

# **Chapter 8: Relational Database Design**

## **Part III. Decomposition**

# Lossless-join Decomposition

- For the case of  $R = (R_1, R_2)$ , we require that for all possible relations  $r$  on schema  $R$

$$r = \Pi_{R_1}(r) \bowtie \Pi_{R_2}(r)$$

- A decomposition of  $R$  into  $R_1$  and  $R_2$  is lossless join if at least one of the following dependencies is in  $F^+$ :
  - $R_1 \cap R_2 \rightarrow R_1$
  - $R_1 \cap R_2 \rightarrow R_2$
- The above functional dependencies are a sufficient condition for lossless join decomposition; the dependencies are a necessary condition only if all constraints are functional dependencies.

# Example

- $R = (A, B, C)$   
 $F = \{A \rightarrow B, B \rightarrow C\}$ 
  - Can be decomposed in two different ways

- $R_1 = (A, B), R_2 = (B, C)$ 
  - Lossless-join decomposition:  
$$R_1 \cap R_2 = \{B\} \text{ and } B \rightarrow BC$$
  - Dependency preserving

- $R_1 = (A, B), R_2 = (A, C)$ 
  - Lossless-join decomposition:  
$$R_1 \cap R_2 = \{A\} \text{ and } A \rightarrow AB$$
  - Not dependency preserving  
(cannot check  $B \rightarrow C$  without computing  $R_1 \bowtie R_2$ )

# Dependency Preservation

- Let  $F_i$  be the set of dependencies  $F^+$  that include only attributes in  $R_i$ .
  - ▶ A decomposition is **dependency preserving**, if
$$(F_1 \cup F_2 \cup \dots \cup F_n)^+ = F^+$$
  - ▶ If it is not, then checking updates for violation of functional dependencies may require computing joins, which is expensive.

# Testing for Dependency Preservation

- To check if a dependency  $\alpha \rightarrow \beta$  is preserved in a decomposition of  $R$  into  $R_1, R_2, \dots, R_n$  we apply the following test (with attribute closure done with respect to  $F$ )
  - $result = \alpha$   
  **while** (changes to  $result$ ) **do**  
    **for each**  $R_i$  in the decomposition  
       $t = (result \cap R_i)^+ \cap R_i$   
       $result = result \cup t$
  - If  $result$  contains all attributes in  $\beta$ , then the functional dependency  $\alpha \rightarrow \beta$  is preserved.
- We apply the test on all dependencies in  $F$  to check if a decomposition is dependency preserving
- This procedure takes polynomial time, instead of the exponential time required to compute  $F^+$  and  $(F_1 \cup F_2 \cup \dots \cup F_n)^+$

# Example

- $R = (A, B, C)$   
 $F = \{A \rightarrow B$   
 $\quad B \rightarrow C\}$   
Key =  $\{A\}$
- $R$  is not in BCNF
- Decomposition  $R_1 = (A, B), R_2 = (B, C)$ 
  - $R_1$  and  $R_2$  in BCNF
  - Lossless-join decomposition
  - Dependency preserving

# Third Normal Form: Motivation

- There are some situations where
  - BCNF is not dependency preserving, and
  - efficient checking for FD violation on updates is important
- Solution: define a weaker normal form, called Third Normal Form (3NF)
  - Allows some redundancy (with resultant problems; we will see examples later)
  - But functional dependencies can be checked on individual relations without computing a join.
  - There is always a lossless-join, dependency-preserving decomposition into 3NF.

# 3NF Example

## ■ Relation *dept\_advisor*:

- *dept\_advisor* (*s\_ID*, *i\_ID*, *dept\_name*)  
 $F = \{s\_ID, dept\_name \rightarrow i\_ID, i\_ID \rightarrow dept\_name\}$
- Two candidate keys: *s\_ID*, *dept\_name*, and *i\_ID*, *s\_ID*
- *R* is in 3NF
  - ▶  $s\_ID, dept\_name \rightarrow i\_ID \quad s\_ID$ 
    - *dept\_name* is a superkey
  - ▶  $i\_ID \rightarrow dept\_name$ 
    - *dept\_name* is contained in a candidate key



# Testing for 3NF

- Optimization: Need to check only FDs in  $F$ , need not check all FDs in  $F^+$ .
- Use attribute closure to check for each dependency  $\alpha \rightarrow \beta$ , if  $\alpha$  is a superkey.
- If  $\alpha$  is not a superkey, we have to verify if each attribute in  $\beta$  is contained in a candidate key of  $R$ 
  - this test is rather more expensive, since it involve finding candidate keys
  - testing for 3NF has been shown to be NP-hard
  - Interestingly, decomposition into third normal form (described shortly) can be done in polynomial time

