

Tutorial Business Analytics

Tutorial 2: Statistics

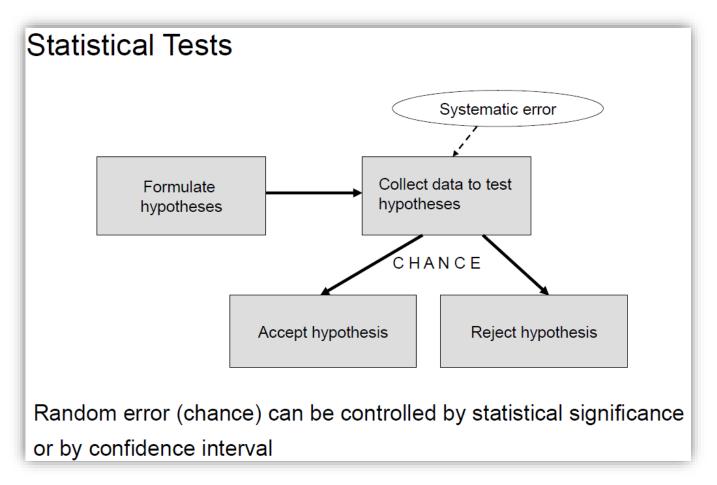
Decision Sciences & Systems (DSS)

Department of Informatics

TU München



What we will focus on in this tutorial:





Agenda

1. Theory: How does **Hypothesis testing** work?

2. Calculation **Example**

3. Practice: Exercises in Live Tutorial Session

Recommendations

- Use paper and a scientific calculator for the exercises (except R exercises)
- Pay attention to the theory and the example part
- Do all exercises and homework



Statistical Testing

- We are trying to validate a claim about a statistic of a population, only based upon (a) sample(s)
- This **statistical hypothesis** is tested by observing random variables
- · Common cases are
 - Sample statistic is compared against a synthetic (population) statistic
 - Two samples are compared
- A hypothesis is proposed for the statistical relationship between the two statistics; this is compared to a null hypothesis
- The comparison is denoted as statistically significant if the relationship between the statistics (i.e., drawing respective sample(s)) would be unlikely under the null hypothesis according to a threshold probability



"Test Manual" - Overview

1. i) 1 sample or 2 samples

ii) If 1 sample: σ_x known or unknown If 2 samples: dependent or independent

- 2. State H_0 and H_1 (given)
- 3. Select and calculate the test statistic
- 4. Select α (given)
- 5. Find the critical value in the table
- 6. Result



"Test Manual" – 2nd Step

There exist three possible alternative hypotheses H_1 :

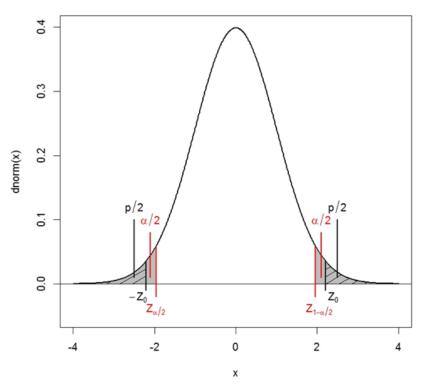
| Hypothesis | H _o | H ₁ |
|------------|------------------------|--------------------|
| Two-sided | $\mu_x = \mu_0$ | $\mu_x \neq \mu_0$ |
| One-sided | $\mu_{x} \leq \mu_{0}$ | $\mu_x > \mu_0$ |
| One-sided | $\mu_x \ge \mu_0$ | $\mu_x < \mu_0$ |



