# Analysis of curves and matrixes

# 1. Confusion Matrix:

# **Understanding the Confusion Matrix:**

- True Positive (TP): The number of times the class was correctly predicted.
- True Negative (TN): The number of times a different class was correctly predicted.
- False Positive (FP): The number of times a different class was incorrectly predicted as the class in question.
- False Negative (FN): The number of times the class was incorrectly predicted as a different class.

Bl derja: TP: heki heya bravo | | FP: predecteha ka class x w heya mahech heki wala mch mawjouda aslan

FN: mapredectehech raghmli heki heya | TN: mahech Iclasse heki w ma predectehech keka jawou behi

## **Calculating Metrics:**

**Accuracy**: This is the ratio of correctly predicted instances to the total instances.

$$Accuracy = \frac{\sum True\ Positives\ (diagonal\ elements)}{\sum Total\ instances}$$

**Precision**: This is the ratio of correctly predicted positive observations to the total predicted positives.

$$Precision = \frac{TP}{TP + FP}$$

where TP is True Positives and FP is False Positives.

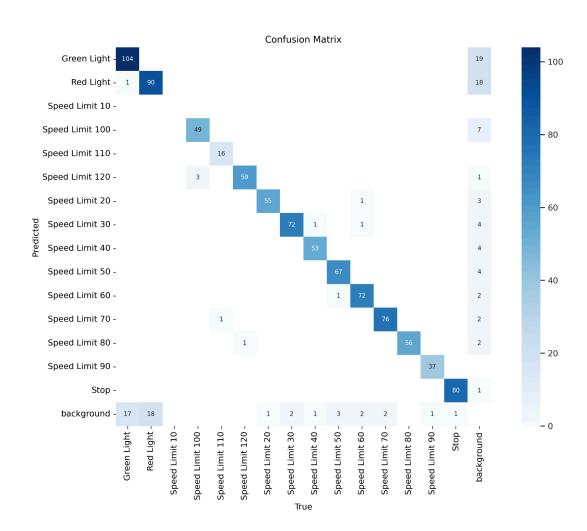
**Recall**: This is the ratio of correctly predicted positive observations to the all observations in actual class.

$$\text{Recall} = \frac{TP}{TP + FN}$$

where FN is False Negatives.

High values along the diagonal indicate good performance, as these are the correct predictions.

High off-diagonal values indicate confusion between classes, which may suggest that the model has difficulty distinguishing between certain classes.



## **Overall Observations:**

- The confusion matrix shows the performance of the model in predicting different traffic signs.
- The diagonal elements represent correct predictions, while off-diagonal elements represent misclassifications.

# **Class-wise Analysis:**

# Green Light:

- Correctly predicted 104 times.
- Misclassified as Red Light 1 time and Background 17 times.

# • Red Light:

- o Correctly predicted 90 times.
- Misclassified as Background 18 times.

# Speed Limit 10:

no predictions

# Speed Limit 100:

- o Correctly predicted 49 times.
- o Misclassified as Speed Limit 120 3 times.

# Speed Limit 110:

- Correctly predicted 16 times.
- o Misclassified as Speed Limit 70 1 time.

## Speed Limit 120:

- Correctly predicted 59 times.
- Misclassified as Speed Limit 80 1 time.

# • Speed Limit 20:

- Correctly predicted 55 times.
- Misclassified as Background 1 time.

## Speed Limit 30:

- Correctly predicted 72 times.
- Misclassified as Background 2 times.

## Speed Limit 40:

- Correctly predicted 53 times.
- Misclassified as Background 1 time and as Speed Limit 30 1 time .

## Speed Limit 50:

- Correctly predicted 67 times.
- o Misclassified as Background 3 times and as Speed Limit 60 1 time.

## • Speed Limit 60:

- Correctly predicted 72 times.
- Misclassified as Background 2 times and as Speed Limit 30 1 time and as Speed Limit 20 1 time.

# • Speed Limit 70:

- Correctly predicted 76 times.
- Misclassified as Background 2 times.

# Speed Limit 80:

Correctly predicted 56 times.

## Speed Limit 90:

- Correctly predicted 37 times.
- Misclassified as Background 1 times.

# • Stop:

- Correctly predicted 80 times.
- Misclassified as Background 1 time.

