

# Business Analytics WS 2021 Exam

Business Analytics (IN2028) (Technische Universität München)







#### Compliance to the code of conduct

I hereby assure that I solve and submit this exam myself under my own name by only using the allowed tools listed below.

Signature or full name if no pen input available

## **Business Analytics: Endterm Exam**

Exam: IN2028 / Endterm Date: Wednesday 17<sup>th</sup> February, 2021

**Examiner:** Prof. Dr. Martin Bichler Time: 08:00 - 09:30

### Working instructions

- This exam consists of 22 pages with a total of 6 problems.
- The total amount of achievable credits in this exam is 90 credits.
- Allowed resources: open book.
- Subproblems marked by \* can be solved without results of previous subproblems.
- · Answers are only accepted if the solution approach is documented. Give a reason for each answer unless explicitly stated otherwise in the respective subproblem.
- · Do not write in red or green colors.
- · Any intermediate or final numbers in your calculations may be rounded to four (4) digits.

Exam empty







## Problem 1 Regression Analysis (15 credits)

You collected the following data about n = 73 different locations in Germany for a representative winter day in 2020:

Variable	Range	Explanation
snowfall	{0,1}	occurrence of snowfall
temperature	$\mathbb{R}$	air temperature [°C]
humidity	$\mathbb{R}_{\geq 0}$	absolute humidity [g/m³]
speed	$\mathbb{R}_{>0}^-$	wind speed [km/h]
direction	$\{\overline{N}$ orth, East, South, West $\}$	wind direction

You would like to model *snowfall* by applying a logistic regression.

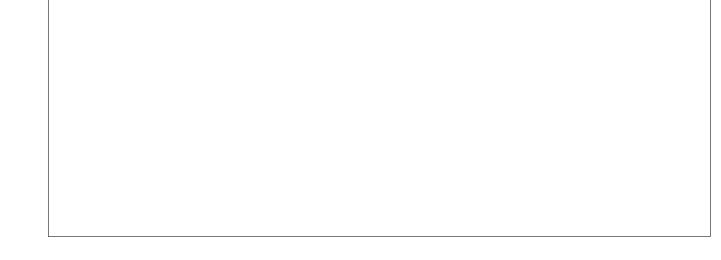
0	
1	
2	

- a)\* Briefly describe the data set:
  - 1. Name the dependent and independent variables.
  - 2. What scale of measurement does the variable *direction* belong to? How would you process the variable *direction* for the regression?

<del></del>		

0		
1	Н	Ш
_	Н	
2		

b)\* You decide to remove the variable *direction* since you consider it too unspecific. The remaining variables serve as an input to the logistic regression. Provide a formula to compute the likelihood function. The formula should include the variable names.









You apply a logistic regression and obtain the following output:

Residual	s
i toolaaa	•

Min	1Q	Median	3Q	Max
-0.86769	-0.28210	-0.02866	0.31464	0.65301

#### Coefficients:

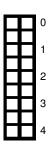
	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-0.977291	0.229796	-4.253	6.51e-05	***
temperature	-0.019453	0.009514	-2.045	0.0447	*
humidity	0.086000	0.014033	6.128	4.85e-08	***
speed	-0.006464	0.006168	-1.048	0.2983	

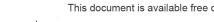
Signif. codes: 0 '\*\*\* 0.001 '\*\* 0.01 '\* 0.05 '. 0.1 ' 1

Null deviance: 15.7534 on 72 degrees of freedom Residual deviance: 9.6931 on 69 degrees of freedom

#### c)\* Interpret the estimated model:

- 1. Which variables are statistically significant at 5%? Explain your reasoning.
- 2. Interpret the *intercept* and the coefficient for *humidity*. Refer to the odds and provide necessary calculation steps.

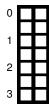












d)\* The McFadden R² for this model is 0.130623. Interpret this value. Explain the meaning of the McFadden R²

and how it differs conceptually from the R<sup>2</sup> measure for OLS regression.