"**Test Manual**" – **2**nd **Step:** Two-Sided Hypothesis Test

$$H_0$$
: $\mu_x = \mu_0$ H_1 : $\mu_x \neq \mu_0$

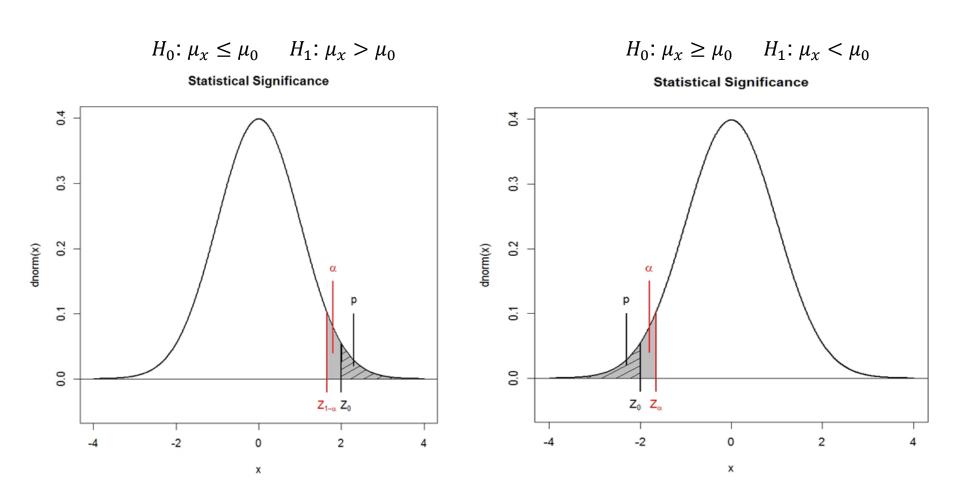
Statistical Significance



© Chair of Decision Sciences and Systems, Technical University of Munich



"Test Manual" – 2nd Step: One-Sided Hypothesis Test





"Test Manual" - 3rd Step

When to use which test? We want to make a statement about the mean of a population, μ_x , based on a sample with size n_x and mean \bar{x}

1 Sample

- σ_{χ} known \rightarrow Gauss/z-test $z_0 = \frac{\bar{x} \mu_0}{\sigma_{\chi}} \sqrt{n} \sim N(0,1)$
- σ_x unknown \rightarrow t-test $t_0 = \frac{\bar{x} \mu_o}{s_x} \sqrt{n} \sim t_{n-1}$ with $s_x^2 = \frac{1}{n-1} \cdot \sum_{i=1}^n (x_i \bar{x})^2$

2 Samples

- independent \to Welch-test $t_0 = \frac{\bar{x} \bar{w} \mu_0}{s_{\bar{x} \bar{w}}} \sim_{\mathrm{approx}} t_{\mathrm{df}}$ with $s_{\bar{x} \bar{w}}^2 = \frac{s_x^2}{n_x} + \frac{s_w^2}{n_w}$ and
 - $s_x^2 = \frac{1}{n-1} \cdot \sum_{i=1}^n (x_i \bar{x})^2 \quad \text{(df} = \frac{\left(s_{\bar{x} \bar{w}}^2\right)^2}{\frac{s_x^4}{n_x^2(n_x 1)} + \frac{s_w^4}{n_w^2(n_w 1)}} \text{ rounded to nearest integer number)}$
- dependent \to Paired t-test $t_0=\frac{\bar{d}-\mu_0}{s_d}\sqrt{n}\sim t_{n-1}$ with $s_d^2=\frac{1}{n-1}\cdot\sum_{i=1}^n(d_i-\bar{d})^2$ and $\bar{d}=\frac{1}{n}\sum_{i=1}^nd_i=\bar{x}-\bar{w}$, $d_i=x_i-w_i$, $\mu_D=\mu_X-\mu_W$



"Test Manual" – 5th Step

How to find the critical value in the table? For

Gauss/z-Test

→ use normal distribution

• t-Test, Welch-Test and Paired t-Test → use t-distribution

| H ₁ | t ^c range | t ^c value |
|--------------------|-------------------------------------|---|
| $\mu_x \neq \mu_0$ | can be any, ℝ | $\left t_{1-\frac{\alpha}{2};\mathrm{df}}^{c}\right = \left t_{\frac{\alpha}{2};\mathrm{df}}^{c}\right $ |
| $\mu_x > \mu_0$ | must be positive, $\mathbb{R}_{>0}$ | $t_{1-\alpha;\mathrm{df}}^c$ |
| $\mu_x < \mu_0$ | must be negative, $\mathbb{R}_{<0}$ | $t^c_{lpha;\mathrm{df}}$ |



