

Main code (210010039.py)

Importing required packages (numpy and matplotlib.pyplot)

Initialising the required constants (α , Δt , Δx), and required arrays (spatial grid and temperature grid)

Calling different functions to compute the Temperature variation across the grid using different methods

FTCS function

It takes the constants and initial temperature grid as parameters and using the explicit FTCS method updates the temperature grid for future timesteps

crank_nicolson function

It takes the constants and initial temperature grid as parameters and using the implicit Crank-Nicolson method updates the temperature grid for future timesteps. The equation is solved using `numpy.linalg.solve()` function to solve the basic $Ax=b$ equation

exact function

It takes the constants as parameters and using the given series expansion for the exact solution it returns the Temperature grid for various timesteps

The main code gets the returned values from the three functions to obtain T_{FTCS} , T_{CN} and T_{exact} . These are then used to calculate error values $error_{FTCS}$ and $error_{CN}$

PLOTS are now made using these Temperature matrices at the required times and the error is also plotted for the two methods. An unstable timestep is also taken to verify the stability conditions of the FTCS method