You are advised to include air pressure as another covariate. Introducing the variable pressure, your regression yields the following results:

Residuals:

Min	1Q	Median	3Q	Max
-0.87087	-0.28837	-0.03777	0.31686	0.66502

Coefficients:

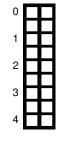
	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-0.991148	0.239284	-4.142	9.72e-05	***
temperature	-0.019600	0.009602	-2.041	0.0451	*
humidity	0.069450	0.074152	0.937	0.3523	
speed	-0.006407	0.006216	-1.031	0.3063	
pressure	0.017353	0.076327	0.227	0.8208	

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Null deviance: 15.7534 on 72 degrees of freedom Residual deviance: 9.6857 on 69 degrees of freedom

The new McFadden R<sup>2</sup> is 0.132009.

- e)\* Analyze these results:
  - 1. Examine the significance and the McFadden R<sup>2</sup>. What is the impact of adding the variable *pressure*?
  - 2. Explain these results. Which Gauss-Markov property is affected and how can you test for it?





## Problem 2 Data Preparation (10 credits)

You have obtained a dataset with metadata about 2,731 videos uploaded to a popular streaming platform. Some videos get featured on the platform's main page which usually helps video creators to reach a much wider audience. Based on your available data, you want to use a general linear model in R, i.e. a logistic regression, and perform statistical inference to determine the main drivers behind the platform's decision whether or not to feature a video.

While looking at the data, you realize that there are several data preparation steps you will need to undertake before you can run your model. Below, you are given three resources: (A) a short description of the variables in your data, (C) a summary of each column's distribution, as well as (B) the correlation between the numerical variables.

**Resource A** Your dataset has the following columns (see table below for types and distributions):

- 1. video\_id: A unique identifier of each video.
- 2. views: The number of views the video has received on the platform.
- 3. rating: The star-rating (from 1 star '\*' to 5 stars '\*\*\*\*\*').
- 4. earnings: earnings in US\$ that were paid out to the video creator as part of a revenue-sharing agreement with the platform.
- 5. **account gender**: the gender of the video creator
- 6. **account age**: the age (in years) of the video creator
- 7. sentiment english: A score between 0.0 (very negative comments) and 1.0 (very positive comments) that describes the sentiment of user comments posted below the video in English language.
- 8. sentiment other: A score between 0.0 (very negative comments) and 1.0 (very positive comments) that describes the sentiment of user comments posted below the video in languages other than English.
- 9. **featured**: Whether or not the video was featured on the home page or not.

#### **Resource B** The *correlation matrix* between numerical features is given below:

	views	earnings a	account_age	sentiment_english	sentiment_other
views	1.00000000	0.7658272	1 NA	0.01824006	0.01940797
earnings	0.76582721	1.0000000	0 NA	0.01947576	0.02048991
account_age	NA	NA	. 1	NA	NA
sentiment_english	0.01824006	0.0194757	6 NA	1.00000000	0.99860600
sentiment_other	0.01940797	0.0204899	1 NA	0.99860600	1.00000000