## **Accuracy**

Accuracy is the proportion of correct predictions made by the model. It is calculated as the total number of correct predictions divided by the total number of predictions. In the confusion matrix provided, the total number of correct predictions is 104+90+49+16+59+55+72+53+67+72+76+56+37+80=886. The total number of predictions is 886+1+17+18+3+1+1+2+1+1+1+3+1+1+2+2+1+1+1+2+2+4+4+4+3+1+7+18+19=1011. Therefore, the accuracy is 886/1011=0.876

### **Precision**

Precision is the proportion of positive predictions that are actually positive. It is calculated as the number of true positives divided by the number of true positives and false positives. In the confusion matrix provided, the number of true positives is 886 The number of true positives and false positives (FP=19+18+7+1+3+4+4+4+2+2+1+(1+3+1+1+1+1+1+1)=77) is 886+77=963. Therefore, the precision is 886/963=0.923

### Recall

Recall is the proportion of actual positives that are correctly identified as positive. It is calculated as the number of true positives divided by the number of true positives and false negatives. In the confusion matrix provided, the number of true positives is 886. The number of true positives and false negatives(FN=17+18+1+2+1+3+2+2+1+1+(1+3+1+1+1+1+1)=58) is 886+58=944. Therefore, the recall is 886/944=0.938.

## Interpretation:

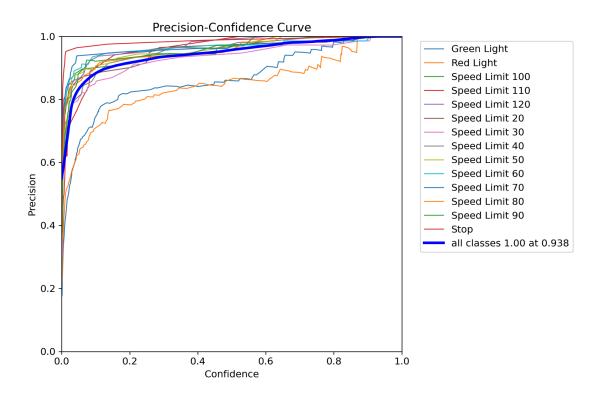
• **Accuracy** is a good overall measure of the model's performance, but it can be misleading if the classes are imbalanced. In this case, the accuracy is 0.876, which is

- relatively high. **Precision** is a good measure of how confident the model is in its predictions. In this case, the precision is 0.923, which means that 92.3% of the time the model predicted a sign it was correct.
- **Recall** is a good measure of how many of the actual positive cases the model correctly identified. In this case, the recall is 0.938, which means that 93.8% of the time a car was actually a certain sign, the model correctly identified it as it is.

# 2. Precision-Confidence Curve:

The Precision-Confidence curve is a critical tool for understanding how the model's precision changes as you adjust the confidence threshold.

• **Precision** is defined as the number of true positive predictions divided by the total number of positive predictions (true positives + false positives). It answers the question: "Of all the instances the model predicted as positive, how many were actually correct?"



Key observations:

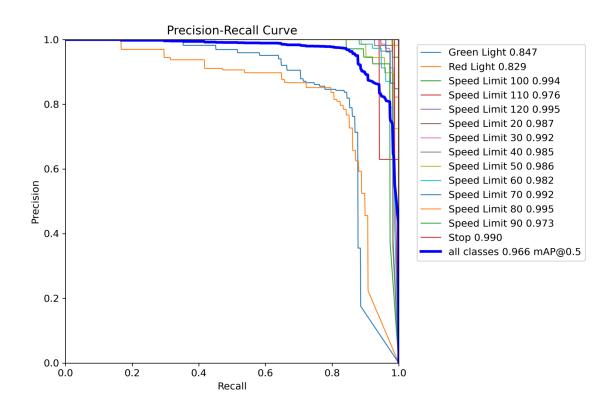
The overall performance shows a precision of 1.00 at a confidence of 0.938, meaning at this high confidence threshold, all positive predictions are correct.

 Precision tends to increase with confidence for all classes, as higher confidence values generally mean fewer false positives.  Some classes, like "Green Light" and "Red Light," show more variability in precision across different confidence values.

