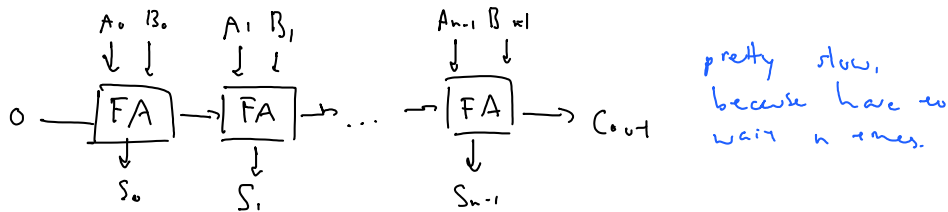


Lecture 4

Wednesday, September 9, 2015 10:01 AM

N-bit adder circuit (ripple carry adder)



In real life, you would actually build a (carry lookahead adder)

As CS majors, we're content with ripple carry adders

Representing Numbers

$$123 = 1 \cdot 10^2 + 2 \cdot 10^1 + 3 \cdot 10^0$$

0, 1, ..., 9 → 10 digits (base 10)

Positional number system

With each extra digit, multiply by another factor of ten.

But circuits aren't good with 10's.

So we get the

BINARY SYSTEM - digits 0, 1

with numbers being represented by powers of 2. (base 2)

$$1111011 = 1 \cdot 2^6 + 1 \cdot 2^5 + 1 \cdot 2^4 + 1 \cdot 2^3 + 0 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0$$

binary decimal

$$= 64 + 32 + 16 + 8 + 2 + 1 = 123$$

unsigned numbers

Octal System - digits 0, 1, 2, 3, 4, 5, 6, 7 | (base 8)

Hexadecimal System - digits 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F | (base 16)

001111011
1 7 3 011 1011
7 B 1011 sequence of bits

DEADBEEF

AFFE = 45054

-123, can't just say its negative, have to encode in the bits

Signed binary numbers

Unsigned

000	0	0 00	+0
001	1	0 01	+1
010	2	0 10	+2
011	3	0 11	+3
100	4	1 00	-0

$$\begin{array}{r} 001 \leftarrow -11 \\ 101 \leftarrow -1 \\ \hline 111 \leftarrow -2 \end{array}$$

101	5	<u>1</u> 01	-1
110	6	<u>1</u> 10	-2
111	7	1 11	-3

Sign and magnitude

Standard WAY

Another way to do it is called
ONES COMPLIMENT

TWOS COMPLIMENT

000	0	0 00	+0
001	1	0 01	+1
010	2	0 10	+2
011	3	0 11	+3
100	4	1 00	-3
101	5	1 01	-2
110	6	1 10	-1
111	7	1 11	-0

0 00	+0
0 01	+1
0 10	+2
0 11	+3
1 00	-4
1 01	-3
1 10	-2
1 11	-1

no positive 4

flip the bits

flip all the bits and
ADD 1

$$\begin{array}{r}
 100 \leftarrow -4 \\
 \underline{010} \leftarrow 2 \\
 \underline{110} \leftarrow -2
 \end{array}$$