Lecture SAT Example Depth First Search

Prepared by S. Baskaran

State Space

The start state is "11111".

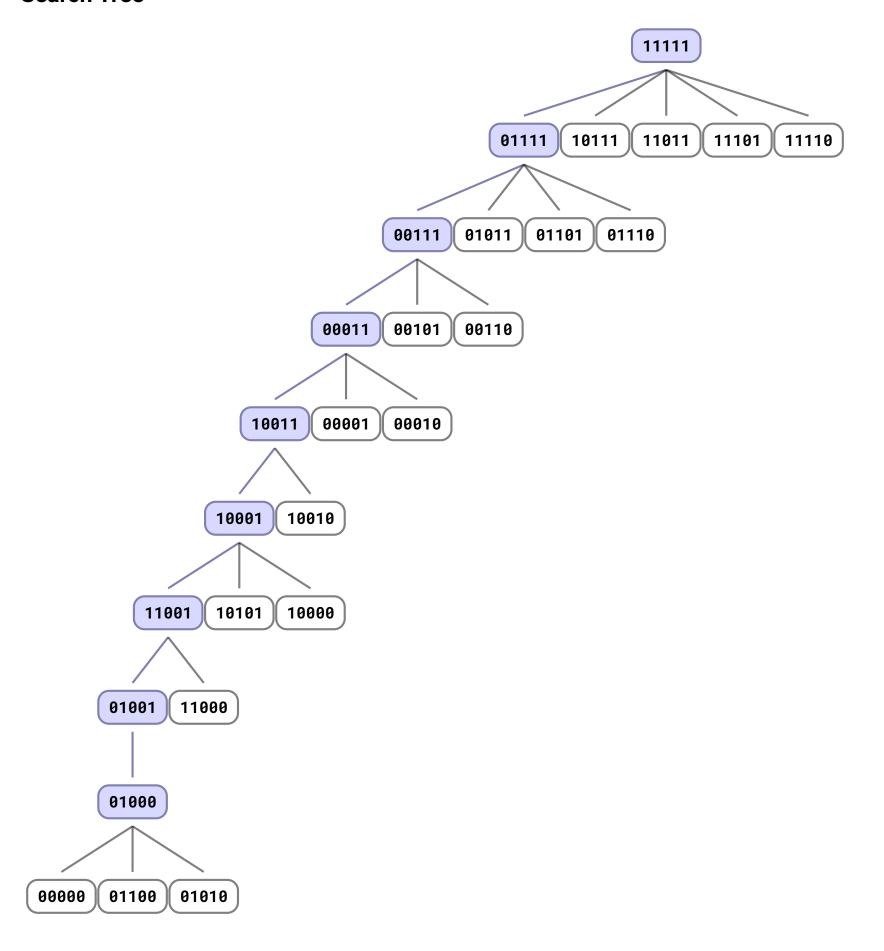
MoveGen is a one bit flip function.

It flips the bits from left to right, one bit at a time, and accordingly returns the neighbours.

 $\mathsf{F}(\mathsf{abcde}) = (\mathsf{b} \, \mathsf{V} \, \neg \mathsf{c}) \, \wedge \, (\mathsf{c} \, \mathsf{V} \, \neg \mathsf{d}) \, \wedge \, (\neg \mathsf{b}) \, \wedge \, (\neg \mathsf{a} \, \mathsf{V} \, \neg \mathsf{e}) \, \wedge \, (\mathsf{e} \, \mathsf{V} \, \neg \mathsf{c}) \, \wedge \, (\neg \mathsf{c} \, \mathsf{V} \, \neg \mathsf{d})$

