

		$D_1$	$D_2$	$D_3$	$a_i$
Q	$O_1$	5	1	8	12
Sol.	$O_2$	2	4	0	14
	$O_3$	3	6	7	4
	$b_j$	9	10	11	

i) North-West Corner Rule

	$D_1$	$D_2$	$D_3$	$a_i$
$O_1$	9   5	3   1	8	12 (3) (0)
$O_2$	2	7   4	7   0	14 (7) (0)
$O_3$	3	6	4   7	4 (0)
$b_j$	9 (0)	10 (7) (0)	11 (4)	

no of basic variables  $(m+n-1) = 3+3-1 = 5$

$$x_{11} = 9, x_{12} = 3, x_{22} = 7, x_{23} = 7, x_{33} = 4$$

$$\begin{aligned} \text{Cost of soln} &= 9 \times 5 + 3 \times 1 + 7 \times 4 + 7 \times 0 + 4 \times 7 \\ &= 45 + 3 + 28 + 28 \\ &= 104 \end{aligned}$$

ii) Vogel's Approximation Method (VAM)

	$D_1$	$D_2$	$D_3$	$a_i$
$O_1$	5	1	8	12 (4)
$O_2$	2	4	11   0	14 (2) (3)
$O_3$	3	6	7	4 (3)
$b_j$	9 (1)	10 (3)	11 (7)	

	D <sub>1</sub>	D <sub>2</sub>	
O <sub>1</sub>	5	10   1	12 (4) (2)
O <sub>2</sub>	2	4	3 (2)
O <sub>3</sub>	3	6	4 (3)
	9	10	
	(1)	(3)	
		(2)	

	D <sub>1</sub>	
O <sub>1</sub>	2   5	2 (0)
O <sub>2</sub>	3   2	3 (0)
O <sub>3</sub>	4   3	4 (0)
	9	
	(1)	

	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	q <sub>i</sub>
O <sub>1</sub>	2   5	10   1	8	12
O <sub>2</sub>	3   2	4	11   0	14
O <sub>3</sub>	4   3	6	7	4
b <sub>j</sub>	9	10	11	

$$\begin{aligned} \lambda_{11} &= 2 & \lambda_{12} &= 10 \\ \lambda_{21} &= 3 & \lambda_{23} &= 11 \\ \lambda_{31} &= 4 \end{aligned}$$

no of feasible basic variables =  $(m+n-1) = 5$

$$\begin{aligned} \text{Cost of soln} &= 2 \times 5 + 10 \times 1 + 3 \times 2 + 11 \times 0 + 4 \times 3 \\ &= 10 + 10 + 6 + 12 \\ &= 38 \end{aligned}$$