# 3. Precision-Recall Curve:

**Recall** measures how well a model finds all relevant instances of a particular class. It focuses on minimizing missed detections of the positive class.

- If the recall is high, the model correctly identifies most of the positive instances (most of the signs are detected).
- If the recall is low, the model misses many positive instances (many signs go undetected).



## Key observations:

- Overall Performance: The bold blue line shows a mean Average Precision (mAP) of 0.966 at an intersection over union (IoU) threshold of 0.5. This high mAP value indicates that the model performs well across all classes.
- Class-Specific Trends:

- Green Light and Red Light: These classes achieve lower precision and recall compared to others, suggesting more difficulty in distinguishing these classes accurately.
- Speed Limits: These classes generally achieve high precision and recall, indicating the model's strong ability to correctly identify speed limit signs.
- Stop: This class also shows high precision and recall, reflecting the model's effectiveness in identifying stop signs.

# 4. F1-Confidence Curve:

The F1-Confidence curve is an essential tool for understanding how the F1 score of a model changes as you adjust the confidence threshold. This helps in finding the optimal balance between precision and recall for different classes.

• **F1 Score**: The **F1 score** is the harmonic mean of precision and recall, providing a single metric that balances the two. It is particularly useful when you want to find a balance between the accuracy of positive predictions (precision) and the ability to find all positive instances (recall).

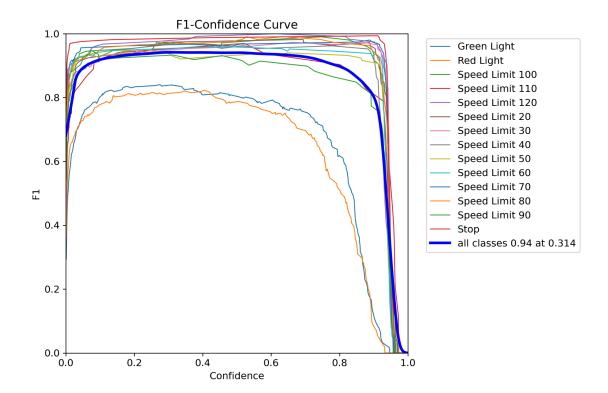
#### F1 Score

The **F1 score** is the harmonic mean of precision and recall, providing a single metric that balances the two. It is particularly useful when you want to find a balance between the accuracy of positive predictions (precision) and the ability to find all positive instances (recall).

 $\overline{ ext{F1 Score}} = 2 imes rac{ ext{Precision} imes ext{Recall}}{ ext{Precision} + ext{Recall}}$ 

**Confidence Threshold:** The **confidence threshold** determines the minimum confidence level at which the model will accept its prediction as positive.

- Low Confidence Threshold: The model accepts predictions with lower confidence scores as positive. This can lead to higher recall (identifying more true positives) but typically results in lower precision because more false positives are included.
- High Confidence Threshold: The model requires higher confidence in its predictions before accepting them as positive. This increases precision because only the most confident predictions are accepted, but it can decrease recall because some true positives may be excluded.



## Key observations:

- Most classes maintain high F1 scores for a wide range of confidence values.
- The overall performance across all classes (indicated by the bold blue line) shows an F1 score of 0.94 at a confidence of 0.314. This suggests that the model performs well even at relatively low confidence thresholds.
- Certain classes like "Green Light" and "Red Light" show a decline in F1 score at higher confidence values, indicating a drop in recall as confidence increases.

# 5. Recall-Confidence Curve:

A Recall-Confidence Curve is a graphical representation used to evaluate the performance of a classification model, particularly in contexts where confidence scores are available for the predictions. Here's a detailed explanation:

### **Key Concepts**

- 1. Recall (Also known as Sensitivity or True Positive Rate):
  - It is the ratio of correctly predicted positive observations to all actual positives.

