

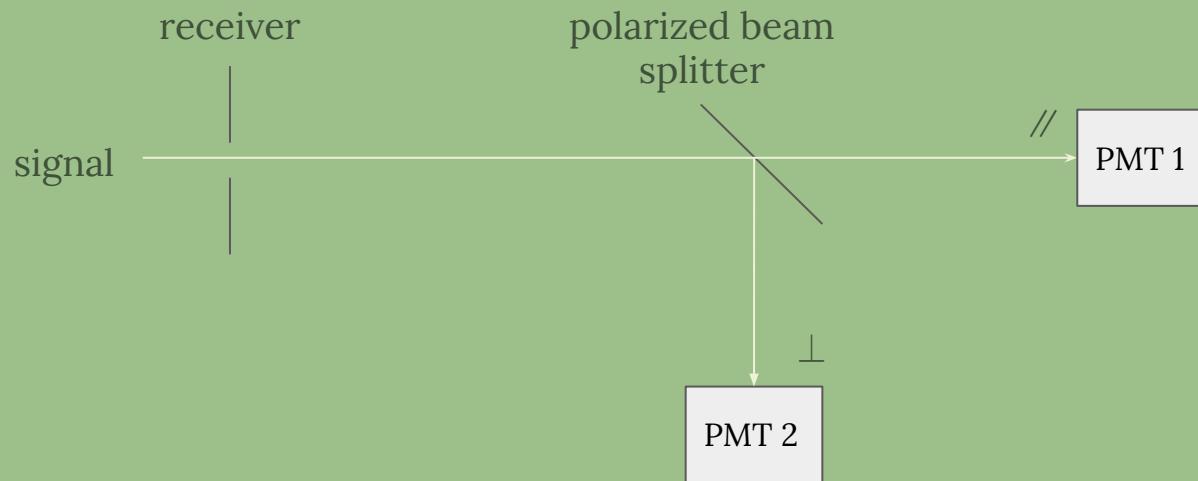
# Multi-Channel Polarized Ranging LiDAR

By Maya Greenstein

# Main Principle

Multiple detectors with different polarization properties

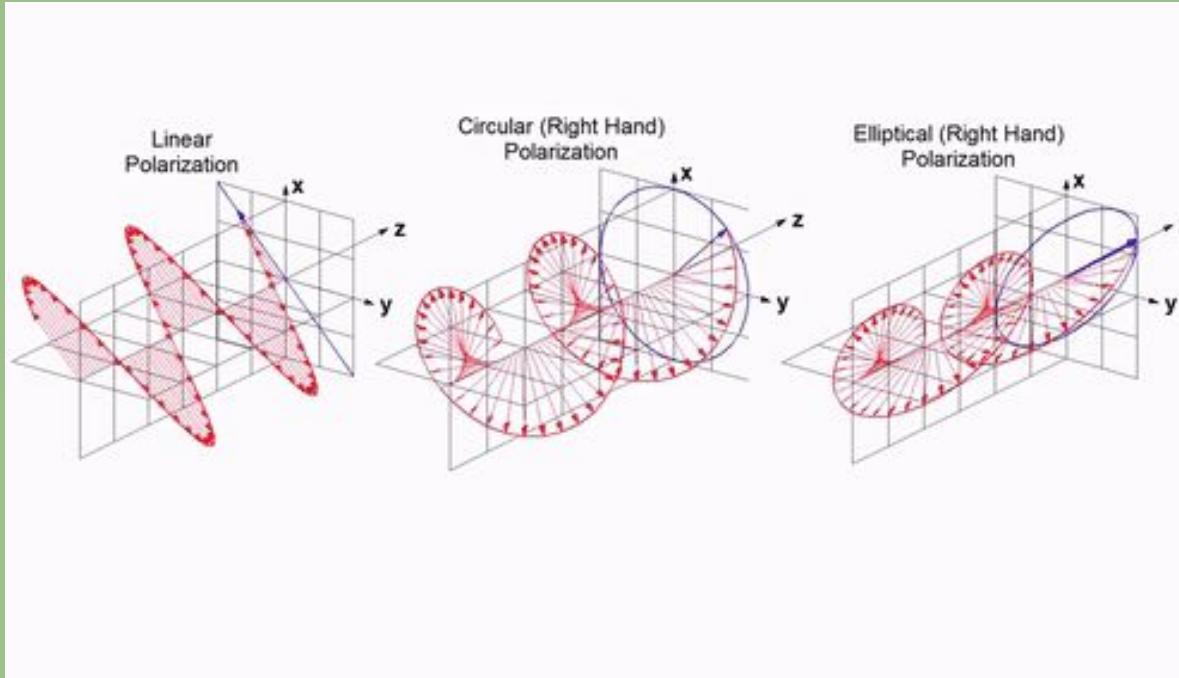
- Usually 2 - horizontal and vertical - but can be more



