

Q Using big-M Method solve

$$\max(Z) = -x_1 - x_2 - x_3 \text{ s.t.}$$

$$x_1 - x_2 + 2x_3 = 2$$

$$-x_1 + 2x_2 - x_3 = 1$$

$$x_1, x_2, x_3 \geq 0$$

Sol  $\max(Z) = -x_1 - x_2 - x_3 - M \cdot x_4 - M \cdot x_5$   
s.t.,

$$x_1 - x_2 + 2x_3 + x_4 = 2$$

$$-x_1 + 2x_2 - x_3 + x_5 = 1$$

$$x_1, x_2, x_3, x_4, x_5 \geq 0$$

$$C_j \quad -1 \quad -1 \quad -1 \quad -M \quad -M \quad b/a_2$$

$C_B$	$B$	$X_B$	$b$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	min ratio	Operation
$-M$	$a_4$	$x_4$	2	1	-1	2	1	0	$\infty$	
$-M$	$a_5$	$x_5$	1	-1	2	-1	0	1	$1/2$	
	$Z_j - C_j$			1	$-M$	$-M$	0	0		
					$+1$	$+1$			$b/a_3$	
$-M$	$a_4$	$x_4$	$5/2$	$1/2$	0	$3/2$	1		$5/3$	$R_1' \leftarrow R_1 + R_2'$
$-1$	$a_2$	$x_2$	$1/2$	$-1/2$	1	$-1/2$	0		$\infty$	$R_2' \leftarrow R_2/2$
	$Z_j - C_j$			$-1/2 M$	0	$-1/2 M$	0			
				$-1/2$		$-1/2$				
$-1$	$a_3$	$x_3$	$5/3$	$1/3$	0	1				$R_1' \leftarrow R_1 \times 2/3$
$-1$	$a_2$	$x_2$	$4/3$	$-1/3$	1	0				$R_2' \leftarrow R_2 + 1/3 R_1'$
	$Z_j - C_j$		$-3$	1	0	0				

$\therefore$  all  $Z_j - C_j \geq 0$  optimal solution is obtained

$$Z = -3 \quad x_1 = 0 \quad x_2 = 0 \quad x_3 = 5/3$$