Formula: Recall = 
$$\frac{TP}{TP+FN}$$

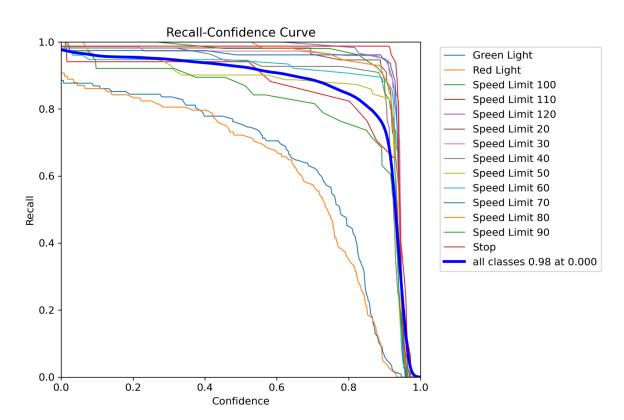
- TP (True Positives): Correctly predicted positive cases.
- FN (False Negatives): Actual positive cases that were incorrectly predicted as negative.

### 2. Confidence:

- The probability score that the model assigns to a prediction.
- Higher confidence means the model is more certain about its prediction.

### **Purpose of the Recall-Confidence Curve**

The Recall-Confidence Curve helps to understand how the recall varies with different confidence thresholds. This is particularly useful in applications where it is important to balance recall and precision based on the confidence level of the predictions.



### **Key observations:**

The curve indicates a good balance between recall and confidence, with a high recall maintained until a confidence level of about 0.8.

At very high confidence levels (close to 1.0), recall drops off sharply, indicating that at these levels, the model is very precise but may miss more instances (lower recall).

**High Performing Classes**: Green Light, Stop, and higher speed limits (100, 110, 120) show high recall across various confidence levels, indicating strong model performance for these classes.

**Lower Performing Classes**: Red Light and lower speed limits show a quicker drop in recall with increasing confidence, suggesting areas where the model may need improvement. **Overall Performance**: The overall performance is quite strong, with high recall maintained until around 0.8 confidence, but a sharp drop-off at very high confidence levels.

# How to tell if there's overfitting?

The curve that helps us determine if there is overfitting is the **learning curve**. Specifically, we look at two learning curves:

- 1. **Training Learning Curve**: This shows the performance of the model on the training data
- 2. **Validation Learning Curve**: This shows the performance of the model on a separate validation set.

To diagnose overfitting using these curves, we look for the following patterns:

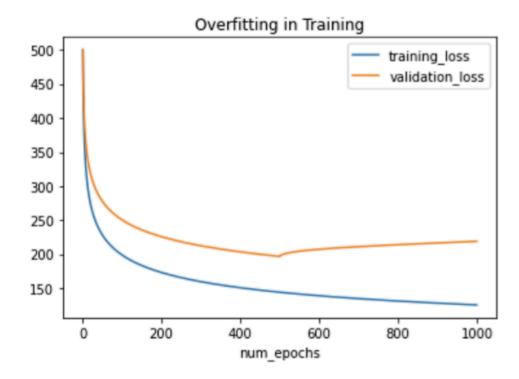
- **Overfitting**: If the training curve shows low error (high performance) while the validation curve shows high error (low performance), the model is likely overfitting. This means the model performs well on training data but poorly on unseen data.
- **Underfitting**: If both training and validation curves show high error, the model is likely underfitting. This means the model is too simple to capture the underlying patterns in the data.
- **Good Fit**: If both training and validation curves show low error and are close to each other, the model is likely well-fit, balancing bias and variance effectively.

Here's a visual representation of these scenarios:

### 1. Overfitting:

Training error: LowValidation error: High

o Pattern: Large gap between the training and validation curves.



An example of overfitting during training

0

## 2. Underfitting:

Training error: HighValidation error: High

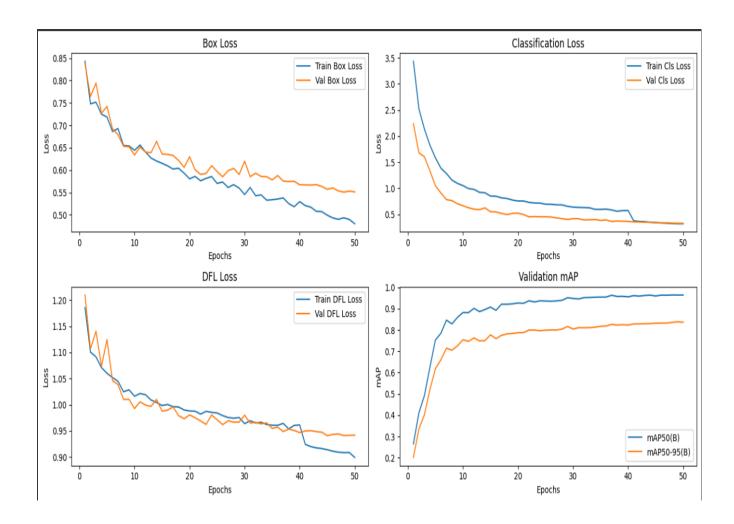
o Pattern: Both curves have high error and are close together.

