

A304

NOTE *
representing space
character as ' '

phrase = 'to be or not to be'
alphabet = 26
space char = 1 } $\#|V| = 27$

① No smoothing probabilities.

x	$\#x$	$P(x)$
t	= 3	3/18
e	= 4	4/18
b	= 2	2/18
c	= 2	2/18
o	= 1	1/18
n	= 1	1/18
space character ← ' '	= 5	5/18
*	0 = 0	0
anything else		

② probabilities after Laplace smoothing

Laplace smoothing is to add '1' to all events in beginning.

x	$\#(x)$	$p(x)$
t	= 4	4/45
o	= 5	5/45
b	= 3	3/45
c	= 3	3/45
r	= 2	2/45
n	= 2	2/45
'	= 6	6/45
a(x)	= 1	1/45
b	= 1	1/45
c	= 1	1/45
'	= 1	1/45
'	= 1	1/45
'	= 1	1/45
'	= 1	1/45
2	= 1	1/45
27 + 18 = 45		1

if we have a word, we can find its probability by Laplace smoothing. This is the way to find the probability of a word in a language.

③ Witten-Bell Smoothing

so, let us say we start train this sequence and for every new character we mark it.

~~(((, bcc, ccc, n b t c c c c~~

* t * o * ' * b * c ' ' o * r ' * n o t ' ' t o ' ' b c

so whenever we see new characters we mark those.

X	# X	P(X)
*	= 7	7/25
t	= 3	3/25
o	= 4	4/25
b	= 2	2/25
c	= 2	2/25
r	= 1	1/25
n	= 1	1/25
'	= 5	5/25
25		

$P(*) = 7/25$ } so, this is probability of all unseen events

$$P(\star) = \frac{7}{25}$$

a
b
c
⋮
z

So, probability of each unseen event will be

$$\frac{\frac{7}{25}}{(27-7)} = \frac{7/25}{20} = \frac{7}{25 \times 20}$$

$$P(\text{unseen}) = \frac{7}{500}$$

probability of single unseen event.