Tutorial 2 Business Analytics

Normal Distribution (z-table)

• If X is a normally distribution random variable with mean μ and standard deviation σ ,

$$Z = \frac{X - \mu}{\sigma}$$

is standard normally distributed

- The table contains the probabilities that a statistic is less than z, i.e., between negative infinity and z
- The values are calculated using the cumulative distribution function Φ
- Examples:
 - $\Phi(0.72) = 0.76424$
 - $\Phi(-1.48) = 1 \Phi(1.48) = 0.06944$
 - If quantile $z_{0.9}$ is needed:

$$\Phi(z_{0.9}) = 0.9 \implies z_{0.9} \approx 1.28$$

| Z | +0.00 | +0.01 | +0.02 | +0.03 | +0.04 | +0.05 | +0.06 | +0.07 | +0.08 | +0.09 |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 0.0 | 0.50000 | 0.50399 | 0.50798 | 0.51197 | 0.51595 | 0.51994 | 0.52392 | 0.52790 | 0.53188 | 0.53586 |
| 0.1 | 0.53983 | 0.54380 | 0.54776 | 0.55172 | 0.55567 | 0.55966 | 0.56360 | 0.56749 | 0.57142 | 0.57535 |
| 0.2 | 0.57926 | 0.58317 | 0.58706 | 0.59095 | 0.59483 | 0.59871 | 0.60257 | 0.60642 | 0.61026 | 0.61409 |
| 0.3 | 0.61791 | 0.62172 | 0.62552 | 0.62930 | 0.63307 | 0.63683 | 0.64058 | 0.64431 | 0.64803 | 0.65173 |
| 0.4 | 0.65542 | 0.65910 | 0.66276 | 0.66640 | 0.67003 | 0.67364 | 0.67724 | 0.68082 | 0.68439 | 0.68793 |
| 0.5 | 0.69146 | 0.69497 | 0.69847 | 0.70194 | 0.70540 | 0.70884 | 0.71226 | 0.71566 | 0.71904 | 0.72240 |
| 0.6 | 0.72575 | 0.72907 | 0.73237 | 0.73565 | 0.73891 | 0.74215 | 0.74537 | 0.74857 | 0.75175 | 0.75490 |
| 0.7 | 0.75804 | 0.76115 | 0.76424 | 0.76730 | 0.77035 | 0.77337 | 0.77637 | 0.77935 | 0.78230 | 0.78524 |
| 8.0 | 0.78814 | 0.79103 | 0.79389 | 0.79673 | 0.79955 | 0.80234 | 0.80511 | 0.80785 | 0.81057 | 0.81327 |
| 0.9 | 0.81594 | 0.81859 | 0.82121 | 0.82381 | 0.82639 | 0.82894 | 0.83147 | 0.83398 | 0.83646 | 0.83891 |
