# On modelling optimization problems via Julia JuMP

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#### Outlines

- Lecture 1: an overview of Julia Language
  - Simple examples, Handling input and output data;
  - JuMP: commands, examples, modeling classical problems: knapsack, transportation, TSP, exercises;
- Lecture 2: Assembly Line Balancing Problems (ALBPs)
  - SALBP-1 and SALBP-2;
  - ALWABP;
  - Exercises.
- Lecture 3: Vehicle Routing Problem (VRP) and Production Planning
  - Modeling a variant of VRP;
  - Modeling a production planning problem;
  - Exercise.

#### Outlines

- Lecture 4: Problems on Graphs
  - Maximum Dispersion Problem (MaxDP);
  - Promoting Eulerian Districts for Arc Routing;
  - Exercise.
- Lecture 5: Final test

#### Universidade Federal de Lavras (UFLA)

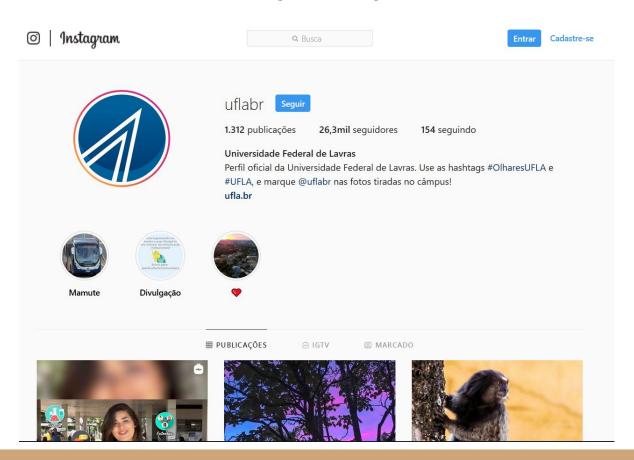
- TOP 10 in the Brazilian Ranking of Courses (2018);
- Approximately 800 professors and 16,000 students;
- 35 undergraduate courses, and 43 graduate programs;
- Prize "Blue University": Reference on Water Sustainability;
- The incentive to entrepreneurship: innovation hubs and, technological park (*LavrasTec*).

#### Universidade Federal de Lavras (UFLA)



#### Universidade Federal de Lavras (UFLA)

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### Department of Computer Science

- 40 professors (Ph.D.) and 8 administrative technicians;
- 2 undergraduate courses: Information Systems and Computer Science;
- MSc. Computer Science (13 advisors): Software Engineering, Computational Intelligence, Operations Research, and Computer Networks;
- Teaching and Research Infrastructure.

## Department of Computer Science



#### L-LOOP: Lavras Laboratory of Optimization

- 4 professors;
- 10 undergraduate students and 5 MSc. students;
- 4 projects funded by CNPq and FAPEMIG;
- Expertise: Theory and Practice of Operations Research.

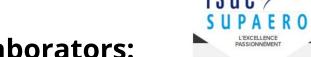


Lavras
Lab of Optimization

L-LOOP: since 2016

#### A short bio: Moreira, M. C. O.

- Professor at UFLA since 2015;
- Ph.D. at Universidade de São Paulo (USP);
  - Research stages: UPV (Valencia, Spain), UPC (Barcelona, Spain) and CIRRELT (Montreal, Canada);
- Funded by: CNPq, FAPEMIG and UFLA.













"We want a language that's open source, (...) We want the **speed of C** with the dynamism of Ruby. (...) familiar mathematical notation like Matlab. (...) general programming as Python, as easy for statistics as R, as natural for string processing as Perl, (...). We want it **interactive** and we want it compiled."