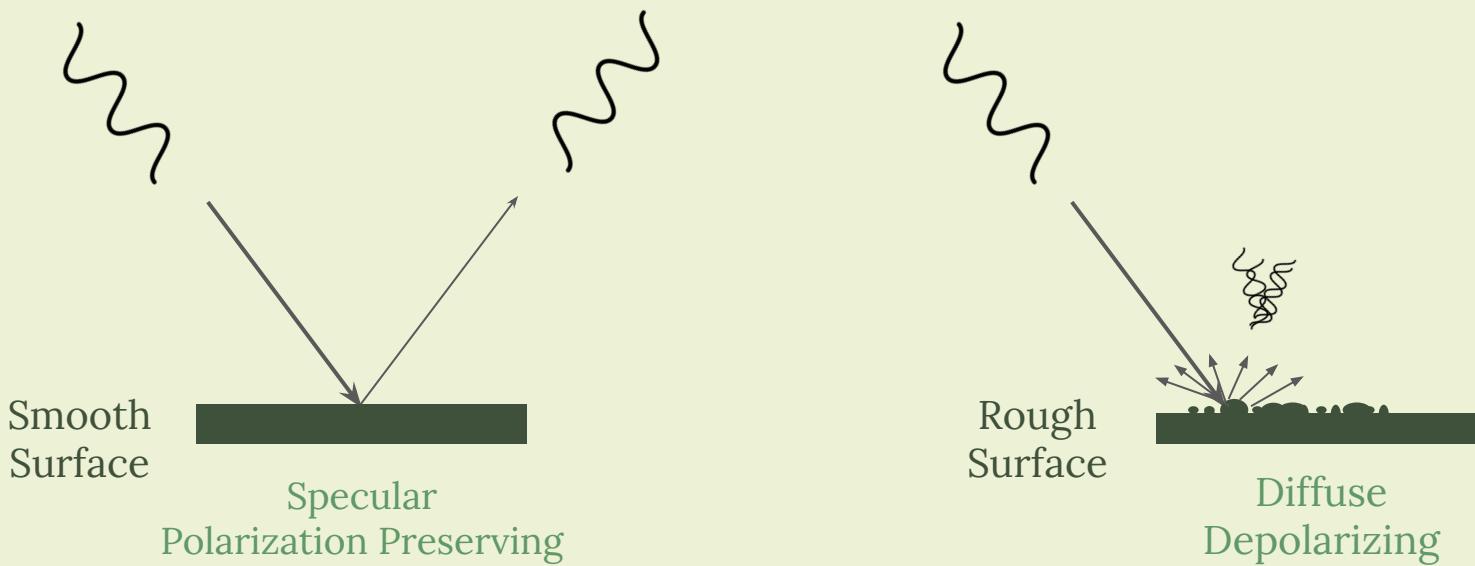
# Applications

- Surface mapping
- Bathymetry
- Vegetation measurement
- Clouds
- Aerosols
- Mars atmospheric research

# Polarization



# Surface Scattering



# Implications

If the lidar can detect the polarization of the returned signal, it can understand properties of the scatterer

**Bathymetry:** Water is an almost ideally smooth surface, will consistently maintain polarization of signal while the returns from the bottom will be depolarized

**Vegetation Detection:** When looking at a canopy of trees, can determine leaf type, and thus species by the intensities of the polarized returns

**Clouds:** Method of measuring the backscatter coefficient to understand the properties of the clouds

# Stokes Vectors

Using 4-element matrix, describe light polarization and intensity

$$\mathbf{S} = \begin{pmatrix} S_0 \\ S_1 \\ S_2 \\ S_3 \end{pmatrix} = \begin{pmatrix} \text{Intensity} \\ \text{Linear polarization} \\ 45^\circ \text{ linear polarization} \\ \text{Circular Polarization} \end{pmatrix}$$

