1303482 0.02422882 -0.1659166 -0.7245298 -0.3095754
#> 4 -0.3330312 -0.2323731 0.51106649 0.5354731 -0.9194235 0.2733954
#> 5  0.2246644  0.1717084  -0.11616742  -0.1530405  0.5353685  0.2856662
         644
                645
                      646
                                 647
                                       648
#> 1 -0.75818793 -0.7550176 -0.5973837 -0.02594651 -0.67796449 0.3316787
#> 2 -0.22041450 -0.2824935 -0.3037970 -0.09845102 -0.09671321 -0.1008213
#> 3  0.04139395  0.3212715  0.6840516  -0.32742288  0.03766026  -0.3319749
#> 4 -0.04733667  0.2970168 -0.2635305  1.08991722  0.81930982 -0.3650937
#> 5  0.37653062 -0.1860294  0.1496849 -0.38318878 -0.68855414  0.6951554
                 651
                          652
                                           654
        650
                                   653
#> 2 0.1657179 -0.02686991 -0.006628834 -0.18802533 -0.1372751 -0.35572284
#> 3  0.1955770 -0.36174030  0.520350357 -0.52345710 -0.1588285  0.19156701
#> 4  0.1919937 -0.18861322 -0.105041759 -0.35380138 -0.4751043 -0.71131421
657
                     658
#>
         656
                              659
                                          660
#> 1 0.03306812 -0.4019955 0.92256054 0.5161954 -0.78472508 -0.30146050
#> 2 0.04991135 -0.5278061 -0.05520837 -0.4021425 -0.37506414 0.07549421
```

```
#> 4  0.02979424 -0.5401871 -0.20941615 -0.2733654 -0.74284346 -0.15500357
#> 5 0.45120187 -0.3999969 0.01370616 0.9805620 0.43523113 -0.19219605
         662 663
                               665
                        664
                                    666
#> 1 0.21637296 0.2284269 -0.7792670 1.1405268 0.484637010 -0.16907579
#> 2  0.04004293  0.1354282  -0.1279531  0.1715344  -0.417567074  -0.31426715
#> 4  0.66351174  0.1906362 -0.2853676  0.1369349 -0.243712551 -0.03631988
#> 5 -0.30830141 -0.3895533 -0.4005695 0.3947441 -0.005062882 0.17294183
         668
                  669
                          670
                                   671
                                           672
#> 2 -0.45618066 -0.36665408 -0.21684955 -0.32375570 -0.4983792 0.02875551
#> 4  0.89100000  0.65503279  0.04894025  -0.24631393  0.4049745  0.13990890
#> 5 0.32118778 -0.28544779 -0.41040128 0.09784549 -0.4515075 0.25921450
         674
                 675
                          676
                                   677
#> 1 -0.82890985 -0.07207794 0.59370354 0.6765826 0.18253173 0.372963077
#> 2 -0.08116334 -0.03197162 0.07921775 -0.3490365 -0.32517011 0.271364893
#> 3  0.11539990  0.51413960  -0.02880544  0.1230124  0.04563101  -0.066333986
#> 4 -0.23461907 -0.35188057 -0.79879534 -0.4213100 0.07797576 0.004025683
680
                 681
                          682
                                   683
                                           684
#> 1 -0.7376649  0.26089873  0.42186943 -0.03434275  0.1634847 -0.64493879
#> 3 -0.4816124 -0.55644404 -0.27829847 -0.14186878 -0.2778691 -0.15750127
#> 4  0.9791349  1.55573235  -0.78297761  0.16351883  0.2926203  0.22255146
#> 5 0.1434497 0.04404559 0.40433985 -0.47898547 -0.1903288 -0.82847985
#>
                 687
                                  689
                                     690
         686
                         688
#> 1 -0.74514297 -0.4353818 -0.3463873 -0.3439567 -0.9761569 0.03993129
#> 2 0.00311837 -0.2906127 -0.8549816 -0.2722705 -0.2281551 -0.39516080
#> 4 -0.19555896 -0.4533566 -0.1041303 -0.1356800 0.4148138 0.32508220
#> 5  0.26712872  0.1545440  -0.3636197  -0.3521782  -0.3408093  -0.96235506
         692
               693
                     694
                              695 696
#> 1 -0.2742084  0.5706896 -0.1946953 -0.1197391  0.006736103  0.005600253
#> 2 -0.2053871 -0.1392215 -0.2854024 -0.1730843 0.029438464 -0.123884412
#> 4  0.6636647 -0.8919831 -0.1560283  0.8411816 -0.599818299  0.043273940
#> 5 -0.3377940 -0.2138556  0.1284227  0.7783996  0.007540417  0.144980950
                                          702
         698
                  699
                         700
                                  701
#> 1 -0.04509849 -0.25771697 -0.2835010 -0.2223465 0.04973261 -0.52996344
#> 3  0.11183916  0.46698148  0.7861663  0.2381989  -0.23296632  -0.82090810
#> 4  0.34458507  0.05990218  -0.2264275  0.3803395  1.13269731  -0.04663370