### Why Julia?



Jeff Bezanson
JeffBezanson



Viral B. Shah ViralBShah



Alan Edelman

Professor of Applied Mathematics Computer Science and Al Laboratories Applied Computing Group Leader

» Stefan Karpinski «

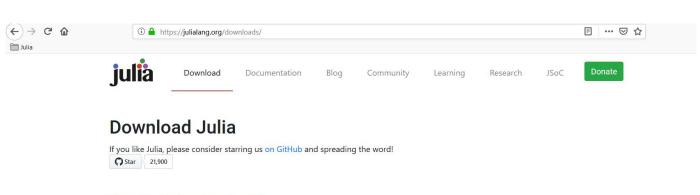


- High Performance language;
- Rich language of descriptive datatypes;
- Free and open source;
- Just-in-time compilation;
- Julia has: garbage collector, efficient libraries for floating-point calculations, linear algebra, random number generation, and regular expression matching.

# Download and install (Windows, MacOS and

Linux)

Remember to set up path variable.



We provide several ways for you to run Julia:

- In the terminal using the built-in Julia command line.
- In the browser on JuliaBox.com with Jupyter notebooks. No installation is required -- just point your browser there, login and start computing.
- Using Docker images from Docker Hub maintained by the Docker Community.
- JuliaPro by Julia Computing includes Julia and the Juno IDE, along with access to a curated set of packages for plotting, optimization, machine learning, databases and much more (requires registration).

Please see platform specific instructions for further installation instructions and if you have trouble installing Julia. If the provided download files do not work for you, please file an issue in the Julia project. Different OSes and architectures have varying tiers of support, and are listed at the bottom of this page.

#### Current stable release: v1.1.0

Windows Self-Extracting Archive (.exe) [help]	32-bit	64-bit
	Windows 7/Windows Server 2012 users also require Windows Management Framework 3.0 or later	
macOS 10.8+ Package (.dmg) [help]		64-bit

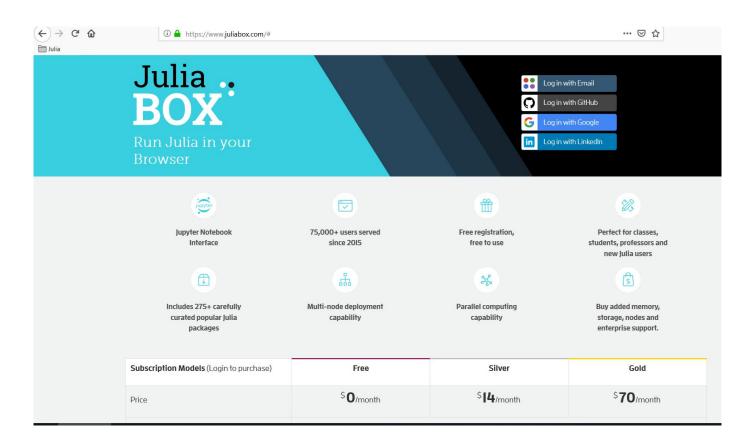
- Currently: Version 1.1.0;
- Other Resources
  - Learning (tutorials, texts and books):
    - https://julialang.org/learning/
    - Coursera: www.coursera.org/learn/julia-programming
  - Official channel: <a href="https://julialang.org/community/">https://julialang.org/community/</a>
  - Documentation: <a href="https://docs.julialang.org/en/v1/">https://docs.julialang.org/en/v1/</a>
- Learn by examples (version 0.6.2):
   <a href="https://juliabyexample.helpmanual.io/">https://juliabyexample.helpmanual.io/</a>
- IDE: <u>luno</u>.



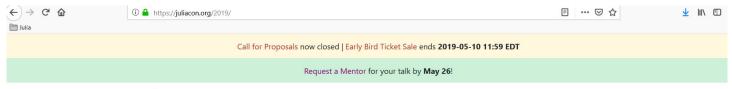
- Some ecosystems
  - Bioinformatics and Computational Biology in Julia
    - BioJulia <a href="https://github.com/BioJulia">https://github.com/BioJulia</a>
  - Optimization packages
    - JuliaOpt <a href="https://www.juliaopt.org/">https://www.juliaopt.org/</a>
  - Image Processing
    - Julialmages <a href="https://juliaimages.org/latest/">https://juliaimages.org/latest/</a>
  - Quantum Systems
    - QuantumBFS https://github.com/QuantumBFS
    - QuantumOptics <a href="https://github.com/qojulia/QuantumOptics.jl">https://github.com/qojulia/QuantumOptics.jl</a>
  - Complex Systems
    - JuliaDynamics <a href="https://github.com/JuliaDynamics">https://github.com/JuliaDynamics</a>