Fully Polarized:  $S_0^2 = S_1^2 + S_2^2 + S_3^2$

Otherwise:  $S_0^2 > S_1^2 + S_2^2 + S_3^2$

# Mueller Matrices

$$\mathbf{S}' = \mathbf{M} \cdot \mathbf{S}$$

$$M = \begin{pmatrix} m_{00} & m_{01} & m_{02} & m_{03} \\ m_{10} & m_{11} & m_{12} & m_{13} \\ m_{20} & m_{21} & m_{22} & \\ m_{23} & & & \\ m_{30} & m_{31} & m_{32} & \\ m_{33} & & & \end{pmatrix}$$

$$S'_0 = m_{00}S_0 + m_{01}S_1 + m_{02}S_2 + m_{03}S_3$$

$$S'_1 = m_{10}S_0 + m_{11}S_1 + m_{12}S_2 + m_{13}S_3$$

$$S'_2 = m_{20}S_0 + m_{21}S_1 + m_{22}S_2 + m_{23}S_3$$

$$S'_3 = m_{30}S_0 + m_{31}S_1 + m_{32}S_2 + m_{33}S_3$$

# Stokes Vector Lidar Equation (SVLE)

$$\vec{S}_{Rx}(R) = M_{Rx} \left[ (G(R) \frac{A}{R^2} \Delta R) T_{atm}(\vec{k}_i, R) \times F(\vec{k}_i, \vec{k}_s, R) T_{atm}(\vec{k}_s, R) M_{Tx} \vec{S}_{Tx} + \vec{S}_B \right]$$

$M_{Tx}, M_{Rx}$	= Descriptions of transmitter and receivers	
$T_{atm}$	= Transmission	$G(R)$ = Overlap Function
$F$	= Scattering phase matrix	$A$ = Area of receiver
$S_{Tx}$	= Transmitted stokes vector	$R$ = Distance
$S_B$	= Stokes of background Counts	$\Delta R$ = Bin size
$k_i, k_s$	= Incident and scattered wave vectors	

# Mueller Matrices - Depolarization

Depolarization

$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1-d & 0 & 0 \\ 0 & 0 & d-1 & 0 \\ 0 & 0 & 0 & 2*d-1 \end{pmatrix}$$

Depolarization Ratio

$$\delta = \frac{I_{\perp}}{I_{\parallel}} \quad d = \frac{2 * \delta}{1 + \delta}$$

d is a measure of the likelihood of a scatterer to depolarize laser light

# Mueller Matrices - Transmission

Transmission

$$\begin{pmatrix} T & 0 & 0 & 0 \\ 0 & T & 0 & 0 \\ 0 & 0 & T & 0 \\ 0 & 0 & 0 & T \end{pmatrix}$$

$$\beta_{Rayleigh} = 2.938 \times 10^{-32} \frac{P(z)}{T(z)} * \frac{1}{\lambda^{4.0117}}$$

$$P(\theta) = .7629 \times (1 + .9324 \cos^2(\theta))$$

$$\beta_{Total}(\theta = \pi) = \frac{4\pi \beta_{Rayleigh}}{P(\theta)}$$

$$\alpha_{Total} = \alpha_{mol} = \beta_{Total}$$

$$T = e^{\int_0^R \alpha_{Total}(R) dR}$$

# Mueller Matrices - Water Surface

Fresnel Water Reflection

$$\begin{pmatrix} \alpha + \eta & \alpha - \eta & 0 & 0 \\ \alpha - \eta & \alpha + \eta & 0 & 0 \\ 0 & 0 & \gamma_{\text{Re}} & -\gamma_{\text{Im}} \\ 0 & 0 & \gamma_{\text{Im}} & \gamma_{\text{Re}} \end{pmatrix}$$

$$\alpha = .5 \left[ \frac{\tan(\theta_i - \theta_t)}{\tan(\theta_i + \theta_t)} \right]^2$$

$$\eta = .5 \left[ \frac{\sin(\theta_i - \theta_t)}{\sin(\theta_i + \theta_t)} \right]^2$$

$$\gamma_{\text{Re}} = -\frac{\tan(\theta_i - \theta_t) \sin(\theta_i - \theta_t)}{\tan(\theta_i + \theta_t) \sin(\theta_i + \theta_t)}$$

