Lista 05 - Atividade

Questão 1

i)
$$\int M SEN 5 \times dx$$
 $U = M = du = dx$

$$J = \int SeN(SM) dM$$

$$dV = 12M(SM) dM \qquad J = -\frac{1}{5} \cos(SX)$$

$$\int u \, dv = \int v \, du$$

$$\int m \, sen(5m) = m \left(-\frac{1}{5}\cos(5m)\right) - \int \left(-\frac{1}{5}\cos(5m)\right) \, dm$$

$$\int m \, sen(5m) \, dm = -\frac{1}{5}m\cos(5m) + \frac{1}{5}\int\cos(5m) \, dm$$

$$\int m \, sen(5m) \, dm = -\frac{1}{5}m\cos(5m) + \frac{1}{5}\cdot\left(\frac{1}{5}\sin(5m)\right) + C$$

$$\int m \, sen(5m) \, dm = -\frac{1}{5}m\cos(5m) + \frac{1}{25}\sin(5m) + C$$

ii) I'm In 3 ne don Juanos para formula

iii) $\int x^2 e^{xx} dx = x^2 \cdot e^x - \int e^x \cdot 2x \cdot dx = x^2 \cdot e^x - 2 \int x \cdot e^x dx =$ Sudv = uv - Svdu Sudv= u-v- Svdu u= x -> du= 1dx u=m2 - D du = 2m dm du= er - v= ex dv= ex . dx → v= ex $P = x^{2} \cdot e^{x} - 2(x \cdot e^{x} - \int e^{x} \cdot 1 \cdot dx) = x^{2} \cdot e^{x} - 2x \cdot e^{x} + 2e^{x} = e^{x}(x^{2} - 2x + 2) + C$ iv) Je32 cos 4m da Je cos (nx) dx + 1/4 Je cos (nx) dx = e cos (4x) + 4e x sm(4x) V = cos (4m) du = -4 sen (4x) dx $\frac{25}{9} \int_{-\infty}^{2x} \cos(4x) dx = \frac{3e^{2x}}{9} \cos(4x) + 4e^{3x} \sin(4x)$ dr= e3m dn $\int_{-2x}^{3x} \cos(ux) dx = \frac{3x}{25} \cdot [3\cos(ux) + 4 \sin(4x)]$ V = e $\int e^{3n} \cos(4n) dn = \frac{e^{3n}}{3} \cos(4x) + \frac{4}{3} \int e^{3n} \sin(4n) dn$ * REsolverdo a outra parete... Ser sen (un) da u = sen (4 m) du = 4 cos (4m) da dr= e V = 03 Je m (4m) dn = e m (9m) - 43 Je cos (4m) dn * substituindo o valor da integral na equação. $\int e^{3n} \cos (4n) dn = \frac{3n}{3} \cos (4n) + \frac{4}{3} \left(\frac{e^{3n}}{3} \sin (4n) - \frac{n}{3} \int e^{3x} \cos (4n) \right)$ 6 34 (14) 14 - 24 00 (HW) + HE NW (HW) - 16 } & coo (HW) qu

V) $\int x^2 \cos \theta = x du$ $u = x^2$ du = Zx du $dv = \cos x du$ v = x en x $\int u dv = uv - \int v du$ $\int x^2 \cos x du = x^2 x en x - \int x en x \cdot 2x dx$ $I = x^2 x en x - 2 \int x en x en x dx$ u = x en x dx $v = -\cos x e$

* Aplicando metodo de integração.

mb (m co)] - m coo m - = xb m man m? a

 $I_{J} = -m \cos m + \int \cos m \, dm$ $I_{J} = -m \cos m + \sin m + c_{J}$

* substituindo en (I), obtemos a integral de

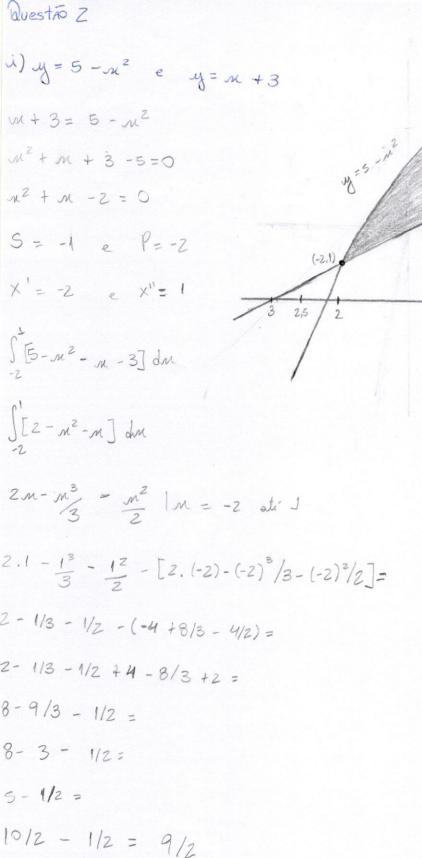
I = m2 mm m - ZI,

 $J = m^2 sen m - z \cdot (-m cos m + sen m) + C$

I = m2 sen x + zx cos x - z. sen x + C

I = (m²-2) ren m + Zm coo m + C

 $\int m^2 \cos m \, dm = (m^2 - 2) \sin m + 2m \cos m + C$



* ARRUMAND A FUNCAS.