#> 5  0.08522969  0.19505020 -0.2982987  0.2620118  0.06269250  0.06827924
         704
                 705
                         706
                                  707
                                           708
#> 1 0.51948711 -0.4183856 0.1021773 0.85714697 0.9159266 -0.3599615
#> 2  0.01082181  0.1205428 -0.4532698 -0.28624003 -0.3673289 -0.4308675
#> 3  0.56841282 -0.4047001  0.4154842  0.34113626 -0.4975752  0.2504577
#> 4 0.18322692 1.0537069 0.6705157 -0.36623061 0.5218670 -0.2115982
711 712
                              713 714
```

```
#> 3 -0.2250433 -0.381284532 -0.3285417 -0.65303914 -0.60848721 0.40294256
#> 5  0.1219199  0.005415081  -0.4846126  0.09040336  -0.71096683  0.10522060
                        718
        716
                717
                                719
#> 1 -0.66637257 1.0155255 0.06261742 0.77750522 0.3550789 0.1279315
#> 2 -0.04815252 -0.2554630 -0.16659214 -0.31167677 -0.2681751 -0.2746189
#> 3  0.39041170 -0.6117601  0.18023562  0.13677370  0.2786458  0.3261700
#> 4  0.70227764 -0.3718416 -0.27884236  0.21465870  0.2761764 -0.6454151
722
                723
                        724
                                725
                                        726
#> 5 0.43200857 0.2334210 -0.66501186 0.46447015 -0.2412476 0.23194246
        728
               729
                        730
                               731
                                      732
#> 2 -0.2271431 -0.1287634 -0.02936578 -0.3978503 -0.3200450 -0.05286793
#> 4 0.4260747 -0.5668188 -0.22471483 0.3989090 0.4429404 0.23231208
#> 5 0.4456188 0.6608856 0.45803604 0.3665830 0.5645989 -0.25961736
#>
        734
                735
                         736
                                737
                                        738
#> 1 0.1367838 0.03077847 -0.007713943 0.5439873 0.1904630 0.3224925
#> 2 -0.3656345 -0.58610503 -0.044137990 -0.1860757 -0.2375712 -0.1273673
#> 3  0.5947154 -0.62480610 -0.011437858 -1.1001841 -0.5389739  0.4019868
#> 4 -0.1199934 -0.15998974 -0.759998833 0.3787147 -0.3592389 -0.1756570
#> 5  0.3294171  0.72016514  -0.329163402  -0.1683104  -1.0157485  -0.2174441
                                   743
                  741
                          742
#> 1 0.029053033 0.21263772 0.96025255 -0.798994899 -0.5047170 1.3767690
#> 3  0.001481269  0.68063087 -0.51284869 -0.244206563  0.3516270 -0.5063077
#> 4 1.052432527 -0.64100212 0.84861432 -0.007499401 -0.3792545 0.7704553
746
                747
                        748
                                749
                                        750
#> 1 0.1170576 0.06932312 -0.11901909 -0.46844331 0.6562701 -0.3033275
#> 2 -0.4650988 -0.16476901 0.04751925 -0.22481411 -0.2036347 0.1960953
#> 4  0.7465634  0.14436874  -0.39826587  -0.55061620  0.9561729  -0.2038388
#> 5  0.1017506 -0.27505971  0.08978050  0.09702494  0.3398703 -0.5119346
        752
                753
                        754
                                755
                                       756
#> 1 -0.1485494 -0.13410947 0.29256362 0.5901337 -0.5655443 -0.17848338
#> 2 -0.5483752 -0.24738812 -0.05066223 -0.4164422 -0.1542149 -0.33397461
#> 4 -0.3378481 -1.61171260 0.06441016 -0.1420786 0.0820767 0.44357590
#> 5  0.4591719 -0.08356481  0.04598752 -0.5978820  0.4560032 -0.23600243
        758
                 759
                        760
                                761
                                        762
#> 2 -0.03410466 -0.18740150 -0.3866756 -0.2997781 0.06359542 -0.56859454
#> 3  0.50338733  0.07779602 -0.0321857  0.5149076 -0.40294750 -0.64006214
#> 4 0.03286225 -0.22891504 0.1938222 0.1741100 -0.11529033 0.09464144
#> 5 0.15540697 0.34370673 -0.2760366 0.2918274 0.30375222 -0.18328053
                 765
                         766
                                 767
```

```
#> 4  0.1185480 -0.036347285 -0.01759887  0.4012410  0.28610568 -0.4323499
#> 5  0.2541132  0.361366890  0.32596385  0.2442816  0.12185123  -0.5040138
         770
                 771
                         772
                                 773
                                         774
#> 1 -0.44349239 -0.15380438 -0.1385837 -0.1499774 -0.4723680 -0.4413517
#> 2 -0.40640138 -0.03070465 -0.0575740 -0.1368262 -0.2345637 -0.3483941