# 3NF Decomposition Algorithm

6<sup>th</sup> edition, p. 352

```
Let  $F_c$  be a canonical cover for  $F$ ;  
 $i := 0$ ;  
for each functional dependency  $\alpha \rightarrow \beta$  in  $F_c$  do  
     $i := i + 1$ ;  
     $R_i := \alpha \beta$ ;  
end;  
if none of the schemas  $R_j$ ,  $1 \leq j \leq i$  contains a candidate key for  $R$   
then begin  
     $i := i + 1$ ;  
     $R_i :=$  any candidate key for  $R$ ;  
end;  
/* Optionally, remove redundant relations */  
repeat  
if any schema  $R_j$  is contained in another schema  $R_k$   
    then /* delete  $R_j$  */  
         $R_j = R_i$ ;  
         $i = i - 1$ ;  
return  $(R_1, R_2, \dots, R_i)$ ;
```

# 3NF Decomposition Algorithm (Cont.)

- Above algorithm ensures:
  - each relation schema  $R_i$  is in 3NF
  - decomposition is dependency preserving and lossless-join
  - Proof of correctness is at end of this presentation ([click here](#))

# 3NF Decomposition: An Example

- Relation schema:

*cust\_banker\_branch* = (*customer\_id*, *employee\_id*, *branch\_name*, *type* )

- The functional dependencies for this relation schema are:

1. *customer\_id*, *employee\_id* → *branch\_name*, *type*

2. *employee\_id* → *branch\_name*

3. *customer\_id*, *branch\_name* → *employee\_id*

- We first compute a canonical cover

- *branch\_name* is extraneous in the r.h.s. of the 1<sup>st</sup> dependency

- No other attribute is extraneous, so we get  $F_C =$

*customer\_id*, *employee\_id* → *type*

*employee\_id* → *branch\_name*

*customer\_id*, *branch\_name* → *employee\_id*

# 3NF Decomposition Example (Cont.)

- The **for** loop generates following 3NF schema:

*(customer\_id, employee\_id, type )*

*(employee\_id, branch\_name)*

*(customer\_id, branch\_name, employee\_id)*

- Observe that *(customer\_id, employee\_id, type )* contains a candidate key of the original schema, so no further relation schema needs be added
- At end of for loop, detect and delete schemas, such as *(employee\_id, branch\_name)*, which are subsets of other schemas
  - result will not depend on the order in which FDs are considered
- The resultant simplified 3NF schema is:

*(customer\_id, employee\_id, type)*

*(customer\_id, branch\_name, employee\_id)*

# Testing for BCNF

- To check if a non-trivial dependency  $\alpha \rightarrow \beta$  causes a violation of BCNF
  1. compute  $\alpha^+$  (the attribute closure of  $\alpha$ ), and
  2. verify that it includes all attributes of  $R$ , that is, it is a superkey of  $R$ .
- **Simplified test:** To check if a relation schema  $R$  is in BCNF, it suffices to check only the dependencies in the given set  $F$  for violation of BCNF, rather than checking all dependencies in  $F^+$ .
  - If none of the dependencies in  $F$  causes a violation of BCNF, then none of the dependencies in  $F^+$  will cause a violation of BCNF either.
- However, **simplified test using only  $F$  is incorrect when testing a relation in a decomposition of  $R$** 
  - Consider  $R = (A, B, C, D, E)$ , with  $F = \{ A \rightarrow B, BC \rightarrow D \}$ 
    - ▶ Decompose  $R$  into  $R_1 = (A, B)$  and  $R_2 = (A, C, D, E)$
    - ▶ Neither of the dependencies in  $F$  contain only attributes from  $(A, C, D, E)$  so we might be misled into thinking  $R_2$  satisfies BCNF.
    - ▶ In fact, dependency  $AC \rightarrow D$  in  $F^+$  shows  $R_2$  is not in BCNF.

# BCNF Decomposition Algorithm

```
result := {R };
done := false;
compute  $F^+$ ;
while (not done) do
    if (there is a schema  $R_i$  in result that is not in BCNF)
        then begin
            let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that
                holds on  $R_i$  such that  $\alpha \rightarrow R_i$  is not in  $F^+$ ,
                and  $\alpha \cap \beta = \emptyset$ ;
            result := (result -  $R_i$ )  $\cup$  ( $R_i - \beta$ )  $\cup$  ( $\alpha, \beta$ );
        end
    else done := true;
```

Note: each  $R_i$  is in BCNF, and decomposition is lossless-join.