### 3. Good Fit:

Training error: LowValidation error: Low

o Pattern: Both curves have low error and are close together.

By analyzing these curves, you can adjust your model's complexity and training process to reduce overfitting or underfitting.



### 1. Classification Loss

**Classification loss** measures how well the model classifies the objects it detects. In object detection, the model not only needs to find objects but also correctly identify their categories (e.g., car, pedestrian, bicycle). This loss is typically computed using a categorical cross-entropy or similar loss function, which compares the predicted class probabilities to the actual class labels. Lower classification loss indicates that the model is correctly identifying the objects' classes.

### 2. Box Loss

**Box loss** evaluates how accurately the model predicts the bounding boxes for detected objects. The bounding box is the rectangle drawn around the object, defining its location and size in the image. This loss usually consists of two components:

- Localization loss: Measures how accurately the predicted bounding box matches the ground truth bounding box.
- **Regression loss**: Often computed using a smooth L1 loss or IoU (Intersection over Union), which penalizes deviations from the actual bounding box coordinates.

Lower box loss means that the predicted bounding boxes are closer to the true bounding boxes.

### 3. DFL Loss (Distribution Focal Loss)

**DFL loss (Distribution Focal Loss)** is specific to advanced object detection models like YOLOv8. It is a type of loss used to refine the bounding box regression by focusing on the most important parts of the distribution of possible bounding boxes. This loss helps the model to more precisely localize objects by emphasizing harder-to-predict areas. DFL helps in improving the overall accuracy of the bounding box predictions.

# 4. Validation mAP (Mean Average Precision)

**Validation mAP** is a metric that evaluates the performance of the object detection model on the validation dataset. It summarizes how well the model is at detecting objects and classifying them correctly across different categories. Here's a breakdown:

- mAP@50 (mAP50): The mean Average Precision at an IoU threshold of 0.50. This means a predicted bounding box is considered correct if it overlaps with the ground truth bounding box by at least 50%.
- mAP@50:95 (mAP50-95): The mean Average Precision across multiple IoU thresholds ranging from 0.50 to 0.95 in steps of 0.05. This gives a more comprehensive evaluation of the model's precision and recall.

Higher mAP values indicate better performance, as the model is more accurate in detecting and classifying objects in the validation dataset.

### **Summary:**

- Classification Loss: Measures how well the model identifies the categories of detected objects.
- **Box Loss**: Evaluates the accuracy of the predicted bounding box locations.
- **DFL Loss**: Refines the bounding box predictions by focusing on the distribution of possible boxes.
- **Validation mAP**: Summarizes the overall detection and classification performance on the validation set.

These metrics together provide a detailed understanding of the model's performance, highlighting areas of strength and aspects that may need improvement.

## **Analysis of the Learning Curves**

### 1. Box Loss:

- Training and validation box losses both decrease over epochs.
- The gap between the training and validation box losses is relatively small and consistent.

### 2. Classification Loss:

- Both training and validation classification losses decrease over epochs.
- The validation loss remains consistently higher than the training loss, but the gap narrows as training progresses.

### 3. **DFL Loss**:

- Training and validation DFL losses both decrease and are quite close to each other.
- There is a slight gap, but it remains small and consistent.

#### 4. Validation mAP:

- Both mAP50 and mAP50-95 metrics increase over epochs and seem to plateau towards the end.
- The mAP metrics do not show signs of decreasing, which indicates stable performance on the validation set.

### Conclusion

Based on the analysis of these curves:

### No Overfitting:

- The training and validation losses decrease and stay relatively close to each other, indicating that the model generalizes well.
- The validation mAP metrics improve and plateau, suggesting that the model's performance on the validation set remains strong without degrading.