#> 3  0.27064685 -0.79642066  0.3030222 -0.3761496  0.1615977  1.1563718
#> 4  0.18135924  -0.15901367  -1.0425542  0.3723856  -0.5461600  0.3396432
776
                 777
                         778
                                  779
                                           780
#> 1 0.8941945 0.42030247 1.03669791 0.55172175 0.64971337 -0.27364456
#> 2 -0.2322941 -0.32992470 -0.08923046 -0.06949418 -0.18933635 0.01323172
#> 3  0.4799514  0.64220582  -0.13326421  -0.80246227  0.10026367  0.33332940
#> 4 -0.4601956 -0.29630684 -0.28355578 0.22921594 -0.06415509 -0.78901248
#> 5  0.2908594  0.07066432 -1.22115780  0.32173941 -0.12426407 -0.04842855
        782
                783
                       784
                              785
                                      786
#> 1 -0.1824620  0.76456424  0.45556580  1.286441873  -0.5761655  -0.3043940
#> 2 -0.1257239 -0.06621611 -0.16633513 0.008883771 -0.3778296 -0.2330477
#> 3 0.3258105 0.21235557 -0.08098279 0.343177635 -0.4738083 -0.7124170
788
                789
                        790
                                 791
                                         792
#> 1 0.3793404 -0.3283243 0.6420398 -0.69538227 -0.09802471 -0.1305552
#> 2 -0.2719596 -0.2865668 -0.2869630 -0.30074163 0.34236438 -0.1331582
#> 4 0.3051092 0.4882545 -0.3397571 0.25359281 0.37409676 0.9292887
#> 5  0.2554339  0.2495839  -0.1945262  -0.05324586  0.32904699  -0.6000654
#>
        794
                 795
                         796
                                 797
                                          798
                                                   799
#> 3 -0.5674139 -0.06650055 -0.65356837 -0.4911723 -0.05465414 -0.36466331
#> 5 -0.2742674 -0.32772467 -0.49864614 0.8399166 0.31612730 -0.16784303
                 801
                          802
         800
                                  803
                                            804
#> 1 0.62022847 -0.19985602 -0.34244435 0.3228096 -0.7275175805 0.22913547
#> 2 -0.08788291 -0.02340793 -0.36179200 -0.3369655 -0.0004163018 -0.34819658
#> 3 0.74970897 -0.82495992 -0.06977456 -0.1800873 0.2304193189 1.15486843
#> 4 -0.66679347 -0.38460744 -0.60098547 -0.8867472 0.3124122969 -0.02905405
#> 5  0.23371275  -0.33825302  0.51879272  -0.5331370  -0.5639578214  0.28030542
         806
                 807
                           808
                                   809
                                           810
#> 1 0.06758725 0.64511111 -0.109004327 -0.20944662 0.4621416 0.3230224
#> 2  0.08451213  -0.27434480  -0.006235752  -0.30733981  -0.2951776  -0.1699731
#> 4  0.13139299 -0.97447673  0.915700890  0.47606258 -0.7027147 -0.2290441
#> 5 0.17108817 0.29779687 -0.233486887 0.07717832 -0.1500005 -0.2506605
          812
                 813
                         814
                                815
                                          816
#> 2 0.112397898 -0.2371181 -0.1097228 -0.2030742 -0.32886502 -0.1852719
#> 4 0.009389146 0.6226795 -0.1333140 0.3264324 -0.03876508 0.2203449
#> 5 0.048522413 0.1480816 0.2004710 -0.3332577 -0.22454455 -0.3877516
```

```
#> 818 819 820 821 822
#> 1 0.02586141 0.3919226 0.1240226 0.1622295 1.09088226 0.66855409
#> 2 -0.23018677 -0.1235977 -0.1747192 -0.1351410 -0.26384798 -0.27225394
#> 3  0.44785986  0.3134591 -0.2146810  0.4639324  1.35665679  0.01280969
#> 4 -0.09467367 -0.6859235  0.7145133 -0.7289202  0.03852003  0.01527166
#> 5 -0.43699899 -0.1333767 0.5175301 0.2738808 -0.17445076 -0.28788625
                 825
                           826
                                  827
                                          828
         824
#> 1 0.38972035 0.93271854 0.07899116 0.1579410 0.4150498 -1.07046636
#> 2 0.05116985 0.09096116 -0.11598551 -0.3045434 -0.3390843 -0.12821232
#> 3  0.65398959  -0.31368498  -0.22430610  0.7771410  -0.2360817  -0.51248107
#> 5 -0.22535042 -0.09442711 -0.19804654 -0.1411587 0.5812637 0.06608121
                 831
                         832
#>
        830
                                  833
                                          834
#> 1 0.9144812 0.094861148 0.1160273 0.84739293 -0.3700056 3.268897e-01
#> 2 -0.4855275 -0.126915064 -0.3331462 0.01347359 -0.2420884 -9.235255e-05
#> 3 -0.3637749 -0.492371576 0.4175618 -0.10494296 -0.2397548 8.856214e-02
