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% TIME SHIFTING PROPERTY OF FOURIER COEFFICIENTS
% Sinusoidal wave and Line spectrum of coefficients
% As proven in class, shifting a function results in coefficients of
  all
%   same magnitude but shifted phases. know  $f(t) \Rightarrow C_n$ 
%    $f(t-t_0) = \exp(-j(n)(\omega_0)(t_0)) * C_n$  so same plot as before but
  shift
%   so time shift property is confirmed

T = 2;                                % PERIOD
wo = pi;

M = 200;                              % DISCRETIZATION OF THE TIME AXIS
deltT = T/M;
t = [0:deltT:T-deltT];               % TIME AXIS

% Modified  $x(t)$  to  $x(t-t_0)$  so signal delayed by  $t_0$  seconds as seen
x = abs(cos(pi*(t-0.2)));             % COMPUTE SAMPLES OF  $x(t-0.2)$  ON GRID

N = 20;                              % COMPUTE FS COEFFICIENTS  $C(0) \dots C(N)$ 
J = sqrt(-1);
c = zeros(1,N+1);                   % COMPUTE  $C(k)$  WITH A SUM
c(1) = 1/T * deltT * sum(x);

for k = 1:N
    c(k+1) = 1/T * deltT * sum(x .* exp(-J*k*wo*[0:M-1]*deltT));
    % note: because Matlab indexing begins with 1 instead of 0,
    % it is necessary to add 1 to the index. c(k+1) means 'c(k)!'
end

% NOTE:  $C(-k) = \text{conj}(C(k))$  because  $x(t)$  is a REAL signal.
% Therefore only compute  $c(k)$  for  $k \geq 0$ .

figure(1)                            % PLOT THE LINE SPECTRUM
stem([0:N]/T,abs(c),'.')             % (THE LINE SPECTRUM IS A PLOT OF  $C(k)$ )
xlabel('Hertz')
ylabel('|C(k)|')
title('LINE SPECTRUM')

t = [0:500]/500*T;                  % PLOT TWO PERIODS OF THE SIGNAL
y = c(1) * ones(size(t));           % SYNTHESIZED FROM THE NUMERICALLY
for k = 1:N                          % OBTAINED FS COEFFICIENTS
    y = y + c(k+1)*exp(J*k*wo*t) + conj(c(k+1))*exp(-J*k*wo*t);
end
figure(2)
plot(t,real(y));

figure(3);
clf;
subplot(2,2,[1 2]);
%Time Shifted graph
plot(t, real(y));