### No Underfitting:

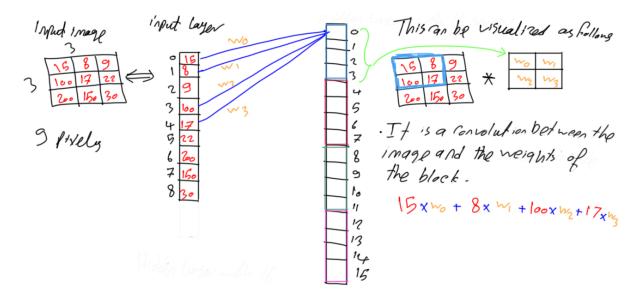
- The losses decrease consistently over epochs, indicating that the model is learning effectively from the data.
- The validation mAP metrics increase and plateau, showing that the model is capturing the underlying patterns in the data.

Overall, the learning curves suggest that the model is neither overfitting nor underfitting. The training process appears to be well-balanced, with the model achieving good generalization performance on the validation set.

# What are weights in CNN?

The term **weight** in the context of ML, DL, and NN is a synonym for **parameter** (sometimes, in some contexts, such as linear regression, it is also known as **coefficient**), which can be constant (i.e. do not change during, for example, learning/training) or learnable (i.e. change during the training/learning process). In a feedforward neural network (FFNN), with and without recurrent connections, the weights are the numbers on the connections between neurons in different or same layers. They are called **weights** to emphasize that their role is to weigh the effect of one neuron on the other.

In a CNN, the weights are the kernels/filters of the CNN, i.e. the matrices that you use to perform the convolution (or cross-correlation) operation in a convolutional layer.



In Convolutional Neural Networks (CNNs), weights are the parameters that the network learns during training to identify patterns and features in the input data. Here's a detailed explanation of weights in CNNs:

## **Convolutional Layers**

### 1. Filters/Kernels:

- A filter (or kernel) in a convolutional layer is a small matrix of weights. For example, a 3x3 filter has 9 weights.
- Filters slide over the input image (or feature map) and perform the convolution operation, which involves element-wise multiplication followed by summation.
- Each filter is responsible for detecting a specific feature, such as edges, textures, or other patterns.

### 2. Weight Initialization:

- Filters are initialized with small random values before training begins.
- Proper initialization is crucial to ensure that the network converges efficiently during training.

### 3. Learning Weights:

- During training, the CNN adjusts the weights of the filters to minimize the loss function (a measure of how well the network's predictions match the actual labels).
- This adjustment is done using backpropagation and gradient descent. The gradients of the loss with respect to the weights are computed, and the weights are updated in the direction that reduces the loss.

### **Fully Connected Layers**

### 1. Neurons and Weights:

- Fully connected (dense) layers consist of neurons, where each neuron is connected to every neuron in the previous layer.
- Each connection has an associated weight. These weights are also learned during training.
- The output of a neuron is computed as a weighted sum of its inputs, followed by an activation function.

### 2. Weight Matrix:

 The weights in a fully connected layer can be represented as a matrix, where each entry corresponds to the weight of a connection between neurons from consecutive layers.

## **Importance of Weights**

### 1. Feature Detection:

- In the early layers of a CNN, filters typically learn to detect simple features like edges and corners.
- In deeper layers, filters combine these simple features to detect more complex patterns and objects.

### 2. Model Performance:

- The effectiveness of a CNN in recognizing patterns and making accurate predictions depends on the quality of the learned weights.
- Proper training and optimization of these weights are critical for the network's performance on tasks like image classification, object detection, and segmentation.

## **Visualization and Interpretation**

### 1. Filter Visualization:

- Visualizing the learned filters can provide insights into what the network is focusing on at different layers.
- Techniques like activation maximization can be used to visualize the patterns that activate specific filters the most.

### 2. Weight Pruning and Regularization:

 Techniques like weight pruning (removing less important weights) and regularization (adding penalties to the loss function) help in reducing overfitting and improving generalization. In summary, weights in CNNs are crucial parameters that are learned during training to identify and extract features from the input data. These weights are present in both convolutional layers (as filters) and fully connected layers (as weight matrices) and are adjusted through optimization techniques to improve the network's performance.