- Some ecosystems
  - Quantitative economic modeling
    - QuantEcon <a href="https://github.com/QuantEcon">https://github.com/QuantEcon</a>
  - Astronomy and Astrophysics
    - Julia Astro <a href="http://juliaastro.github.io/">http://juliaastro.github.io/</a>
  - Ecology
    - EcoJulia <a href="https://github.com/EcoJulia">https://github.com/EcoJulia</a>
  - Machine Learning and Artificial Intelligence
    - Flux <a href="https://juliacomputing.com/domains/ml-and-ai.html">https://juliacomputing.com/domains/ml-and-ai.html</a>
  - Statistics
    - JuliaStats https://github.com/JuliaStats

*JuliaBox*: run in your browser!



*Julia Conference!* 





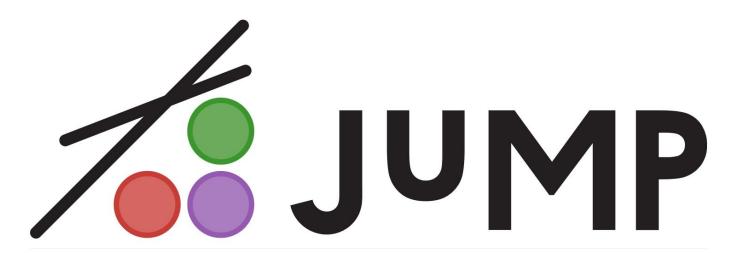
PREVIOUS EDITIONS / 2018 / 2017 / 2016 / 2015 / 2014

#### JuliaCon is coming to Baltimore



## Why JuMP?

**■ README.md** 



powered by NumFOCUS

JuMP is a domain-specific modeling language for mathematical optimization embedded in Julia. It currently supports a number of open-source and commercial solvers (Artelys Knitro, BARON, Bonmin, Cbc, Clp, Couenne, CPLEX, ECOS, FICO Xpress, GLPK, Gurobi, Ipopt, MOSEK, NLopt, SCS) for a variety of problem classes, including linear programming, (mixed) integer programming, second-order conic programming, semidefinite programming, and nonlinear programming.

## Why JuMP?

- Syntax close to mathematical notation!
- "easy to specify and solve optimization problems without expert knowledge" (https://github.com/JuliaOpt/JuMP.jl);

#### Online examples:

- https://github.com/JuliaOpt/JuMP.jl/tree/master/exam ples
- https://github.com/JuliaOpt/juliaopt-notebooks/blob/m aster/notebooks/Shuvomoy%20-%20Column%20genera tion.ipynb

## Let's practice!

We will use: Julia 1.1.0, JuMP 0.19.0, <u>Cbc</u> (*solver*), and <u>Jupyter</u>.

#### Go to:

https://github.com/mayronmoreira/ ufla-unimore-julia-jump

### Other References

- Bezanson, J., Edelman, A., Karpinski, S., & Shah, V. B. (2017).
   Julia: A fresh approach to numerical computing. *SIAM review*, 59(1), 65-98.
- Bezanson, J., Karpinski, S., Shah, V. B., & Edelman, A. (2012).
   Julia: A fast dynamic language for technical computing. arXiv preprint arXiv:1209.5145.
- Changhyun Kwon (2019). <u>Julia Programming for Operations</u> <u>Research</u>, 2nd Edition.
- Lubin, M., & Dunning, I. (2015). Computing in operations research using Julia. *INFORMS Journal on Computing*, *27*(2), 238-248.

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