# Bathymetric Lidar Parameters

Downward Pointing

Low Energy: 5  $\mu\text{J}$

Mobile/drone-based

Wavelength: 532nm

Fixed wavelength, narrowband transmitter and receiver

Configuration: Coaxial and monostatic\*

Pulse Width: 500ps

Resolution: 25ps

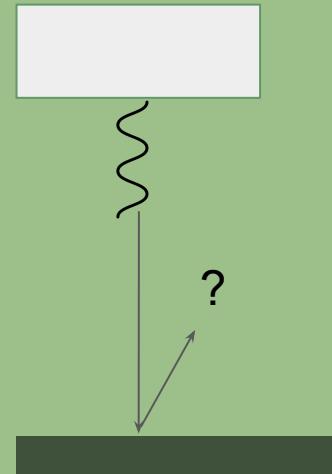
Repetition rate: 50 $\mu\text{s}$

Single Photon Counting

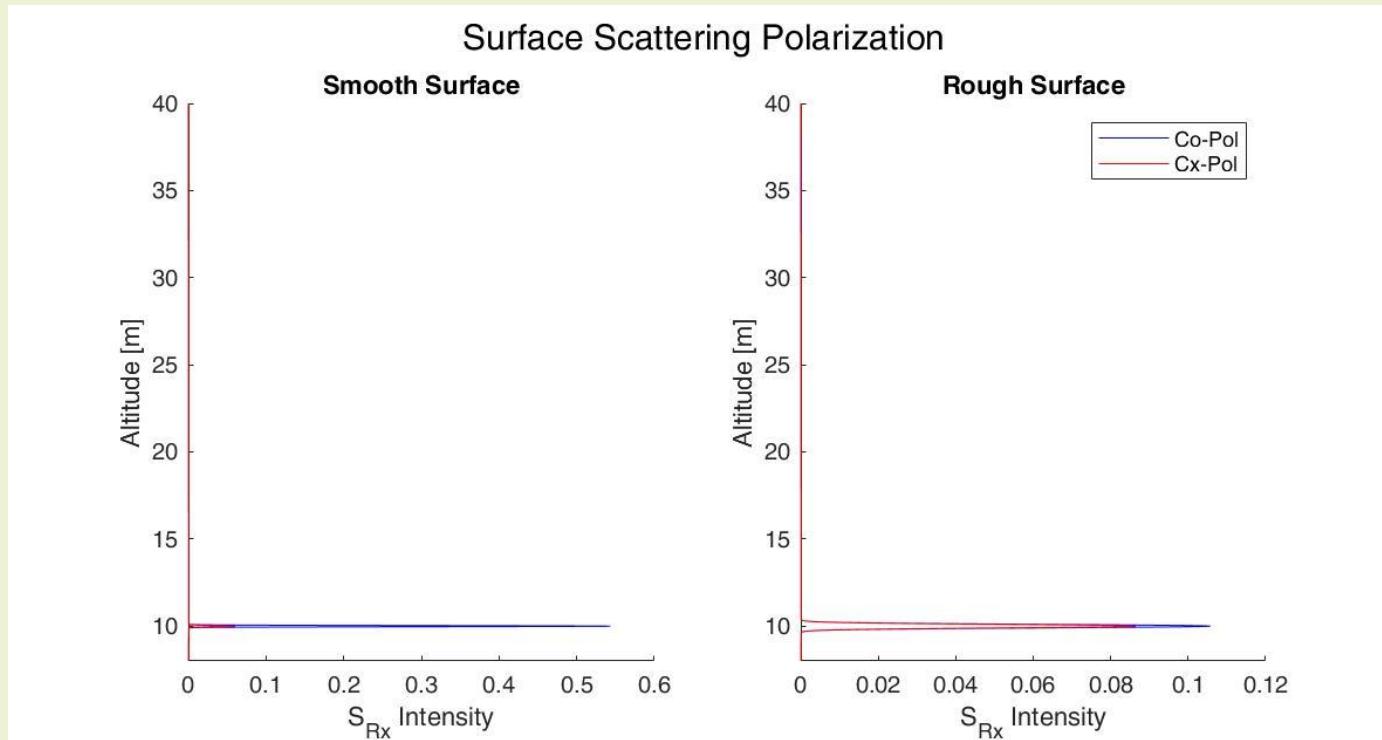
# Simulation

Simulate lidar scattering off of a rough, smooth and water surface to understand the properties of those returns