Page empty







### Resource C Summary of each variable's distribution

No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Valid	Missing
1	video_id [character]	1. 00Etx6TK 2. 016AmFYV 3. 01nrJJBC 4. 025OtRki 5. 02Kf4xNZ 6. 02VPhDIb 7. 03Xe0Uza 8. 06PdjMvm 9. 07yFfne3 10. 082cBmZJ [ 2721 others ]	1 ( 0.0%) 1 ( 0.0%) 2721 (99.6%)		2731 (100%)	0 (0%)
2	views [numeric]	Mean (sd): 9300.9 (28084) min < med < max: 26 < 2824 < 799669 IQR (CV): 7080 (3)	2351 distinct values		2731 (100%)	0 (0%)
3	rating [character]	1. * 2. ** 3. *** 4. **** 5. ****	543 (19.9%) 538 (19.7%) 533 (19.5%) 561 (20.5%) 556 (20.4%)		2731 (100%)	0 (0%)
4	earnings [numeric]	Mean (sd): 194.3 (679.2) min < med < max: 0 < 39.7 < 19567 IQR (CV): 147.5 (3.5)	2230 distinct values		2731 (100%)	0 (0%)
5	account_gender [character]	1. F 2. M	1236 (51.8%) 1152 (48.2%)		2388 (87.44%)	343 (12.56%)
6	account_age [integer]	Mean (sd): 40.9 (13.2) min < med < max: 18 < 41 < 64 IQR (CV): 23 (0.3)	47 distinct values		2388 (87.44%)	343 (12.56%)
7	sentiment_english [numeric]	Mean (sd): 0.5 (0.3) min < med < max: 0 < 0.5 < 1 IQR (CV): 0.5 (0.6)	2731 distinct values		273 <b>1</b> (100%)	0 (0%)
8	sentiment_other [numeric]	Mean (sd): 0.5 (0.3) min < med < max: 0 < 0.5 < 1 IQR (CV): 0.5 (0.5)	2731 distinct values		2731 (100%)	0 (0%)
9	featured [character]	1. No 2. Yes	2599 (95.2%) 132 ( 4.8%)		2731 (100%)	0 (0%)



Based on the resources and the goal above, identify <b>five problems</b> of the data set in its current form. For each, quickly describe why it is problematic in the given context, and name a possible data preparation strategy to overcome it. After performing the steps you describe, the resulting data set should be suitable to fit your model given the following specification in R:	0 1 2
model <- glm(featured ~ ., data=video_data_clean, family='binomial')	3 4 5 6 7 8 9









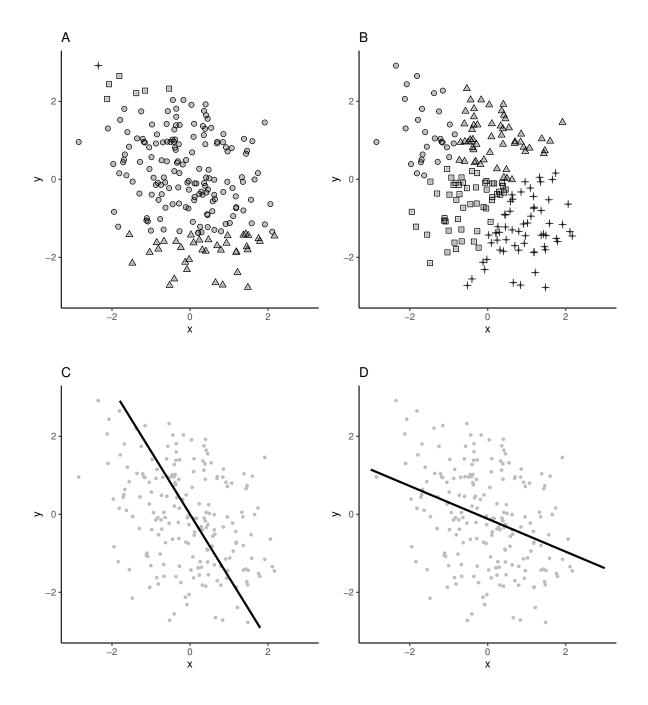
## Problem 3 Identify Models (10 credits)

You have been hired by a client to help them understand a problem in one of their business processes. In your analysis, you have collected a dataset of 200 problem instances and fitted several statistical models on the data:

- · linear regression (OLS),
- · k-means,
- · principal components analysis,
- · decision tree.

You are about to present your results to the clients and have printed handouts with visualizations of your models, but suddenly you realize that your assistant has forgotten to label each visualization with its title.