| 1.0 | 0.84134 | 0.84375 | 0.84614 | 0.84849 | 0.85083 | 0.85314 | 0.85543 | 0.85769 | 0.85993 | 0.86214 |
| 1.1 | 0.86433 | 0.86650 | 0.86864 | 0.87076 | 0.87286 | 0.87493 | 0.87698 | 0.87900 | 0.88100 | 0.88298 |
| 1.2 | 0.88493 | 0.88686 | 0.88877 | 0.89065 | 0.89251 | 0.89435 | 0.89617 | 0.89796 | 0.89973 | 0.90147 |
| 1.3 | 0.90320 | 0.90490 | 0.90658 | 0.90824 | 0.90988 | 0.91149 | 0.91308 | 0.91466 | 0.91621 | 0.91774 |
| 1.4 | 0.91924 | 0.92073 | 0.92220 | 0.92364 | 0.92507 | 0.92647 | 0.92785 | 0.92922 | 0.93056 | 0.93189 |
| 1.5 | 0.93319 | 0.93448 | 0.93574 | 0.93699 | 0.93822 | 0.93943 | 0.94062 | 0.94179 | 0.94295 | 0.94408 |
| 1.6 | 0.94520 | 0.94630 | 0.94738 | 0.94845 | 0.94950 | 0.95053 | 0.95154 | 0.95254 | 0.95352 | 0.95449 |
| 1.7 | 0.95543 | 0.95637 | 0.95728 | 0.95818 | 0.95907 | 0.95994 | 0.96080 | 0.96164 | 0.96246 | 0.96327 |
| 1.8 | 0.96407 | 0.96485 | 0.96562 | 0.96638 | 0.96712 | 0.96784 | 0.96856 | 0.96926 | 0.96995 | 0.97062 |
| 1.9 | 0.97128 | 0.97193 | 0.97257 | 0.97320 | 0.97381 | 0.97441 | 0.97500 | 0.97558 | 0.97615 | 0.97670 |
| 2.0 | 0.97725 | 0.97778 | 0.97831 | 0.97882 | 0.97932 | 0.97982 | 0.98030 | 0.98077 | 0.98124 | 0.98169 |
| 2.1 | 0.98214 | 0.98257 | 0.98300 | 0.98341 | 0.98382 | 0.98422 | 0.98461 | 0.98500 | 0.98537 | 0.98574 |
| 2.2 | 0.98610 | 0.98645 | 0.98679 | 0.98713 | 0.98745 | 0.98778 | 0.98809 | 0.98840 | 0.98870 | 0.98899 |
| 2.3 | 0.98928 | 0.98956 | 0.98983 | 0.99010 | 0.99036 | 0.99061 | 0.99086 | 0.99111 | 0.99134 | 0.99158 |
| 2.4 | 0.99180 | 0.99202 | 0.99224 | 0.99245 | 0.99266 | 0.99286 | 0.99305 | 0.99324 | 0.99343 | 0.99361 |
| 2.5 | 0.99379 | 0.99396 | 0.99413 | 0.99430 | 0.99446 | 0.99461 | 0.99477 | 0.99492 | 0.99506 | 0.99520 |