#> 4 0.1075120 0.677026432 -0.1324737 -0.87120520 0.1430129 -3.971384e-01
#> 5 -0.1728118 -0.004263926 -0.6931754 -0.29526964 -0.2509703 -7.553047e-01
                  837
                            838
                                    839
         836
                                             840
#> 1 -0.138525345 -0.00981995 0.779034550 0.71908494 0.4309698 0.20966815
#> 2  0.005421612 -0.30751212 -0.002357671 -0.44992216 -0.4266049  0.02551043
#> 3 -0.690390773 -0.05807532 0.116122307 -0.01855515 0.5546779 -0.35418431
#> 5  0.164481474  -0.16539365  0.253269642  -0.67825997  0.1733622  -0.79513818
        842
                 843
                      844
                             845
                                         846
#> 1 0.5004006 0.36153819 -0.2657065 0.1057673 -0.10067409 -0.49599042
#> 2 -0.2422559 -0.08862137 -0.3662263 -0.3334672 0.11805051 -0.41922973
#> 5 0.4507631 0.15034463 0.2896972 0.8184687 -0.65134044 0.04865934
                  849
                          850
                                 851
#> 1 -0.37735986  0.87804096 -0.18787272 -0.8771883 -0.3068408 -0.6953335
#> 2 -0.08880614 -0.09474761 -0.33138033 0.1729763 0.4184833 -0.1776955
#> 3  0.19261981  0.19621669  -0.31131141  -0.1810001  -0.2869783  -0.1780897
855
        854
                         856
                                  857
                                           858
#> 1 0.7443467 -0.36886053 0.6582869 0.38580287 0.41718772 -0.47628109
#> 2 -0.2526549 -0.09502200 -0.0685519 0.06861395 -0.17488470 0.02532586
#> 3 0.4556086 0.08700410 -0.4631689 0.69525924 -0.13249344 -0.90891838
#> 4 -0.2126043 -0.09460227 -0.3860810 0.03292558 -0.13093423 0.69544938
860
                 861
                          862
                                   863 864
#> 2 0.09229224 -0.49485652 -0.35795045 -0.002755344 -0.1000324 -0.27694398
#> 3 -0.20414362 1.01900136 0.37124926 -0.182974708 -0.3881067 -0.14090840
#> 5  0.04998766 -0.34653708  0.09002599  0.296668433  0.6839981 -0.08265082
         866
                  867
                           868
                                  869
                                           870
#> 2 0.03525046 -0.46955111 -0.50779892 0.1861691 -0.4660202 -0.3102743
#> 3 0.51073185 -0.56152053 0.59521161 0.2463708 0.1892512 0.3795448
```

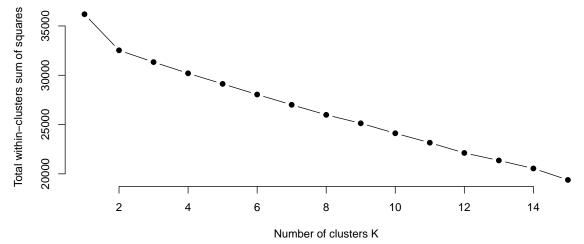
```
872
             873 874 875
#> 1 -0.08048723 -0.1493317245 0.56130413 0.437593674 0.386234477
#> 2  0.01066211  0.0389764867 -0.07038718 -0.499817531 -0.051069137
#> 3  0.05913867  0.4685624230  0.81903001 -0.649772042  0.116457389
#> 4 0.30450687 0.4214313099 0.08978815 -0.001762203 0.705085161
879
                                    880
         877
                  878
#> 2 0.00593532 -0.06793132 -0.50894940 -0.60056105 -0.3980324 -0.48852242
#> 3 -0.08308360 -0.30483729 -0.41155499 0.35237006 -0.1254756 0.62084021
#> 4  0.29911757 -1.00329309  0.01594382 -0.19188054 -0.5564362 -1.24257913
#> 5  0.27144234  -0.07465133  -0.23941169  -0.12555031  0.2326800  0.03765357
         883
                  884
                         885
                                  886
                                            887
#> 1 -0.3546641 -0.43002404 -0.9457595 -0.9331361 -0.2558326639 -0.54171791
#> 3  0.1365479 -0.21628526  0.2373969  0.3220362  0.7669248431 -0.17350321
#> 5 -0.9572056 -0.28027218  0.1616487 -0.2721760 -0.0003980947  0.08784904
        889 890 891 892 893
#> 1 0.08436273 0.4808880 -0.12875828 -0.20817937 -0.153610314 -0.6235001
#> 2 -0.09181601 -0.5060207 -0.01713622 0.02855613 -0.178064042 -0.4777918
#> 3  0.59912627 -0.7874663  0.05105522 -0.13482622 -0.296875131 -0.3105203
#> 4  0.33194983  -0.3945991  -1.19023729  0.78235651  0.006748591  0.1115081
#> 5  0.28303252  -0.5763110  -0.02323331  0.05573237  0.661076393  0.7437463
         895
                   896
                            897
                                     898
                                            899
#> 1 -0.12198566 -0.279500631 -0.62100321 0.56623220 -0.2068409 -0.2812690
#> 2 0.19704915 0.001879772 -0.06209988 -0.21983174 0.0168379 -0.1872877
#> 3 -0.01109515 -0.042163684 -0.65150508 -0.21009345 -0.1513093 -0.2201011
#> 4 -0.33823744 -0.779467834 -0.07827332 -0.00333141 -0.3008498 -0.4345396
901
                 902 903