0 N -	.	L / C)		(b.) (-)	(-) (-1)	(L)	eval	(-)	(a.v1\
S.No.	abcde	h(F)	eval(F)	(b V ¬c)	(c v ¬d)	(¬b)	(¬a∨¬e)	(e V ¬c)	(¬c ∨ ¬d)
1	00000	6	1	1	1	1	1	1	1
2	00001	6	1	1	1	1	1	1	1
3	00010	5	0	1	0	1	1	1	1
4	00011	5	0	1	0	1	1	1	1
5	00100	4	0	0	1	1	1	0	1
6	00101	5	0	0	1	1	1	1	1
7	00110	3	0	0	1	1	1	0	0
8	00111	4	0	0	1	1	1	1	0
9	01000	5	0	1	1	0	1	1	1
10 11	01001 01010	5 4	0 0	1 1	1 0	0 0	1	1	1 1
12	01011	4	0	1	0	0	1	1	1
13	01100	4	0	1	1	0	1	0	1
14	01101	5	0	1	1	0	1	1	1
15	01110	3	0	1	1	0	1	0	0
16	01111	4	0	1	1	0	1	1	0
17	10000	6	1	1	1	1	1	1	1
18	10001	5	0	1	1	1	0	1	1
19	10010	5	0	1	0	1	1	1	1
20	10011	4	0	1	0	1	0	1	1
21	10100	4	0	0	1	1	1	0	1
22	10101	4	0	0	1	1	0	1	1
23	10110	3	0	0	1	1	1	0	0
24	10111	3	0	0	1	1	0	1	0
25	11000	5	0	1	1	0	1	1	1
26	11001	4	0	1	1	0	0	1	1
27	11010	4	0	1	0	0	1	1	1
28	11011	3	0	1	0	0	0	1	1
29	11100	4	0	1	1	0	1	0	1
30	11101	4	0	1	1	0	0	1	1
31	11110	3	0	1	1	0	1	0	0
32	11111	3	0	1	1	0	0	1	0

