

Formula Sheet EE2M11

MaybE_Tree

2022-09-07

Principal Argument	$-\pi < \theta \leq \pi$	
Triangle Inequality	$\begin{cases} z_1 \pm z_2 \leq z_1 + z_2 \\ z_1 \pm z_2 \geq z_1 - z_2 \end{cases}$	
Limits to Infinity	$\begin{cases} \lim_{z \rightarrow z_0} f(z) = \infty \iff \lim_{z \rightarrow z_0} \frac{1}{f(z)} = 0 \\ \lim_{z \rightarrow \infty} f(z) = L \iff \lim_{z \rightarrow 0} f\left(\frac{1}{z}\right) = L \end{cases}$	<i>L must be finite, maybe??</i>
Cauchy-Riemann	<div>CR1</div> <div> $\begin{matrix} u & v \\ x & \frac{du}{dx} \quad \frac{dv}{dx} \\ y & \frac{du}{dy} \quad \frac{dv}{dy} \end{matrix}$ </div>	<i>For</i> $f(x, y) = u(x + y) + iv(x, y)$
Harmonic Check	$\frac{\delta^2 u}{\delta x^2} + \frac{\delta^2 u}{\delta y^2} = 0 \implies \frac{\iint_D f(z)}{\text{Area}(D)} = f(z_c)$	<i>For</i> $f(x, y) = u(x + y) + iv(x, y)$ <i>Around a circular domain D with centerpointn z_c</i>
Exponential Function	$e^z = e^x(\cos y + i \sin y)$	
Trig Functions	$\begin{cases} \sin z = \frac{1}{2i}(e^{iz} - e^{-iz}) \\ \cos z = \frac{1}{2}(e^{iz} + e^{-iz}) \end{cases}$	<i>All the familiar identities apply, but range is no longer ± 1 .</i>
Cauchy's Formula	$\frac{2\pi i}{n!} f^n(z_0) = \oint_C \frac{f(z)}{(z - z_0)^{n+1}}$	<i>For $n = 0, 1, 2, \dots$</i>
Parama	$\int_C f(z) dz = \int_a^b f(z(t)) z'(t) dt$	

	0	$1/6\pi$	$1/4\pi$	$1/3\pi$	$1/2\pi$
sin	0	$1/2$	$\sqrt{2}/2$	$\sqrt{3}/2$	1
cos	1	$\sqrt{3}/2$	$\sqrt{2}/2$	$1/2$	0
tan	0	$\sqrt{3}/3$	1	$\sqrt{3}$???