Declaration d ::= v :: τ = e Syntax Node h ::= e | τ Term Variable v ::= x, y, z Type variable a ::= a, b, c Type constant t ::= Int | Bool Expression e ::= v | λ x.e | e1 e2 | let d in e2 Type τ ::= a | t | τ 1 \rightarrow τ 2

B. Prolog Syntax

C. Auxiliary Functions

$$gen(h, T) \rightarrow T$$
 $fresh() \rightarrow V$ $gen_decl(d) \rightarrow P$ $var(v \mid a) \rightarrow V$ $atom(t) \rightarrow A$

D. Constraints Generation Rules

$$\frac{gen(x, V), x \in \Gamma, \ var(x) \Rightarrow V_x}{unify(V, V_x)} [VAR1]$$

$$\frac{gen(x, V), x \notin \Gamma, \ x_1, x_2, \dots \in \Gamma, \ var(x_1) \Rightarrow V_1, \ var(x_2) \Rightarrow V_2, \dots}{x(V, [V_1, V_2, \dots | _])} [VAR2]$$

$$\frac{gen(Ax.e, V), \ var(x) \Rightarrow V_x, \ fresh \Rightarrow V_e}{unify(V, \ fun(V_x, V_e)), \ \Gamma, \ x \vdash gen(e, V_e)} [ABS]$$

$$\frac{gen(e_1 \ e_2, V), \ fresh \Rightarrow V_1, \ fresh \Rightarrow V_2}{unify(fun(V_2, V), V_1), \ \Gamma \vdash gen(e_1, V_1), \ gen(e_2, V_2)} [APP]$$

$$\frac{gen(t, V), \ atom(t) \Rightarrow A}{unify(A, V)} [TYPE-CON] \frac{gen(a, V), \ var(a) \Rightarrow V_a}{unify(V, V_a)} [TYPE-VAR]$$

$$\frac{gen(\tau_1 \rightarrow \tau_2, V)}{unify(V, \ fun(V_1, V_2), \ \Gamma \vdash gen(\tau_1, V_1), \ gen(\tau_2, V_2)} [TYPE-FUN]$$

$$\frac{gen(let x :: \tau = e1 \ in \ e2, V), \ fresh \Rightarrow V_1, \ fresh \Rightarrow V_2, \ \Gamma \vdash gen_decl(x :: \tau = e_1)}{unify(T, V_2), \ \Gamma \vdash gen(e_2, V_2)} [LET]$$

E. Predicates Generation Rules

$$\frac{\text{gen_decl}(x :: \tau = e), x_1, x_2, \dots \in \Gamma, \text{var}(x_1) \Rightarrow V_1, \text{var}(x_2) \Rightarrow V_2, \dots}{x(V, [V_1, V_2, \dots |_]) \leftarrow \Gamma \vdash \text{gen}(e, V), \text{gen}(\tau, V).} \text{[DECL]}$$