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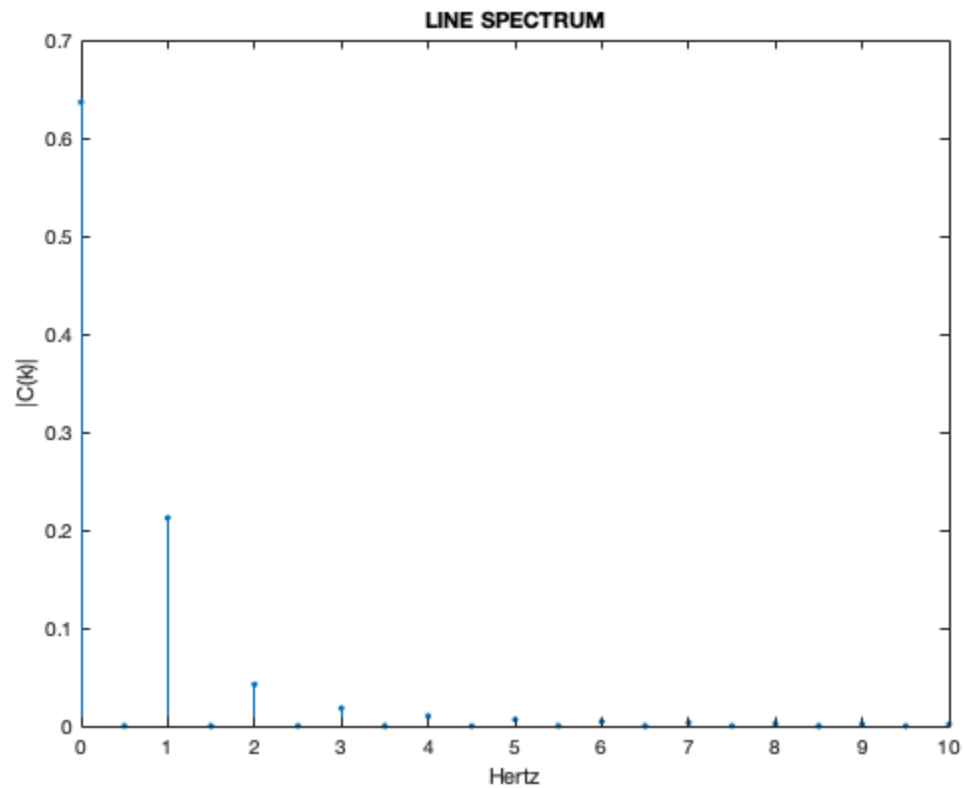
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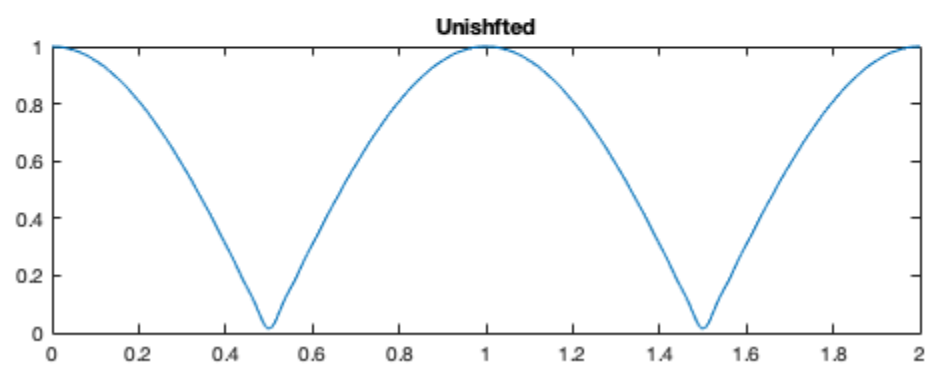
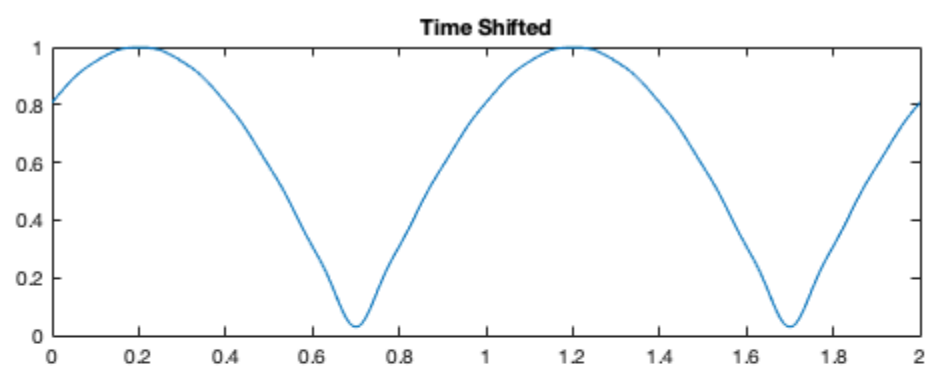
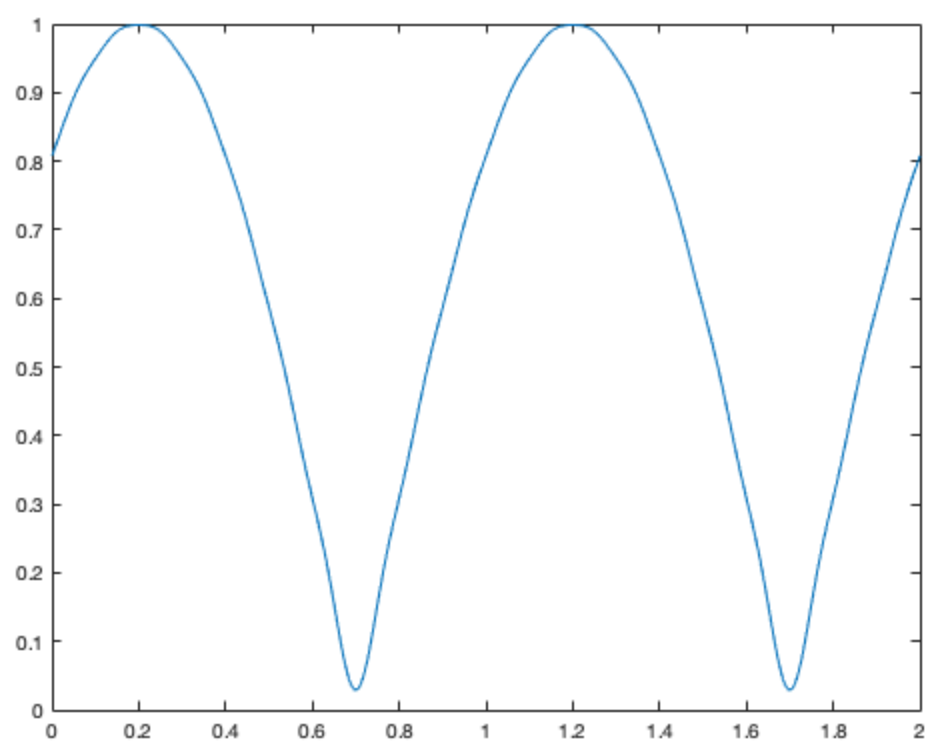
title("Time Shifted");
subplot(2,2,[3 4]);

% Old Unshifted Graph
T = 1;
wo = 2*pi/T;
M = 200;
delT = T/M;
t = [0:delT:T-delT];
x = abs(cos(pi*t));
N = 20;
J = sqrt(-1);
c = zeros(1,N+1);
c(1) = 1/T * delT * sum(x);
for k = 1:N
    c(k+1) = 1/T * delT * sum(x .* exp(-J*k*wo*[0:M-1]*delT));
end
t = [0:500]/500*2*T;
y = c(1) * ones(size(t));
for k = 1:N
    y = y + c(k+1)*exp(J*k*wo*t) + conj(c(k+1))*exp(-J*k*wo*t);
end

plot(t,real(y));
title("Unishfted");

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