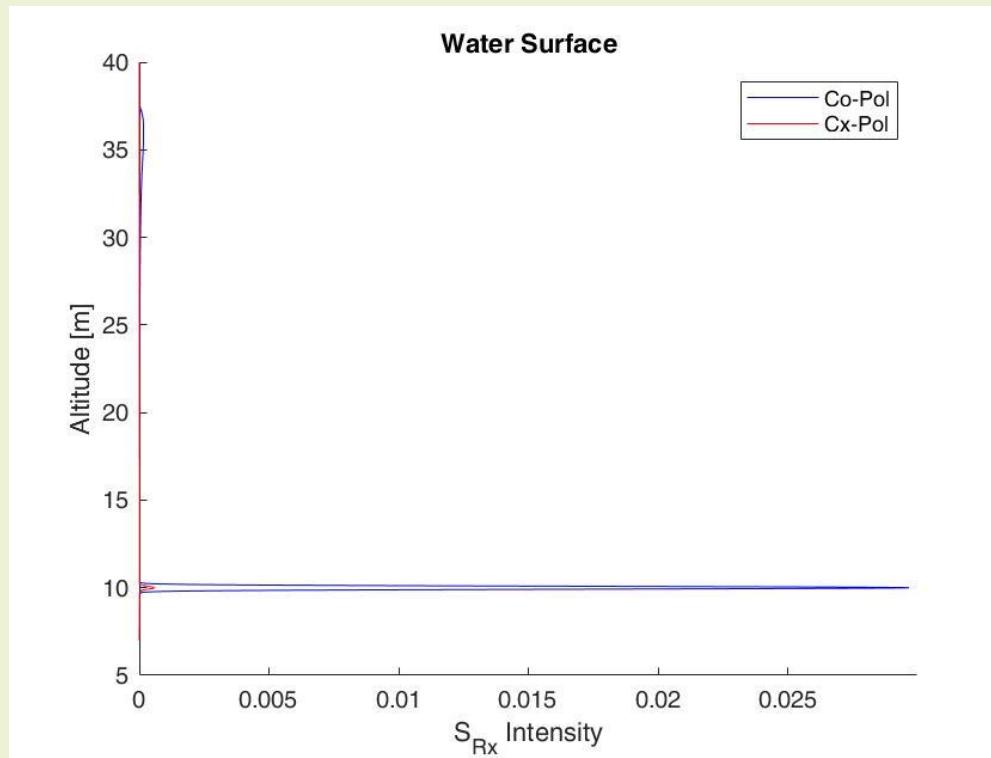
- For air propagation, only consider Rayleigh scattering
- Directly nadir pointing
- No background counts
- Estimate surface properties