$$=\int_{0}^{\infty}\left(e^{m}\right)^{2}\pi=\frac{1}{2}\pi\left[e^{2m}\right]_{0}^{1}$$

$$=\int \mathcal{I}_{2}\left[e^{2}-e^{0}\right]=\left[\frac{1}{2}\left[e^{2}-1\right]\right]$$

* Delimitada , organizand FICARIA ASSIM:

$$\int_{0}^{2\pi} 2 \sin n \, dn = \left[-z \cos n \right]_{0}^{2\pi} = -2 \cos 2\pi + z \cos 0 = 4u \cdot c^{2}$$

$$=\int \frac{\pi}{2} \left[e^2 - e^0 \right] = \frac{\pi}{2} \left[e^2 - 1 \right]$$

Jest 3 Spen 6 m cos x dn Spen 6 m (1- sen 2 m) cos m dn Spen 6 m cos m dn - Spen 8 m cos m dn $\frac{1}{2}$ $\frac{1}{2$ $\int_{0}^{\infty} \sin^{2} x dx + \cos^{2} x = 1$ $\int_{0}^{\infty} \cos^{2} x dx = 1 - \sin^{2} x dx$ $\int_{0}^{\infty} \int_{0}^{\infty} dx = \frac{\sqrt{x+1}}{x+1}$ $\int_{0}^{\infty} \int_{0}^{\infty} dx = \frac{\sqrt{x+1}}{x+1}$

ii)
$$\int \cos^{5}(m) dn = \int \cos^{4}(m) \cdot \cos(m) dn = \int ((\cos^{2}(m))^{2} \cos(m) dn = \int (1-\sin^{2}(x))^{2} \cdot \cos(x) dx = \lim_{n \to \infty} (n)$$

$$= \int (1 - u^{2})^{2} du = \int (1 - zu^{2} + u^{4}) du =$$

$$= u - 2 \cdot \frac{u^{3}}{3} + \frac{u^{5}}{5} = \left[\sin (m) - \frac{z}{3} \sin^{3}(m) + \frac{z}{5} \sin^{5}(x) + C \right]$$

* usando Funcas trigonométrica! i) Sen (Tim) cos (Tim) da

Spen2 (TIM) cos (TIM) dm = f Spen2 toso t dt

FUAMOS SEPARAR O $\cos^s t = \cos^4 t \cos t = (1-\sin^2 t)^2 \cos t$:

 $\int \operatorname{sen}^{2}(\Pi n) \cos^{5}(\Pi n) dn = \int \int \operatorname{sen}^{2}t (1-\operatorname{sen}^{2}t)^{2} \cos t dt$

* substituind pela integral u= sent

 $\int nen^{2}(\Pi m) \cos^{5}(\Pi m) dm = \prod_{n=1}^{\infty} \int u^{2}(1-u^{2})^{2} du = \prod_{n=1}^{\infty} \int u^{2}(1-2u^{2}+u^{4}) du$

 $\int n^2 (\pi n) \cos^5 (\pi n) dn = \frac{1}{\pi} \int (u^2 - 2u^4 + u^6) du$

*voltande on a variavel original con u = sen (TM).

Spen 2 (Mm) cos (Mm) dm = + (\frac{1}{3} \cdot Nm^3. (Mm) - \frac{2}{5} \cdot nm^5 (Mm) + \frac{1}{7} \cdot nm^7 (Mm)) + C

(V)
$$\int \sec^{2} \frac{8\pi}{8\pi} \cos^{2} \frac{5x}{5x} dx$$
 $\int \frac{8x + 5x = 13x}{8x + 5x = 13x}$
 $= \frac{1}{2} \int \sec^{2} (3x) + \sec^{2} (13x) dx$
 $= \frac{1}{2} \left(-\frac{1}{3} \cos^{2} (3x) - \frac{1}{13} \cos^{2} (13x) \right)$
 $= \left[-\frac{1}{6} \cos^{2} (3x) - \frac{1}{26} \cos^{2} (13x) \right] + C$

$$\int \cos 70 \cos 50 d0 = \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \left[\cos (70-50) + \cos (70+50) \right] d0$$

$$\int \cos 70 \cos 50 d0 = \frac{1}{2} \int \left[\cos (20) + \cos (120) \right] d0$$

$$\int \cos 70 \cos 50 d0 = \frac{1}{2} \int \cos (20) d0 + \frac{1}{2} \int \cos (120) d0$$

$$\int \cos 70 \cos 50 d0 = \frac{1}{4} \int 2 \cos (20) d0 + \frac{1}{24} \int 12 \cos (120) d0$$

$$\int \cos 70 \cos 50 d0 = \frac{1}{4} \int 2 \cos (20) d0 + \frac{1}{24} \int 12 \cos (120) d0$$

VI) 5 TIZ Men 2 one cost ne da

$$\int_{0}^{11/2} ren^{2}(x) cos^{2}(m) dm = \frac{1}{4} \cdot \int [2 ren (m) cos (m)]^{2} dm = \frac{1}{4} \cdot \int m^{2}(2m) dm = \frac{1}{4} \cdot \int (1 - cos (4m)) dm = \frac{1}{8} - ren \frac{4m}{32} + K$$