For each printout (A,B,C,D) below, (a) name which of the models is shown, (b) quickly summarize the visualization (What aspect(s) of the model are shown?) (c) justify your choice. (Why is it this model and not one of the others?)







lacksquare	F
	F
	F
│	F
│ H	F
	E
<b>□ □</b> □ □	L
⊢⊟	E
⊢⊟	L
H	F
∣ <b>H</b>	F
_	









## Problem 4 Evaluation (18 credits)

Your cybersecurity company has developed two new email spam filters. The managers would like to have an analysis on both software systems (A and B). You have received a small but representative trial of experimental results:

True class	Probability of Classifier A	Probability of Classifier B
+	0.87	0.81
-	0.21	0.25
-	0.78	0.79
+	0.53	0.68
+	0.94	0.91
-	0.68	0.89
-	0.37	0.54
+	0.83	0.88
-	0.02	0.17
+	0.67	0.77

Each row represents an email, which is either spam (positive label) or no spam (negative label). The probabilities indicate the likelihood of being classified as spam by the respective software. The default cutoff value for both systems is 0.76.

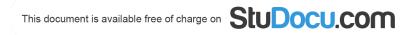
a)\* Calculate the *accuracy* of both software systems. Provide formula and calculations.





	\$5655 A 1855
b)* Provide formulas and calculate recall and specificity for both software systems. Explain the results and characterize both software systems accordingly.	
c)* Many customers prefer that a high share of the emails classified as spam are indeed spam emails. Which software would you recommend? Name and calculate a meaningful metric.	0 1 2



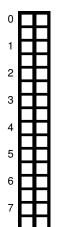




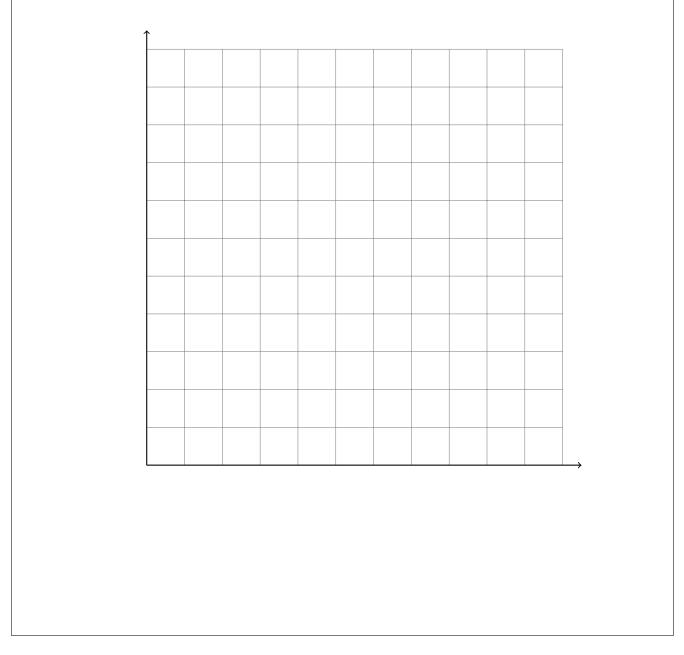


Note: Table identical as above (depicted here for ease of readability).

True class	Probability of Classifier A	Probability of Classifier B
+	0.87	0.81
-	0.21	0.25
-	0.78	0.79
+	0.53	0.68
+	0.94	0.91
-	0.68	0.89
-	0.37	0.54
+	0.83	0.88
-	0.02	0.17
+	0.67	0.77



d)\* Draw the ROC curve of software A. Name the axes and write down the (x,y)-coordinates for every point. Mark the point corresponding to the default cutoff value of 0.76. Would you argue that this cutoff value is appropriate? Explain your reasoning.



<b>35.4 下</b> 线
-----------------

easily computed from nnecting the origin and		





Page empty



## Problem 5 Decision Trees (17 credits)

A laundry manager wants to optimize her energy and detergent usage. Therefore, she tested the washing results for various settings and reported her results in Table 5.1.

Temperature	Detergent	Dirt	Result
30	low	low	good
60	low	high	bad
30	low	medium	bad
30	high	high	bad
40	low	low	good
40	low	medium	bad
40	high	high	bad
60	low	medium	good
60	high	medium	good
60	high	high	good

Table 5.1: Laundry results.