# Simulation Results



# Simulation Results



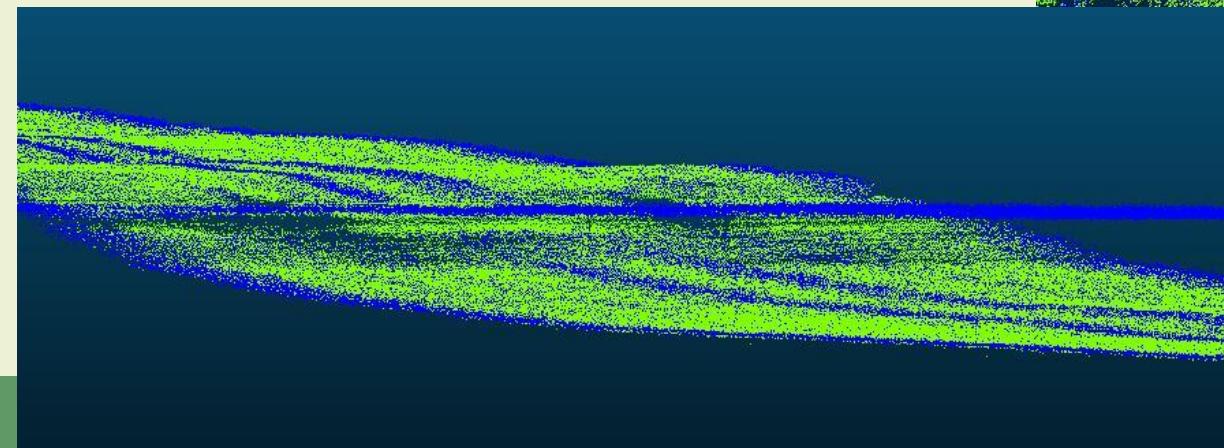
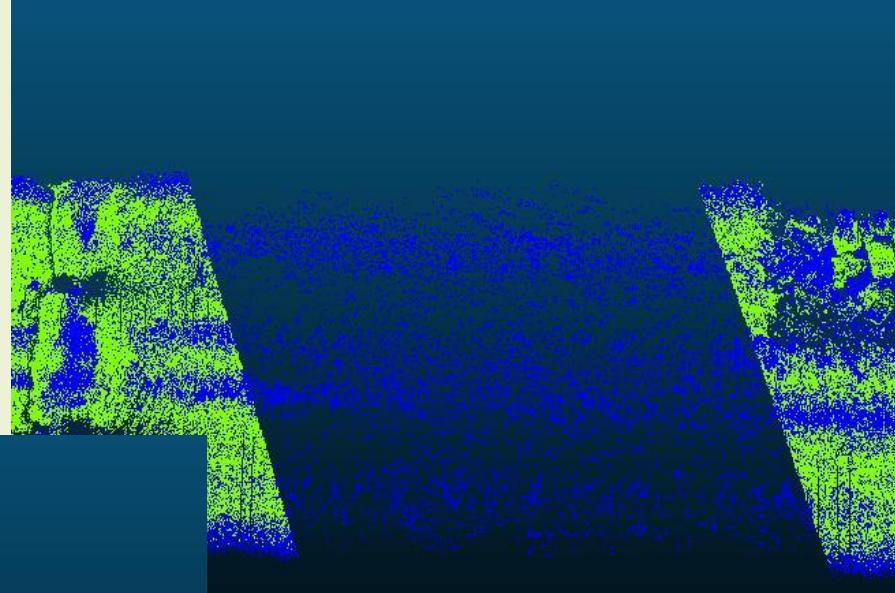
# Results

- Much more signal back from smooth vs rough surface
  - Specular vs lambertian scattering
- A lot less signal reflected by water surface
  - A lot of transmission through to water column
- Much higher co-polarized from smooth surface and water surface
  - Smooth surfaces polarization preserving
- More cx-polarized signal from rough surface
  - Depolarizing

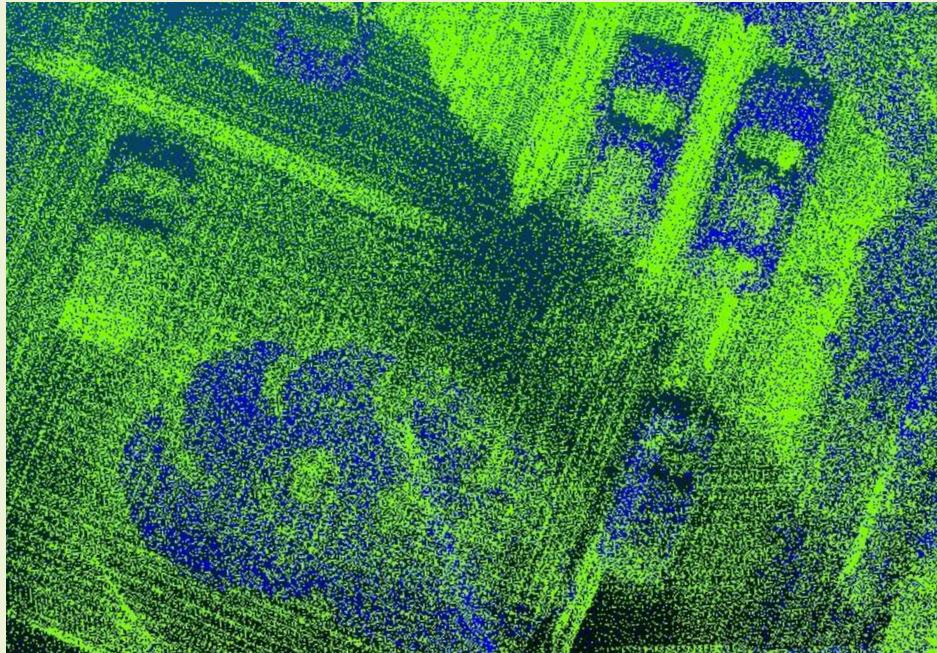
# Real Data

Co-Polarized

Cx-Polarized



# Real Data



# Bibliography

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# Questions?

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