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MODULE *skeenAlgorithm*

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EXTENDS *TLC*, *Naturals*, *FiniteSets*, *Sequences*

CONSTANTS *NPROCESS*, *MESSAGES*

VARIABLES *pc*, *sent*, *pending*, *received*, *lc*, *messages*

ASSUME (*NPROCESS*  $\in$  *Nat*)  $\wedge$  (*MESSAGES*  $\neq$   $\{\}$ )

ASSUME (*NPROCESS*  $> 1$ )

vars  $\triangleq \langle pc, sent, pending, received, lc, messages \rangle$

*Processes*  $\triangleq 1 \dots NPROCESS$

*Init*  $\triangleq$

$\wedge messages = [i \in Processes \mapsto MESSAGES]$   
 $\wedge pending = [i \in Processes \mapsto \{\}]$   
 $\wedge received = [i \in Processes \mapsto \{\}]$   
 $\wedge sent = [i \in Processes \mapsto [bcast \mapsto \{\}, ts \mapsto \{\}, sn \mapsto \{\}]]$   
 $\wedge pc \in [Processes \rightarrow \{\text{"BCAST"}, \text{" "}\}]$   
 $\wedge lc = [i \in Processes \mapsto 0]$

*UpponBCAST*(*self*)  $\triangleq$

$\wedge (pc[self] = \text{"BCAST"}) \wedge (messages[self] \neq \{\})$   
 $\wedge \text{LET } currentMessage \triangleq \text{CHOOSE } x \in messages[self] : \text{TRUE}$   
 IN  $\wedge sent' = [i \in Processes \mapsto [sent[self] \text{ EXCEPT } !.bcast = sent[self].bcast \cup \{[source \mapsto self, m$   
 $\wedge messages' = [messages \text{ EXCEPT } ![self] = messages[self] \setminus \{currentMessage\}]$   
 $\wedge \text{UNCHANGED } \langle lc, pending, pc, received \rangle$

*ReceivedBCAST*(*self*)  $\triangleq$

$\wedge pc[self] \neq \text{"SN"}$   
 $\wedge \exists m \in sent[self].bcast :$   
 $\wedge m \notin pending[self]$   
 $\wedge pending' = [pending \text{ EXCEPT } ![self] = pending[self] \cup \{m\}]$   
 $\wedge sent' = [sent \text{ EXCEPT } ![m.source].ts = sent[m.source].ts \cup \{[source \mapsto self, message \mapsto m.message$   
 $\wedge lc' = [lc \text{ EXCEPT } ![self] = lc[self] + 1]$   
 $\wedge \text{UNCHANGED } \langle received, pc, messages \rangle$

*MaxTSAllProcess*(*S*)  $\triangleq \text{CHOOSE } t \in S : \forall s \in S : s.ts \leq t.ts$

*ReceivedTS*(*self*)  $\triangleq$

$\wedge pc[self] \neq \text{"SN"}$   
 $\wedge \text{LET } msgs \triangleq sent[self].ts$   
 IN  $\wedge \text{Cardinality}(msgs) = NPROCESS$   
 $\wedge \text{LET } maxTS \triangleq \text{MaxTSAllProcess}(msgs).ts$   
 IN  $\wedge \exists m \in msgs :$   
 $\wedge [source \mapsto self, message \mapsto m.message, ts \mapsto maxTS] \notin sent[self].sn$

$$\begin{aligned}
& \wedge sent' = [i \in Processes \mapsto [sent[self] \text{ EXCEPT } !.sn = sent[self].sn \cup \{[source \mapsto \\
& \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"SN"}] \\
& \wedge \text{UNCHANGED } \langle pending, received, lc, messages \rangle
\end{aligned}$$

$$\begin{aligned}
& \text{FIX RECEIVED} \\
Accept(self) & \triangleq \\
& \wedge (Cardinality(MESSAGES) = Cardinality(sent[self].sn)) \\
& \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"AC"}] \\
& \wedge received' = [received \text{ EXCEPT } ![self] = sent[self].sn] \\
& \wedge \text{UNCHANGED } \langle sent, pending, lc, messages \rangle
\end{aligned}$$

$$\begin{aligned}
Steps(self) & \triangleq \\
& \vee UpponBCAST(self) \\
& \vee ReceivedBCAST(self) \\
& \vee ReceivedTS(self) \\
& \vee Accept(self) \\
& \vee \text{UNCHANGED } vars
\end{aligned}$$

$$Next \triangleq (\exists self \in Processes : Steps(self))$$

$$Fairness \triangleq WF_{vars}(Next)$$

$$Spec \triangleq Init \wedge \Box[Next]_{vars}$$

$$\begin{aligned}
TypeOK & \triangleq \\
& \wedge pc \in [Processes \rightarrow \{\text{"BCAST"}, \text{"SN"}, \text{"AC"}, \text{" "}\}]
\end{aligned}$$

Properties

$$Agreement \triangleq \Box((\forall self \in Processes : pc[self] = \text{"AC"}) \Rightarrow \Diamond(\exists self \in Processes : pc[self] = \text{"AC"}))$$

$$GetMessage \triangleq \text{CHOOSE } m \in MESSAGES : \text{TRUE}$$

$$Validity \triangleq WF_{-}(\langle \forall p \in Processes : \langle p, GetMessage \rangle \in deliveryBuffer[p] \rangle)$$

$$Integrity \triangleq ()$$

$$TotalOrder \triangleq ()$$