

Homework 04 - 4.4, 4.14, 4.24, 4.26, 4.34, 4.40, 4.48

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September 9, 2015

4.4

- a. The point estimate is the mean in this case, which is 171.1, and the median is 170.3.
- b. The point estimate of the SD is 9.4, the IQR is $177.8 - 163.8 = 14$.
- c. Anything over mean + 2SD is considered abnormal. So anything over 189.1 in this case. 180cm is below this level, so the person is considered a normal height.
- d. The sample mean and sd would be somewhat similar, but it's unlikely they would be identical. When taking a sample, depending on the CI, the mean can vary, but will usually be in a relative range.
- e. SE will be used in this case. It is 0.4174687.

4.14

- a. False, we are 95% confident that the population mean is within the CI.
- b. False, one of the conditions state that the population should not be strongly skewed.
- c. False, we are looking at the population mean, not the sample means.
- d. True, this is what the CI means.
- e. True, the "net" is narrower, and is less likely to contain the population mean in this case.
- f. False, it would need to be 9 times larger, as the n is under a square root.
- g. True, the margin of error is half the CI.

4.24

- a. The individuals are independent, it is assumed to be a SRS, and it likely less than 10% of the population.
- b. null: mean = 32, alternative: mean \neq 32. I will reject the null hypothesis if the p-value is less than 0.10.

```
z <- (30.69 - 32) / (4.31 / sqrt(36)) # z score
p <- pnorm(z, 0, 1); p # p value
```

```
## [1] 0.0341013
```

The p value is less than 0.10, which means I reject the null hypothesis.

- c. The p value is essentially the probability of incorrectly rejecting the null hypothesis. In this case, there is evidence that the p-value is less than the significance level, which means the null can be rejected.
- d.

```
mean <- 30.69
SE <- 4.31 / sqrt(36)
z <- 1.645
lower <- mean - z * SE
upper <- mean + z * SE
```

The interval is 29.5083417, 31.8716583.

- e. The results disagree, as the p value test and CI test both conclude that 32 is unlikely to happen with a 90% CI.

4.26

- a. The two means are very different, so the z score / p value might be weird.

null: mean = 100, alternative: mean > 100. I will reject the null hypothesis if the p-value is less than 0.10.

```
z <- (118.2 - 100) / (6.5 / sqrt(36)) # z score
p <- pnorm(z, 0, 1); p # p value
```

```
## [1] 1
```

The p value is higher than .10, which means we fail to reject the null hypothesis.

- b.

```
mean <- 118.2
SE <- 6.5 / sqrt(36)
z <- 1.645
lower <- mean - z * SE
upper <- mean + z * SE
```

The interval is 116.4179167, 119.9820833.

- c. The value is not in the CI, but the p value test does not reject the null.

4.34 The sampling distribution is the distribution of point estimates taken from all possible samples of a fixed size from a population. With a larger sample size, the sampling distribution becomes more normal, the center will closer to the population mean, and the spread will be smaller.

4.40

- a.

```
z <- (10500 - 9000) / (1000 / sqrt(1))
pnorm(z)
```

```
## [1] 0.9331928
```

- b.

```
mean <- 9000
sd <- (1000 / sqrt(15))
```

The distribution is $N(9000, 258.1988897)$.

c.

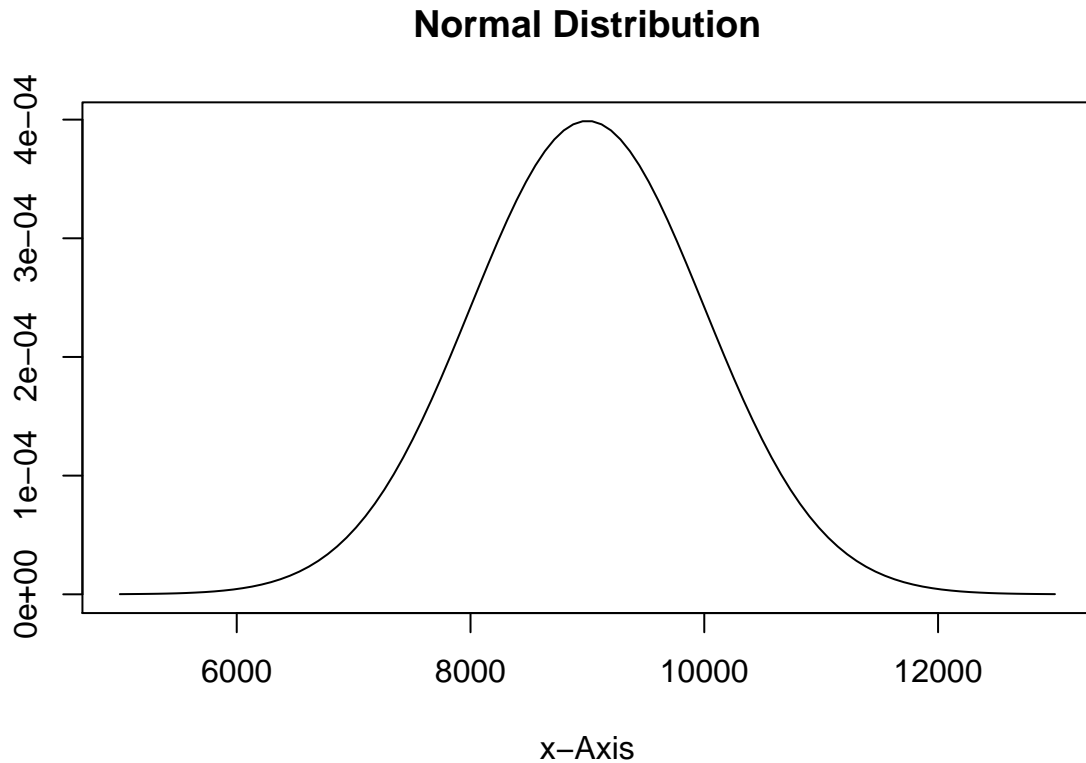
```
z <- (10500 - 9000) / (1000 / sqrt(15))
1 - pnorm(z)
```

```
## [1] 3.133452e-09
```

