

	variable			class variable
articles	D	E	F	C
10	t	t	t	t
1	t	t	t	f
27	t	t	f	t
8	t	t	f	f
13	t	f	t	t
1	t	f	t	f
9	t	f	t	t
33	t	f	f	f
1	f	t	t	t
3	f	t	f	t
14	f	t	f	f
5	f	f	t	t
6	f	f	t	f
1	f	f	f	t
68	f	f	f	f

200 ← Total

N.B model Says

$$P(D, E, F, C) = P(C) \cdot P(D|C) \cdot P(E|C) \cdot P(F|C)$$

C	P(C)
t	$\frac{10+27+13+9+1+3+5+1}{200} = \frac{69}{200} = 0.345$
f	$\frac{1+8+1+33+14+6+68}{200} = \frac{131}{200} = 0.655$

table - 1

(1) Conditional Probability Tables (CPT's)

D	C	P(D C)
* *	* f	
N	Y	
N	N	



# Conditional probability tables (CPT's)

a)

D | C | P(D|C)

t	t	$\frac{10+27+13+9}{10+27+13+9+1+3+5+1} = \frac{59}{69} \approx 0.8550$
t	f	$\frac{1+8+1+33}{1+8+1+33+14+6+68} = \frac{43}{131} \approx 0.328$
f	t	$\frac{1+3+5+1}{10+27+13+9+1+3+5+1} = \frac{10}{69} \approx 0.145$
f	f	$\frac{14+6+8}{1+8+1+33+14+6+68} = \frac{88}{131} \approx 0.672$

table-2

E | C | P(E|C)

t	t	$\frac{10+27+1+3}{10+27+13+9+1+3+5+1} = \frac{41}{69} \approx 0.594$
t	f	$\frac{1+8+14}{1+8+1+33+14+6+68} = \frac{23}{131} \approx 0.1756$
f	t	$\frac{13+9+5+1}{10+27+13+9+1+3+5+1} = \frac{28}{69} \approx 0.406$
f	f	$\frac{1+8+3+6+68}{1+8+1+33+14+6+68} = \frac{108}{131} \approx 0.8244$

table-3

F | C | P(F|C)

t	t	$\frac{10+13+1+5}{10+27+13+9+1+3+5} = \frac{29}{69} \approx 0.420$
t	f	$\frac{1+1+6}{1+8+1+33+14+6+68} = \frac{8}{131} \approx 0.061$
f	t	$\frac{27+9+3+1}{10+27+13+9+1+3+5+1} = \frac{40}{69} \approx 0.58$
f	f	$\frac{8+33+14+68}{1+8+1+33+14+6+68} = \frac{123}{131} \approx 0.94$

table-4



$$b) P(C=t \mid D=f, E=t, F=t)$$

$$= P(C=t, D \neq t, E=t, F=t) \quad \text{--- (i)}$$

$$P(D=f, E=t, F=t) \text{ --- (ii)}$$

(i)  $\rightarrow$  Calculating Numerator

$$P(C=t, D=f, E=t, F=t) = P(C=t) \times P(D=f|C=t) \times P(E=t|C=t) \times P(F=t|C=t)$$

$$\begin{array}{ccccccc} & \text{from table 1} & & \text{from table 2} & & \text{from table 3} & & \text{from table 7} \\ & \downarrow & & \downarrow & & \downarrow & & \downarrow \\ 0.345 & \times & 0.145 & \times & 0.594 & \times & 0.420 \\ & & & & = & & 0.0125 \end{array}$$

(ii)  $\rightarrow$  calculating denominator

$$P(D=f; E=t, F=t) \\ = P(C=t, D=f, E=t, F=t)$$

f

$$P(C=f, D=f, E=t, F=t)$$

by definition  
is equal to  
summation  
of all probability  
of  $C$  where  $C = t$   
and  $C = f$   
in this case.



$$= 0.0125 + P(C=f, D=f, E=t, F=t)$$

$$P(C=f) \times P(D=f|C=f) \times P(E=t|C=f) \times P(F=t|C=f)$$

$$0.655 \times 0.672 \times 0.1756 \times 0.061$$

$$\approx 0.0047$$

$$\Rightarrow 0.0125 + 0.0047$$

$$= 0.0172$$

this conditional probability represent  
Conditioning computational  
task in probabilistic modelling

$$\left[ \begin{array}{l} P(C=t|D=f, E=t, F=t) \approx \frac{0.0125}{0.0172} \text{ --- i)} \\ \text{Conditioning} \approx 0.728 \text{ --- ii)} \end{array} \right]$$

c) from above calculations we can  
see that for partial configuration  
 $P(D=f, E=t, F=t)$  gives higher value  
for when class variable  $C=t$   
which is 0.0125. So, most likely  
value is  $C=\text{true}$  for partial  
configuration  $P(D=f, E=t, F=t)$



d)  $P(C=t | D=f, E=t, F=t)$  for joint distribution mode

what is the probability that article is financial given  $D=f, E=t, F=t$ ;

so from table we can see is

equal to  $\frac{1}{200}$  ie 100%.

another way to calculate is we can find

marginal probability of  $P(C=t, D=f, E=t, F=t)$   
marginal prob  $P(D=f, E=t, F=t)$

$$= \frac{1}{1} = 1$$

c)  $P(C=t | D=f, E=t, F=t)$  - for fully independent model:

$$= P(C=t | D=f) \cdot P(C=t | E=t) \cdot P(C=t | F=t)$$

table 2                      table 3                      table 4

$$= 0.145 \times \frac{0.400}{0.594} \times 0.420$$

~~0.00097~~

$\approx 0.0362$