

# PREDICTION

To predict a continuous value rather than a categorical label.

The prediction of continuous values can be modeled by statistical techniques of Regression.

## (I) Linear Regression.

Data are modeled using a straight line.

## (II) <sup>Bivariate</sup> ~~Bivariate~~ Linear Regression.

It models a random ~~value~~ variable  $(Y)$  (called a response var.) as a linear function of another random variable  $(X)$

i.e.  $Y = \alpha + \beta X$  (called a predictor var.)

variance of  $Y$  is assumed to be constant

$\alpha$  is the regression coefficient specifying the  $Y$  intercept

$\beta$  is the regression coefficient specifying slope of the line.

Coefficients can be solved by the method of

Least Square, which minimised the error b/w the actual data and estimate of the line.

Samples or data points are  $(x_1, y_1), (x_2, y_2), \dots, (x_s, y_s)$

$$\beta = \frac{\sum_{i=1}^s (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^s (x_i - \bar{x})^2}$$

$$\alpha = \bar{y} - \beta \bar{x}$$



→ There are marks on steps as well

Develop a model to predict the salary of college graduates with 10 years of work experience,  
predict the salary of a college graduate -

	years-experience)	Salary			
	X	Y (salary) \$1000s	$(X - \bar{X})$	$(X - \bar{X})^2$	$(Y - \bar{Y})$
1	3	30			
2	8	57			
3	9	64			
4	13	72			
5	3	36			
6	6	43			
7	11	59			
8	21	90			
9	1	20			
10	16	83			

$$\sum X = 91$$

$$\sum Y = 554$$

$$n = 10$$

predict where  $X = 10$

$$\bar{X} = 9.1$$

$$\bar{Y} = 55.4$$

$$B = \frac{(3 - 9.1)(30 - 55.4)}{(3 - 9.1)^2} + \dots$$

$$B = 3.5374$$

$$\alpha = \bar{Y} - B\bar{X}$$

$$\alpha = 55.4 - 3.5374(9.1)$$

$$= 23.2096$$

Ans) So the salary of  
a college graduate  
with 10 years of  
experience is  
\$ 58.58 K

$$Y = \alpha + B X \quad \text{For } X = 10$$

$$Y = 23.2096 + 3.5374(10)$$

$$Y = 58.58$$