

MTO (Module-2)

①

Day Bulb Temp: The day bulb air temp. refers basically to the ambient air temperature. It is indicated by a thermometer not affected by the moisture of the air.

Wet Bulb Temp: The wet bulb temperature is the temperature of adiabatic saturation. This is the temperature indicated by a moistened thermometer bulb exposed to the air flow.

Dew Point Temp: It is the temperature at which first dew is formed and the temp. at which air becomes saturated

* At D. Point temp:

$$\overline{P}_A = \overline{P}_{Asat} \text{ & Rel. Humid} = 1$$

For any unsaturated air:

$$\Delta BT > WBT > \text{Dew. Pt. Temp.}$$

Absolute Humidity/Mass Humidity/Humidity: It is the ratio of Mass of Water Vapour per mass of ~~moist~~ air.

$$H_A = \frac{M_v}{M_a}$$

$$H_A = \frac{\overline{P}_A}{\overline{P}_T - \overline{P}_A} \times \frac{18}{29}$$

\overline{P}_A : → Partial Pressure of water-vapour in air-gas mixture

Molar Humidity:

$$H_M = \frac{\overline{P}_A}{\overline{P}_T - \overline{P}_A}$$

$$H_A = \frac{18}{29} \times H_M$$

Saturation Humidity:

$$H_S = \frac{\overline{P}_A^{\text{Sat}}}{\overline{P}_T - \overline{P}_A^{\text{Sat}}} \times \frac{18}{29}$$

Relative Humidity

$$RH = \frac{\overline{P}_A}{\overline{P}_{Asat}}$$

* For unsaturated air ($\overline{P}_A^{\text{Sat}} > \overline{P}_A$)

$$\% RH > \% S$$

* For saturated air ($\overline{P}_A = \overline{P}_{Asat}$)

$$\% S = \% RH = 100\%$$

Humid Heat: amount of heat energy required to raise the temperature of dry air accompanying vapour mixture by 1°C .

$$C_H = \{1.005\} + \{1.88Y'\}$$

\downarrow dry air \downarrow vap. mix.

unit $\rightarrow \text{kJ/kg dry air} \cdot \text{K}$

For Air-Water System

$$\ln P_A^v = 11.96481 - \frac{3984.923}{T - 39.724}$$

~~DBT~~ # Psychometric Chart

$$\text{DBT} = 50^{\circ}$$

$$\text{WBT} = 32.4^{\circ}$$

Find: Abs. Humid., Molar Humid., Percentage Humid., Rel. Humid., Dew Point, Humid Vol., Humid Heat, Enthalpy.

① Absol. Humid.: WBT \rightarrow 100% humidity \rightarrow Adiabatic Saturation cutting \rightarrow DBT \rightarrow Horizontal line to y-axis.

$$Y' = 0.024$$

② Molar Humid. $Y \Rightarrow Y = Y' \times \frac{18}{29} \Rightarrow Y = Y' \times \frac{29}{18} = 0.024 \times \frac{29}{18} \Rightarrow Y = 0.03866$

③ % Humidity \Rightarrow Extend the DBT and AS curve parallel to the Humid-% curves.

$$\text{P.M.} = 280/0$$

④ Rel. Humid. $= \frac{P_A}{P_{\text{sat}}} \times 100\% \Rightarrow \frac{Y}{P_A} \text{ as } P_A = 0.03866$

$$\text{Rel. Humid.} = 30.86\%$$

⑤ DPT \Rightarrow Extend the molar humid line to 100% humidity and drop it to 27.5°C.

$$= 27.5^{\circ}\text{C}$$

$$\text{Sat. Humid.} = \frac{P_{\text{sat}}}{P_{\text{atm}}} \times \frac{18}{29} = 0.0851$$

⑥ Humid Vol. \Rightarrow Extend DBT to Sp. Vol. Dry air curve and then join horizontally to humid vol. $\rightarrow 0.91$