                               904 905
#> 1 -0.6304459 -0.45102715  0.187211214 -0.3038926  0.7487273  0.1813533
#> 2 -0.2748914 -0.01419353 -0.249991777 -0.2918445 -0.2357016 -0.0447524
#> 3  0.2739311 -0.65713768 -0.448962163  0.1014562 -0.6791512  0.4874801
#> 5 -0.4702334 -0.06286179 -0.009171061 0.3234240 -0.0240298 0.6522296
         907
                 908
                         909
                                   910
                                            911
#> 1  0.4109582 -0.3702743 -0.75402286 -0.01253961  0.025432387 -0.1435224
#> 2 -0.2248324 -0.4847065 -0.06466259 -0.13073557 -0.428669328 -0.2216384
#> 4  0.8208870  0.1890872  0.75887691 -0.03648739  0.006208877 -0.3962428
#> 5  0.3159157 -0.1721366 -0.20248892  0.23718697  0.033363659  0.4494812
         913
                 914
                          915
                                  916
                                          917
                                                    918
#> 1 -0.3332395 -0.07713992 0.8058535 -0.41644672 -0.5578503 -1.07481441
#> 2 0.1270801 -0.17090345 -0.1115031 -0.08149816 -0.3359158 -0.07038508
#> 4 0.1240636 0.94583061 0.7373727 -0.12795671 0.1092541 0.07001787
#> 5 0.7522076 0.14073346 -0.9757967 0.06763811 -0.2748847 0.11557255
               920
                     921
                                  922 923
#> 2 -0.2384565 -0.3231424 -0.07543868 0.02842824 -0.50565007 -0.1758806
#> 3 -0.8308118  0.5713272 -0.21388601  0.05157633  0.05663348 -0.5053143
```

```
927
        925
                926
                                928
                                         929
#> 1 0.84866841 0.6002481 -0.2468977 -0.43404141 0.371612477 -0.2444907
#> 2  0.01263115 -0.5382058 -0.2145030 -0.18059279 -0.230575748 -0.2516704
#> 3  0.04855175  -0.5568205  -0.4613276  -0.35579301  -0.076273033  -0.2107523
#> 4 -0.50070231 -0.3572626  0.0558407 -0.02962356  0.005285005 -0.4485422
#> 5 -0.13113797 -0.4388269 0.2175911 0.14937083 -0.550394273 0.7311262
             932 933
                             934
                                    935
        931
                                                 936
#> 1  0.04591207 -0.7886644 -0.99205131  0.1237920 -0.07039423 -0.30220562
#> 2 0.02780574 -0.1872114 -0.09000613 -0.4790011 -0.16989772 -0.03780131
#> 3  0.71117714 -0.3412825  0.68613044 -0.2217237  0.36533820  0.75010680
937
                938
                       939
                                       941
                                940
#> 1 -1.1321238 -0.3420790 -0.1363565 0.24902087 0.3759461 0.5334722
#> 3 -0.7519345 -0.3652874 -0.2032828 0.01850937 -0.2407702 -0.3411952
#> 5  0.3560271  -0.6602366  0.3778288  -0.51260000  -0.1683220  0.1779950
#>
        943
                944
                      945
                                946
                                      947
                                                  948
#> 1 0.04516103 0.34700871 -1.1855156 -0.01559563 1.478496995 0.39745236
#> 2 0.05833538 -0.01546944 -0.2760283 0.05793133 -0.009277419 -0.05987117
#> 3  0.11474587 -0.89783944  0.5000407  0.37193783  0.152828051  0.53856468
#> 4 -0.13777564 -0.53818471 -0.4218741 0.07982394 0.650218587 0.21875731
#> 5  0.21393494  0.50286233  -0.1326163  0.23370360  0.237716774  -0.20822326
        949 950 951 952
                                    953
#> 2 -0.2027654 -0.10656315 0.0154074 -0.27738068 -0.56022726 -0.24046236
955
                956
                        957
                               958
                                        959
#> 1 -0.29236799  0.5170009  0.19456702 -0.4383396  0.63591851  0.49578812
#> 2 -0.05131833 -0.5298076 -0.26531408 -0.1710295 -0.03697572 -0.27363341
#> 3  0.03730141 -0.3453849 -0.51310161  0.2234710 -0.03611338 -0.26313893
961
                962
                       963
                                964
                                    965
#> 2 -0.24364831 -0.4599659 -0.3605081 -0.23856302 -0.46812316 0.2806135
#> 3 -0.07494199 -0.4981764 -0.6270087 -0.24831359 0.17256173 -0.6460807
#> 4 0.27509973 0.7179181 0.3931114 0.08296127 0.06064456 -0.2715134
#> 5 1.04592049 -0.4445711 0.3319211 -0.13223254 0.07965834 -0.1086562
         967
                968
                        969
                                970
                                        971
