

# Questions

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We have three equations that we want to solve.

$$u = -\frac{k}{\mu_c} \nabla p,$$

$$\mu_c = \left( \frac{c}{mu_o^{\frac{1}{4}}} + \frac{1-c}{mu_s^{\frac{1}{4}}} \right)^{-4}$$

and,

$$\varphi \frac{\delta c}{\delta t} + \nabla(uc) = \nabla(\kappa \nabla c)$$

I am trying to understand how these equations are encoded in uw3.

I believe I understand how the Darcy velocity equation is encoded and solved. You define a Darcy model that takes velocity  $u$  and pressure  $p$ . You give this model a constitutive equation in the form  $q + D \frac{d}{dx}(\phi) = 0$ . Somehow, and I'm not sure where in the code this is, but  $q$  gets set to the velocity  $u$ , and the flux term  $\phi$ , gets set to  $p$ . You then give  $D$  to be  $\frac{k}{\mu_c}$ . This encodes our Darcy flow equation in uw3.

Now, I am trying to understand how you specify the advection diffusion equation. You give the advection diffusion solver the material, velocity and something called `u_Star_fn`, which I think is some sort of history variable for the material. You then give it a diffusion equation constitutive model. This is again of the form

$$q = D \frac{d\phi}{dx}, \tag{1}$$

where  $\phi$  is some flux term. How is  $\phi$  specified, where can I find this in the code, and how should  $D$  be defined?