0	Щ
1	坩
2	坩
3	坩
4	Ш
5	

a)\* Of the first three attributes, find that one that would be at the root of a decision tree using the information gain criterion. For the numeric attribute *Temperature* consider binary splits.

*Note:* For this exercise, we will again use  $0 \cdot \log(0) = 0$ .

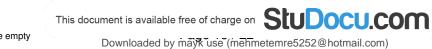


b)\* Assume there is an additional data point with a missing value:

Temperature	Detergent	Dirt	Result
40	low	?	good

	40	IOW	, (	jood	
wever, your colleague had a 569 for the attribute <i>Dirt</i> . What	ccess to all dat at is the missing	a (including th value marked	e new obs by the que	ervation) and ca	lculated a gain ratio
What is the reason for prunir	ng and how doe	s the pruning r	nethod sub	tree replacemen	t work?
Generally, why is it not a goo	od idea to discre	etize numerical	attributes i	nto many bins?	









0		
1	Н	
_		
2	Ш	

e)* You build a decision tree with pruning activated. Nevertheless, it is still large and difficult to interpreyou do to make it smaller?	et. What car





## Problem 6 Inference and Causality (20 credits)

The following scenario is based on real events, however numbers and other details are adjusted for academic purposes.

The Federal Reserve Act divided Mississippi between the 6th (Atlanta) and 8th (St. Louis) Districts. During the Great Depression, these districts' policies differed. Atlanta championed monetary activism and the extension of aid to support banks. St. Louis denied such an aid for banks. During the banking crisis that started at the end of 1930 and lasted for 2 years, Atlanta lent money to banks in need while St. Louis did not. In a study you want to address the following question: "Did providing liquidity (or credibly committing to do so) reduce rates of bank suspension and liquidation?"

* What type of experiment/study does the above described scenario allow for? Provide 2-3 arguments.			
	-		

#### BANK SUSPENSIONS AND LIQUIDATIONS

Begin July 1		End June 30	PERCENTAGE OF BANKS SUSPENDING			PERCENTAGE OF BANKS LIQUIDATING		
			All (1)	Federal Reserve District		121	Federal Reserve District	
				6th Atlanta (2)	8th St. Louis (3)	All (4)	6th Atlanta (5)	8th St. Louis (6)
1929	to	1930	4.8	7.1	3.0	4.5	7.1	2.4
1930	to	1931	28.9	14.2	39.5	13.6	7.1	18.6
1931	to	1932	13.2	14.9	11.8	8.0	7.9	8.1
1932	to	1933	7.7	7.5	7.9	7.3	6.5	7.9
1933	to	1934	.9	.0	1.7	.9	.0	1.7
1929	to	$1934^{a}$	49.8	38.7	59.2	30.9	26.8	34.4

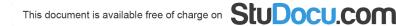
SOURCE. - Rand McNally Bankers Directory and National Archives and Records Administration Record Group 82. See Section II and Richardson (2006, 2007a, 2007b, 2008) for details.

- b)\* You are provided with the data in the table above.
  - 1. What technique can you apply to identify causal effects in this setting? Explain the technique and argue briefly why you choose it (3-4 sentences). (6P)
  - 2. Why do you need that technique and cannot simply make a causality statement based on the data of Atlanta only? (3P)



Downloaded by mayk use (mehmetemre5252@hotmail.com)









<sup>\*</sup>The last row indicates the percentage of banks operating on July 1, 1929, that either suspended or liquidated by June 30, 1933.



c)*		
·)	Fictional	
and you know which b Now, you want to mak	anks failed in 1931. a statement of whether the program helped the banks to avoid suspension/liquidati	on.
1 Namo ono appro	priate technique to help you identify causal effects in this setting. (2P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se		
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	
2. Explain in 2-3 se	ntences why it is appropriate. (3P)	













Additional space for solutions-clearly mark the (sub)problem your answers are related to and strike out invalid solutions.