#> 1 -0.51091926 -0.3862390 -0.2678973 0.34715472 -0.3537663 0.4710499
#> 2 -0.25558911 -0.4698696 -0.1698527 -0.03827192 -0.2622173 -0.2149532
#> 3  0.22641922 -0.2708356 -0.6536129 -0.05220790  0.1507415  0.8900265
#> 4 0.07301291 1.5854646 -0.2897068 -0.03470577 -0.6583049 -0.3238652
#> 5  0.23335499  -0.2586735  0.3177551  -0.02247834  -0.4056628  -0.1053866
                                    977
        973
                        975
                             976
#>
               974
#> 1 0.44753342 0.1980659 -0.42386379 -0.20316345 0.48070025 -0.15223062
#> 2 -0.05656158 -0.1150551 -0.34627070 -0.25724103 -0.34777541 0.08644216
```

```
#> 3  0.93709770 -0.1949217  0.02409844 -0.06810831 -0.01307385 -0.34215085
#> 5 -0.19299942 -0.5434200 -0.50051586 0.54794056 0.28211830 0.52413168
#> 979 980 981 982 983 98L
#> 2 -0.2673652 -0.43104875 -0.21156964 0.01731834 -0.3589901 -0.012474619
#> 3 0.1019480 0.38937700 0.84865681 0.45853683 0.1408300 0.730091799
#> 4 1.0399011 -0.85293307 -0.51318521 0.01418099 -1.1964435 -0.594574847
#> 5 -0.2784783  0.09411387 -0.07981137 -0.09071290 -0.3113317 -0.799791445
         985
                 986
                      987
                                  988
                                          989
#> 2 -0.00349239 -0.21470386 -0.1416711 -0.05977998 -0.43172593 -0.14560705
#> 3 -0.57785374 -0.43668802 0.1137881 -0.20478486 0.09390983 0.03354041
#> 4 0.47222975 -0.86073690 -0.8688942 0.45727879 -0.20736417 0.57161781
991 992 993 994 995
#> 2 -0.003537708 -0.26031019 -0.32712730 -0.03168406 -0.23624319 -0.33453575
#> 3  0.270546406 -0.42135611 -0.07762101 -0.23580073  0.12874047 -0.37912622
#> 4 0.550913388 0.46557552 0.34995551 0.30228586 0.34736731 -0.32268958
#> 5  0.145432657  0.18235081 -0.09022613  0.04245718 -0.05924426 -0.39912477
        997
                998
                         999
#> 1  0.6496092 -0.3212383 -0.01658663
#> 2 -0.2623600 -0.3079115 -0.41400480
#> 3 0.4227699 0.1991706 -0.65264424
#> 4 -0.2215555   0.3727847 -0.01778748
#> 5 -0.7543713 0.1722276 0.38435187
#>
#> Clustering vector:
  X.0.9619334 X0.4418028 X.0.9750051 X1.417504
                                        X0.8188148
             1 5
#>
   X0.3162937 X.0.02496682
                     X.0.063966 X0.03149702 X.0.3503106
    4 1
                       3
                                5
                       X1.337515
                                X0.7019798
#>
   X.0.7227299 X.0.2819547
             X0.6385951
                      X0.2867807 X.0.2270782 X.0.2200452
#>
   X.0.4653828
             1
                               5
#>
       5
                                         .5
                                         X.1.325008
#>
   X.1.242573 X.0.1085056
                      X.1.864262 X.0.5005122
#>
        2 2
                     2
    X1.063411 X.0.2963712 X.0.1216457 X0.08516605
#>
                               2
#>
        2
            2 2
   X.0.5095915 X.0.2167255 X.0.05550597 X.0.4844491 X.0.5215811
     2 2 2 2
#>
    X1.949135
#>
             X1.324335
                      X0.4681471
                                  X1.0611
                                          X1.65597
#>
          2
                   2
#>
#> Within cluster sum of squares by cluster:
#> [1] 2889.281 13540.079 3916.534 2854.316 5927.410
  (between_SS / total_SS = 19.5 %)
#> Available components:
#> [1] "cluster"
               "centers" "totss"
                                     "withinss"
```

Elbow-Method

```
#Elbow Method for finding the optimal number of clusters
set.seed(42)
# Compute and plot wss for k = 2 to k = 15.
k.max < -15
data <- scaled_data
wss <- sapply(1:k.max,
              function(k){kmeans(data, k, nstart=60,iter.max = 15 )$tot.withinss})
WSS
#>
    [1] 36190.83 32531.95 31337.21 30197.84 29125.14 28050.54 27003.94
   [8] 25985.95 25128.65 24116.89 23159.64 22120.76 21359.88 20547.72
#> [15] 19384.38
plot(1:k.max, wss,
     type="b", pch = 19, frame = FALSE,
     xlab="Number of clusters K",
     ylab="Total within-clusters sum of squares")
```



Kriterium: Beim Elbow-Kriterium werden die Fehlerquadratsummen in ein Diagramm abgetragen. Zeigt sich im Kurvenverlauf ein Knick ("Ellbogen"), so kann dieser Wert als Entscheidungskriterium für die Clusteranzahl verwendet werden.

