
MODULE *skeenAlgorithm*

EXTENDS *TLC*, *Naturals*, *FiniteSets*

CONSTANTS *PROCESS_NUMBER*

VARIABLES *stamped*, *received*, *LC*, *deliverable*, *pc*, *sentM*, *sentTS*, *sequenceNumber*

vars $\triangleq \langle \textit{stamped}, \textit{received}, \textit{LC}, \textit{deliverable}, \textit{pc}, \textit{sentM}, \textit{sentTS}, \textit{sequenceNumber} \rangle$

PC STATES:

BCAST = *p* send *m* to destinations *WAITING* = *p* waiting

ASSUME *PROCESS_NUMBER* \in *Nat*

Processes $\triangleq 1 \dots \textit{PROCESS_NUMBER}$

Message $\triangleq \{ \text{"MESSAGE"} \}$

Max(*S*) \triangleq CHOOSE *t* \in *S* : $\forall s \in S : t[3] \geq s[3]$

Init \triangleq

$\wedge \textit{stamped} = [i \in \textit{Processes} \mapsto \{\}]$
 $\wedge \textit{received} = [i \in \textit{Processes} \mapsto \{\}]$
 $\wedge \textit{deliverable} = [i \in \textit{Processes} \mapsto \{\}]$
 $\wedge \textit{pc} \in [\textit{Processes} \rightarrow \{ \text{"BCAST"}, "" \}]$
 $\wedge \textit{LC} \in [\textit{Processes} \rightarrow \{0\}]$
 $\wedge \textit{sentM} = \{\}$
 $\wedge \textit{sentTS} = \{\}$
 $\wedge \textit{sequenceNumber} = 0$

UponBCAST(*self*) \triangleq

$\wedge \textit{pc}[\textit{self}] = \text{"BCAST"}$
 $\wedge \textit{sentM}' = \textit{sentM} \cup \{ \langle \textit{self}, \text{"MESSAGE"} \rangle \}$
 $\wedge \textit{pc}' = [\textit{pc} \text{ EXCEPT } ![\textit{self}] = \text{"PENDING"}]$
 $\wedge \text{UNCHANGED } \langle \textit{stamped}, \textit{deliverable}, \textit{sentTS}, \textit{LC}, \textit{received}, \textit{sequenceNumber} \rangle$

ReceivedMessage(*self*) \triangleq

$\wedge \textit{sentM} \neq \{\}$
 $\wedge \exists \textit{msg} \in \textit{sentM} :$
 $\wedge \textit{received}' = [\textit{received} \text{ EXCEPT } ![\textit{self}] = \textit{received}[\textit{self}] \cup \{ \langle \textit{msg}[1], \textit{msg}[2], \textit{LC}[\textit{self}] \rangle \}]$
 $\wedge \textit{sentTS}' = \textit{sentTS} \cup \{ \langle \textit{self}, \text{"MESSAGE"}, \textit{LC}[\textit{self}], \textit{msg}[1] \rangle \}$
 $\wedge \textit{LC}' = [\textit{LC} \text{ EXCEPT } ![\textit{self}] = \textit{LC}[\textit{self}] + 1]$
 $\wedge \text{UNCHANGED } \langle \textit{stamped}, \textit{pc}, \textit{deliverable}, \textit{sentM}, \textit{LC}, \textit{sequenceNumber} \rangle$

ReceivedStampppedMessage(*self*) \triangleq

$\wedge \textit{pc}[\textit{self}] = \text{"PENDING"} \wedge \textit{PROCESS_NUMBER} = \text{Cardinality}(\{x \in \textit{sentTS} : x[4] = \textit{self}\})$
 $\wedge \text{Print}(\text{Max}(\{x \in \textit{sentTS} : x[4] = \textit{self}\}), \text{TRUE})$
 $\wedge \textit{sentTS}' = \textit{sentTS} \setminus \{x \in \textit{sentTS} : x[4] = \textit{self}\}$

$$\begin{aligned}
& \wedge sequenceNumber' = Max(\{x \in sentTS : x[4] = self\})[3] \\
& \wedge stamped' = [stamped \text{ EXCEPT } ![self] = stamped[self] \cup \{\langle self, \text{"MESSAGE"}, sequenceNumber \rangle\}] \\
& \wedge \forall mi \in \{x \in stamped[self] : x[4] = self\} : \\
& \quad \wedge \forall mii \in received[self] : mi[3] < mii[3] \\
& \quad \wedge deliverable' = [deliverable \text{ EXCEPT } ![self] = deliverable[self] \cup \{mi\}] \\
& \wedge \forall msg \in deliverable[self] : \wedge sentM' = sentM \cup \{\langle self, \text{"MESSAGE"} \rangle\} \\
& \wedge stamped' = [stamped \text{ EXCEPT } ![self] = stamped[self] \setminus deliverable[self]] \\
& \wedge \text{UNCHANGED } \langle stamped, sentM, pc, LC, deliverable, received \rangle \\
\\
Step(self) & \triangleq \\
& \quad \vee UpponBCAST(self) \\
& \quad \vee ReceivedMessage(self) \\
& \quad \vee ReceivedStampppedMessage(self) \\
& \quad \vee \text{UNCHANGED } \langle stamped, received, pc, sentM, sentTS, LC, deliverable, sequenceNumber \rangle \\
\\
Next & \triangleq (\exists p \in Processes : Step(p)) \\
\\
Spec & \triangleq Init \wedge \Box [Next]_{vars}
\end{aligned}$$
