

Week 5 - Assignment

Exercise :- Implement Vectorized Gradient Descent for Linear Regression problem

Sol:- Cost function

$$\min (J(\theta)) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x_i) - y_i)^2$$

goal is to minimize θ_0, θ_1 , $J(\theta)$

using Vectorized gradient Descent approach

$$h_{\theta} = \theta^T X$$

h_{θ} = hypothesis
 X = input feature vector

loop until converge

$$\theta_j = \theta_j - \frac{1}{m} \alpha \frac{\partial J(\theta)}{\partial \theta_j}$$

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Here $\frac{\partial J(\theta)}{\partial \theta_j}$ = gradient α = ~~the~~ learning rate

Advantage of vectorized approach is ,

- i) easy to debug
- ii) This approach decreases the time taken for execution of gradient descent

Algorithm

- 1) Set the weight step to zero: $\Delta w_i = 0$
- 2) For each record in the training data:
 - 2.1) Make a forward pass through the network, calculating the outputs $\hat{y} = f(\sum_i w_i x_i)$
 - 2.2) Calculate the error term for the output unit

$$\delta = (y - \hat{y}) * f'(\sum_i w_i x_i)$$
 - 2.3) Update the weight step $\Delta w_i = \Delta w_i + \delta x_i$
- 3) Update the weights $w_i = w_i + \frac{\eta}{n} \Delta w_i$. Where η is the learning rate and n is the number of records. Here we're averaging the weight steps to help reduce any large variations in the training data.
- 4) Repeat for e epochs