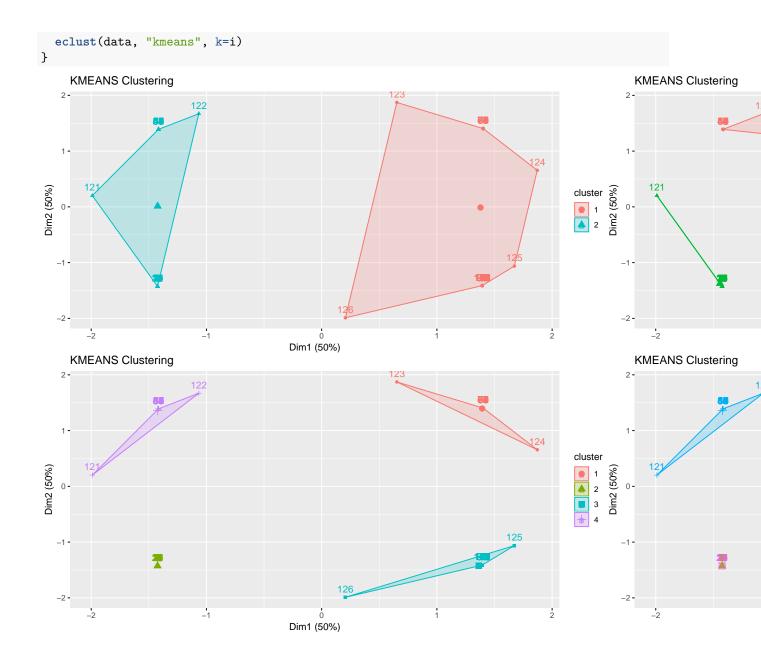
Elbow-

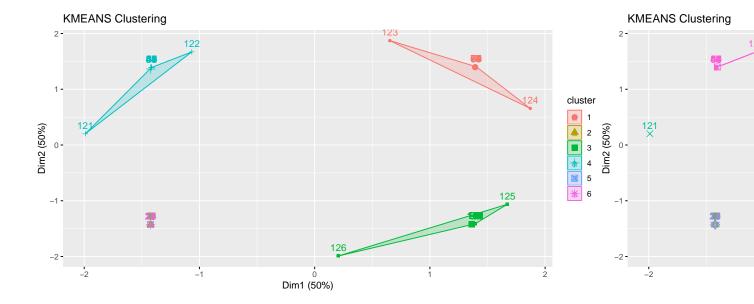
Optimale Anzahl der Cluster K=4.

Aufgabe 2 a)

In diesem Aufgabenteil fuehren wir den Kmeans Algorithmus auf den clust Datensatz durch fuer die Werte $k=\{2,\ldots,7\}$ und visualisieren anschliessend die Cluster.

```
load("clust.RData")
packageTest("cluster")
packageTest("factoextra")
data <- clust
colnames(data) <- c("x1", "x2", "x3", "x4")
data <- scale(data)
for(i in 2:7) {
   par(mfrow=c(6,1))</pre>
```

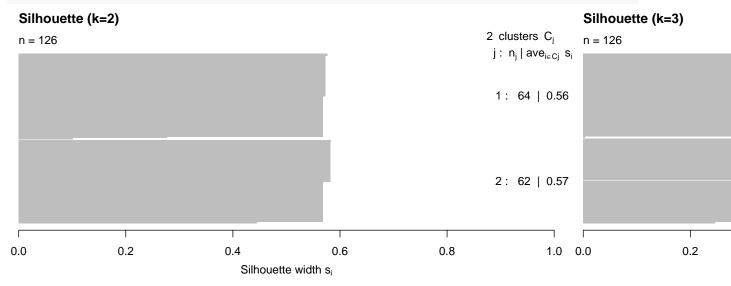




b)

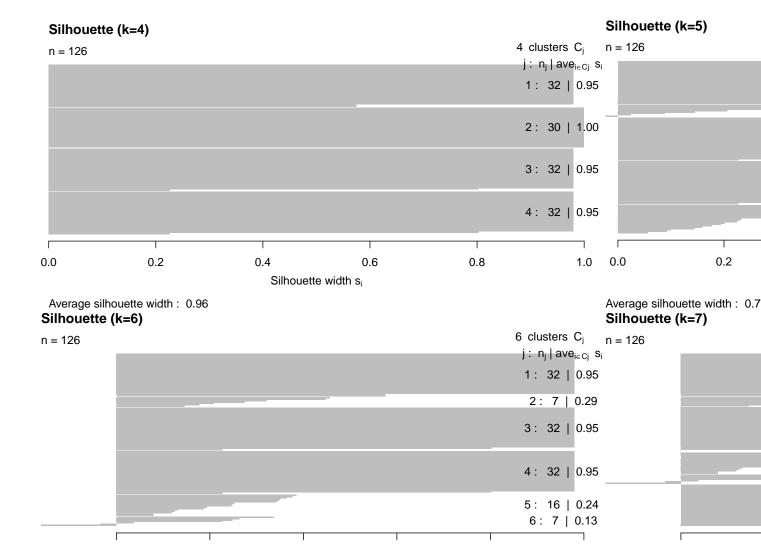
Nun berechnen wir die Silhouetten sowie die Silhouetten-Koeffizienten fuer die Clusterungen aus a) und visualisieren anschliessend die Silhouetten inkl der Koeffizienten.

```
for(i in 2:7){
  km.res <- eclust(data, "kmeans", k=i, graph=FALSE)
  sil <- silhouette(km.res$cluster, dist(data))
  plot(sil, main=sprintf("Silhouette (k=%d)",i))
}</pre>
```



Average silhouette width: 0.57

Average silhouette width: 0.