\rightarrow Extend DBT to Sat. Humid Vol. Curve $\rightarrow 1.045$

$$\begin{array}{l} Y \\ 0 \\ 0.024 \\ 0.0851 \end{array} \quad \begin{array}{l} V_H \\ 0.91 \\ 0.2 \\ 1.045 \end{array}$$

$$\frac{0.0851 - 0}{0.0851 - 0.024} = \frac{1.045 - 0.91}{1.045 - n}$$

$$\rightarrow n = V_H = 0.948 \text{ m}^3/\text{kg-dry air}$$

⑦ Humid Heat: $C_H = \{1.005\} + \{1.88 \times 0.024\}$

$$C_H = 1.05 \frac{\text{kJ}}{\text{kg dry air} \cdot \text{K}}$$

⑧ Enthalpy

$$\begin{array}{l} Y \\ 0 \\ 0.024 \\ 0.0851 \end{array} \quad \begin{array}{l} H \\ 50 \\ n \\ 275 \end{array}$$

$$n = H = 112.5 \frac{\text{kJ}}{\text{kg dry air}}$$

COOLING TOWER

- Special type of heat exchanger in which the warm water & the air being are brought in direct contact for
- 6 **Evaporative cooling.**
- Provides a very good contact of air and water while keeping air pressure drop low.
- Enthalpy of air is lower than enthalpy of water.
- Sensible heat and latent heat transfer take place from water drop to surrounding air.

Factors that govern the operation of cooling tower:

- Dry bulb & wet bulb temperatures of air
- Temperature of warm water.
- Efficiency of contact between air & water in terms of volumetric mass transfer coefficient.
- Contact time between air & water.
- Air pressure drop
- Desired temp. of cooled water.

Atmospheric Towers

- It is a big rectangular chamber with two opposite lowered walls.
- Tower is packed with a suitable 'tower fill'.
- Atmospheric air enters the tower through lower denser by its own velocity.
- Direction and velocity of wind greatly influence its performance.

Natural Draft Towers

- Large reinforced concrete shell of hyperbolic shape.
- Natural flow of air occurs through the tower.

- Factors responsible for creating natural draft
- 1) rise in temp. & humidity of air in the column reduces its density
- 2) wind velocity at the tower bottom.

- # Why my hyperbolic shape
 - More packing materials can be placed at the bottom
 - The entering air gets smoothly directed towards the centre
 - Greater structural strength and stability

Mechanical Draft Towers

1) Forced Draft Towers: Has one or more fans located at the tower bottom to push air into tower.

Advantages:

- 1) It makes energy efficient than induced draft.
- 2) Less susceptible to vibrations as fans are installed near the ground.

Disadvantages:

- 1) Air flow through the packing may not be uniform.
- 2) Recirculation of warm and humid air back.
- 3) It is not popular except for small quantities.

1) Induced Draft Towers:

→ top of the tower.
 → cross flow

→ counter flow.

disadvantages:

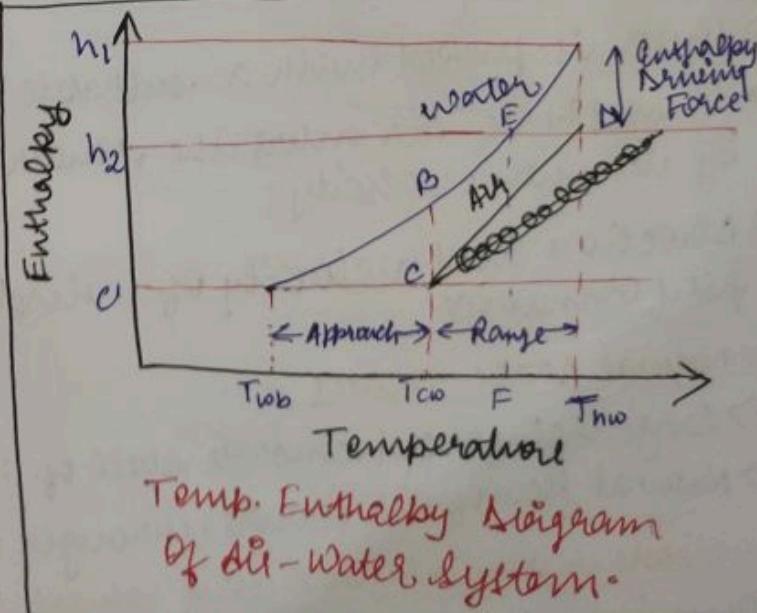
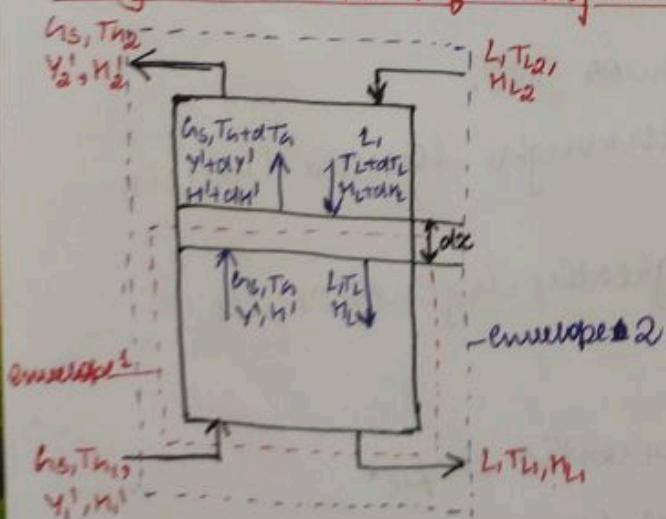
- 1) Relatively dry air contacts the coldest water at the bottom of the cooling tower.
- 2) Humid air is in contact with the warm water and hence maximum D.F. for both NTR & MT.