Tutorial 2 Business Analytics

t-Distribution (t-table)

- A random variable with t-distribution arises, e.g., when estimating the mean of a normally distributed population in situations with a small sample size and unknown population standard deviation
- The numbers in the body of the table, $t_{1-\alpha;\,\mathrm{df}}^c$, are the critical values needed for the t-test
 - df: degrees of freedom
 - α : significance level

| cum. prob | t _{.50} | t.75 | t.80 | t .85 | t.90 | t.95 | t.975 | t .99 | t.995 | t.999 | t.9995 |
|-----------|------------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| one-tail | 0.50 | 0.25 | 0.20 | 0.15 | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 | 0.001 | 0.0005 |
| two-tails | 1.00 | 0.50 | 0.40 | 0.30 | 0.20 | 0.10 | 0.05 | 0.02 | 0.01 | 0.002 | 0.001 |
| df | | | | | | | | | | | |
| 1 | 0.000 | 1.000 | 1.376 | 1.963 | 3.078 | 6.314 | 12.71 | 31.82 | 63.66 | 318.31 | 636.62 |
| 2 | 0.000 | 0.816 | 1.061 | 1.386 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 22.327 | 31.599 |
| 3 | 0.000 | 0.765 | 0.978 | 1.250 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 | 10.215 | 12.924 |
| 4 | 0.000 | 0.741 | 0.941 | 1.190 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 7.173 | 8.610 |
| 5 | 0.000 | 0.727 | 0.920 | 1.156 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 5.893 | 6.869 |
| 6 | 0.000 | 0.718 | 0.906 | 1.134 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 5.208 | 5.959 |
| 7 | 0.000 | 0.711 | 0.896 | 1.119 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 4.785 | 5.408 |
| 8 | 0.000 | 0.706 | 0.889 | 1.108 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 4.501 | 5.041 |
| 9 | 0.000 | 0.703 | 0.883 | 1.100 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 4.297 | 4.781 |
| 10 11 | 0.000 | 0.700 0.697 | 0.879 0.876 | 1.093 1.088 | 1.372 1.363 | 1.812 1.796 | 2.228 2.201 | 2.764 2.718 | 3.169 3.106 | 4.144 4.025 | 4.587 4.437 |
| 12 | 0.000 | 0.695 | 0.878 | 1.083 | 1.353 | 1.796 | 2.201 | 2.681 | 3.106 | 3.930 | 4.437 |
| 13 | 0.000 | 0.694 | 0.873 | 1.003 | 1.350 | 1.702 | 2.179 | 2.650 | 3.012 | 3.852 | 4.221 |
| 14 | 0.000 | 0.692 | 0.868 | 1.079 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 3.787 | 4.140 |
| 15 | 0.000 | 0.691 | 0.866 | 1.074 | 1.341 | 1.753 | 2.143 | 2.602 | 2.947 | 3.733 | 4.073 |
| 16 | 0.000 | 0.690 | 0.865 | 1.074 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 3.686 | 4.015 |
| 17 | 0.000 | 0.689 | 0.863 | 1.069 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 3.646 | 3.965 |
| 18 | 0.000 | 0.688 | 0.862 | 1.067 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 3.610 | 3.922 |
| 19 | 0.000 | 0.688 | 0.861 | 1.066 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 3.579 | 3.883 |
| 20 | 0.000 | 0.687 | 0.860 | 1.064 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 3.552 | 3.850 |
| 21 | 0.000 | 0.686 | 0.859 | 1.063 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 3.527 | 3.819 |
| 22 | 0.000 | 0.686 | 0.858 | 1.061 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 3.505 | 3.792 |
| 23 | 0.000 | 0.685 | 0.858 | 1.060 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 3.485 | 3.768 |
| 24 | 0.000 | 0.685 | 0.857 | 1.059 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 3.467 | 3.745 |
| 25 | 0.000 | 0.684 | 0.856 | 1.058 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 | 3.450 | 3.725 |
| 26 | 0.000 | 0.684 | 0.856 | 1.058 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 3.435 | 3.707 |
| 27 | 0.000 | 0.684 | 0.855 | 1.057 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 3.421 | 3.690 |
| 28 | 0.000 | 0.683 | 0.855 | 1.056 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 3.408 | 3.674 |
| 29 | 0.000 | 0.683 | 0.854 | 1.055 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 3.396 | 3.659 |
| 30 | 0.000 | 0.683 | 0.854 | 1.055 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 | 3.385 | 3.646 |
| 40 | 0.000 | 0.681 | 0.851 | 1.050 | 1.303 | 1.684 | 2.021 | 2.423 | 2.704 | 3.307 | 3.551 |
| 60 | 0.000 | 0.679 | 0.848 | 1.045 | 1.296 | 1.671 | 2.000 | 2.390 | 2.660 | 3.232 | 3.460 |
| 80 | 0.000 | 0.678 | 0.846 | 1.043 | 1.292 | 1.664 | 1.990 | 2.374 | 2.639 | 3.195 | 3.416 |
| 100 | 0.000 | 0.677 | 0.845 | 1.042 | 1.290 | 1.660 | 1.984 | 2.364 | 2.626 | 3.174 | 3.390 |
| 1000 | 0.000 | 0.675 | 0.842 | 1.037 | 1.282 | 1.646 | 1.962 | 2.330 | 2.581 | 3.098 | 3.300 |
| z | 0.000 | 0.674 | 0.842 | 1.036 | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 | 3.090 | 3.291 |
| | 0% | 50% | 60% | 70% | 80% | 90% | 95% | 98% | 99% | 99.8% | 99.9% |
| I | Confidence Level | | | | | | | | | | |