Search Tree



OPEN CLOSED 1. NODE close

```
Solution
OPEN and CLOSED carry pairs: (NODE, PARENT)
           (11111, null):[]
           11111
           (11111, null)
moveGen
           01111:10111:11011:11101:11110:[]
           01111:10111:11011:11101:11110:[]
newNodes
newPairs
           (01111, 11111):(10111, 11111):(11011, 11111):(11101, 11111):
           (11110, 11111):[]
OPEN
           (01111, 11111):(10111, 11111):(11011, 11111):(11101, 11111):
           (11110, 11111):[]
           (11111, null):[]
CLOSED
2.
NODE
           01111
close
           (01111, 11111)
moveGen
           11111:00111:01011:01101:01110:[]
           00111:01011:01101:01110:[]
newNodes
           (00111,01111):(01011,01111):(01101,01111):(01110,01111):[]
newPairs
OPEN
           (00111,01111):(01011,01111):(01101,01111):(01110,01111):
           (10111, 11111):(11011, 11111):(11101, 11111):(11110, 11111):[]
           (01111,11111):(11111,null):[]
CLOSED
3.
           00111
NODE
           (00111,01111)
close
           10111:01111:00011:00101:00110:[]
moveGen
           00011:00101:00110:[]
newNodes
           (00011,00111):(00101,00111):(00110,00111):[]
newPairs
           (00011,00111):(00101,00111):(00110,00111):(01011,01111):
OPEN
           (01101, 01111):(01110, 01111):(10111, 11111):(11011, 11111):
           (11101, 11111):(11110, 11111):[]
CLOSED
           (00111,01111):(01111,11111):(11111,null):[]
4.
NODE
           00011
close
           (00011,00111)
           10011:01011:00111:00001:00010:[]
moveGen
newNodes
           10011:00001:00010:[]
           (10011,00011):(00001,00011):(00010,00011):[]
newPairs
OPEN
            (10011,00011):(00001,00011):(00010,00011):(00101,00111):
           (00110,00111):(01011,01111):(01101,01111):(01110,01111):
           (10111, 11111):(11011, 11111):(11101, 11111):(11110, 11111):[]
           (00011,00111):(00111,01111):(01111,11111):(11111,null):[]
CLOSED
5.
NODE
           10011
close
           (10011,00011)
moveGen
           00011:11011:10111:10001:10010:[]
newNodes
           10001:10010:[]
           (10001, 10011):(10010, 10011):[]
newPairs
OPEN
           (10001, 10011):(10010, 10011):(00001, 00011):(00010, 00011):
           (00101,00111):(00110,00111):(01011,01111):(01101,01111):
           (01110, 01111):(10111, 11111):(11011, 11111):(11101, 11111):
           (11110,11111):[]
           (10011,00011):(00011,00111):(00111,01111):(01111,11111):
CLOSED
           (11111, null):[]
6.
NODE
           10001
close
           (10001, 10011)
           00001:11001:10101:10011:10000:[]
moveGen
newNodes
           11001:10101:10000:[]
           (11001, 10001):(10101, 10001):(10000, 10001):[]
newPairs
OPEN
           (11001, 10001):(10101, 10001):(10000, 10001):(10010, 10011):
           (00001,00011):(00010,00011):(00101,00111):(00110,00111):
           (01011, 01111):(01101, 01111):(01110, 01111):(10111, 11111):
           (11011, 11111):(11101, 11111):(11110, 11111):[]
CLOSED
           (10001, 10011):(10011, 00011):(00011, 00111):(00111, 01111):
           (01111,11111):(11111,null):[]
7.
NODE
           11001
close
           (11001, 10001)
moveGen
           01001:10001:11101:11011:11000:[]
           01001:11000:[]
newNodes
           (01001, 11001):(11000, 11001):[]
newPairs
           (01001, 11001): (11000, 11001): (10101, 10001): (10000, 10001):
OPEN
           (10010, 10011):(00001, 00011):(00010, 00011):(00101, 00111):
           (00110,00111):(01011,01111):(01101,01111):(01110,01111):
           (10111, 11111):(11011, 11111):(11101, 11111):(11110, 11111):[]
           (11001, 10001): (10001, 10011): (10011, 00011): (00011, 00111):
CLOSED
           (00111,01111):(01111,11111):(11111,null):[]
           01001
           (01001, 11001)
           11001:00001:01101:01011:01000:[]
           01000:[]
           (01000,01001):[]
           (01000,01001):(11000,11001):(10101,10001):(10000,10001):
           (10010, 10011):(00001, 00011):(00010, 00011):(00101, 00111):
           (00110,00111):(01011,01111):(01101,01111):(01110,01111):
           (10111, 11111):(11011, 11111):(11101, 11111):(11110, 11111):[]
           (01001, 11001):(11001, 10001):(10001, 10011):(10011, 00011):
           (00011,00111):(00111,01111):(01111,11111):(11111,null):[]
           01000
           (01000.01001)
           11000:00000:01100:01010:01001:[]
           00000:01100:01010:[]
           (00000,01000):(01100,01000):(01010,01000):[]
           (00000,01000):(01100,01000):(01010,01000):(11000,11001):
           (10101, 10001): (10000, 10001): (10010, 10011): (00001, 00011):
           (00010,00011):(00101,00111):(00110,00111):(01011,01111):
           (01101, 01111):(01110, 01111):(10111, 11111):(11011, 11111):
           (11101, 11111):(11110, 11111):[]
           (01000,01001):(01001,11001):(11001,10001):(10001,10011):
           (10011,00011):(00011,00111):(00111,01111):(01111,11111):
           (11111, null):[]
           00000
           00000
           (00000,01000):(01100,01000):(01010,01000):(11000,11001):
           (10101, 10001):(10000, 10001):(10010, 10011):(00001, 00011):
           (00010,00011):(00101,00111):(00110,00111):(01011,01111):
```

```
8.
NODE
close
moveGen
newNodes
newPairs
OPEN
CLOSED
9.
NODE
close
moveGen
newNodes
newPairs
OPEN
CLOSED
10.
NODE
GOAL
OPEN
           (01101, 01111):(01110, 01111):(10111, 11111):(11011, 11111):
            (11101, 11111):(11110, 11111):[]
CLOSED
           (01000,01001):(01001,11001):(11001,10001):(10001,10011):
           (10011,00011):(00011,00111):(00111,01111):(01111,11111):
           (11111, null):[]
PATH
           11111:01111:00111:00011:10011:10001:11001:01001:01000:00000:[]
```