Advantages:

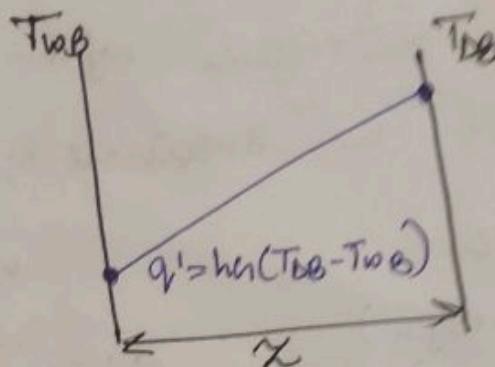
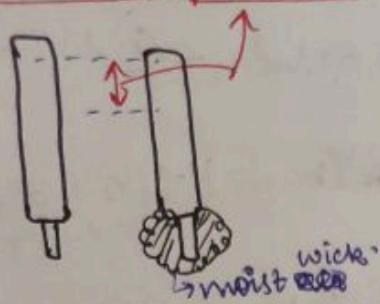
- 1) It consumes more horsepower.

* Cross-flow induced draft cooling tower requires less motor HP than countercurrent induced draft cooling towers.

Design Calculation of Cooling Tower



Wet-Bulb Depression



Enthalpy [H']

$$H' = \lambda_w Y^I + C_H [T_{dB} - T_0]$$

Latent heat Sensible heat.

$T_0 \rightarrow$ reference temp.

Humid volume (V_H)

$$V_H = \left(\frac{1}{28.97} + \frac{Y^I}{18.02} \right) \times 22.4 \times \left(\frac{T_0 + 273}{273} \right)$$

$\frac{m^3}{dry-air}$

$$\text{Heat flux, } q_v = h_v(T_b - T_w)$$

$$q_v = h_v(T_b - T_w) = \lambda_m K_m (Y_w^I - Y^I)$$

COOLING TOWER CONTINUES

Enthalpy balance over envelope 1.

$$L C_{wL} (T_L - T_{L1}) = h_s (H' - H'_1)$$

Enthalpy balance over envelope 2.

$$L C_{wL} (T_{L2} - T_{L1}) = h_s (H'_2 - H'_1)$$

$$\text{Q1} \quad T_{L2} = 45^\circ\text{C}, T_{L1} = 30^\circ\text{C}, \Delta BT = 21^\circ\text{C}, wBT = \frac{22}{6000} = 0.00367, L = 5500 \text{ kg/m}^2\text{h}^{22^\circ\text{C}} \text{ at } 6000 \text{ kg/m}^2\text{h}$$

$$Q_2 = h_s \times 1.4 \times 6000 \text{ min} \quad k' \bar{a} = 5500 \text{ kg/m}^2\text{-h} < (\Delta Y')$$

