



Workshop 3

COMP90051 Machine Learning
Semester 2, 2020

Learning outcomes

At the end of this workshop you should:

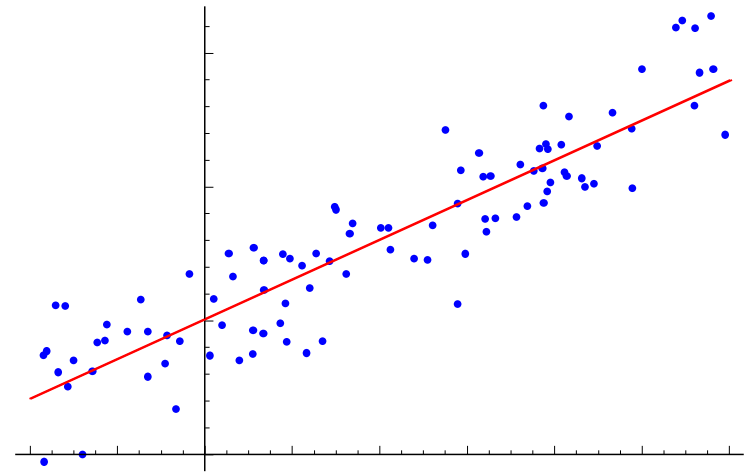
- be able to implement **linear regression** using numerical linear algebra functions
- be familiar with the **scikit-learn interface** for linear regression
- be able to implement **polynomial regression**
- be able to explain the **benefits/drawbacks** of linear regression versus polynomial regression

Quick review: linear regression

Assume the response y is a *linear* function of the features $\mathbf{x} = [x_1, \dots, x_m]^T$:

$$y = w_0 + \sum_{i=1}^m w_i \cdot x_i$$

Write this more compactly as $y = \mathbf{x}^T \mathbf{w}$ by redefining $\mathbf{x} = [x_0, x_1, \dots, x_m]^T$ with $x_0 = 1$ and defining $\mathbf{w} = [w_0, \dots, w_m]^T$



Question: How do we choose the weights?

Quick review: linear regression

Decision theoretic view

Make decision that minimises the empirical risk

$$\hat{R} = \frac{1}{n} \sum_{i=1}^n L(y_i, \hat{y}_i)$$

and choose the square loss
 $L(y, \hat{y}) = (\hat{y} - y)^2$.

Optimal decision for \mathbf{w}
minimises the sum-squared error.

Probabilistic view

Assume

$$y|\mathbf{x}, \mathbf{w} \sim \mathcal{N}(\mathbf{x}^T \mathbf{w}; \sigma^2)$$

Can write down the likelihood for the observations

$$\begin{aligned} L(\mathbf{w}|\mathbf{X}, \mathbf{Y}) \\ = \prod_{i=1}^n p(y_i|\mathbf{x}_i, \mathbf{w}, \sigma) \end{aligned}$$

MLE for \mathbf{w} minimises the sum-squared error.

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