

[601]

$$X: \{1, 2, \dots, 6\} \rightarrow \{2, 3, \dots, 6\}$$

$$P_X = \begin{cases} \frac{2}{6}, & x=6 \\ \frac{1}{6}, & x \in \{2, 3, 4, 5\} \end{cases}$$

$$\begin{aligned} EX &= 6 \cdot \frac{2}{6} + \frac{1}{6} \cdot (2+3+4+5) = 2 + \frac{14}{6} = \frac{12+14}{6} = \\ &= 4,3 = \frac{13}{3} \end{aligned}$$

[602]

$$f_X(x) = \frac{2x}{a^2} \quad 0 \leq x \leq a$$

$$EX = \int_0^a x \cdot \frac{2x}{a^2} dx = \left| \frac{2}{a^2} \cdot \frac{x^3}{3} \right|_0^a = \frac{2 \cdot a}{3}$$

[603]

609

$$D(X) = \sqrt{V(X)} = \sqrt{81} = 9$$

$$R(X) = \frac{D(X)}{V(X)} = \frac{9}{81} = \frac{1}{9}$$

610

$$f_X(x) = 3x^{-4} \quad (x \geq 1)$$

$$E(X) = \int_1^{+\infty} x \cdot 3x^{-4} dx = 3 \cdot \frac{x^{-2}}{-2} \Big|_1^{+\infty} =$$

$$= +\frac{3}{2}$$

$$V(X) = E(X^2) - (EX)^2$$

$$E(X^2) = \int_1^{+\infty} x^2 \cdot 3x^{-4} dx = \frac{3x^{-1}}{-1} \Big|_1^{+\infty} = 3$$

$$V(X) = 3 - \left(\frac{3}{2}\right)^2 = \frac{3}{4}$$

