

## CS 3530: Assignment 2a

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### Exercise 2.1abcd (10 points)

#### Problem

Recall the CFG  $G_4$  that we gave in example 2.4. For convenience, let's rename its variables with single letters as follows.

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T \times F \mid F$$

$$F \rightarrow (E) \mid a$$

Give derivations for each string.

a.  $a$

b.  $a + a$

c.  $a + a + a$

d.  $((a))$

#### Solution

a:

$$E \Rightarrow T, E \Rightarrow F, E \Rightarrow a$$

b:  $E \Rightarrow E + T$

$$E \Rightarrow T + T$$

$$E \Rightarrow F + T$$

$$E \Rightarrow a + T$$

$$E \Rightarrow a + F$$

$$E \Rightarrow a + a$$

c:  $E \Rightarrow E + T$

$$E \Rightarrow E + T + T$$

$$E \Rightarrow T + T + T$$

$$E \Rightarrow F + T + T$$

$$E \Rightarrow a + T + T$$

$$E \Rightarrow a + F + T$$

$$E \Rightarrow a + a + T$$

$E \Rightarrow a+a+F$

$E \Rightarrow a+a+a$

d:  $E \Rightarrow T$

$E \Rightarrow F$

$E \Rightarrow (E)$

$E \Rightarrow (T)$

$E \Rightarrow (F)$

$E \Rightarrow ((E))$

$E \Rightarrow ((T))$

$E \Rightarrow ((F))$

$E \Rightarrow ((a))$

## Exercise 2.4bc (10 points)

### Problem

Give context-free grammars that generate the following languages. In all parts, the alphabet  $\Sigma$  is  $\{0, 1\}$ .

**b.**  $\{w \mid w \text{ starts and ends with the same symbol} \}$

**c.**  $\{w \mid \text{the length of } w \text{ is odd} \}$

### Solution

b.

$S \Rightarrow 0P0 \mid 1P1 \mid 0 \mid 1$

$P \Rightarrow 0P \mid 1P \mid \varepsilon$

c.

$S \Rightarrow 0 \mid 1 \mid 0S0 \mid 0S1 \mid 1S0 \mid 1S1$