Average silhouette width: 0.78 Average silhouette width: 0.78

0.6

8.0

1.0

0.0

c)

0.0

Die Silhouette eines Datenpunktes entspricht einem Guetekriterium der Cluster. Sie gibt an, wie aehnlich bzw. unaehnlich ein Datenpunk zu seinen Nachbarpunkten im Mittel ist. Dabei werden die Vergleiche zwischen dem Datenpunkt und den Nachbarpunkten innerhalb des eigenen Clusters gemacht sowie zwischen dem Datenpunk und den Nachbarpunkten des nächsten Nachbar-Clusters.

0.4

Silhouette width si

Die Silhouette kann Werte aus dem Intervall [-1,1] annehmen.

0.2

1 bedeutet dabei, dass der Datenpunkt im Mittel relativ zentral innerhalb des eigenen Clusters liegt und somit weiter entfernt zu den Nachbarklustern ist. Diese Eigenschaft entspricht einem guten Clustering.

-1 bedeutet, dass der Datenpunkt im Mittel naeher zum Nachbar-Cluster liegt als zum eigenen Cluster. 0 wird einem Datenpunkt zugeordnet, wenn ein Cluster ausschliesslich diesen Datenpunkt enthaelt. maximimieren wir den Wert der Silhouette, so erhalten wir den Silhouetten-Koeffizienten.

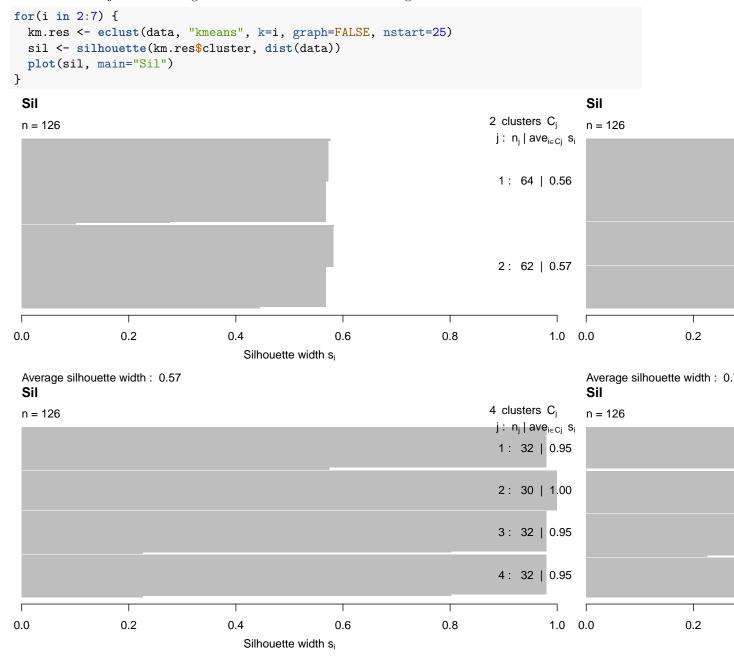
Vergleichen wir die Modelle mit unterschiedlichen Anzahl an Cluster, so waehlen wir das Modell mit k=4, da dieser die hoechste Silhouette besitzt sowie niedrigste Komplexitaet. Alle Cluster sind aehnlich gefuellt. Erhoehen wir die Anzahl der Cluster, so bleibt der Wert der Silhouette gleich, jedoch erhalten wir Silhouetten

Werte gleich 0, diese entsprechen einem Cluster von einem Datenpunkt.

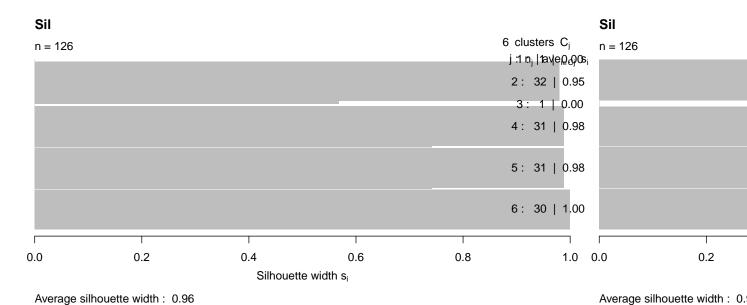
d)

Average silhouette width: 0.96

Da das Ergebnis des K-Means-Verfahrens sehr stark von dem Initialzustand abhaengt, wiederholen wir im Folgenden den Algorithmus und setzen dabei fuer jeden Wert $k \in \{2, ..., 7\}$ zufaellig einen Startzustand. Diese Option wird mit dem parameter nstart erreicht, den wir z.B. auf 25 setzen, so dass der Algorithmus 25 Mal durchlaeuft mit jeweils zufaelligem Startzustand. Im default betraegt dieser Parameterwert 1.



Average silhouette width: 0.



In unserem Fall erkennen keine signifikanten Unterschiede zu unserer Beobachtung auf Aufgabenteil b).