Difference Equations. (first-order.)

$$a_0y(n) + a_1y(n-i) = b_0 \times (n) + b_1 \times (n-i)$$
 $n \in \mathbb{Z}$
 $x(n) \rightarrow f$
 $y(n) \rightarrow f$
 y

Se cond-order System.

$$y(n) = b_0 x(n) + b_1 x(n-1) + b_2 x(n-2)$$

- $a_1 y(n-1) - a_2 y(n-2)$.

$$|-|(2)| = \frac{|a_1 + b_1 + b_2 + b_2$$

$$= \frac{b_0 z^2 + b_1 z + b_2}{z^2 + a_1 z + a_2} = \frac{b_0 (z - z_1)(z - z_2)}{(z - p_1)(z - p_2)}$$

$$P_{i} = re^{j\omega_{i}}, \quad P_{z} = re^{-j\omega_{i}}$$

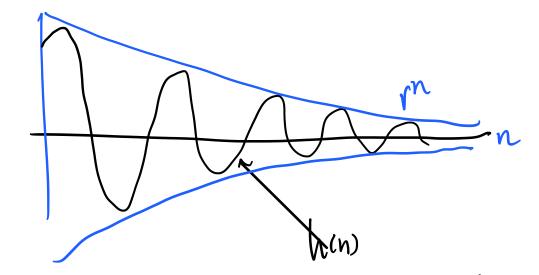
u : step fon.

C, is determined via partial frac. expansion.

C, = Rejo

$$h(n) = \left[R e^{j\theta} (e^{j\omega_1})^n + R e^{-j\theta} (e^{-j\omega_1})^n \right] u(n)$$

$$= R r^n \left[e^{j(\theta + \omega_1 n)} + e^{-j(\theta + \omega_1 n)} \right] u(n)$$



pole radics and angle (w.) determis the behavior of the imp resp.

$$H(z) = \frac{1}{1 + a_1 z^1 + a_2 z^2} = \frac{z^2}{z^2 + a_1 z + a_2}$$

$$=\frac{z^2}{(z-re^{j\omega_i})(z-re^{j\omega_i})}$$

$$\rightarrow 2^2 - 3(re^{j\omega_1} + re^{-j\omega_1}) + r^2e^{-j\omega_1}e^{j\omega_1}$$

$$\rightarrow$$
 7^2 - 72 rcos(w_1) + r^2

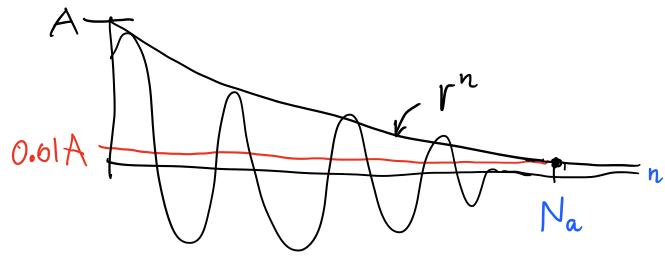
$$= 7^2 + a_1 + a_2$$

$$= 2^{2} + a_{1} + a_{2}$$

$$a_{1} = -2 \operatorname{r} \cos(\omega_{1}) \qquad a_{2} = \int^{2}$$

$$a = [a0 \ a1 \ a2]$$

 $a = [1 \ -2 \ r \ cos(om1) \ r^2]$



Q: How to set r so that Na has a poresribed value?

"Given Na, how should we set r?"

$$V^{Na} = 0.01 \qquad \Gamma = (0.01)^{1/Na}$$

$$\log r^{Na} = \log 0.01$$

$$N_{a} \log r = \log 0.01$$

$$N_{a} = \frac{\log 0.01}{\log r}$$