$$h_s = 1029 \times 6000 \text{ min} \quad k' \bar{a} = 5500 \text{ kg/m}^2\text{-h} < (\Delta Y')$$

$$h_s = 0.059 L^{0.51} C_s \quad \text{Assume } \eta = 1 \quad \ln P_A''(\text{bar}) = 11.9648 \frac{1 - 33.84 \cdot 9.72}{(T - 33.84 \cdot 9.72)}$$

$$T_{A1} = T_{DBT} = 31^\circ\text{C}$$

$$T_{wBT} = 22^\circ\text{C}$$

$$Y_1 = 0.012 \text{ (From Psych.)}$$

$$H_1' = [0.005 + 1.88 \times 0.012] (31 - 0) + 2500 Y_1' = 64.8 \text{ KJ/Kg dry air}$$

Change in enthalpy of water = $L \cdot C_{WL} \cdot \Delta t$
Change in enthalpy of Air = $C_s \cdot dH'$

slope of the tangent = $10.76 = \frac{L C_{WL}}{h_{s, \text{min}}}$

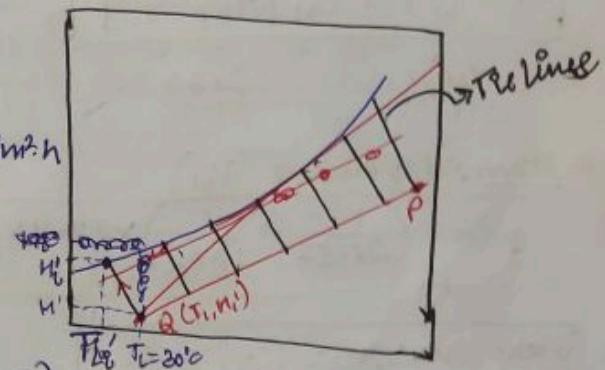
$$C_s = 1.4 h_{s, \text{min}} \quad h_{s, \text{min}} = 2325 \text{ kg/m}^2\text{h}$$

$$C_s = 3270 \text{ kg/m}^2\text{h}$$

$$L C_{WL} (T_{L2} - T_{L1}) = h (H_2 - H_1)$$

$$(6000)(4.187)(45 - 30) = 3270(H_2 - 64.8)$$

$$H_2 = 179.6 \text{ KJ/Kg}$$



* Locate the point P (T_{L2}, H_2) = ($45^\circ\text{C}, 179.6 \text{ KJ/Kg}$)

