

Pushdown Automata

(
 Q – set of states
 Σ – input alphabet
 Γ – stack alphabet
 $\delta: Q \times \Sigma_{\epsilon} \times \Gamma_{\epsilon} \rightarrow P(Q \times \Gamma_{\epsilon})$ – transition function
 $q_o \in Q$ – start state
 $F \subseteq Q$ – accept states
)

Turing machine

(
 Q – set of states
 Σ – input alphabet (without \diamond - blank symbol)
 Γ – tape alphabet ($\diamond \in \Gamma, \Sigma \subseteq \Gamma$)
 $\delta: Q \times \Gamma \rightarrow Q \times \Gamma \times \{L, R\}$ – transition function
 $q_o \in Q$ – start state
 $q_{accept} \in Q$ – accept state
 $q_{reject} \in Q$ – reject state, $q_{reject} \neq q_{accept}$
)

uqv - Configuration (q - current state, u - tape.slice(0,current), v - tape.slice(current))

Configuration c_1 yields c_2 if can go from c_1 to c_2 in a single step

Start configuration - at q_o

Accepting and rejecting configurations are halting - halts execution in them

Language recognized by a Turing machine is Turing-recognizable

Any state change can lead to accept, fail or loop (neither)

Pumping lemma

$s = uv^nxy^nz$ where $n \geq 0$. Show that it can't be pumped

Turing description:

1. Mark first unmarked 0. If none, go to 6.
2. Move the head to the front
3. Mark first unmarked 1. If none, reject
4. Move the head to the front

5. Go to 1

6. Scan if there is any unmarked 1. If so, reject. Else accept