# Decomposing a Schema into BCNF

- Suppose we have a schema  $R$  and a non-trivial dependency  $\alpha \rightarrow \beta$  causes a violation of BCNF.

We decompose  $R$  into:

- $(\alpha \cup \beta)$  and
  - $(R - (\beta - \alpha))$
- In our example,
    - $\alpha = dept\_name$
    - $\beta = building, budget$and *inst\_dept* is replaced by
    - $(\alpha \cup \beta) = (dept\_name, building, budget)$
    - $(R - (\beta - \alpha)) = (ID, name, salary, dept\_name)$



# Example of BCNF Decomposition

- $R = (A, B, C)$   
 $F = \{A \rightarrow B$   
 $B \rightarrow C\}$   
Key =  $\{A\}$
- $R$  is not in BCNF ( $B \rightarrow C$  but  $B$  is not a superkey)
- Decomposition
  - $R_1 = (B, C)$
  - $R_2 = (A, B)$

# Example of BCNF Decomposition

- *class* (*course\_id*, *title*, *dept\_name*, *credits*, *sec\_id*, *semester*, *year*, *building*, *room\_number*, *capacity*, *time\_slot\_id*)
- Functional dependencies:
  - *course\_id* → *title*, *dept\_name*, *credits*
  - *building*, *room\_number* → *capacity*
  - *course\_id*, *sec\_id*, *semester*, *year* → *building*, *room\_number*, *time\_slot\_id*
- A candidate key {*course\_id*, *sec\_id*, *semester*, *year*}.
- BCNF Decomposition:
  - *course\_id* → *title*, *dept\_name*, *credits* holds
    - ▶ but *course\_id* is not a superkey.
  - We replace *class* by:
    - ▶ *course*(*course\_id*, *title*, *dept\_name*, *credits*)
    - ▶ *class-1* (*course\_id*, *sec\_id*, *semester*, *year*, *building*, *room\_number*, *capacity*, *time\_slot\_id*)

# BCNF Decomposition (Cont.)

- *course* is in BCNF
  - How do we know this?
- *building, room\_number* → *capacity* holds on *class-1*
  - but {*building, room\_number*} is not a superkey for *class-1*.
  - We replace *class-1* by:
    - ▶ *classroom* (*building, room\_number, capacity*)
    - ▶ *section* (*course\_id, sec\_id, semester, year, building, room\_number, time\_slot\_id*)
- *classroom* and *section* are in BCNF.

# BCNF and Dependency Preservation

It is not always possible to get a BCNF decomposition that is dependency preserving.

■  $R = (J, K, L)$

$F = \{JK \rightarrow L$   
 $L \rightarrow K\}$

Two candidate keys =  $JK$  and  $JL$

■  $R$  is not in BCNF

■ Any decomposition of  $R$  will fail to preserve

$JK \rightarrow L$

This implies that testing for  $JK \rightarrow L$  requires a join.

# BCNF and Dependency Preservation

- Constraints, including functional dependencies, are costly to check in practice unless they pertain to only one relation.
- If it is sufficient to test only those dependencies on each individual relation of a decomposition in order to ensure that *all* functional dependencies hold, then that decomposition is *dependency preserving*.
- Because it is not always possible to achieve both BCNF and dependency preservation, we consider a weaker normal form, known as *third normal form*.

# Comparison of BCNF and 3NF

- It is always possible to decompose a relation into a set of relations that are in 3NF such that:
  - the decomposition is lossless
  - the dependencies are preserved
- It is always possible to decompose a relation into a set of relations that are in BCNF such that:
  - the decomposition is lossless
  - it may not be possible to preserve dependencies.

# Design Goals

- Goal for a relational database design is:
  - BCNF.
  - Lossless join.
  - Dependency preservation.
- If we cannot achieve this, we accept one of
  - Lack of dependency preservation
  - Redundancy due to use of 3NF
- Interestingly, SQL does not provide a direct way of specifying functional dependencies other than superkeys.

Can specify FDs using assertions, but they are expensive to test, (and currently not supported by any of the widely used databases!)
- Even if we had a dependency preserving decomposition, using SQL we would not be able to efficiently test a functional dependency whose left hand side is not a key.