* Slope of Tie-lines = $-\frac{h_{s, \bar{a}}}{k' \bar{a}}$

T_{L1}	
H_1'	
T_{L2}	
H_2'	
$\frac{1}{H_2' - H_1'}$	

$$= -\frac{68,280 \text{ KJ/h.mB}}{6000} = -11.4$$

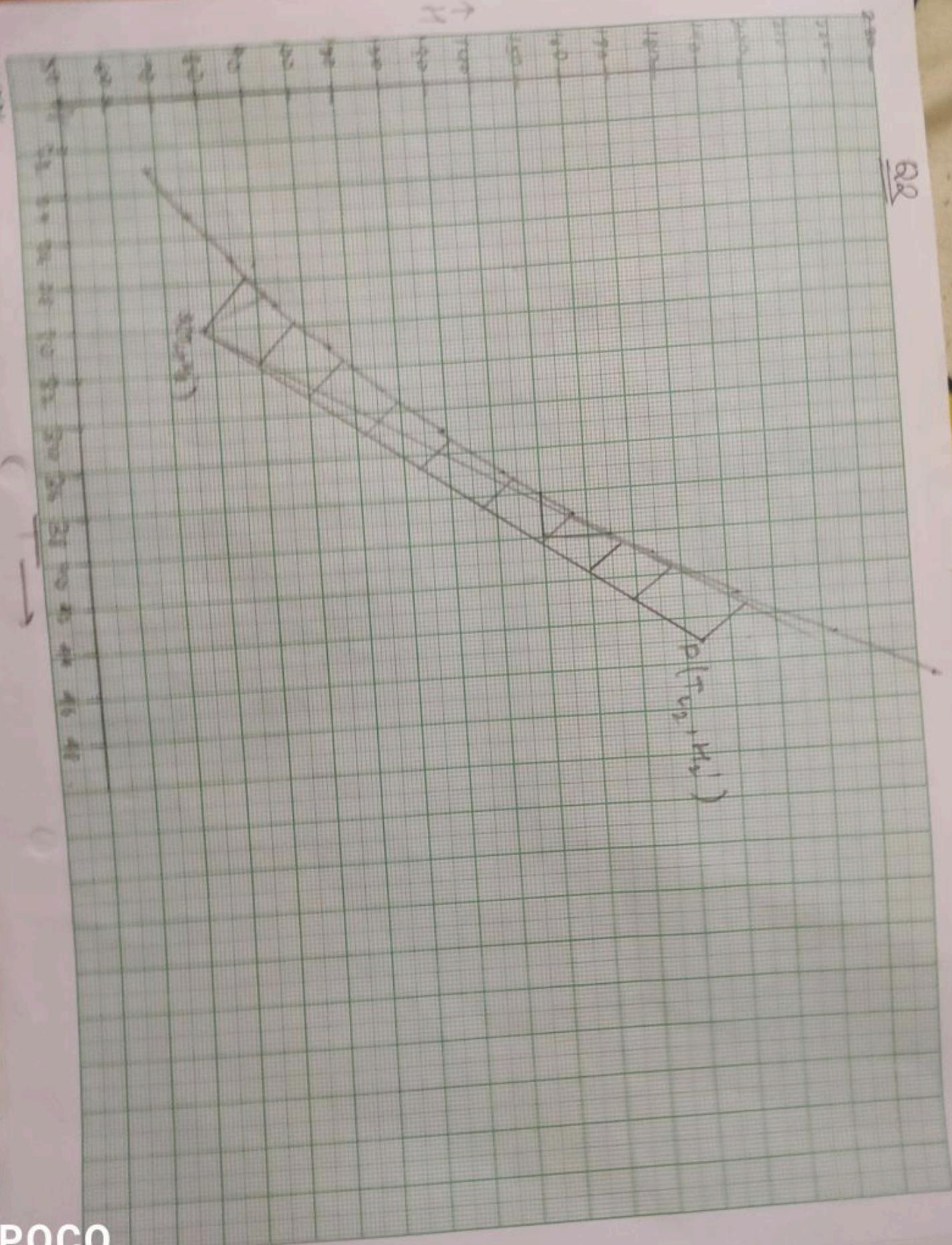
* $h_{s, \bar{a}} = \frac{h_s}{k' \bar{a}} = 0.545$

Area under the curve = $(H_2' - H_1') \times \text{Avg. } \left(\frac{1}{H_2' - H_1'} \right) \approx 6 \Rightarrow N_{BT}$

$$N_{BT} = 0.545$$

$$Z = N_{BT} \times N_{BT} = 3.68 \text{ m}$$

b) wB depression \rightarrow at bottom
wB depression = Air Temp. - wBT
= $31 - 22 = 9^\circ\text{C}$



Given: $T_{L2} = 45^\circ\text{C}$, $T_{L1} = 30^\circ\text{C}$, $T_{OB} = 30^\circ\text{C}$, $T_{iOB} = 25^\circ\text{C}$ (1)

$L = 5500 \text{ kg/m}^2\cdot\text{h}$, $C_s = 1.25 \text{ kJ/kg min}$, $K_y \bar{\alpha} = 5743.5 \text{ kg/m}^3\text{h} (\text{AY})$

$$h_i \bar{\alpha} = 0.059 L^{0.51} C_s$$

$$H_1' = 0.019, H_1 = [(1.005 + 1.88 \times 0.019) \times (30 - 0) + 2500 \times 0.019]$$
$$H_1' = 78.7 \text{ kJ/kg}$$