"Test Manual" – 6th Step

Reject H₀:

| H ₁ | p-value criterion | test statistic criterion |
|--------------------|-------------------|---|
| $\mu_x \neq \mu_0$ | p < α | $ t_0 > \left t_{1-\frac{\alpha}{2}; \mathrm{df}}^c \right $ |
| $\mu_x > \mu_0$ | p < α | $t_0 > t_{1-\alpha;\mathrm{df}}^c$ |
| $\mu_x < \mu_0$ | p < α | $t_0 < t_{\alpha;\mathrm{df}}^c$ |



Example: Learning Method Comparison

In order to compare two learning methods, results have been measured for a group of students. Test if the students got better (higher) results using method 2. Assume the difference follows a normal distribution, (significance level of 5%, i.e., $\alpha = 0.05$).

| student | 1 | 2 | 3 | 4 | 5 |
|--------------|----|---|---|----|---|
| method 1 (x) | 8 | 6 | 8 | 8 | 4 |
| method 2 (w) | 10 | 9 | 7 | 12 | 7 |

1.) i) 2 samples

ii) dependent

2.)
$$H_0$$
: $\mu_D = \mu_X - \mu_W \ge \mu_0 = 0$

$$H_0$$
: $\mu_D = \mu_X - \mu_W \ge \mu_0 = 0$ H_1 : $\mu_D = \mu_X - \mu_W < \mu_0 = 0$

3.)
$$o$$
 Paired t-Test: $t_0 = \frac{\bar{d} - \mu_0}{s_d} \sqrt{n} \sim t_{n-1}$ with unbiased sample variance $s_d^2 = \frac{1}{n-1} \sum_{i=1}^n (d_i - \bar{d})^2$

sample means: $\bar{x} = 6.8$, $\bar{w} = 9.0$, difference $\bar{d} = -2.2$,

$$s_d^2 = 3.7$$
, $s_d = 1.9235 \implies t_0 = -2.5574$

4.) $\alpha = 0.05$

5.)
$$\rightarrow t_{\alpha;n-1}^c = -t_{1-\alpha;n-1}^c \text{ (sym.)} \Rightarrow t_{0.05;4}^c = -t_{0.95;4}^c \stackrel{\text{table}}{=} -2.132$$

6.)
$$t_0 = -2.557 < -2.132 = t_{0.05;4}^c \Rightarrow \text{Reject } H_0: \text{Learning method 2 is significantly better.}$$



Example: Learning Method Comparison – step 3 details

In order to compare two learning methods, results have been measured for a group of students. Test if the students got better (higher) results using method 2. Assume the difference follows a normal distribution, (significance level of 5%, i.e., $\alpha = 0.05$).

| student | 1 | 2 | 3 | 4 | 5 |
|--------------|----|---|---|----|---|
| method 1 (x) | 8 | 6 | 8 | 8 | 4 |
| method 2 (w) | 10 | 9 | 7 | 12 | 7 |

3.)

sample means:
$$\bar{x} = \frac{1}{5}(8+6+8+8+4) = 6.8$$
, $\bar{w} = \frac{1}{5}(10+9+8+12+7) = 9.0$

difference:
$$\bar{d} = \frac{1}{n} \sum_{i=1}^{n} d_i = \bar{x} - \bar{w} = -2.2$$

sample variance:
$$s_d^2 = \frac{1}{n-1} \sum_{i=1}^n (d_i - \bar{d})^2$$
, $d_i = x_i - w_i$,

$$s_d^2 = \frac{1}{4} \left((8 - 10 + 2.2)^2 + (6 - 9 + 2.2)^2 + (8 - 7 + 2.2)^2 + (8 - 12 + 2.2)^2 + (4 - 7 + 2.2)^2 \right) = 3.7$$

$$s_d = 1.9235$$



Confidence Intervals

Find confidence intervals for μ_x , which—under H_0 —contain the true value μ_x with a probability of at least $1 - \alpha$ (confidence level). We differentiate two cases:

• σ_x known:

confidence interval:

$$[I_u(x), I_o(x)] = \left[\bar{x} - z_{1-\frac{\alpha}{2}}^c \frac{\sigma_x}{\sqrt{n}}, \ \bar{x} + z_{1-\alpha/2}^c \frac{\sigma_x}{\sqrt{n}}\right]$$

• σ_x unknown, use s_x as estimate instead:

confidence interval:
$$[I_u(x), I_o(x)] = \left[\bar{x} - t_{1-\frac{a}{2}; n-1}^c \frac{s_x}{\sqrt{n}}, \bar{x} + t_{1-\frac{a}{2}; n-1}^c \frac{s_x}{\sqrt{n}}\right]$$

- Values of μ_0 within the confidence interval cannot be rejected regarding a significance level of α
 - \rightarrow Reject H_0 if μ_0 is not in the confidence interval



Exercise 2.1

The consumption per person is measured in index values, where a high index value represents a high consumption. The following table embodies index values for 10 individuals before and after a tax increase.

| Individual | Index | Difference, | |
|------------|--|-----------------------------|-----------|
| number, i | previous to tax increase, \boldsymbol{a} | after tax increase, $\it b$ | d = a - b |
| 1 | 27 | 40 | -13 |
| 2 | 31 | 36 | -5 |
| 3 | 23 | 43 | -20 |
| 4 | 35 | 34 | 1 |
| 5 | 26 | 25 | 1 |
| 6 | 27 | 41 | -14 |
| 7 | 26 | 32 | -6 |
| 8 | 18 | 29 | -11 |
| 9 | 22 | 21 | 1 |
| 10 | 21 | 36 | -15 |

- a) Determine if there is a significant difference in consumption prior to the tax increase and after, utilizing a hypothesis test (significance level $\alpha=0.05$). The difference is assumed to be normally distributed.
- b) Check your result by applying t.test() in R.



Exercise 2.2

According to the information supplied by the manufacturer of a certain type of car, its gas consumption in city traffic is approximately normally distributed with expected value $\mu=9.5\ell/100 {\rm km}$. The standard deviation $\sigma=2.5\ell/100 {\rm km}$ is commonly known (to the general public and the manufacturer). In order to review the manufacturer's prediction, a consumer organization has performed a test on 25 cars which yielded the following result:

Average gas consumption: $\bar{x} = 10.5\ell/100 \text{km}$

Check the manufacturer's statement with a suitable test at significance level of $\alpha = 0.05$ and a second time with $\alpha = 0.01$.



Exercise 2.3

During a recent study project, a friend of yours asked 8 men and 10 women how many hours per day they wear a mask during the ongoing COVID-19 pandemic. The following table shows their answers. Afterwards he/she set the hypothesis to "On average, women wear their mask longer per day".

- a) Test the hypothesis "by hand" with significance level $\alpha = 0.05$ and 16 degrees of freedom.
- b) Find out how to solve this exercise using R.

| Individual no. i | Hours per day | Gender |
|------------------|---------------|--------|
| 1 | 4 | female |
| 2 | 2 | female |
| 3 | 3 | female |
| 4 | 5 | female |
| 5 | 7 | female |
| 6 | 2 | female |
| 7 | 7 | female |
| 8 | 3 | female |
| 9 | 5 | female |
| 10 | 2 | female |
| 11 | 2 | male |
| 12 | 1 | male |
| 13 | 5 | male |
| 14 | 3 | male |
| 15 | 1 | male |
| 16 | 3 | male |
| 17 | 2 | male |
| 18 | 3 | male |