The probability of the mean being higher than 10500, is nearly 0.

d. Using a snip of the code from the normalPlot code, and changing it a bit.

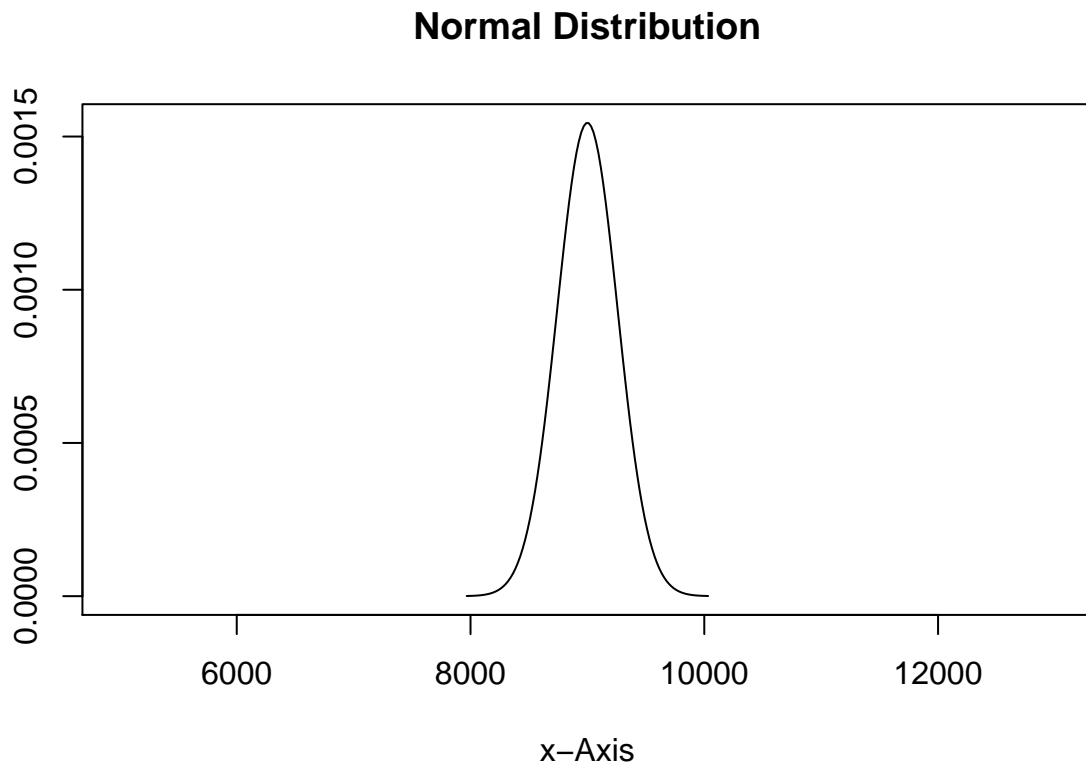
```
mean = 9000
sd = 1000
x <- seq(-4, 4, length = 100) * sd + mean
hx <- dnorm(x, mean, sd)
plot(x, hx, type = "l", xlab = "x-Axis", ylab = "", main = "Normal Distribution", xlim = c(5000, 13000))
```



```

mean = 9000
sd = (1000 / sqrt(15))
x <- seq(-4, 4, length = 100) * sd + mean
hx <- dnorm(x, mean, sd)
plot(x, hx, type = "l", xlab = "x-Axis", ylab = "", main = "Normal Distribution", xlim = c(5000, 13000))

```



e. You could estimate, but the the numbers would likely be off.

4.48

a. As sample size increases, the p value decreases. The coin example is perfect here. If you flip a coin 10 times, and get 7 heads it's somewhat normal. If you flip it 1000 times, and get 700 heads it's much stranger. So in this case, the p value would be much lower to compensate.