By graph slope = 8.78

$$\text{slope} = \frac{L \times C_w L}{C_s \text{min}} \Rightarrow C_s \text{min} = \frac{5500 \times 4.2}{8.78} = 2680$$

$$C_s = 1.25 \times 2680 = 3280 \text{ kg/m}^2\cdot\text{h}$$

$$L C_w L (T_{L2} - T_{L1}) = C_s (H_2' - H_1')$$

$$H_2' = 184 \text{ kJ/kg}$$

$$\text{slope of Tie Line} \rightarrow -\frac{h_i \bar{\alpha}}{K_y \bar{\alpha}} \approx$$

$$h_i \bar{\alpha} = 0.059 L^{0.51} C_s$$

$$= 15687.9 \text{ kcal/m}^3\text{ht}$$

$$\downarrow$$

$$= 15687.9 \times 4.18$$

$$= 65475 \text{ kJ/m}^3\text{ht}$$

$$\rightarrow \frac{-65475}{5743.5} \rightarrow \underline{\underline{-11.4}}$$

$$H_{tch} = \frac{C_s}{K_y \bar{\alpha}} = \frac{3280}{5743.5} = 0.57$$

From the graph we can get T_L , H_1' , T_{Li} , H_2' and $\frac{1}{(H_2' - H_1')}$

$$N_{tch} = (H_2' - H_1') \left[\text{slo} \text{ of } \frac{1}{(H_2' - H_1')} \right]$$

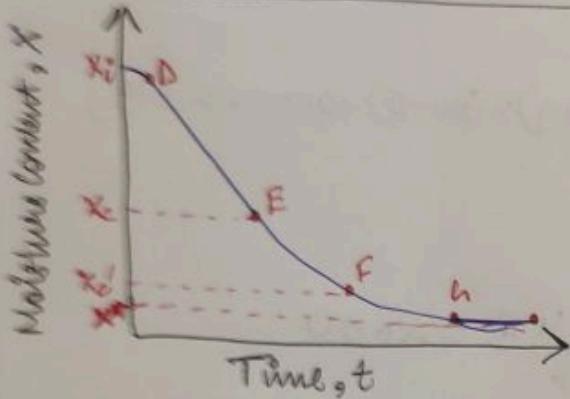
$$N_{tch} = 9.26$$

$$x = N_{tch} \times H_{tch} = 9.26 \times 0.57$$

$$\underline{\underline{x}} = \underline{\underline{5.28 \text{ m dm}}}$$

DRYING (UNISEMS)

$$t = t_0 + b_f = \frac{w_s(x_i - x_c)}{\alpha N_c} + \frac{w_s(x_c - x^*)}{\alpha N_c} \ln \left(\frac{x_c - x^*}{x_f - x^*} \right)$$



$X_i \rightarrow D$: Heating of solids & releasing of moisture

$D \rightarrow E$: constant rate period

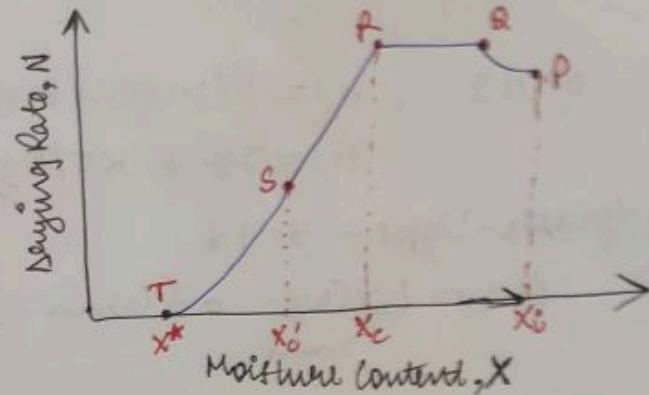
$$N_B = \frac{dx}{dt} = \text{const.}$$

$E \rightarrow F \rightarrow G \rightarrow h$: falling rate period $N \neq \text{const.}$, linear drop of moisture content.

G : The eq. moisture content (x^*) is reached at h , no further loss of moisture.

*** Read more from the book.

*** Practice Questions.



$P \rightarrow Q$: Solid gradually gets heated and the rate of drying increases

$Q \rightarrow R$: constant rate period $N = \text{const.}$

R : where the constant rate period terminates is called the critical moisture content, x_c .

$R \rightarrow S \& S \rightarrow T$: First & Second Falling rate periods respectively.